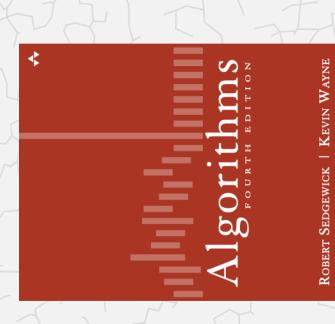
Algorithms



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3.1 SYMBOL TABLES

API

elementary implementations

ordered operations

▶ API

elementary implementations
 ordered operations

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Symbol tables

Key-value pair abstraction.

- * Insert a value with specified key.
- * Given a key, search for the corresponding value.

Ex. DNS lookup.

- Insert domain name with specified IP address.
- * Given domain name, find corresponding IP address.

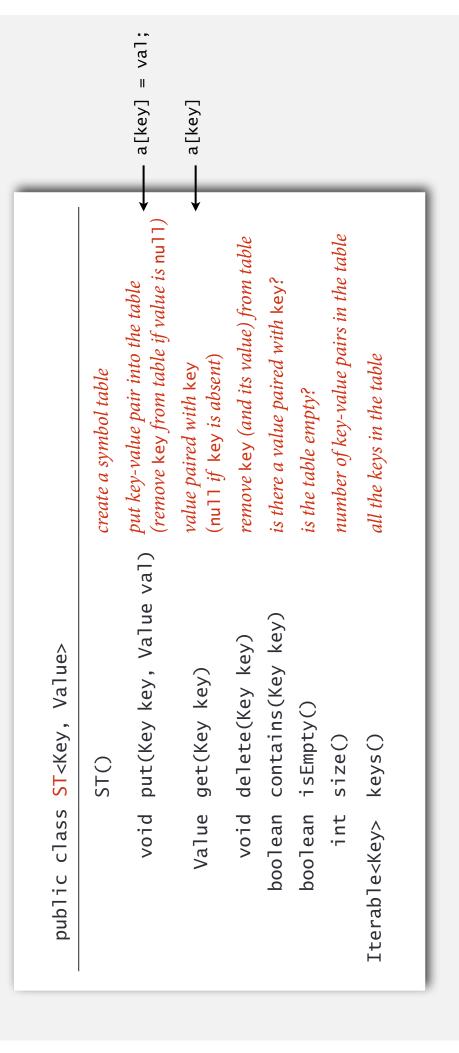
domain name	IP address
www.cs.princeton.edu	128.112.136.11
www.princeton.edu	128.112.128.15
www.yale.edu	130.132.143.21
www.harvard.edu	128.103.060.55
www.simpsons.com	209.052.165.60
_	
key	value

Symbol table applications

value	definition	list of page numbers	computer ID	transaction details	list of page names	type and value	best route	IP address	domain name	known positions	location on disk
key	word	term	name of song	account number	keyword	variable name	destination	domain name	IP address	DNA string	filename
purpose of search	find definition	find relevant pages	find song to download	process transactions	find relevant web pages	find properties of variables	route Internet packets	find IP address	find domain name	find markers	find file on disk
application	dictionary	book index	file share	financial account	web search	compiler	routing table	DNS	reverse DNS	genomics	file system

Basic symbol table API

Associative array abstraction. Associate one value with each key.



Conventions

- * Values are not null.
- Method get() returns null if key not present.
- * Method put() overwrites old value with new value.

Intended consequences.

* Easy to implement contains().

```
public boolean contains(Key key)
{    return get(key) != null;  }
```

Can implement lazy version of delete().

```
public void delete(Key key)
{  put(key, null); }
```

Keys and values

Value type. Any generic type.

Key type: several natural assumptions.

specify Comparable in API.

- Assume keys are Comparable, use compareTo().
- * Assume keys are any generic type, use equals() to test equality.
- Assume keys are any generic type, use equals() to test equality; use hashCode() to scramble key.

built-in to Java (stay tuned)

Best practices. Use immutable types for symbol table keys.

- Immutable in Java: Integer, Double, String, java.io.File,
- Mutable in Java: StringBuilder, java.net.URL, arrays, ...

Equality test

All Java classes inherit a method equals().

Java requirements. For any references x, y and z:

```
x Reflexive: x.equals(x) is true.
```

equivalence relation

x Symmetric: x.equals(y) iff y.equals(x).

* Transitive: if x.equals(y) and y.equals(z), then x.equals(z).

x Non-null: x.equals(null) is false.

do x and y refer to

the same object?

Default implementation. (x == y)

Customized implementations. Integer, Double, String, java.io.File, ...

User-defined implementations. Some care needed.

Implementing equals for user-defined types

Seems easy.

```
check that all significant
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fields are the same
    class Date implements Comparable<Date>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (this.day != that.day ) return false;
if (this.month != that.month) return false;
if (this.year != that.year ) return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               != that.year ) return false;
                                                                                                                                                                                                          public boolean equals(Date that)
                                                           private final int month;
                                                                                      private final int day;
private final int year;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return true;
public
```

Implementing equals for user-defined types

(religion: getClass() vs. instanceof) objects must be in the same class typically unsafe to use equals() with inheritance optimize for true object equality cast is guaranteed to succeed Why? Experts still debate. check that all significant fields are the same must be Object. check for null (would violate symmetry) public final class Date implements Comparable<Date> if (this.day != that.day) return false; if (this.month != that.month) return false; if (this.year != that.year) return false; if (y.getClass() != this.getClass()) Seems easy, but requires some care. if (y == null) return false; public boolean equals(Object y) if (y == this) return true; Date that = (Date) y; private final int month; private final int year; private final int day; return false; return true;

Equals design

"Standard" recipe for user-defined types.

- * Optimization for reference equality.
- Check against null.
- Check that two objects are of the same type and cast.
- Compare each significant field:
- if field is a primitive type, use ==
- if field is an object, use equals()
- alternatively, use Arrays.equals(a, b) if field is an array, apply to each entry ←

apply rule recursively
alternatively, use Arrays.equal
or Arrays.deepEquals(a, b),
but not a.equals(b)

Best practices.

- No need to use calculated fields that depend on other fields.
- Compare fields mostly likely to differ first.
- * Make compareTo() consistent with equals().



ST test client for traces

Build ST by associating value i with ith string from standard input.

```
ST<String, Integer> st = new ST<String, Integer>();
                                                                                                                                                                                                                                                                                                                  StdOut.println(s + " " + st.get(s));
                                                                                                      for (int i = 0; !StdIn.isEmpty(); i++)
public static void main(String[] args)
                                                                                                                                                                       String key = StdIn.readString();
                                                                                                                                                                                                                                                                           for (String s : st.keys())
                                                                                                                                                                                                           st.put(key, i);
```

```
Σ
工
       values 0
keys
```

output

```
A 8
C 4
H 5
H 5
N 9
X 7
```

ST test client for analysis

Frequency counter. Read a sequence of strings from standard input and print out one that occurs with highest frequency.

```
(21,191,455 words, 534,580 distinct)
                                                                                                                                                                                                                                                                                                                                                                                                    (135,635 words, 10,769 distinct)
                                                                                                                                                                                                                                                                                                                              (60 words, 20 distinct)
                                                                                                                                                                                                                                                                                                       tiny example
                                                                                                                                                                                                                                                                                                                                                                                                                                                        real example
                                                                                                                                                                                                                                                                                                                                                                              real example
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 % java FrequencyCounter 10 < leipzig1M.txt
                                                                                                                                                                                                                                                                                                           % java FrequencyCounter 1 < tinyTale.txt</pre>
                                                                                                                                                                                                                                                                                                                                                                                      % java FrequencyCounter 8 < tale.txt
                                                                                                                                                the epoch of incredulity
                                                                                               age of foolishness
                                                                                                                                                                                                     season of darkness
                                                                                                                                                                                                                                                       the winter of despair
                                                                                                                          the epoch of belief
                                                                                                                                                                              season of light
                                                                                                                                                                                                                              spring of hope
                                               the worst of times
                                                                         it was the age of wisdom
                        it was the best of times
% more tinyTale.txt
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           government 24763
                                                                                                                                                                                                                                                                                                                                                                                                               business 122
                                                                                                   the
                                                                                                                                                                               the
                                                                                                                                                                                                                                                          it was
                                                                                                                            it was
```

Frequency counter implementation

```
update frequency
                                                                                                                                                                                                                                                                                          read string and
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     with max freq
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         print a string
                                                                                                                                                    create ST
                                                                                                                                                                                                                                                        ignore short strings
                                                                                                                                                                                                                                                                                                                                               st.put(word, st.get(word) + 1);
                                                                                                                                                        ST<String, Integer> st = new ST<String, Integer>();
                                                                                                                                                                                                                                                                               if (word.length() < minlen) continue;
if (!st.contains(word)) st.put(word, 1);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     StdOut.println(max + " " + st.get(max));
                                                                                                                     int minlen = Integer.parseInt(args[0]);
                                                                                                                                                                                                                                                  String word = StdIn.readString();
                                                       public static void main(String[] args)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (st.get(word) > st.get(max))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (String word : st.keys())
                                                                                                                                                                                   while (!StdIn.isEmpty())
public class FrequencyCounter
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           max = word;
                                                                                                                                                                                                                                                                                                                                                                                                          String max = "";
                                                                                                                                                                                                                                                                                                                                                                                                                                             st.put(max, 0);
```

▶ API

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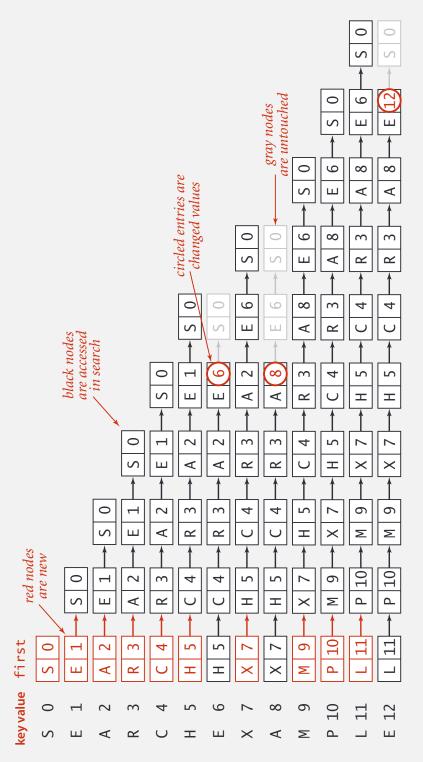
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Sequential search in a linked list

Data structure. Maintain an (unordered) linked list of key-value pairs.

Search. Scan through all keys until find a match.

Insert. Scan through all keys until find a match; if no match add to front.



Trace of linked-list ST implementation for standard indexing client

Elementary ST implementations: summary

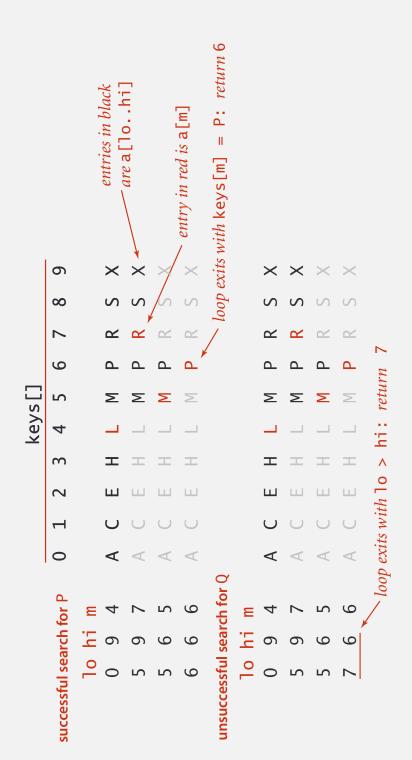
key interface		equals()
ordered iteration?		no
average case (after N random inserts)	insert	Z
avera (after N ran	search hit	N / 2
ise cost inserts)	insert	Z
worst-case cost (after N inserts)	search	Z
ST implementation		sequential search (unordered list)

Challenge. Efficient implementations of both search and insert.

Binary search in an ordered array

Data structure. Maintain an ordered array of key-value pairs.

Rank helper function. How many keys < k?



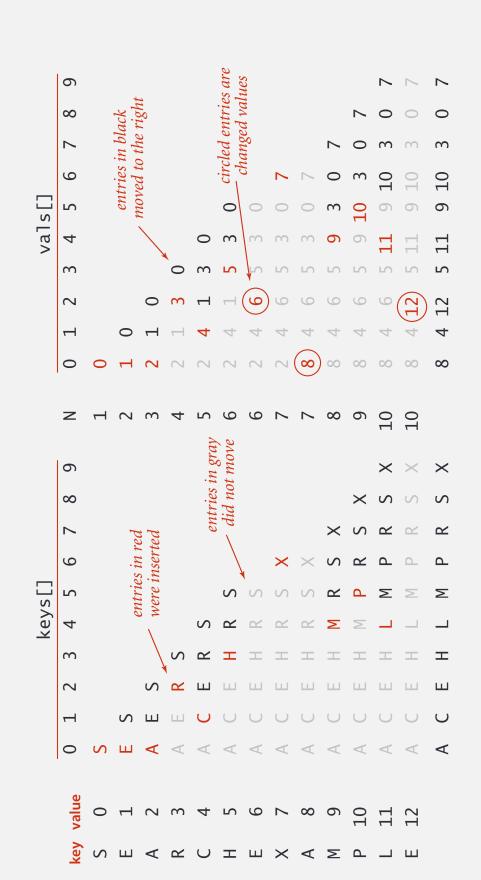
Trace of binary search for rank in an ordered array

Binary search: Java implementation

```
int i = rank(key);
if (i < N && keys[i].compareTo(key) == 0) return vals[i];</pre>
                                                                                                                                                                 number of keys < key
                                                                                                                                                                                                                                                                                      int mid = lo + (hi - lo) / 2;
                                    if (isEmpty()) return null;
public Value get(Key key)
                                                                                                                                                                private int rank(Key key)
                                                                                                                                                                                                      int lo = 0, hi = N-1;
                                                                                                    else return null;
                                                                                                                                                                                                                            while (lo <= hi)
                                                                                                                                                                                                                                                                                                                                                                                              return lo;
```

Binary search: trace of standard indexing client

Problem. To insert, need to shift all greater keys over.



Elementary ST implementations: summary

key interface		equals()	compareTo()
ordered		no	yes
average case (after N random inserts)	insert	z	N / 2
avera (after N rar	search hit	N / 2	log N
ase cost inserts)	insert	Z	Z
worst-case cost (after N inserts)	search	z	N gol
ST implementation		sequential search (unordered list)	binary search (ordered array)

Challenge. Efficient implementations of both search and insert.

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Examples of ordered symbol table API

```
Chicago
Seattle
Seattle
Phoenix
Chicago
Chicago
Chicago
Seattle
                                                                                                                                                                    Chicago
Chicago
                                             Chicago
Houston
              Chicago
                                   Houston
v lues
                                   09:00:13
                                             09:00:59
09:01:10
                                                                                                                        09:19:46
09:21:05
                                                                                         -09:10:25
09:14:25
09:19:32
                                                                   -09:03:13
09:10:11
                        09:00:03
              00:00:60 ←
                                                                                                                                               09:22:43
                                                                                                                                                         09:22:54
                                                                                                                                                                                                                       size(09:15:00, 09:25:00) is
                                             get(09:00:13)
                                                                    floor(09:05:00)
                                                                                           select(7)
                                                                                                                                                                                ceiling(09:30:00)
                                                                                                                                     keys(09:15:00, 09:25:00)
                                                                                                                                                                                                                                rank(09:10:25) is 7
```

Ordered symbol table API

le <key> Value></key>	create an ordered symbol table	put key-value pair into the table (remove key from table if value is nu11)	<pre>value paired with key (null if key is absent)</pre>	remove key (and its value) from table	is there a value paired with key?	is the table empty?	number of key-value pairs	smallest key	largest key	largest key less than or equal to key	smallest key greater than or equal to key	number of keys less than key	key of rank k	delete smallest key	delete largest key	number of keys in [10hi]	keys in [10hi], in sorted order	all keys in the table, in sorted order
class ST <key(extends comparable<key="">) Value></key(extends>	ST()	void put(Key key, Value val)	get(Key key)	delete(Key key)	contains(Key key)	isEmpty()	size()	min()	max()	Key floor(Key key)	ceiling(Key key)	rank(Key key)	select(int k)	deleteMin()	deleteMax()	size(Key lo, Key hi)	keys(Key lo, Key hi)	keys()
public class		void	Value	void	boolean	boolean	int	Key	Key	Key	Key	int	Key	void	void	int	Iterable <key></key>	Iterable <key> keys()</key>

Binary search: ordered symbol table operations summary

	sequential search	binary search
search	Z	N S
insert / delete	Z	Z
min / max	Z	_
floor / ceiling	Z	Z S
rank	Z	Z S
select	Z	_
ordered iteration	N lg N	z

order of growth of the running time for ordered symbol table operations

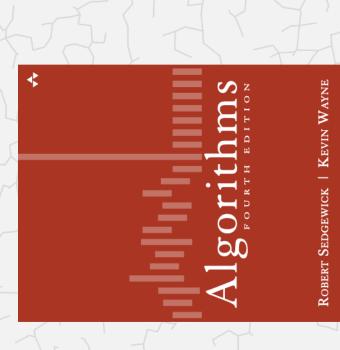
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