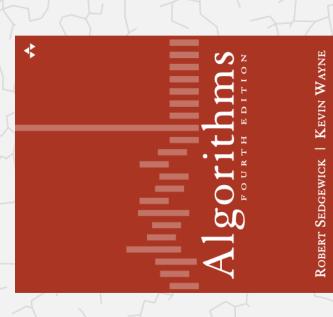
Algorithms



http://algs4.cs.princeton.edu

3.5 SYMBOL TABLE APPLICATIONS

- sets
- dictionary clients
- · indexing clients
- sparse vectors

sets

dictionary clients
 indexing clients

Sparse vectors

Algorithms

Robert Sedgewick | Kevin Wayne

Set API

Mathematical set. A collection of distinct keys.

ends Comparable <key>></key>	create an empty set	add the key to the set	is the key in the set?	remove the key from the set	return the number of keys in the set	iterator through keys in the set
public class SET <key comparable<key="" extends="">></key>	SET()	void add(Key key)	boolean contains(Key key)	void remove(Key key)	int size()	<pre>Iterator<key> iterator()</key></pre>

Q. How to implement?

Exception filter

- * Read in a list of words from one file.
- Print out all words from standard input that are { in, not in } the list.



Exception filter applications

- * Read in a list of words from one file.
- * Print out all words from standard input that are { in, not in } the list.

in list	dictionary words	visited pages	bad sites	positions	spam addresses	stolen cards
key	word dicti	URL	URL	board	IP address spai	number st
purpose	identify misspelled words	mark visited pages	block sites	detect draw	eliminate spam	check for stolen cards
application	spell checker	browser	parental controls	chess	spam filter	credit cards

Exception filter: Java implementation

- * Read in a list of words from one file.
- * Print out all words from standard input that are in the list.

```
create empty set of strings
                                                                                                                                                                                                                                                                                                                                                                    print words not in list
                                                                                                                                                                                                    read in whitelist
                                                                                                              = new SET<String>();
                                                                                                                                                                                                                                                                                                                                            String word = StdIn.readString();
                                                   public static void main(String[] args)
                                                                                                                                                                                                                              set.add(in.readString());
                                                                                                                                                                                                                                                                                                                                                                                                        StdOut.println(word);
                                                                                                                                                                                                                                                                                                                                                                          if (set.contains(word))
                                                                                                                                                                       In in = new In(args[0]);
                                                                                                                                                                                                                                                                                      while (!StdIn.isEmpty())
                                                                                                                                                                                                while (!in.isEmpty())
public class WhiteList
                                                                                                             SET<String> set
```

Exception filter: Java implementation

- Read in a list of words from one file.
- * Print out all words from standard input that are not in the list.

```
create empty set of strings
                                                                                                                                                                                                                                                                                                                                                                      print words not in list
                                                                                                                                                                                                      read in whitelist
                                                                                                                = new SET<String>();
                                                                                                                                                                                                                                                                                                                                              String word = StdIn.readString();
                                                      public static void main(String[] args)
                                                                                                                                                                                                                                set.add(in.readString());
                                                                                                                                                                                                                                                                                                                                                                                                          StdOut.println(word);
                                                                                                                                                                                                                                                                                                                                                                              if (!set.contains(word))
                                                                                                                                                                         In in = new In(args[0]);
                                                                                                                                                                                                                                                                                        while (!StdIn.isEmpty())
                                                                                                                                                                                                  while (!in.isEmpty())
public class BlackList
                                                                                                               SET<String> set
```

sets

dictionary clients
 indexing clients

Sparse vectors

Algorithms

Robert Sedgewick | Kevin Wayne

sets

dictionary clients

indexing clients

Algorithms

Sparse vectors

Robert Sedgewick | Kevin Wayne

Dictionary lookup

Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- x Value field.

Ex 1. DNS lookup.

domain name is key IP is value

% java LookupCSV ip.csv 0 1
adobe.com
192.150.18.60
www.princeton.edu
128.112.128.15
ebay.edu
Not found
% java LookupCSV ip.csv 1 0
128.112.128.15

www.princeton.edu

999.999.999

Not found

```
www.math.princeton.edu,128.112.18.11
                                                              www.cs.princeton.edu,128.112.136.35
                                                                                                                             www.cs.harvard.edu,140.247.50.127
                                www.princeton.edu,128.112.128.15
                                                                                                                                                                                                                     www.econ.yale.edu,128.36.236.74
                                                                                                                                                            www.harvard.edu,128.103.60.24
                                                                                                                                                                                                                                                      www.cs.yale.edu,128.36.229.30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  wikipedia.org,66.230.200.100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        passport.net,65.54.179.226
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  fastclick.com, 205.180.86.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rakuten.co.jp,202.72.51.22
                                                                                                                                                                                          www.yale.edu,130.132.51.8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     blogger.com,66.102.15.100
                                                                                                                                                                                                                                                                                                                                                                                                                                                yahoo.co.jp,202.93.91.141
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              sina.com.cn,202.108.33.32
                                                                                                                                                                                                                                                                                   espn.com,199.181.135.201
                                                                                                                                                                                                                                                                                                                                                                                 google.com,64.233.167.99
                                                                                                                                                                                                                                                                                                                                                                                                                  baidu.com, 202.108.22.33
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         adobe.com, 192.150.18.60
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     daum.net,211.115.77.211
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        nate.com,203.226.253.11
                                                                                                                                                                                                                                                                                                                   yahoo.com, 66.94.234.13
                                                                                                                                                                                                                                                                                                                                                     msn.com,207.68.172.246
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          163.com, 220.181.29.154
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ebay.com,66.135.192.87
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         tom.com,61.135.158.237
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    cnn.com,64.236.16.20
% more ip.csv
```

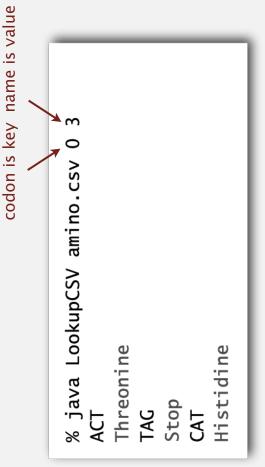
_

Dictionary lookup

Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- × Value field.

Ex 2. Amino acids.



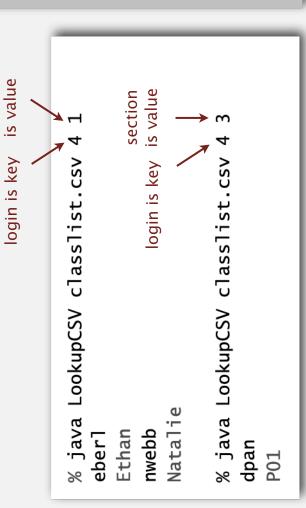
```
TTC, Phe, F, Phenylalanine
                      ITT, Phe, F, Phenylalanine
                                                                                                                                                                                                                                                                                                                                                                                           TGG, Trp, W, Tryptophan
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CAT, His, H, Histidine
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CAC, His, H, Histidine
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CAA,Gln,Q,Glutamine
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CAG, Gln, Q, Glutamine
                                                                                                                                                                                                                                             TAC, Tyr, Y, Tyrosine
                                                                                                                                                                                                                                                                      TAA, Stop, Stop, Stop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CGT, Arg, R, Arginine
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CGC, Arg, R, Arginine
                                                                                                                                                                                                                      TAT, Tyr, Y, Tyrosine
                                                                                                                                                                                                                                                                                              TAG, Stop, Stop, Stop
                                                                                                                                                                                                                                                                                                                       TGT, Cys, C, Cysteine
                                                                                                                                                                                                                                                                                                                                              TGC, Cys, C, Cysteine
                                                                                                                                                                                                                                                                                                                                                                      TGA, Stop, Stop, Stop
                                                                      TTA, Leu, L, Leucine
                                                                                               TTG, Leu, L, Leucine
                                                                                                                                                                                                                                                                                                                                                                                                                      CTT, Leu, L, Leucine
                                                                                                                                                                                                                                                                                                                                                                                                                                              CTC, Leu, L, Leucine
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CTA, Leu, L, Leucine
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CTG, Leu, L, Leucine
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CCT, Pro, P, Proline
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CCC, Pro, P, Proline
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CCA, Pro, P, Proline
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CCG, Pro, P, Proline
                                                                                                                                                                                              TCG, Ser, S, Serine
                                                                                                                      TCT, Ser, S, Serine
                                                                                                                                             TCC, Ser, S, Serine
                                                                                                                                                                      TCA, Ser, S, Serine
% more amino.csv
```

Dictionary lookup

Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- value field.

Ex 3. Class list.



```
12, Hantman, Nicole Samantha, P01, nhantman
                                                                                                                                                                                                                                                                                                           11, Hesterberg, Adam Classen, PO1, ahesterb
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        11,Nastasescu,Maria Monica,P01,mnastase
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             12, Partridge, Brenton Alan, P01, bpartrid
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      11, MacDonald, Graham David, P01, gmacdona
                                                                                                                                                                              10,Douglas,Malia Morioka,P01,malia
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                10,Michal,Brian Thomas,P01,bmichal
                                                                                                                                                                                                                       12, Haddock, Sara Lynn, P01, shaddock
                                                                                  12, Cao, Phillips Minghua, P01, pcao
                                                                                                                                                                                                                                                                                                                                                                                                     13, Hyde, Gregory Thomas, P01, ghyde
                                                                                                                                11, Chehoud, Christel, P01, cchehoud
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        12, Nam, Seung Hyeon, P01, seungnam
                                        13, Berl, Ethan Michael, P01, eberl
                                                                                                                                                                                                                                                                                                                                                           13, Hwang, Roland Lee, P01, rhwang
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 13, Roopakalu, Ajay, P01, aroopaka
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         13,Rilee,Alexander,P01,arilee
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         12, Webb, Natalie Sue, PO1, nwebb
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      12,Korac,Damjan,P01,dkorac
                                                                                                                                                                                                                                                                                                                                                                                                                                               13, Kim, Hyunmoon, PO1, hktwo
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11, Sheng, Ben C, P01, bsheng
% more classlist.csv
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    11, Pan, Di, P01, dpan
```

first name

Dictionary lookup: Java implementation

```
build symbol table
                                                                                                                                              process input file
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           with standard I/O
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 process lookups
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (!st.contains(s)) StdOut.println("Not found");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   StdOut.println(st.get(s));
                                                                                                                                                                                                                            ST<String, String> st = new ST<String, String>();
while (!in.isEmpty())
                                                                                                                                            int keyField = Integer.parseInt(args[1]);
                                                                                                                                                                       int valField = Integer.parseInt(args[2]);
                                                                                                                                                                                                                                                                                                            String line = in.readLine();
String[] tokens = line.split(",");
                                                      public static void main(String[] args)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             String s = StdIn.readString();
                                                                                                                                                                                                                                                                                                                                                                                            String val = tokens[valField];
                                                                                                                                                                                                                                                                                                                                                                  String key = tokens[keyField];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while (!StdIn.isEmpty())
{
                                                                                                                    In in = new In(args[0]);
                                                                                                                                                                                                                                                                                                                                                                                                                           st.put(key, val);
public class LookupCSV
```

sets

dictionary clients

indexing clients

Algorithms

Sparse vectors

Robert Sedgewick | Kevin Wayne

sets

dictionary clientsindexing clients

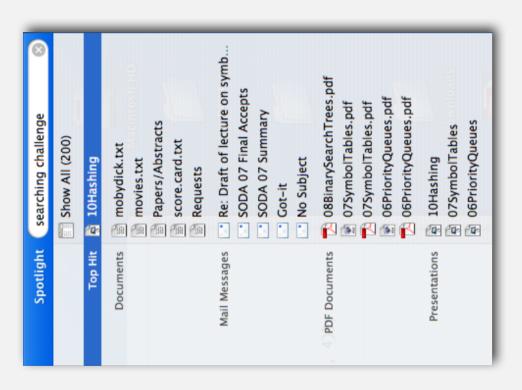
Sparse vectors

Robert Sedgewick | Kevin Wayne

Algorithms

File indexing

Goal. Index a PC (or the web).



File indexing

Goal. Given a list of files specified, create an index so that you can efficiently find all files containing a given query string.

```
% 1s *.txt
aesop.txt magna.txt moby.txt
sawyer.txt tale.txt
% java FileIndex *.txt
freedom
magna.txt moby.txt tale.txt
whale
moby.txt
lamb
sawyer.txt aesop.txt
```

```
% 1s *.java
BlackList.java Concordance.java
BlackList.java ST.java
SET.java WhiteList.java
% java FileIndex *.java
import
FileIndex.java SET.java
Comparator
null
```

Solution. Key = query string; value = set of files containing that string.

File indexing

```
for each word in file,
                                                                                                                                                                                                         from command line
                                                                                                                                                                                                                                                                                                                                   corresponding set
                                                                                                                                                                                list of file names
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          process queries
                                                                                                                   symbol table
                                                                                                                                                                                                                                                                                                        add file to
                                                                                                                         ST<String, SET<File>> st = new ST<String, SET<File>>(); <-
                                                                                                                                                                                                                                                                                                                                                   st.put(key, new SET<File>());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        String query = StdIn.readString();
                                                                public static void main(String[] args)
                                                                                                                                                                                                                                                                                                  String key = in.readString();
if (!st.contains(key))
                                                                                                                                                                                               File file = new File(filename);
In in = new In(file);
                                                                                                                                                                                                                                                                                                                                                                            SET<File> set = st.get(key);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                StdOut.println(st.get(query));
                                                                                                                                                                        for (String filename : args)
                                                                                                                                                                                                                                                 while (!in.isEmpty())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                while (!StdIn.isEmpty())
                                                                                                                                                                                                                                                                                                                                                                                                     set.add(file);
       public class FileIndex
{
import java.io.File;
```

727

Book index

Goal. Index for an e-book.

	stack of int (intStack), 140	and linked lists, 92, 94-95
	symbol table (ST), 503	merging, 349-350
	text index (TI), 525	multidimensional, 117-118
	union-find (UF), 159	references, 86-87, 89
	Abstract in-place merging, 351-	sorting, 265-267, 273-276
	353	and strings, 119
ndex	Abstract operation, 10	two-dimensional, 117-118, 120-
7001	Access control state, 131	124
	Actual data, 31	vectors, 87
	Adapter class, 155-157	visualizations, 295
	Adaptive sort, 268	See also Index, array
	Address, 84-85	Array representation
TOTAL TOTAL TOTAL TOTAL	Adjacency list, 120-123	binary tree, 381
Abstract data type (AD1), 12/-	depth-first search, 251-256	FIFO queue, 168-169
173 abstract classes 163	Adjacency matrix, 120-122	linked lists, 110
abstract classes, 163	Ajtai, M., 464	polynomial ADT, 191-192
collections of isome 137,139	Algorithm, 4-6, 27-64	priority queue, 377-378, 403,
concentral of neiths, 137-137	abstract operations, 10, 31, 34-	406
J. C. Catally, 137-104	35	pushdown stack, 148-150
denned, 128	analysis of, 6	random queue, 170
duplicate tterms, 173-176	average-/worst-case perfor-	symbol table, 508, 511-512,
equivalence-relations, 159-162	mance, 35, 60-62	521
FIFO queues, 163-171	big-Oh notation, 44-47	Asymptotic expression, 45-46
hrst-class, 177-186	binary search, 56-59	Average deviation, 80-81
generic operations, 2/3	computational complexity 62-	Average-case performance, 35, 60-
index items, 177	64	61
insertiremove operations, 138-	efficiency, 6, 30, 32	AVL tree, 583
	empirical analysis 30.37 58	
modular programming, 155	exponential time 719	D 584 693 704
polynomial, 188-192	caponemiai-mie, 217	D tree, 304, 692-704
priority queues, 375-376	implementation, 28-30	external/internal pages, 693
pushdown stack, 138-156	logarithm function, 40-43	4-5-6-7-8 tree, 693-704
stubs, 135	mathematical analysis, 33-36,	Markov chain, 701
symbol table, 497-506	58	remove, 701-703
ADT interfaces	primary parameter, 36	searchfinsert, 697-701
array (myArray), 274	probabilistic, 331	select/sort, 701
complex number (Complex), 181	recurrences, 49-52, 57	Balanced tree, 238, 555-598
existence table (ET), 663	recursive, 198	B tree, 584
full priority queue (PQfull),	running time, 34-40	bottom-up, 576, 584-585
397	search, 53-56, 498	height-balanced, 583
indirect priority queue (PQ1),	steps in, 22-23	indexed sequential access, 690-
403	See also Randomized algorithm	692
itcm (myItem), 273, 498	Amortization approach, 557, 627	performance, 575-576, 581-582,
key (myKey), 498	Arithmetic operator, 177-179,	595-598
polynomial (Poly), 189	188, 191	randomized, 559-564
point (Point), 134	Array, 12, 83	red-black, 577-585
priority queue (PQ), 375	binary search, 57	skip lists, 587-594
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	dimension allocation 07	l 600 871

Concordance

Goal. Preprocess a text corpus to support concordance queries: given a word, find all occurrences with their immediate contexts.

```
of his most gracious *majesty* king george the third
                                                                                                                                                                                   their turnkeys and the *majesty* of the law fired me treason against the *majesty* of the people in
                                                                      tongues of the two *cities* that were blended in
% java Concordance tale.txt
                                                                                                                                                                                                                                                                                                                                                                                  no matches
                                                                                                                                                                                                                                                                                                                                         princeton
                                                                                                                                                    majesty
```

```
process queries
                                                                                                                                                                                                                                      read text and
                                                                                                                                                                                                                                                             build index
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                concordances
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     and print
                                                                                                                                                                                ST<String, SET<Integer>> st = new ST<String, SET<Integer>>();
for (int i = 0; i < words.length; i++)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int k : set)
   // print words[k-4] to words[k+4]
                                                                                                                                                       String[] words = in.readAllStrings();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              String query = StdIn.readString();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SET<Integer> set = st.get(query);
                                                                                                                                                                                                                                                                                                                             st.put(s, new SET<Integer>());
                                                                  public static void main(String[] args)
                                                                                                                                                                                                                                                                                                                                                         SET<Integer> set = st.get(s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while (!StdIn.isEmpty())
                                                                                                                           In in = new In(args[0]);
                                                                                                                                                                                                                                                                    String s = words[i];
                                                                                                                                                                                                                                                                                                 if (!st.contains(s))
public class Concordance
                                                                                                                                                                                                                                                                                                                                                                                      set.add(i);
```

sets

dictionary clientsindexing clients

Sparse vectors

Robert Sedgewick | Kevin Wayne

Algorithms

sers

dictionary clients
 indexing clients

sparse vectors

Robert Sedgewick | Kevin Wayne

Algorithms

Matrix-vector multiplication (standard implementation)

```
      a[][]
      x[]
      b[]

      0 .90 0 0 0
      .05
      .036

      0 0 .36 .36 .18
      .04
      .297

      0 0 0 .90 0
      .36
      = .333

      .90 0 0 0 0
      .37
      .045

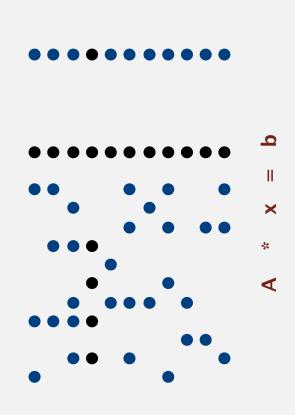
      .47 0 .47 0 0
      .19
      .19
```

```
(N2 running time)
                                                                                                                       nested loops
double[][] a = new double[N][N];
                                                                                                                                                                                                                for (int j = 0; j < N; j++)
                                                                                                                                     for (int i = 0; i < N; i++) ←
                                               double[] b = new double[N];
                     double[] x = new double[N];
                                                                                            // initialize a[][] and x[]
                                                                                                                                                                                                                                      sum += a[i][j]*x[j];
                                                                                                                                                                                                                                                              b[i] = sum;
                                                                                                                                                                                       sum = 0.0;
```

Sparse matrix-vector multiplication

Problem. Sparse matrix-vector multiplication.

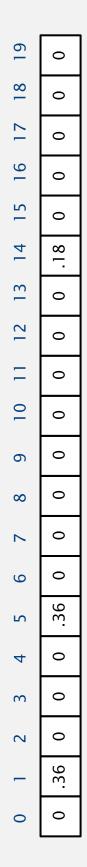
Assumptions. Matrix dimension is 10,000; average nonzeros per row ~ 10.



Vector representations

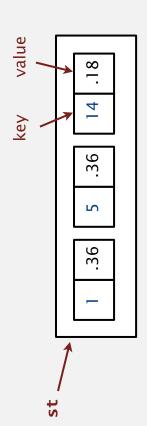
1d array (standard) representation.

- Constant time access to elements.
- Space proportional to N.



Symbol table representation.

- x Key = index, value = entry.
- Efficient iterator.
- Space proportional to number of nonzeros.



Sparse vector data type

```
HashST because order not important

    empty ST represents all 0s vector

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       time for sparse vectors
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              dot product is constant
                                                                                                                                                                                        a[i] = value
                                                                                                                                                                                                                                                                                                                           return a[i]
                                                                                                public SparseVector()
{  v = new HashST<Integer, Double>(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             sum += that[i]*this.get(i);
                                               private HashST<Integer, Double> v;
                                                                                                                                                                                                                                                                                                      if (!v.contains(i)) return 0.0;
                                                                                                                                                                                                                                                                                                                                                                                                            public Iterable<Integer> indices()
                                                                                                                                                                     public void put(int i, double x)
{ v.put(i, x); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              public double dot(double[] that)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       double sum = 0.0;
for (int i : indices())
                                                                                                                                                                                                                                                                                                                                   else return v.get(i);
                                                                                                                                                                                                                                       public double get(int i)
{
public class SparseVector
                                                                                                                                                                                                                                                                                                                                                                                                                                    { return v.keys(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return sum;
```

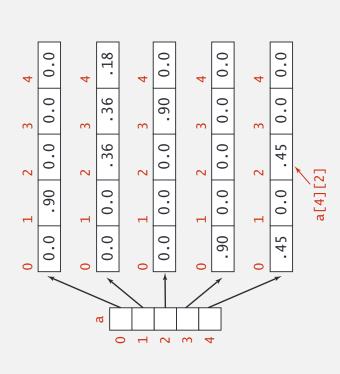
Matrix representations

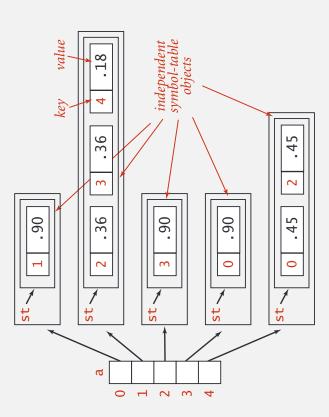
2D array (standard) matrix representation: Each row of matrix is an array.

- Constant time access to elements.
- Space proportional to N².

Sparse matrix representation: Each row of matrix is a sparse vector.

- Efficient access to elements.
- Space proportional to number of nonzeros (plus N).





Sparse matrix-vector multiplication

```
      a[][]
      x[]
      b[]

      0
      .90
      0
      .05
      .036

      0
      .36
      .36
      .18
      .04
      .297

      0
      0
      .36
      .36
      .36

      .90
      0
      0
      .36
      .36

      .90
      0
      0
      .37
      .045

      .47
      0
      .47
      0
      .1927
```

```
linear running time
                                                                                                                                                                    for sparse matrix
SparseVector[] a = new SparseVector[N];
double[] x = new double[N];
double[] b = new double[N];
                                                                                                                                           for (int i = 0; i < N; i++)
b[i] = a[i].dot(x);
                                                                                    ...
// Initialize a[] and x[]
```

sers

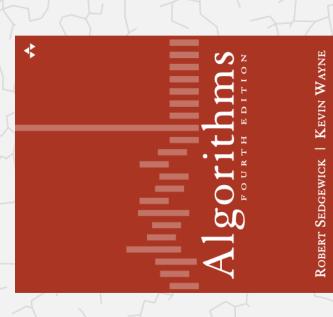
dictionary clients
 indexing clients

sparse vectors

Robert Sedgewick | Kevin Wayne

Algorithms

Algorithms



http://algs4.cs.princeton.edu

3.5 SYMBOL TABLE APPLICATIONS

- sets
- dictionary clients
- · indexing clients
- sparse vectors