

Gauss Jordan Elimination Method

Pseudo-Code:

1. Start
2. Read the order of the matrix 'n' and read the coefficients of the linear equations.
3. Do for i=0 to n-1
 - Do for j=0 to n-1
 - If (i equal to j) then,
 - Set pivot = a[i][i]
 - Do for k=0 to n-1
 - a[j][k] = a[i][k]/pivot;
 - End for k
 - Else
 - Set pivot = a[j][i]/a[i][i]
 - Do for k=0 to n-1
 - a[j][k] = a[j][k] - pivot*a[i][k];
 - End for k
 - Endif
- End for j
- End for i
4. Display Solution:
 - Do for i=0 to n-1
 - x[i] = a[i][n]
 - Display x[i]
 - End for i
5. Stop

Basic Equations:

$$3x + 2y + 1z = 10$$

$$2x + 3y + 2z = 14$$

$$1x + 2y + 3z = 14$$

$$x = 1, y = 2, z = 3$$

$$4x + 2y + 3z = 4$$

$$2x + 2y + z = 6$$

$$x + y + z = 0$$

$$x = 6, y = 1, z = -6$$

$$3x + 2y - 4z + 3u = 2$$

$$2x + 3y - 3z - u = 1$$

$$x + 2y + 3z - u = 10$$

$$2x - y + 2z + 3u = 7$$

$$x = 1, y = 2, z = 2, u = 1$$

Program Code in C

```

/*****
Welcome to GDB Online.
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*****/
#include<stdio.h>
int main(){
    int i, j, k, n=3; float c, pivot_el, x[3], a[3][4] = {{3,2,1,10},{2,3,2,14},{1,2,3,14}};

    for(i=0; i<n; i++){
        for(j=0; j<n; j++){
            if(i==j){
                pivot_el = a[i][i];
                for(k=0; k<n+1; k++){
                    printf("Before: a[%d][%d] = %f and pivot_el = %f",i,k,a[i][k],pivot_el);
                    a[j][k]=a[i][k]/pivot_el;
                    printf("\tAfter: a[%d][%d] = %f\n",i,k,a[i][k]);
                }
                printf("\n");
            }else{
                pivot_el=a[j][i]/a[i][i];
                for(k=0; k<n+1; k++){
                    a[j][k]=a[j][k]-pivot_el*a[i][k];
                }
            }
        }
    }

    // Final Matrix
    printf("The Final Matrix is:\n");
    for(i=0; i<n; i++){
        for(j=0; j<n+1; j++){
            printf("%f\t",a[i][j]);
        }
        printf("\n");
    }

    printf("\n\nThe solution is:\n");
    for(i=0; i<n; i++){
        x[i]=a[i][n];
        printf("x%d=%f\n",i,x[i]);
    }
    return(0);
}

```

Output

Before: $a[0][0] = 3.000000$ and $\text{pivot_el} = 3.000000$ After: $a[0][0] = 1.000000$
Before: $a[0][1] = 2.000000$ and $\text{pivot_el} = 3.000000$ After: $a[0][1] = 0.666667$
Before: $a[0][2] = 1.000000$ and $\text{pivot_el} = 3.000000$ After: $a[0][2] = 0.333333$
Before: $a[0][3] = 10.000000$ and $\text{pivot_el} = 3.000000$ After: $a[0][3] = 3.333333$

Before: $a[1][0] = 0.000000$ and $\text{pivot_el} = 1.666667$ After: $a[1][0] = 0.000000$
Before: $a[1][1] = 1.666667$ and $\text{pivot_el} = 1.666667$ After: $a[1][1] = 1.000000$
Before: $a[1][2] = 1.333333$ and $\text{pivot_el} = 1.666667$ After: $a[1][2] = 0.800000$
Before: $a[1][3] = 7.333333$ and $\text{pivot_el} = 1.666667$ After: $a[1][3] = 4.400000$

Before: $a[2][0] = 0.000000$ and $\text{pivot_el} = 1.600000$ After: $a[2][0] = 0.000000$
Before: $a[2][1] = 0.000000$ and $\text{pivot_el} = 1.600000$ After: $a[2][1] = 0.000000$
Before: $a[2][2] = 1.600000$ and $\text{pivot_el} = 1.600000$ After: $a[2][2] = 1.000000$
Before: $a[2][3] = 4.800001$ and $\text{pivot_el} = 1.600000$ After: $a[2][3] = 3.000000$

The Final Matrix is:

| | | | |
|----------|----------|----------|----------|
| 1.000000 | 0.000000 | 0.000000 | 1.000000 |
| 0.000000 | 1.000000 | 0.000000 | 2.000000 |
| 0.000000 | 0.000000 | 1.000000 | 3.000000 |

The solution is:

$x_0 = 1.000000$
 $x_1 = 2.000000$
 $x_2 = 3.000000$