Assignment 2

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Exercise 1

a)

To investigate whether tree type influences total wood volume, we can perform a one-way ANOVA.

```
tree_df$type <- as.factor(tree_df$type)
tree_type_lm <- lm(volume~type, data=tree_df)
anova(tree_type_lm)</pre>
```

With p > 0.05, we can conclude that type does not have a significant effect on volume. Because the factor type has two levels, we can apply an unpaired two sample t-test.

```
mask <- tree_df$type == "beech"
t.test(tree_df$volume[mask], tree_df$volume[!mask])</pre>
```

Again we see that *type* is not significant. This supports the result from the ANOVA test. The estimated volume is 30.2 for Beech trees and 35.2 for Oak trees.

b)

To investigate this claim, we create two models, each including all three explanatory variables (type,

diameter and height). In the first model, we also include the pairwise interaction between type and diameter.

```
tree_type_d_lm <- lm(volume~height+type*diameter, data=tree_df)</pre>
anova(tree_type_d_lm)
## Analysis of Variance Table
##
## Response: volume
##
                 Df Sum Sq Mean Sq F value Pr(>F)
                       2188
                               2188 206.21 < 2e-16 ***
## height
                  1
                                      40.65 4.2e-08 ***
## type
                  1
                       431
                                431
## diameter
                  1
                       8577
                               8577
                                     808.49 < 2e-16 ***
## type:diameter
                 1
                          6
                                  6
                                       0.52
                                                0.47
## Residuals
                 54
                                 11
                       573
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
In the second model, we include the pairwise interaction between type and height.
tree_type_h_lm <- lm(volume~diameter+type*height, data=tree_df)</pre>
anova(tree_type_h_lm)
## Analysis of Variance Table
##
## Response: volume
##
               Df Sum Sq Mean Sq F value Pr(>F)
                1 10827
                            10827 1045.97 < 2e-16 ***
## diameter
                                            0.041 *
## type
                1
                       45
                               45
                                     4.37
## height
                                    31.32 7.5e-07 ***
                1
                     324
                              324
## type:height 1
                               19
                                     1.88
                                            0.176
                       19
## Residuals
               54
                      559
                               10
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

We see that both pairwise interactions are not significant. Therefore, we can conclude that both height and diameter have the same influence on volume regardless of type.

c)

In (b), we saw that the interactions of *height* and *diameter* with *type* were not significant, and so we will investigate a purely additive model (assuming no interactions).

```
tree_add_all_lm <- lm(volume~diameter+height+type, data=tree_df)
drop1(tree_add_all_lm, test= "F")

## Single term deletions
##

## Model:
## volume ~ diameter + height + type
## Df Sum of Sq RSS AIC F value Pr(>F)
## <none>

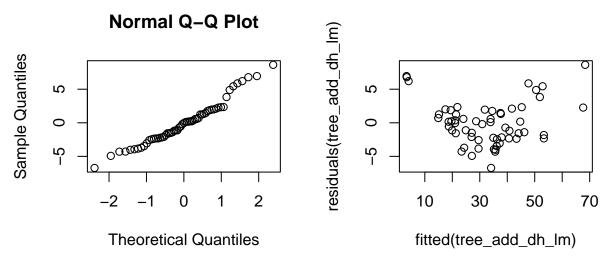
578 143
```

```
815.61 < 2e-16 ***
## diameter
             1
                    8577 9155 304
## height
             1
                     324
                          903 167
                                    30.82 8.4e-07 ***
             1
                      23
                          602 143
                                     2.21
                                             0.14
## type
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

We see that the effect of type is not significant in the additive model. Therefore we will investigate

```
an additive model that excludes type.
tree_add_dh_lm <- lm(volume~diameter+height, data=tree_df)</pre>
anova(tree_add_dh_lm)
## Analysis of Variance Table
##
## Response: volume
##
             Df Sum Sq Mean Sq F value Pr(>F)
## diameter
                 10827
                         10827
                                1007.8 < 2e-16 ***
## height
              1
                   346
                           346
                                   32.2 5.1e-07 ***
## Residuals 56
                   602
                            11
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
summary(tree_add_dh_lm)
##
## Call:
## lm(formula = volume ~ diameter + height, data = tree_df)
##
## Residuals:
##
      Min
              1Q Median
                            3Q
                                   Max
## -6.724 -2.278 -0.034 1.820
                                8.629
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -64.3697
                                    -11.58 < 2e-16 ***
                            5.5577
## diameter
                 4.6325
                            0.1602
                                      28.92 < 2e-16 ***
## height
                 0.4289
                            0.0755
                                       5.68 5.1e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.28 on 56 degrees of freedom
## Multiple R-squared: 0.949, Adjusted R-squared: 0.947
## F-statistic: 520 on 2 and 56 DF, p-value: <2e-16
```

This model has a high R-squared value while using fewer variables, all of which are significant. Since simpler models are generally preferred, this is our model of choice to make predictions. As a final test, we need to check this model's assumptions to ensure that the conclusions we draw from it are valid:



While these plots are not perfect, we believe the model assumptions to be valid.

Therefore, the effects of type, diameter and height can be summarized as follows:

- The tree type does not affect volume significantly.
- Looking at the coefficients, we see that increasing both height and diameter result in an increase in volume, with diameter having a bigger impact (with a gradient of 4.63 compared to *height's* 0.43). This makes sense given that we know volume is proportional to the square of the diameter.

To predict the volume for a tree with the overall average diameter and height, we can use the following linear regression model:

```
volume = -64.37 + 4.63 * diameter + 0.43 * height
```

```
mean_d <- mean(tree_df$diameter)
mean_h <- mean(tree_df$height)
means <- data.frame(diameter=c(mean_d), height=c(mean_h))

predict(tree_add_dh_lm, means, interval = "confidence")

## fit lwr upr
## 1 32.6 31.7 33.4</pre>
```

Therefore we expect the volume for such a tree to be 32.6, with a 95% CI of [31.7, 33.4].

d)

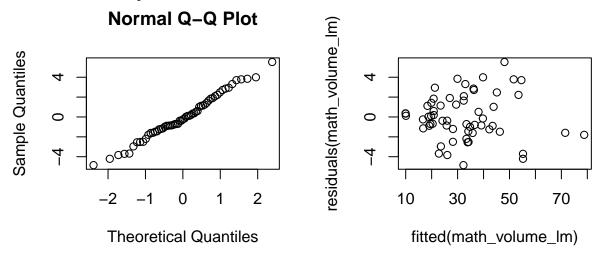
Assuming that a tree is roughly cylindrical, we expect that *volume* would be proportional to the *height* multiplied by the square of *diameter*. We perform this transformation and add it as a new column in the data frame. We could apply the true transformation, $V = h \times \pi (d/2)^2$, but this would just add unnecessary constants which would already be captured in the regression coefficients. We also will not include *type* because it was not significant.

```
tree_df$math_volume <- tree_df$height * tree_df$diameter^2
math_volume_lm <- lm(volume~math_volume, data=tree_df)
anova(math_volume_lm)</pre>
```

```
## Analysis of Variance Table
##
##
  Response: volume
##
               Df Sum Sq Mean Sq F value Pr(>F)
## math volume
                   11477
                            11477
                                     2201 <2e-16 ***
  Residuals
               57
                     297
                                5
##
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
summary(math_volume_lm)
##
## Call:
  lm(formula = volume ~ math_volume, data = tree_df)
##
## Residuals:
##
      Min
              1Q Median
                             3Q
                                   Max
  -4.846 -1.343 -0.245
                                 5.532
                         1.533
##
   Coefficients:
##
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.79e-01
                            7.63e-01
                                        -0.5
                                                  0.62
## math_volume 2.14e-03
                            4.57e-05
                                        46.9
                                                <2e-16 ***
##
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.28 on 57 degrees of freedom
## Multiple R-squared: 0.975, Adjusted R-squared: 0.974
```

F-statistic: 2.2e+03 on 1 and 57 DF, p-value: <2e-16

We see that this transformation does indeed produce an explanatory value with a significant effect. We also see that the R-squared (0.975) and adjusted R-squared (0.974) values are higher than that of the model chosen in (c) (tree_add_dh_lm), indicating that it better explains the data. Finally, we check the assumptions of this model.

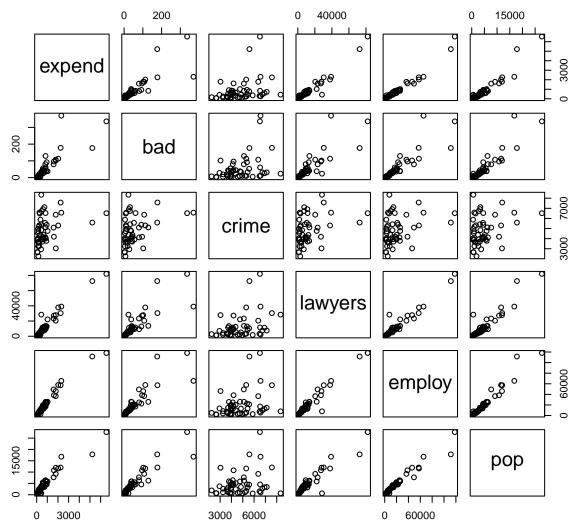


These plots are acceptable, meaning we can accept the model assumptions.

Exercise 2

a)

To investigate the interactions between all the variables of interest, we can plot the pairwise scatter plots for all their combinations:



We see that *expend*, our response variable, appears to have a positive correlation with all the explanatory variables except for *crime*. There appear to be several outliers at the high end of the data which could skew the model. We can also see that collinearity exists between the explanatory variables *bad*, *lawyers*, *employ* and *pop*. This is a problem since the redundant information will make the regression coefficients difficult to estimate.

We can use Cook's distance to find the influence points (a distance greater than 1 indicates an outlier)

```
crime_lm <- lm(expend~bad+crime+lawyers+employ+pop, data=crime_df)
cooks.distance(crime_lm)[cooks.distance(crime_lm) > 1]
```

5 8 35 44 ## 4.91 3.51 1.09 2.70 We can see that indices of 5, 8, 35 and 44 are outliers, which we can remove:

```
crime_df_upd <- crime_df[-c(5,8,35,44),]</pre>
```

To further investigate collinearity, we can examine the correlations between all the explanatory variables, which confirms strong correlations between bad, lawyers, employ and pop.

```
round(cor(crime_df[, c(exp_vars)]), 2)
```

```
##
            bad crime lawyers employ pop
                                 0.87 0.92
## bad
           1.00
                 0.37
                          0.83
                 1.00
                          0.38
## crime
           0.37
                                 0.31 0.28
## lawyers 0.83
                0.38
                          1.00
                                 0.97 0.93
## employ
           0.87
                 0.31
                          0.97
                                 1.00 0.97
                          0.93
                                 0.97 1.00
## pop
           0.92 0.28
```

We can also use the VIF to see which variables are collinear (VIF > 5 is cause for concern).

```
vif(lm(expend~bad+crime+lawyers+employ+pop, data=crime_df))
```

```
## bad crime lawyers employ pop
## 8.36 1.49 16.97 33.59 32.94
```

This further confirms that collinearity exists for the variables bad, lawyers, employ and pop.

From this point on, we will proceed without the influence points.

b)

The step-up process was carried out. The variables added in order were *employ*, *crime* and *pop*, after which no further added variables had significant p-values. Hence the final model is as follows:

```
step_up_lm <- lm(expend~employ+crime+pop, data=crime_df_upd)
summary(step_up_lm)</pre>
```

```
##
## Call:
## lm(formula = expend ~ employ + crime + pop, data = crime_df_upd)
##
## Residuals:
##
       Min
                10
                    Median
                                 30
                                        Max
## -179.99 -49.64
                       0.48
                              51.19
                                     266.63
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.47e+02
                            5.47e+01
                                       -4.52
                                              4.8e-05 ***
## employ
                2.09e-02
                            3.95e-03
                                        5.30
                                              3.7e-06 ***
## crime
                5.43e-02
                            1.13e-02
                                        4.82
                                              1.8e-05 ***
                7.14e-02
                            1.79e-02
                                        4.00
                                              0.00025 ***
## pop
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 91.4 on 43 degrees of freedom
```

```
## Multiple R-squared: 0.974, Adjusted R-squared: 0.973
## F-statistic: 547 on 3 and 43 DF, p-value: <2e-16</pre>
```

Final model: expend = -247 + 0.0209*employ + 0.0543*crime + 0.0714*pop \pm error, with $R^2 = 0.974$. Using VIF we can again check the model for collinearity.

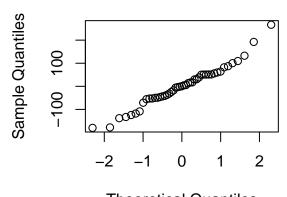
```
vif(step_up_lm)
```

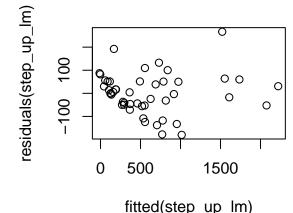
```
## employ crime pop
## 18.08 1.14 17.51
```

We see that the step-up method naturally removes collinearity and produced a better model than was arrived upon using VIF in (a), which had an R-squared value of 0.957. But the VIF gives values greater than 5? Surely we can't say this?

Finally, we check the model assumptions, which can be accepted based on the following plots:

Normal Q-Q Plot





Theoretical Quantiles

Using the step-up model found in (b), the 95% prediction interval for *expend* is given by:

```
new_data <- data.frame(bad=50, crime=5000, lawyers=5000, employ=5000, pop=5000)
predict(step_up_lm, new_data, interval="prediction", level=0.95)</pre>
```

```
## fit lwr upr
## 1 486 258 713
```

We cannot improve this interval since we have already removed the influence points from the data.

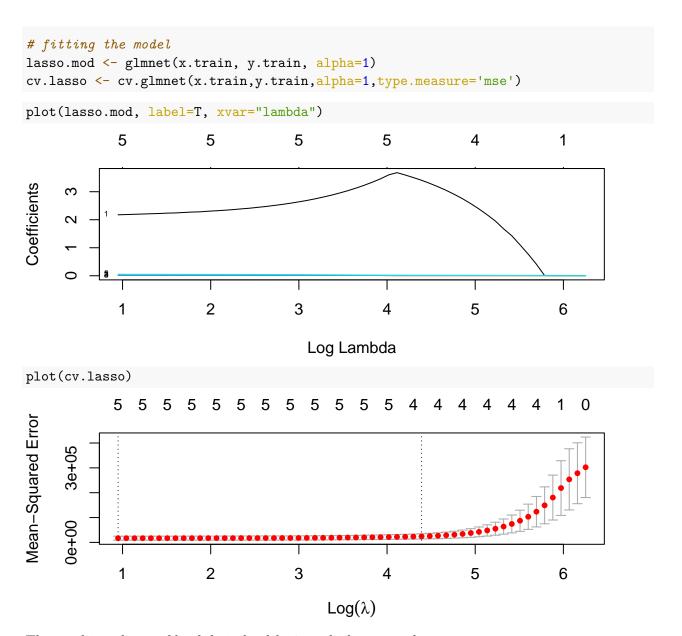
d)

c)

We can apply the LASSO method as follows:

```
x <- as.matrix(crime_df_upd[, exp_vars])
y <- as.matrix(crime_df_upd[, c(response)])

# train-test splitting
train <- (sample(1:nrow(x), 0.67*nrow(x))) # train by using 2/3 of the data
x.train <- x[train,]; y.train <- y[train]
x.test <- x[-train,]; y.test <- y[-train]</pre>
```



The resulting choice of lambda is *lambda.1se*, which is given by:

```
(lambda.1se <- cv.lasso$lambda.1se)
```

[1] 80.8

We can evaluate the resulting model by examining the Mean Squared Error (MSE) on the test set.

```
y.pred <- predict(lasso.mod, s=lambda.1se, newx=x.test)
mse.lasso <- mean((y.test - y.pred)^2); mse.lasso</pre>
```

[1] 15283

To compare this to the step-up model in (b), we can find the MSE for this model on the same test set. Isn't this unfair because the step up model was trained on the entire data set? Do we need to perform step up using only the training dataset? Or maybe we can just point this out but not

actually do it?

```
new_data <- data.frame(x.test)
y.pred <- predict(step_up_lm, new_data, interval="confidence", level=0.95)
mse.step_up <- mean((y.test - y.pred)^2); mse.step_up</pre>
```

```
## [1] 7130
```

We see that the step-up model outperforms the LASSO model, producing a smaller MSE. This could be because LASSO is better suited to situations with many more explanatory variables. Or because the step-model used the entire data set?

Exercise 3

a)

Studying the Data

We can start by looking at the summary data for each column:

```
titanic_df$PClass <- as.factor(titanic_df$PClass)
titanic_df$Sex <- as.factor(titanic_df$Sex)
summary(titanic_df)</pre>
```

##	Name	PClass	Age	Sex	Survived
##	Length:1313	1st:322	Min. : 0	female:462	Min. :0.000
##	Class :character	2nd:280	1st Qu.:21	male :851	1st Qu.:0.000
##	Mode :character	3rd:711	Median :28		Median:0.000
##			Mean :30		Mean :0.343
##			3rd Qu.:39		3rd Qu.:1.000
##			Max. :71		Max. :1.000
##			NA's :557		

We see that there were more people in 3rd class than in 1st and 2nd combined. Half the people were between the ages 21 and 39, with an average of 30 years old. Males made up 65% of the passengers, and 34% of all the passengers survived.

We can also examine how the sexes were distributed over the classes:

```
tot_comb <- xtabs(~PClass+Sex, data=titanic_df)
tot_comb</pre>
```

```
## Sex
## PClass female male
## 1st 143 179
## 2nd 107 173
## 3rd 212 499
```

As expected, there are more males in each category, with the biggest difference in 3rd class.

We can examine the same distribution in terms of percentage of people who survived for each combination:

```
tot_comb.surv <- xtabs(Survived~PClass+Sex, data=titanic_df)
round(tot_comb.surv/tot_comb, 2)</pre>
```

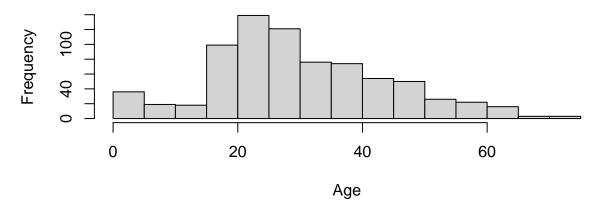
```
## Sex
## PClass female male
## 1st 0.94 0.33
## 2nd 0.88 0.14
## 3rd 0.38 0.12
```

It appears that the survival rate increases from 3rd to 1st class, and is much higher for females in all three cases, although this margin is less pronounced for 3rd class.

Finally, we can plot the distribution of ages:

```
hist(titanic_df$Age, xlab="Age", main="Age Distribution of Passengers")
```

Age Distribution of Passengers



We can see that the bulk of the ages are grouped around 25, with exponentially fewer people for older groupings.

Fitting the Model

##

First, we will removing rows with missing ages:

Survived ~ Age + PClass + Sex

Df Deviance AIC

```
titanic_df_upd <- na.omit(titanic_df)</pre>
```

Next, we can fit a logistic regression model and test it as follows:

```
titanic_df_upd$PClass <- as.factor(titanic_df_upd$PClass)
titanic_df_upd$Sex <- as.factor(titanic_df_upd$Sex)
base_lm <- glm(Survived ~ Age+PClass+Sex, data = titanic_df_upd, family = binomial)
drop1(base_lm, test = "Chisq")

## Single term deletions
##
## Model:</pre>
```

LRT Pr(>Chi)

```
695 705
## <none>
## Age
           1
                   724 732
                            28.5
                                  9.6e-08 ***
## PClass
           2
                   796 802 100.4
                                  < 2e-16 ***
           1
## Sex
                   910 918 214.8
                                  < 2e-16 ***
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

We see that all three variables have a significant effect on the odds of survival. To further interpret the results, we can look at the model summary and its coefficients.

```
summary(base_lm)
```

```
##
## Call:
   glm(formula = Survived ~ Age + PClass + Sex, family = binomial,
##
       data = titanic df upd)
##
  Deviance Residuals:
##
##
      Min
               10
                  Median
                                3Q
                                       Max
## -2.723
           -0.707
                   -0.392
                             0.649
                                     2.529
##
##
  Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                3.75966
                            0.39757
                                       9.46
                                              < 2e-16 ***
## Age
               -0.03918
                            0.00762
                                       -5.14
                                              2.7e-07 ***
## PClass2nd
               -1.29196
                                      -4.97
                                              6.8e-07 ***
                            0.26008
## PClass3rd
               -2.52142
                            0.27666
                                      -9.11
                                              < 2e-16 ***
## Sexmale
               -2.63136
                            0.20151
                                     -13.06
                                              < 2e-16 ***
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 1025.57
                                on 755
                                         degrees of freedom
## Residual deviance:
                      695.14
                                on 751
                                        degrees of freedom
## AIC: 705.1
##
## Number of Fisher Scoring iterations: 5
```

Thus, the estimated odds is:

$$\hat{o}_k = \frac{P(\widehat{Y_k = 1})}{P(\widehat{Y_k = 0})} \approx e^{3.76 - 0.04 * Age_k - 1.29 * PClass2nd_k - 2.52 * PClass3rd_k - 2.63 * Sexmale_k}$$

We see that all the coefficients are negative. This means that increasing age, being male and moving down in class all lower a passenger's odds of survival. Moreover, the magnitude of the coefficients indicates how sensitive these odds are to each variable. From this we can infer that 3rd class has worse odds than 2nd class, and that being a male is the most influential factor in decreasing one's

odds of survival. While increasing age also lowers one's odds, it has the smallest effect compared to to the other two variables.

```
b)
```

```
Investigating the interaction between Age and PClass:
```

```
anova(glm(Survived ~ Age*PClass, data = titanic_df_upd, family = binomial), test="Chisq")
## Analysis of Deviance Table
##
## Model: binomial, link: logit
##
## Response: Survived
##
## Terms added sequentially (first to last)
##
##
##
              Df Deviance Resid. Df Resid. Dev Pr(>Chi)
                                            1026
## NULL
                                 755
               1
                       2.8
                                            1023
                                  754
                                                    0.091 .
## Age
               2
## PClass
                     112.8
                                  752
                                             910
                                                    <2e-16 ***
## Age:PClass
                       1.2
                                  750
                                             909
                                                     0.558
## ---
                    0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
We see that the interaction is not significant. Next, we investigating the interaction between Age
and Sex:
anova(glm(Survived ~ Age*Sex, data = titanic_df_upd, family = binomial), test="Chisq")
## Analysis of Deviance Table
##
## Model: binomial, link: logit
##
## Response: Survived
##
## Terms added sequentially (first to last)
##
##
##
           Df Deviance Resid. Df Resid. Dev Pr(>Chi)
## NULL
                              755
                                         1026
                    2.8
                              754
                                         1023
                                                 0.091 .
## Age
            1
                  227.1
                              753
                                          796
                                               < 2e-16 ***
## Sex
            1
                   25.0
                                              5.6e-07 ***
## Age:Sex
            1
                              752
                                          771
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

Here, the interaction is significant, and so we wish to include it in our model. *PClass* was significant by itself, so we include it in the final model as follows

««< INVESTIGATE VARIABLES USING anova(smaller model, bigger model) »»»

```
final_lm <- glm(Survived ~ PClass+Age*Sex, data = titanic_df_upd, family = binomial)
summary(final_lm, test="Chisq")
##
## Call:
## glm(formula = Survived ~ PClass + Age * Sex, family = binomial,
##
       data = titanic_df_upd)
##
## Deviance Residuals:
##
      Min
               1Q
                   Median
                                3Q
                                       Max
  -2.435
           -0.656
                   -0.353
                             0.696
                                     2.728
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
                                             3.0e-10 ***
## (Intercept)
                2.75656
                            0.43764
                                       6.30
## PClass2nd
                            0.28736
                                      -5.37
                                             7.8e-08 ***
               -1.54337
## PClass3rd
               -2.65398
                            0.29142
                                      -9.11
                                             < 2e-16 ***
## Age
                0.00244
                            0.01141
                                       0.21
                                                 0.83
                                                 0.25
## Sexmale
               -0.50819
                            0.44251
                                      -1.15
## Age:Sexmale -0.07559
                            0.01501
                                      -5.04
                                             4.7e-07 ***
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 1025.57
                                on 755
                                        degrees of freedom
## Residual deviance:
                       667.08
                                on 750
                                        degrees of freedom
## AIC: 679.1
## Number of Fisher Scoring iterations: 5
```

Comments on this result? Is it bad that Age and Sexmale are not significant? Maybe just significant as a whole and that's okay?

Using this model we can predict the estimate for the probability of survival for each combination of levels of the factors PClass and Sex for a person of Age 55:

```
newdata <- data.frame(Age=c(55, 55, 55, 55, 55, 55), PClass=c("1st", "1st", "2nd", "2nd", "3rd
predict(final_lm, newdata, type="response")
## 1 2 3 4 5 6</pre>
```

Again we see that being a women appears to be the dominant factor in increased survival, and that the probability of survival also decreases as you go down in class (from 1st to 3rd)

0.9474 0.1450 0.7937 0.0350 0.5590 0.0118

c)

We can predict the survival status of the individuals by looking at the fitted values produced by the model, which gives the probability of survival. We can then set a threshold of 0.5. We can predict that those with a probability lower than this did not survive, and those with a probability higher

than this did survive. To measure the quality of this prediction method, we can use tools such as a confusion matrix and log likelihood as quality measures.

d)

Survived vs Sex

For 2x2 tables we can obtain exact p-value using the Fisher test as follows:

```
fisher.test(x=titanic_df_upd$Survived, y=titanic_df_upd$Sex)
```

```
##
## Fisher's Exact Test for Count Data
##
## data: titanic_df_upd$Survived and titanic_df_upd$Sex
## p-value <2e-16
## alternative hypothesis: true odds ratio is not equal to 1
## 95 percent confidence interval:
## 0.0586 0.1215
## sample estimates:
## odds ratio
## 0.0848</pre>
```

Therefore Sex and Survived are not independent.

Survived vs PClass

Since we have three classes, we must use the Chi-squared test to investigate the effect of passenger class:

```
chisq.test(x=titanic_df_upd$Survived, y=titanic_df_upd$PClass)
```

```
##
## Pearson's Chi-squared test
##
## data: titanic_df_upd$Survived and titanic_df_upd$PClass
## X-squared = 76, df = 2, p-value <2e-16</pre>
```

Therefore *PClass* and *Survived* are not independent.

e)

No, the approach in (d) is not wrong. Rather there are advantages and disadvantages associated with both methods:

Logistic Regression

Advantages - Can handle a combination of continuous and categorical explanatory variables. Gives you detailed information about the role of explanatory variables since it tells you how the variable affects the response (sign of the coefficient), as well as how sensitive the response is to changes in the variable (magnitude of the coefficient).

Disadvantages - https://careerfoundry.com/en/blog/data-analytics/what-is-logistic-regression/???

vs

Contingency Table.

Advantages - Works for tables larger than 2x2. Works best for categorical explanatory variables. Disadvantages - Does not work for continuous variables. Does not provide an exact p-value, only an approximation. Only tells you whether dependence exists, not the nature of the dependence.

vs

Fisher

Advantages - Provides an exact p-value. Works best for categorical explanatory variables. Disadvantages - Does not work for continuous variables. Only works for 2x2. Only tells you whether dependence exists, not the nature of the dependence.

Exercise 4

Coefficients:

```
coups_df$pollib <- as.factor(coups_df$pollib)</pre>
a)
poison_glm <- glm(miltcoup ~ oligarchy + parties + pctvote + popn + size + numelec + numregim -
drop1(poison_glm, test= "Chisq")
## Single term deletions
##
## Model:
## miltcoup ~ oligarchy + parties + pctvote + popn + size + numelec +
       numregim + pollib
##
             Df Deviance AIC LRT Pr(>Chi)
##
                    28.2 113
## <none>
## oligarchy 1
                    32.4 115 4.10
                                     0.0428 *
## parties
              1
                    35.3 118 7.06
                                     0.0079 **
## pctvote
              1
                    30.6 113 2.32
                                     0.1275
## popn
                    30.6 113 2.35
              1
                                     0.1252
## size
              1
                    29.2 112 0.99
                                     0.3202
                                     0.6705
## numelec
              1
                    28.4 111 0.18
## numregim
                    29.1 112 0.81
                                     0.3681
              1
                                     0.0256 *
## pollib
                    35.6 116 7.33
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
summary(poison_glm)
##
## Call:
## glm(formula = miltcoup ~ oligarchy + parties + pctvote + popn +
##
       size + numelec + numregim + pollib, family = poisson, data = coups_df)
##
## Deviance Residuals:
##
      Min
               1Q Median
                                3Q
                                       Max
## -1.508 -0.953 -0.310
                            0.486
                                     1.646
##
```

```
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.233427
                                       -0.23
                            0.997611
                                               0.8150
## oligarchy
                0.072566
                            0.035346
                                        2.05
                                               0.0401 *
## parties
                                        2.80
                0.031221
                            0.011166
                                               0.0052 **
## pctvote
                0.015441
                            0.010103
                                        1.53
                                               0.1264
## popn
                0.010959
                            0.007149
                                        1.53
                                               0.1253
## size
               -0.000265
                            0.000269
                                       -0.99
                                               0.3244
## numelec
               -0.029619
                            0.069625
                                       -0.43
                                               0.6705
## numregim
                0.210943
                            0.233933
                                        0.90
                                               0.3672
## pollib1
               -1.103244
                            0.655811
                                       -1.68
                                               0.0925 .
                                               0.0125 *
## pollib2
               -1.690306
                            0.676650
                                       -2.50
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 65.945
                               on 35
                                      degrees of freedom
## Residual deviance: 28.249
                               on 26
                                      degrees of freedom
## AIC: 113.1
##
## Number of Fisher Scoring iterations: 5
```

Through Poisson regression, and its summary, we can find that the variables that are significant in predicting number of successful military coups are: oligarchy, pollib, and parties.

b)

The step down method was applied, removing the variables: numelec, size, pctvote, and popn, respectively. After which, all remaining variables were significant, resulting in the model:

```
final_plm <- glm(miltcoup ~ oligarchy + parties + pollib, data = coups_df, family = poisson)</pre>
summary(final_plm, test="Chisq")
##
## Call:
## glm(formula = miltcoup ~ oligarchy + parties + pollib, family = poisson,
##
       data = coups df)
##
## Deviance Residuals:
      Min
##
                10 Median
                                3Q
                                        Max
## -1.361 -1.041 -0.315
                                      1.754
                             0.615
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                 0.2080
                             0.4457
                                        0.47
                                                0.641
                                                5e-05 ***
## oligarchy
                 0.0915
                             0.0226
                                        4.05
## parties
                                        2.46
                 0.0224
                             0.0091
                                                0.014 *
## pollib1
                 -0.4954
                             0.4757
                                       -1.04
                                                0.298
## pollib2
                                      -2.42
                -1.1121
                             0.4595
                                                0.016 *
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 65.945 on 35
                                     degrees of freedom
## Residual deviance: 32.822 on 31 degrees of freedom
## AIC: 107.6
##
## Number of Fisher Scoring iterations: 5
In comparison with a) all the same variables are significant.
c)
coups_df$pollib <- as.factor(coups_df$pollib)</pre>
mean(coups_df$oligarchy); mean(coups_df$parties)
## [1] 5.22
## [1] 17.1
newdata <- data.frame(pollib=c("0", "1", "2"), oligarchy=c(5.22, 5.22), parties=c(17.1,
predict(final_plm, newdata, type="response")
##
       1
                   3
## 2.909 1.772 0.957
```

Our model predicts that there will be roughly 3 successful coups for pollib=0, roughly 2 successful coups for pollib=1, and 1 successful coup for pollib=2.