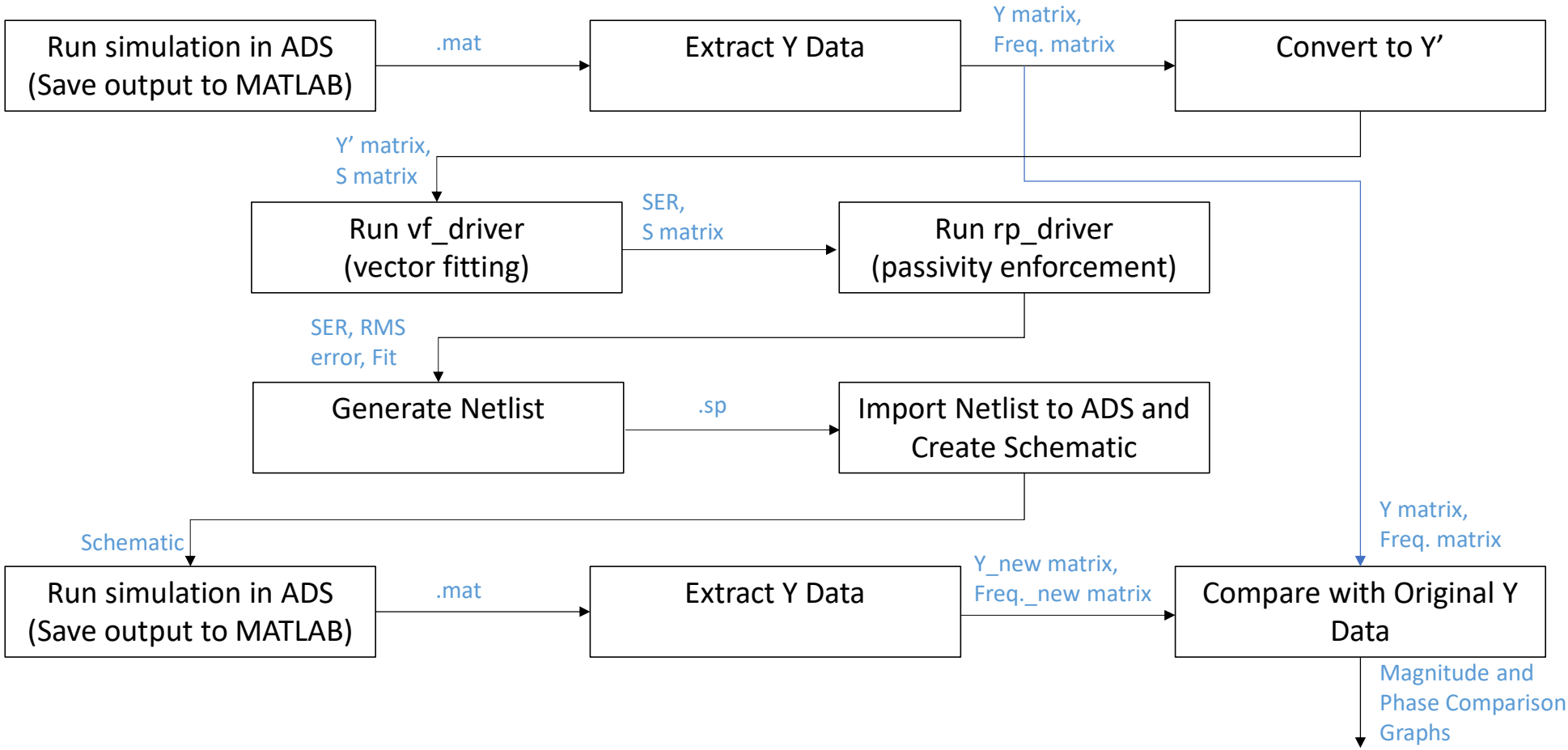
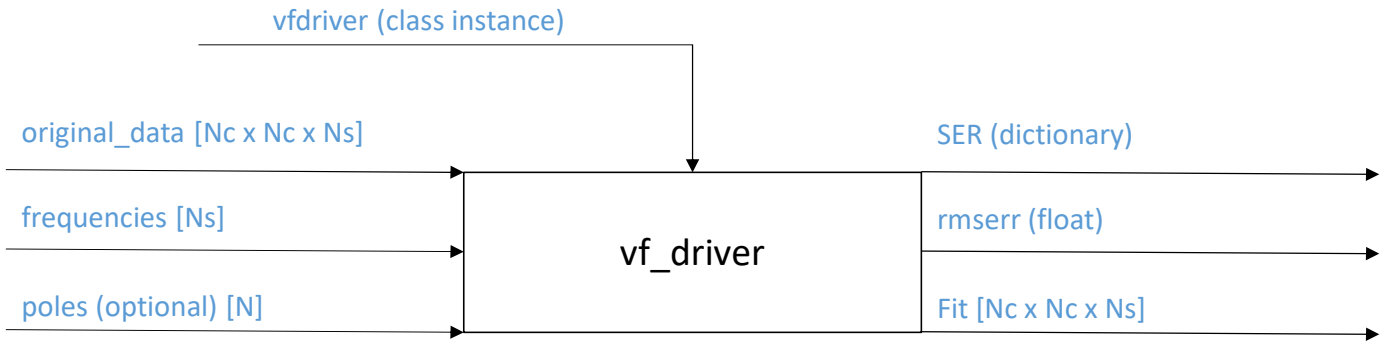
General Flow Chart



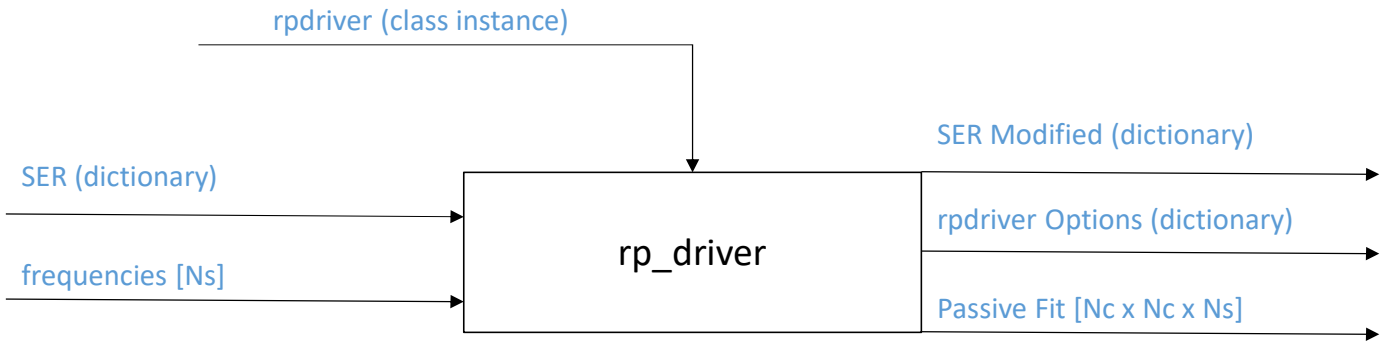
Inputs/Outputs to Python Programs



Nc	Number of Ports
Ns	Number of Freq. Data Points
N	Number of Poles

SER Element	Size
A	[(Nc * N) x (Nc * N)]
B	[(Nc * N) x Nc]
C	[Nc x (Nc * N)]
D	[Nc x Nc]
E	[Nc x Nc]
R	[Nc x Nc x N]
poles	[N]

Inputs/Outputs to Python Programs



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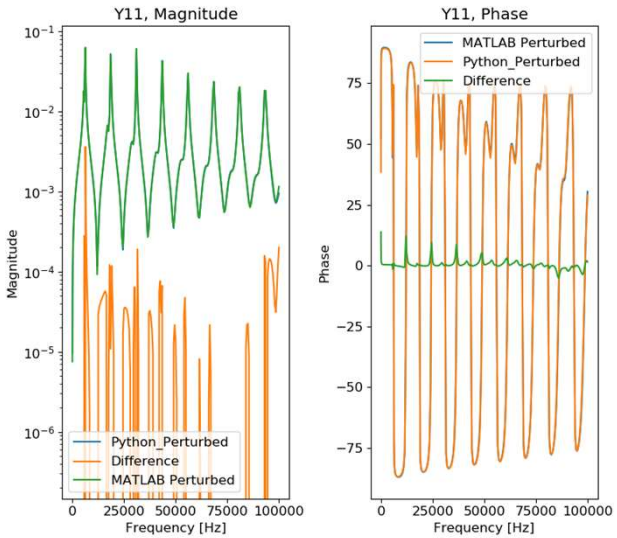
R	[Nc x Nc x N]
poles	[N]

3 Port Python/MATLAB Results

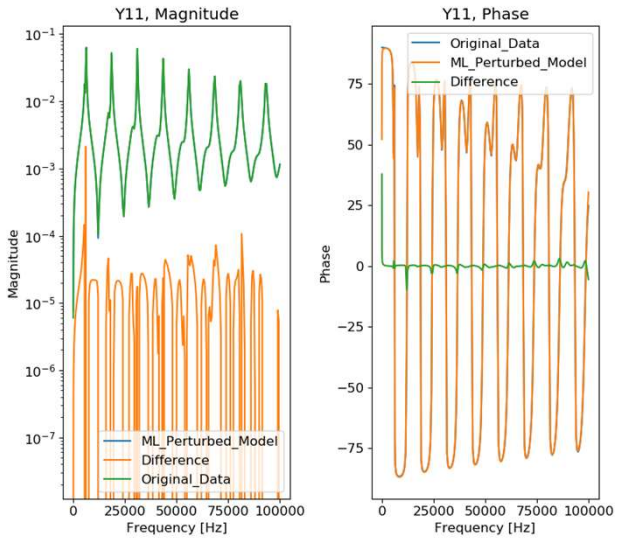
Element	RMS Error (Magnitude) – Python	RMS Error (Phase) - Python	RMS Error (Magnitude) – MATLAB	RMS Error (Phase) - MATLAB
Y11	5.91e-5	0.16	2.59e-4	0.11
Y12	6.64e-5	0.33	2.91e-4	0.23
Y13	7.25e-5	0.48	4.06e-4	0.44
Y21	6.64e-5	0.33	1.91e-4	0.23
Y22	6.28e-5	0.14	3.67e-4	0.21
Y23	6.64e-5	0.33	1.91e-4	0.23
Y31	7.25e-5	0.48	4.06e-4	0.44
Y32	6.64e-5	0.33	1.91e-4	0.23
Y33	5.91e-5	0.16	2.59e-4	0.11

3 Port Results

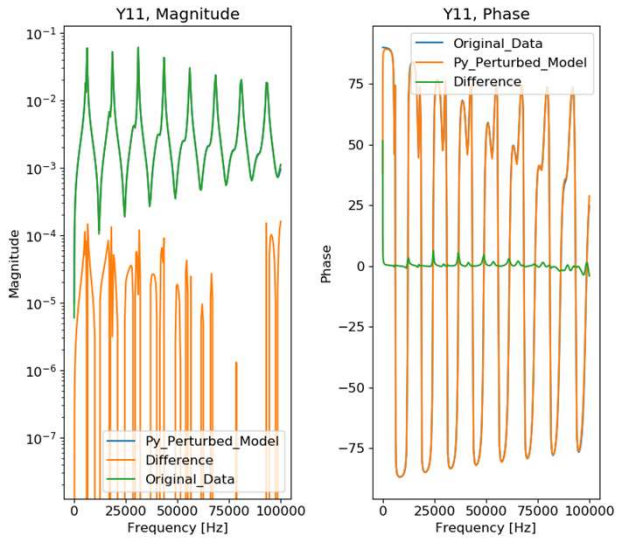
Python / MATLAB



MATLAB

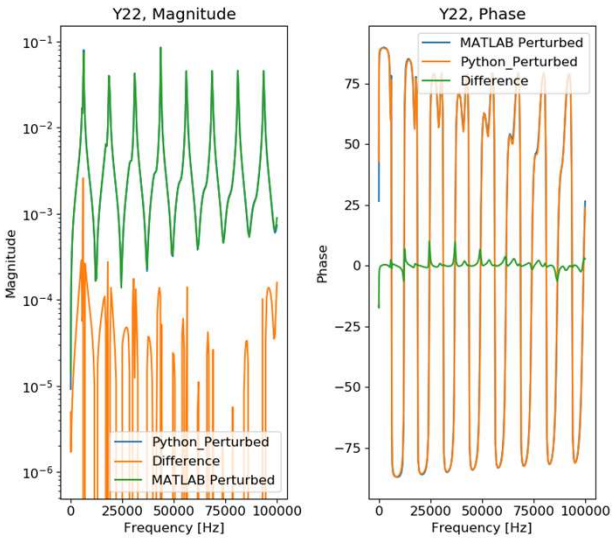


Python

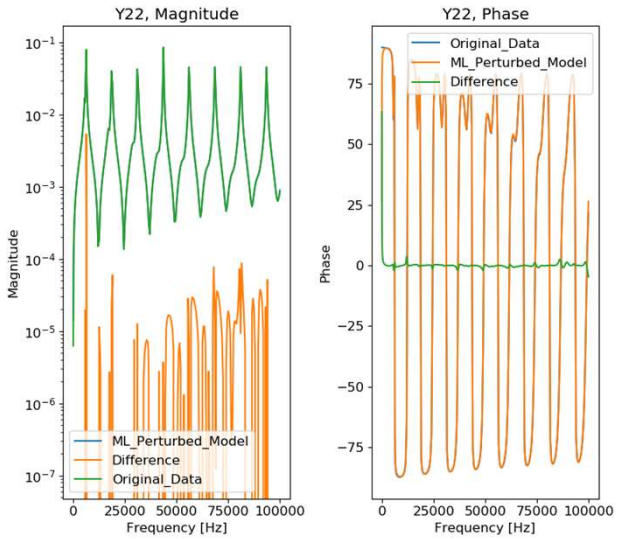


3 Port Results

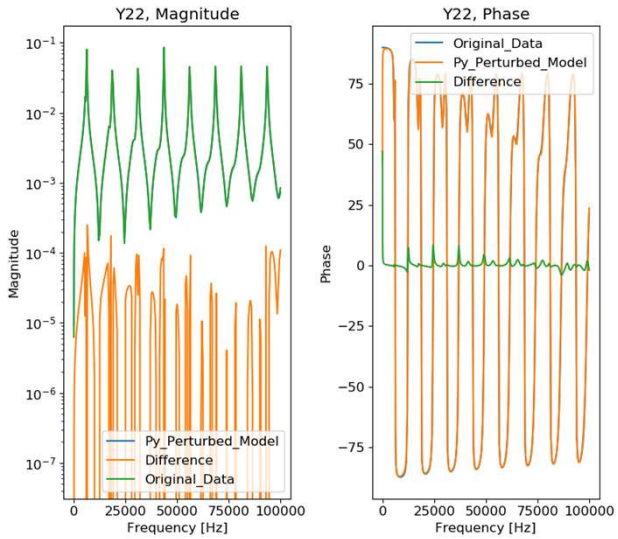
Python / MATLAB



MATLAB

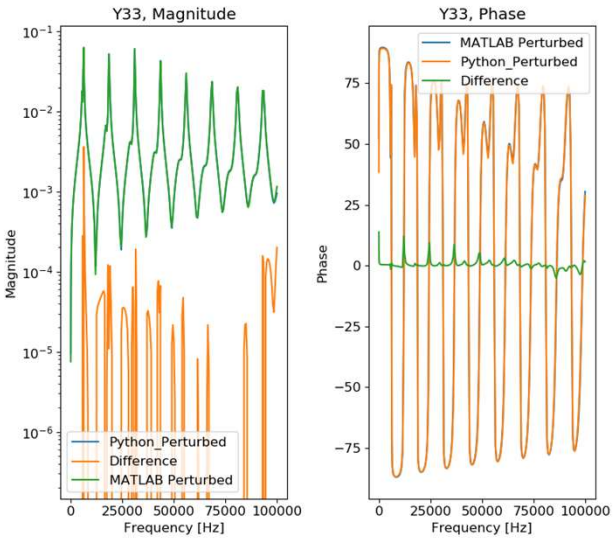


Python

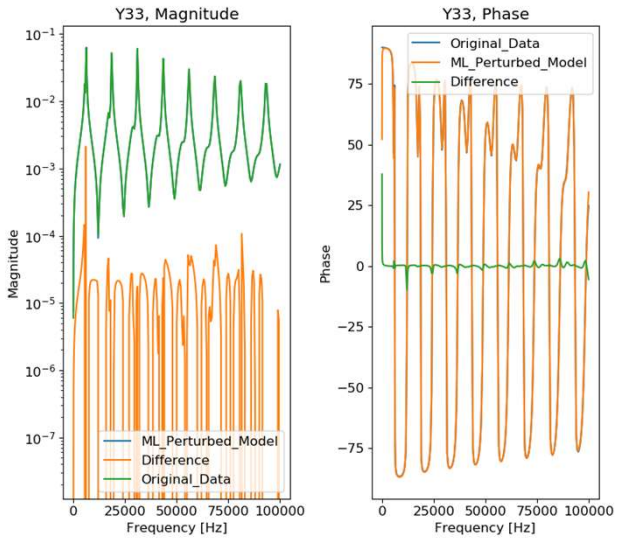


3 Port Results

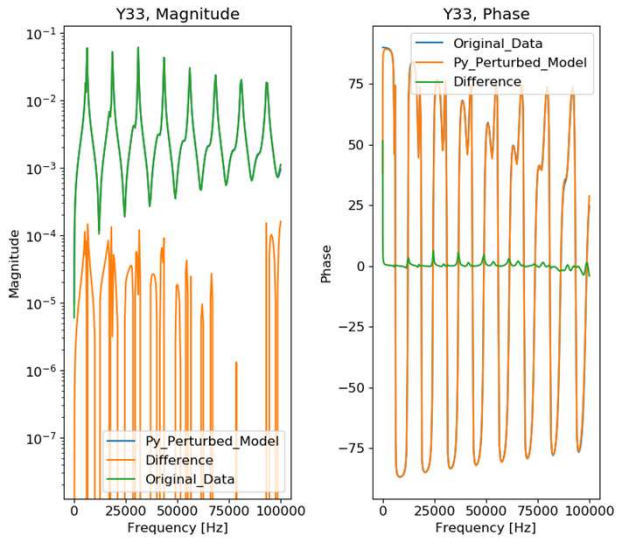
Python / MATLAB



MATLAB

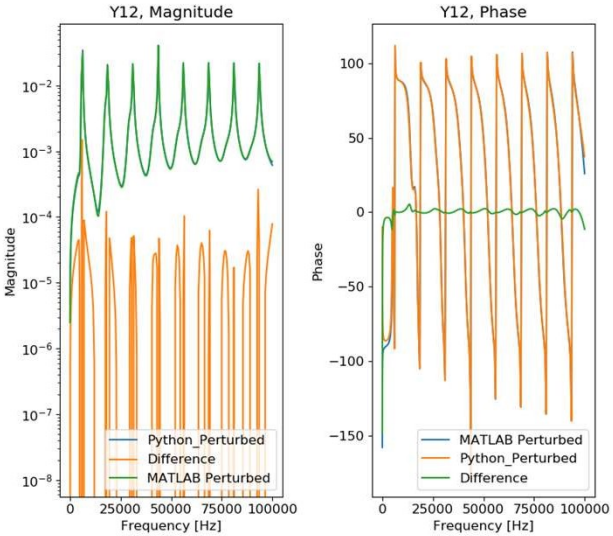


Python

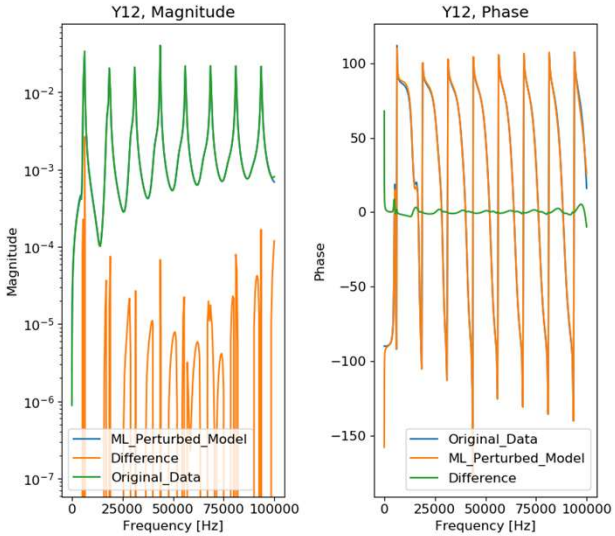


3 Port Results

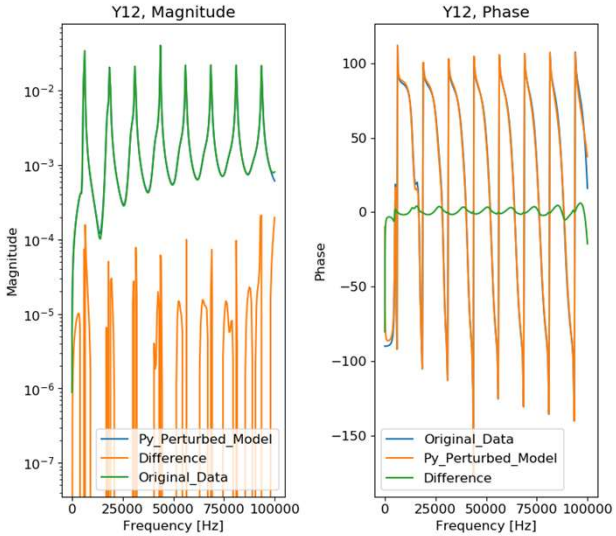
Python / MATLAB



MATLAB

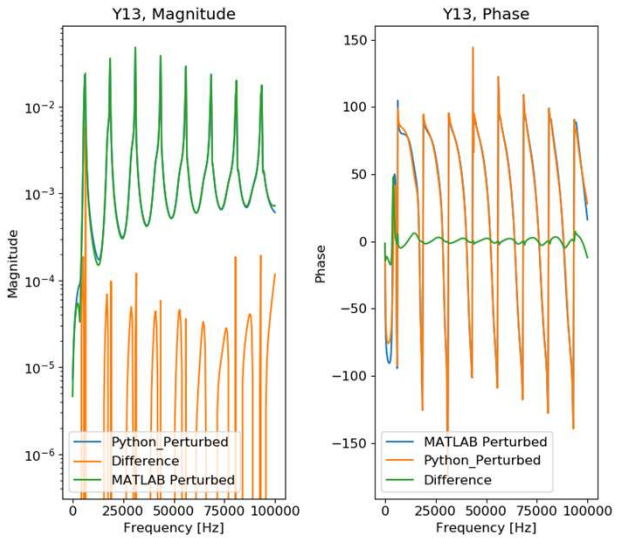


Python

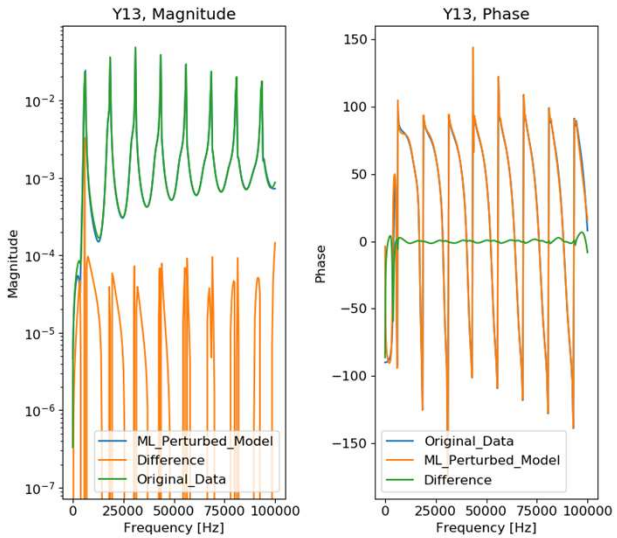


3 Port Results

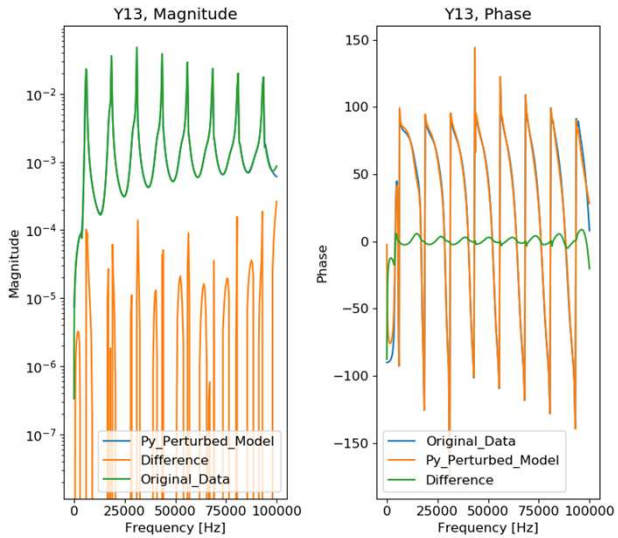
Python / MATLAB



MATLAB



Python



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