## Algorithm Miscellany

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## 1 Job Scheduling / Makespan problem

Given m machines and n jobs with workload  $p_1, ..., p_n$ , give a schedule that

min max{workload for a single machine}

This problem is NP hard. We can use a Greedy algorithm to achieve 4/3 approximation. If the number of distinct workload is restricted to k, there is a DP solution of  $O(n^{2k})$  which gives the exact solution to the corresponding decision problem : Can the m machines finish the job within T times. (Suppose the workload is the time it takes to complete the job for one machine.)

Suppose there are  $b_i$  jobs for workload  $p_i$ , and we have  $(b_1, ..., b_k)$  jobs in total. Let  $M(c_1, ..., c_k)$  denote the minimum number of machines needed to complete  $(c_1, ..., c_k)$  jobs within time T. Then it's easy to check whether  $M(c_1, ..., c_k) > 1$  and quitely clearly, M(0, ..., 0) = 0