

1.

Algorithm: merge(L1,L2)
Requires: two sorted lists L1 and L2
Returns: a merged and sorted list of L1 and L2
1: if isEmpty(L1)
2: return L2
3: elseif isEmpty(L2)
4: return L1
5: elseif value(L1)<value(L2)
6: return cons(value(L1),merge(tail(L1),L2))
7: else
8: return cons(value(L2),merge(L1,tail(L2)))
9: endif

Trace `merge([2,5,10,15],[3,6,7])`

backtracking

L1=[2,5,10,15] L2=[3,6,7]

Line 1,3 False. Line 5 True. `Line 6: return cons(2,merge([5,10,15],[3,6,7]))`

=[2,3,5,6,7,10,15]

L1=[5,10,15] L2=[3,6,7]

Line 1,3,5 False. `Line 8: return cons(3,merge([5,10,15],[6,7]))`

=[3,5,6,7,10,15]

L1=[5,10,15] L2=[6,7]

Line 1,3 False. Line 5 True. `Line 6: return cons(5,merge([10,15],[6,7]))`

=[5,6,7,10,15]

L1=[10,15] L2=[6,7]

Line 1,3,5 False. `Line 8: return cons(6,merge([10,15],[7]))`

=[6,7,10,15]

L1=[10,15] L2=[7]

Line 1,3,5 False. `Line 8: return cons(7,merge([10,15],[]))`

=[7,10,15]

L1=[10,15] L2=[]

Line 1 False. Line 3 True. `Line 4: return [10,15]`Note: steps in **blue colour** are the minimal elements you need to include in the tracing process.

Time complexity is $O(n)$. Because total number of comparisons of two lists' values is linearly related to the size of the merged list.

2. Refer to Lecture 6 slides .

In general, there are about $\log_2 n$ levels of splitting.

We will introduce two functions to round decimal numbers to integers.

Q3 and Q4 will be further explained in Seminar 6.

5. Demonstration with $L1=[24,26,22,29,66,11,20,27,21,23,25,28]$.

Pivots are highlighted on each partition step.

[22,11,20,21,23]	[24]	[26,29,66,27,25,28]	partition
[11,20,21] [22] [23]		[25] [26] [29,66,27,28]	partition
[11] [20,21]		[27,28][29][66]	partition
[20][21]		[27][28]	partition
[20,21]		[27,28]	merge
[11,20,21]		[27,28,29,66]	merge
[11,20,21,22,23]		[25,26,27,28,29,66]	merge
[11,20,21,22,23,24,25,26,27,28,29,66]			merge