Distance estimation in vehicle routing problems

An empirical approach using neural networks and ensemble learning

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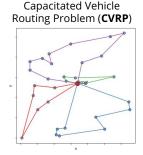
Agenda

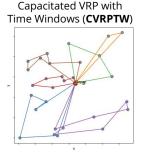
- 1 Vehicle Routing Problems (VRPs)
- Route Distance Estimation Relevance Literature review
- Methodology Research design Dataset Models
- 4 Results
- 5 Discussion

Vehicle Routing Problems (VRPs)

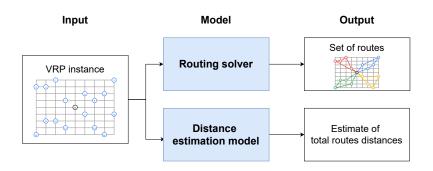
- Group of combinatorial optimization problems
- Problem description:
 - Given: 1. Set of customers, 2. Fleet of vehicles, 3. Various constraints
 - **Determine:** Feasible routes at minimum cost (typically total distance)
- Computationally expensive (NP-hard)

Traveling Salesman Problem (TSP)





Route Distance Estimation



Why is distance estimation relevant?

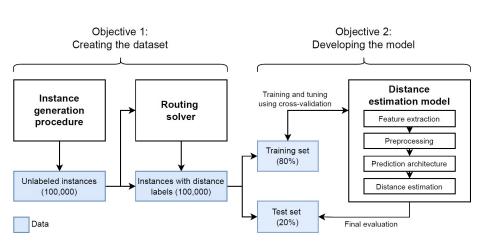
- Integrated routing problems (e.g. location routing)
- Combinatorial auctions
- Managerial decisions

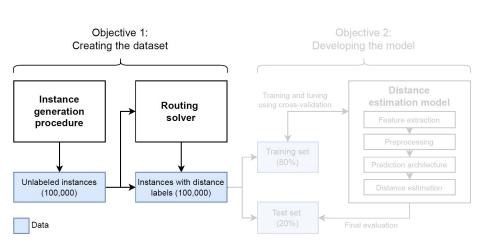
Literature Review

- Mostly linear regression with few predictors and strong assumptions about instance characteristics
- Many papers about the TSP, very few about the CVRPTW
- Current CVRPTW datasets are not well suited for distance estimation.
 - Only four public CVRPTW datasets in VRP-REP
 - Few instances, little variety in instance characteristics, old

Research objectives

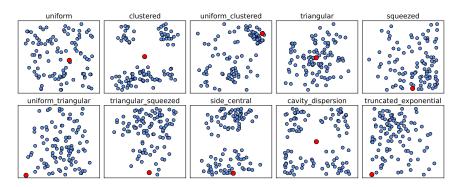
- A large CVRPTW dataset with instance characteristics from a wide variety of distributions
- New estimation models to predict distances more accurately than the linear approaches





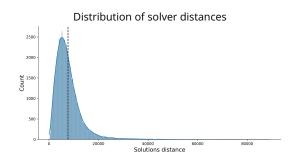
Instance Generation Procedure

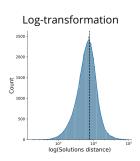
- A CVRPTW instance has 12 characteristics.
- Characteristics are sampled from 28 distributions.
- Examples:
 - The number of customers is uniform between 20 and 100.
 - Customer locations follow one of 10 distributions:

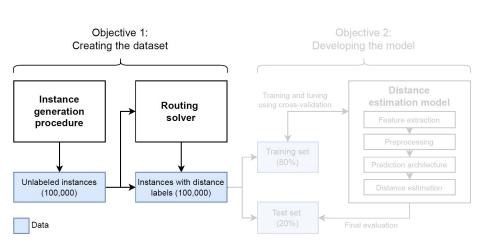


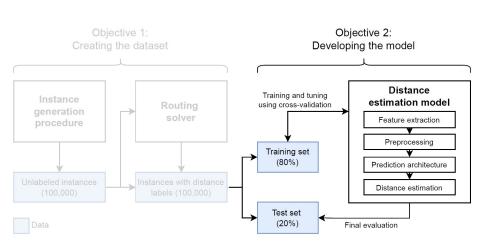
Routing Solver

- Meta-heuristics are most common in practice
- Implementation of 16 strategies using OR-Tools
 - Final solver: Path cheapest arc + Guided local search
 - 0.74% to optimal on benchmark by Solomon (1987)
- Full dataset solved on AWS c6g over 5000 hours (3min per instance)



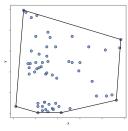






Feature Extraction

- Goal: Capture informative signal from routing instances
- Definition of 45 different features
- Examples:
 - Number of customers
 - Size of the service area
 - Distance from depot to customers
 - Demand coverage
 - Average length of time windows



Convex hull

Model Architectures

Baseline models

- Constant model
- Other variants
- · Greedy heuristic

Linear regression

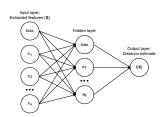
- Target transformation
- Feature selection
- Polynomial terms

Multilayer perceptron (MLP)

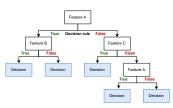
• Standardization $x' = \frac{x-\mu}{\sigma}$

Ensemble methods

- Random forest
- Gradient boosting



Multilayer perceptron



Decision tree

Model Training

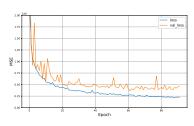
Optimization objective is the Root Mean Squared Error:

RMSE =
$$\sqrt{\frac{1}{n} \sum_{i=1}^{n} (\hat{y}_i - y_i)^2}$$

Hyperparameter tuning:

- Random grid search
- Large parameter space
- Iterative refinement
- Over 100 models fitted

Multilayer perceptron training



Results

Model	RMSE	MAPE	Prediction time / 1,000 instances
Multilayer-perceptron	636.7	4.48%	8.57s
Gradient boosting	695.9	4.80%	8.54s
Polynomial regression	859.2	5.56%	8.55s
Random forest	1045.0	6.83%	8.55s
Greedy heuristic	1115.6	10.11%	734.14s
Linear regression	1982.1	13.54%	8.53s
Daganzo (1984) - CVRP	2055.6	16.93%	2.85s
Beardwood(1959) - TSP	4498.6	28.49%	2.80s
Constant model	5627.0	78.42%	0.00s

- The new models can predict distances more accurately.
- No significant increase in computation time.
- Routing solver are too slow for distance estimation.

Discussion

Opportunities

- More informed decision-making
- Economic value even for small improvements
- · Estimating heuristics is is realistic
- Easily adaptable to other routing variants

Limitations & Future Research

- ullet Bad generalization to larger problems o active research field
- Fixed feature vectors → graph neural networks
- Slow feature extraction → improve code performance
- Real-world data

Conclusion

Topic relevance

 Distance estimation is important in situations that require cost estimates for a large number of instances in short computation time.

Research problems

- Current CVRPTW datasets are not suitable distance estimation.
- Most studies rely on linear models, few predictors, and strong assumptions.

Methodology

- A large CVRPTW dataset with high variance is created and solved.
- Three new distance estimation models are developed.

Results

- The new models achieve better estimates at similar computation time.
- Particularly the MLP and gradient boosting show promising results.
- Further exploration of this approach in richer routing variants is suggested.