Ray-casting & Ray-Tracing with VTK

Introduction

VTK has long evolved beyond just visualization and offers some amazing functionality that just can't be found elsewhere. Such an example would be the 'ray-casting', and consequentially 'ray-tracing', capabilities provided by the <a href="https://vtkobble.com/vtkobb

Disclaimer: The ray-casting and ray-tracing examples I'll be presenting here are severely condensed versions of my posts 'Ray Casting with Python and VTK: Intersecting lines/rays with surface meshes' and 'From Ray Casting to Ray Tracing with Python and VTK' appearing under my blog PyScience. If they pique your interest please visit the aforementioned posts where you can find all the material, code (in the form of IPython Notebooks), and an excruciating amount of detail pertaining to each aspect of the process (as these posts were written for people with little to no experience in VTK).

Ray-Casting vs. Ray-Tracing

I'd like to emphasize a pivotal difference between 'ray-casting' and 'ray-tracing'. In the case of the former we only 'cast' a single ray, test for its intersection with objects, retrieve information regarding the intersection, and stop there. Ray-tracing on the other hand, is more physically accurate as it treats the rays with physics laws on reflection, refraction, attenuation, etc to 'trace', i.e., follow, that ray and its derivative rays. However, ray-casting is the natural precursor to ray-tracing as it tells us what part of which object the ray intersects with and provides all necessary information to cast subsequent rays.

The vtkOBBTree class

The star of this post is the vtkobbtree class, which generates an oriented bounding-box (OBB) 'tree' for a given geometry under a vtkPolyData object. Upon generation of this OBB tree this class allows us to perform intersection tests between the mesh and lines of finite length as well as intersection tests between different meshes. It can then return the point coordinates where intersections were detected as well as the polydata cell IDs where these occurred.

Ray-Casting with vtkOBBTree

For this demonstration we're assuming that we have a surface model of a human skull stored in an .stl file whose contents we've loaded into a vtkPolyData Object named mesh through the vtkSTLReader class. A rendering of this model through the vtkPolyDataMapper class can be seen in Figure 1.



Figure 1. Rendering of the surface model of a human skull which we will use to demonstrate ray-casting.

The center of the skull is centered around the cartesian origin, i.e., the (0.0, 0.0, 0.0) point. Now let's assume we want to cast a ray emanating from (100.0, 100.0, 0.0) and ending at (0.0, 0.0, 0.0) and retrieve the coordinates of the points where this ray intersects with the skull surface. A rendering including the ray, prior to actually casting it, can be seen in Figure 2.

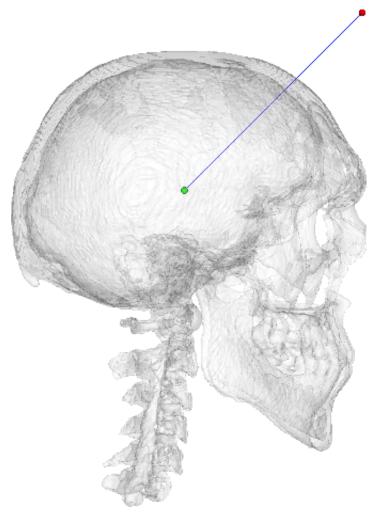


Figure 2. The ray that will be tested for intersection with the skull model. The 'source' point of the ray is rendered as red while the 'target' point is rendered as green.

Prior to intersection, we need to create and initialize a new vtkOBBTree with the vtkPolyData object of our choice, called mesh in our case. This is done as follows:

```
obbTree = vtk.vtkOBBTree()
obbTree.SetDataSet(mesh)
obbTree.BuildLocator()
```

Note the call to the BuildLocator method which creates the OBB tree. That's it! We now have a world-class intersection tester at our disposal. At this point we can use the IntersectWithLine method of the vtkOBBTree class to test for intersection with the aforementioned ray. We merely need to create a vtkPoints and a vtkIdList object to store the results of the intersection test:

As mentioned above, the points and cellIds now contain the point coordinates and cell IDs the ray

intersected with as it was emanated from the first point, i.e., (100.0, 100.0, 0.0), onto the second, i.e., (0.0, 0.0, 0.0), in the order they were 'encountered'. The return value code is an integer which would be equal to 0 if no intersections were found at all. A rendering showing the intersection points can be seen in Figure 3.

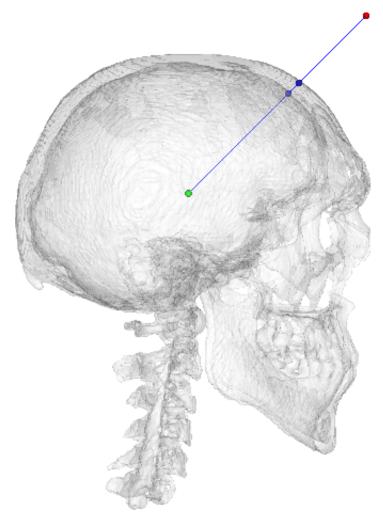


Figure 3. Result of the ray-casting operation and intersection test between the skull model and the ray. The blue points depict the detected intersection points.

As mentioned at the beginning of this article, the entire process shown above, along with all material and code needed to reproduce it, is detailed in my post 'Ray Casting with Python and VTK: Intersecting lines/rays with surface meshes'.

The Python package pycaster wraps the functionality shown above, assuming no VTK experience, and provides additional methods to calculate the distance a given ray has 'traveled' within a closed surface. It is currently being served through PyPI, while the repository can be found on BitBucket here.

Ray-Tracing with vtkOBBTree

Now in order to perform ray-tracing we can take the lessons learned from ray-casting and apply them to a more convoluted scenario. The rationale behind ray-tracing with the vtkobbtree class is the following:

Cast rays from every 'ray source' and test for their intersection with every 'target' mesh in the scene.

If a given ray intersects with a given 'target' then use the intersection points and intersected cells in order
to calculate the normal at that cell, calculate the vectors of the reflected/refracted rays, and cast
subsequent rays off the target.

An excellent, freely available, article entitled 'Reflections and Refractions in Ray-Tracing' (Bram de Greve, 2006) provides a good overview of the math and physics behind ray-tracing.

• Repeat this process for every ray cast from the 'ray source'.

Let's assume a scene comprising a half-sphere dubbed sun, which will act as the ray-source, and a larger nicely textured sphere called earth, which will be the target of those rays. This 'environment' can be seen in Figure 4.

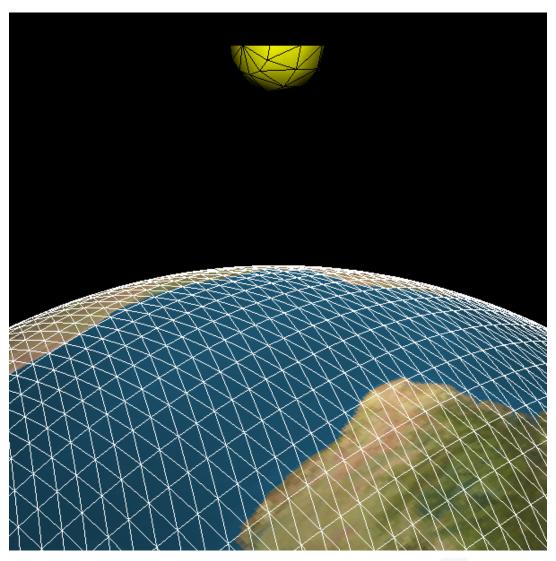


Figure 4. Scene defined for the ray-tracing example. The yellow half-sphere sun acts as the ray-source while the textured sphere earth will be the target of those rays.

In this example, we will be casting a ray from the center of each triangular cell on the sun surface along the direction of that cell's normal vector. The sun cell-centers were calculated through the vtkCellCenters class and stored under pointsCellCenterssun (of type vtkPolyData). The sun cell-normals were calculated through the vtkPolyDataNormals class and stored under normalssun (of type vtkFloatArray). A rendering of the cell-centers as points and cell-normals as glyphs, through the vtkGlyph3D class, can be

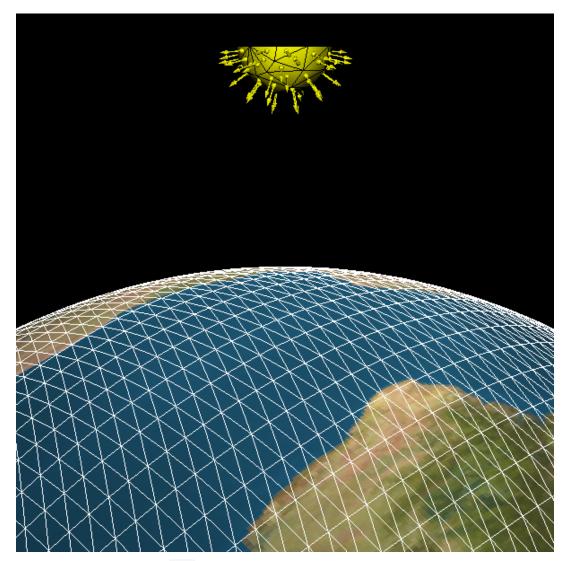


Figure 5. Rendering of the sun cell-centers that will act as source-points for the rays and the cell-normals along which the rays will be cast.

Similarly to what was done in the previous example, prior to ray-casting we first need to create a vtkobbtree object for the earth:

```
obbEarth = vtk.vtkOBBTree()
obbEarth.SetDataSet(earth.GetOutput())
obbEarth.BuildLocator()
```

Now since we'll be casting a large number of rays let's wrap the vtkobbtree functionality in two convenient functions:

```
return True
def GetIntersect(obbTree, pSource, pTarget):
   points = vtk.vtkPoints()
   cellIds = vtk.vtkIdList()
    # Perform intersection test
   code = obbTree.IntersectWithLine(pSource,
                                     pTarget,
                                     points,
                                     cellIds)
   pointData = points.GetData()
   noPoints = pointData.GetNumberOfTuples()
   noIds = cellIds.GetNumberOfIds()
   pointsInter = []
   cellIdsInter = []
   for idx in range(noPoints):
       pointsInter.append(pointData.GetTuple3(idx))
       cellIdsInter.append(cellIds.GetId(idx))
   return pointsInter, cellIdsInter
```

The isHit function will simply return True or False depending on whether a given ray intersects with obbTree, which in our case will only be obbEarth.

The <code>GetIntersect</code> function simply wraps the functionality we saw in the first example. In a nutshell it will return two <code>list</code> objects <code>pointsInter</code> and <code>cellIdsInter</code>. The former will contain a series of <code>tuple</code> objects with the coordinates of the intersection points. The latter will contain the 'id' of the mesh cells that were 'hit' by that ray. This information is vital as through these ids we'll be able to get the correct normal vector for that <code>earth</code> cell and calculate the appropriate reflected vector as we'll see below.

At this point we're ready to perform the ray-tracing. Let's take a look at a condensed version of the code:

```
for idx in range(pointsCellCentersSun.GetNumberOfPoints()):
   pointSun = pointsCellCentersSun.GetPoint(idx)
   normalSun = normalsSun.GetTuple(idx)
    # Calculate the 'target' of the 'sun' ray based on 'RayCastLength'
    pointRayTarget = list(numpy.array(pointSun) +
                         RayCastLength*numpy.array(normalSun))
    if isHit(obbEarth, pointSun, pointRayTarget):
        pointsInter, cellIdsInter = GetIntersect(obbEarth,
                                                 pointSun,
                                                 pointRayTarget)
        # Get the normal vector at the earth cell that intersected with the ray
       normalEarth = normalsEarth.GetTuple(cellIdsInter[0])
        # Calculate the incident ray vector
       vecInc = (numpy.array(pointRayTarget) -
                 numpy.array(pointSun))
        # Calculate the reflected ray vector
       vecRef = (vecInc - 2*numpy.dot(vecInc,
                                       numpy.array(normalEarth)) * numpy.array(normalEarth))
        # Calculate the 'target' of the reflected ray based on 'RayCastLength'
        pointRayReflectedTarget = (numpy.array(pointsInter[0]) +
                              RayCastLength*12n(vecRef))
```

Please note that all rendering code was removed from the above snippet but you can see the entire code in the original post. What is done above in a nutshell is the following:

- We loop through every cell-center on the sun mesh (pointsun), stored under pointscellcenterssun .
- We cast a ray along the direction of that sun cell's normal vector, stored under normalssun. The ray emanates from pointsun to pointRayTarget.

As the vtkobbtree class only allows for intersection tests with lines of finite length, not semi-infinite rays, the rays cast in the code above are given a large (relative to the scene) length to ensure that failure to intersect with earth would only be due to the ray's direction and not an insufficient length.

- Every ray is tested for intersection with the earth through the isHit function and and the obbEarth object defined above.
- If a ray intersects with the earth, the intersection test is repeated through the <code>GetIntersect</code> function in order to retrieve the intersection point coordinates and the intersected cell IDs on the <code>earth</code> mesh. The intersection point coordinates as well as the intersected <code>earth</code> cell normal vector (<code>normalEarth</code>) are used to calculate the normal vector of the reflected ray and cast that ray off the <code>earth</code> surface.

The cell normals on the earth surface were calculated through the vtkPolyDataNormals class and stored under <a href="https://www.normals.

A render of the ray-tracing result can be seen in Figure 6. Note that rays that missed the earth are rendered as white. Rays that intersected with earth are rendered as yellow. You can also see the intersection points, the normal vectors at the intersected earth cells, as well as the reflected rays.

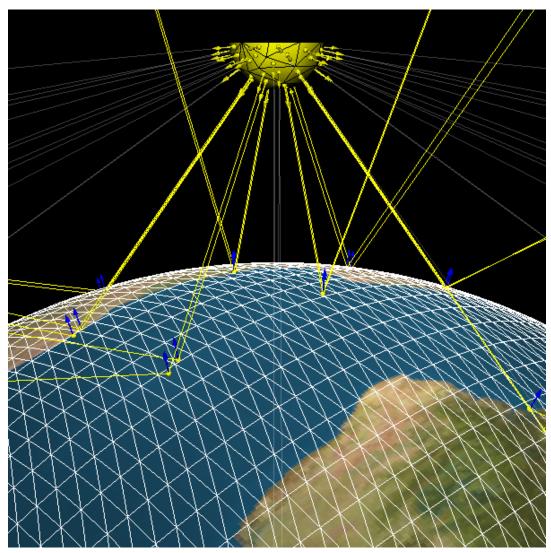


Figure 6. Result of the ray-tracing example. Rays cast from the sun that missed the earth are rendered as white. Rays that intersected with earth are rendered as yellow. The intersection points, normal vectors at the intersected earth cells, as well as the reflected rays can also be seen.

As mentioned at the beginning of this article, the entire process shown above, along with all material and code needed to reproduce it, is detailed in my post 'From Ray Casting to Ray Tracing with Python and VTK'.

Conclusion

As you can see that VTK provides some little-known pearls that offer some fantastic functionality.

While the above examples fall short of real-world ray-tracing applications, as one would need to account effects like refraction and energy attenuation, the sky is the limit!

Bio



Adamos Kyriakou is an Electrical & Computer Engineer with an MSc. in Telecommunications and a Ph.D. in Biomedical Engineering. He is currently working as a Research Associate in Computational Multiphysics at the IT'IS Foundation (ETH Zurich) where his work and research is primarily focused around computational algorithm development, high-performance computing, multi-physics simulations, big-data analysis, and medical imaging/therapy modalities. He has collaborated with medical & technical personnel, researchers, and industrial partners in large international projects such as, safety evaluation of medical devices, treatment planning & optimization of therapeutic modalities, and development of next-generation simulation platforms.

http://pyscience.wordpress.com/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-tracing-with-python-and-vtk/2014/10/05/from-ray-casting-to-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-vtk/2014/10/05/from-ray-casting-with-python-and-with-python-a