# Research Report On B-CNN & MatConvNet

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# 1. [Paper] Bilinear CNN Models for Fine-grained Visual Recognition

Tsung-Tu li et al, UMASS, ICCV15

# 1.1 Overview on Bilinear-CNN (B-CNN) Model

B-CNN is an architecture which consists of two feature extractors whose outputs are multiplied using outer product at each location and then pooled to obtain image descriptors. The descriptors are in a translationally invariant manner which are particular useful for fine-grained categorization. After some normalizations, a linear classifier can be applied directly to these descriptors for classification.

The two feature extractors are usually truncated convolutional neural networks (CNNs) pretrained on **ImageNet** and then truncated at a convolutional layer including non-linearities. Outputs of the two truncated CNNs are then multiplied using outer product. A sum-pooling step is then performed to obtain an image descriptor. The resulting bilinear descriptor is then reshaped as a vector and passed through a signed square-root step followed by a  $l_2$  normalization step. Finally, a linear classifier is applied to perform the classification.

By pre-training the model can benefit from additional training data when domain specific data is scarce. By using only the convolutional layers, another advantage is that the resulting CNN can process images of an arbitrary size in a single forward-propagationstep and produce outputs indexed by the location in the image and the feature model.

Using networks pretrained on the **ImageNet** dataset followed by domain specific fine-tuning, the model achieve 84.1% accuracy on the CUB-200-2011 dataset requiring only category labels at training time, which is state-of-the-art (2015).

#### 1.2 Bilinear Model

A bilinear model  ${\cal B}$  for image classification can be expressed by a quadruple:

$$\mathcal{B} = (f_A, f_B, \mathcal{P}, \mathcal{C}).$$

Where

- $f_A, f_B$  are feature extractor functions:  $f: \mathcal{L} imes \mathcal{I} o \mathcal{R}^{c imes D}$  , where
  - $\circ$   $\mathcal{I}$ : be an input images,
  - $\mathcal{L}$ : be a set of locations,
  - $\mathcal{R}$ : be a set of features of size  $c \times D$  ,
- $\mathcal{P}$  is a pooling function,
- $\mathcal{C}$  is a classification function.

The feature outputs are combined at each location using the matrix outer product, i.e., the *bilinear feature* combination of  $f_A$  and  $f_B$  at location l is given by:

$$bilinear(l, \mathcal{I}, f_A, f_B) = f_A(l, \mathcal{I})^T f_B(l, \mathcal{I}).$$

Where both  $f_A(l,\mathcal{I})$  and  $f_B(l,\mathcal{I})$  must have the same feature dimension c to be compatible.

Followed by the outer product is the pooling function  $\mathcal P$  that simply sum all the bilinear features over all locations  $l\in\mathcal L$ :

$$\mathcal{P} : \hspace{0.1cm} \phi(\mathcal{I}) = \sum_{l \in \mathcal{L}} bilinear(l, \mathcal{I}, f_A, f_B).$$

If  $f_A$  is with size C imes M ,  $f_B$  with C imes N , the  $\phi(\mathcal{I})$  would have size M imes N .

Then  $\phi(\mathcal{I})$  is reshape to a vector with size  $MN \times 1$ :

$$\phi(\mathcal{I}) = reshape(\phi(\mathcal{I}), [MN, 1]).$$

In fact, given two feature maps outputed by CNN(s), what all above said can be implemented by first reshaping them to a vector, and then calculating their inner product. Given n feature maps of size  $m \times m$ , firstly reshaping them to a  $(m*m) \times n$  -dimensional matrix denoted as  $X_{(m*m)\times n}$ , then calculating  $X^TX$ , and finally reshaping the result to a n\*n-dimensional vector call bilinear vector  $\phi(\mathcal{I})$ , that is all what the vl\_nnbilinearpool or vl\_nnbilinearclpool function in bonn source code about.

#### · About matrix outer product.

The outer product usually refers to the tensor product of vectors. If you want something like the outer product between a  $m \times n$  matrix A and a  $p \times q$  matrix B, you can see the generalization of outer product, which is the kronecker product. It is noted  $A \otimes B$  and equals:

$$A \otimes B = \left(egin{array}{ccc} a_{11}B & \dots & a_{1n}B \ dots & \ddots & dots \ a_{m1}B & \dots & a_{mn}B \end{array}
ight)$$

As an example, the outer product of A and B, where

$$A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} \qquad B = \begin{pmatrix} 5 & 6 & 7 \\ 8 & 9 & 10 \end{pmatrix}$$

$$A \otimes B = \begin{pmatrix} \begin{pmatrix} 5 & 6 & 7 \\ 8 & 9 & 10 \end{pmatrix} & \begin{pmatrix} 10 & 12 & 14 \\ 16 & 18 & 20 \end{pmatrix} \\ \begin{pmatrix} 15 & 18 & 21 \\ 24 & 27 & 30 \end{pmatrix} & \begin{pmatrix} 20 & 24 & 28 \\ 32 & 36 & 40 \end{pmatrix} \end{pmatrix}$$

#### 1.3 Bilinear-CNN (B-CNN) model

1. Use as feature extractors  $f_A$  and  $f_B$  two CNNs pretrained on the *ImageNet* dataset and truncated at a convolutional layer including non-linearities.

imagenet-vgg-m.mat truncated at layer 14  $(conv_5 + relu)$ , referred as M-Net, and imagenet-vgg-verydeep-16.mat truncated at layer 30  $(conv_{5\_4} + relu)$ , referred as D-Net, are used in the paper.

- 2. Apply bilinear model presented above to get vector  $x = \phi(\mathcal{I})$  .
- 3. Passed through a signed square-root normalization followed by a  $l_2$  normalization:

$$y \leftarrow sign(x) \sqrt{|x|}$$
  $z \leftarrow rac{y}{||y||_2}$ 

4. Use logistic regression or linear SVM as classification function  $\mathcal C$  . A linear SVM is used in this paper.

#### 1.4 Implementation details

1. y = vl\_nnbilinearclpool(x1, x2, varargin)

**Input**: two different features  $x_1, x_2$  with size  $[h_1, w_1, ch_1]$  and  $[h_2, w_2, ch_2]$  for height, width and number of channels, and  $\nabla_Y Z$  ( dzdy ) which is the gradient of cost function Z w.r.t y.

**Output**: A bilinear vector y with size [ch1\*ch2,1].

- · Feed forward.
  - Resize  $x_1, x_2$  to the same size, i.e., downsampling one of them to ensure  $h_1 * w_1 == h_2 * w_2$ :

```
resize_image(x1, x2)
```

Reshape  $x_1, x_2$  to  $X_a, X_b$  with sizes  $[h_1 * w_1, ch_1]$  and  $[h_2 * w_2, ch_2]$  respectively:

```
Xa = reshape(x1, [h1*w1, ch1])
Xb = reshape(x2, [h2*w2, ch2])
```

Cacultate their outer product:

$$Y = X_a^T X_b$$

• Reshape y to a vector with size  $[ch_1 * ch_2, 1]$ .

```
y = reshape(Y, [ch1 * ch2, 1])
```

Back propagation.

Since  $Y = X_a^T X_b$ , calculate  $\nabla_{X_a} Z$  is easy (Z denote the cost function):

$$egin{aligned} 
abla_{X_a} Z &= 
abla_{X_a} Y \cdot 
abla_Y Z &= X_b \cdot (
abla_Y Z)^T, \ 
abla_{X_b} Z &= 
abla_{X_b} Y \cdot 
abla_Y Z &= X_a \cdot (
abla_Y Z). \end{aligned}$$

Reshape  $x_1, x_2$  to  $X_a, X_b$  with sizes  $[h_1 * w_1, ch_1]$  and  $[h_2 * w_2, ch_2]$  respectively:

```
Xa = reshape(x1, [h1*w1, ch1])
Xb = reshape(x2, [h2*w2, ch2])
```

Reshape input dzdy to size [ch1, ch2] .

```
Delta = reshape(dzdy, [ch1, ch2]
```

Calculate dzdxa and dzdxb

```
dzdxa = Xb * Delta'
dzdxb = Xa * Delta
```

Reshape dzdxa and dzdxb to sizes as with x1 and x2.

```
dzdx1 = reshape(dzdxa, [h1, w1, ch1])
dzdx2 = reshape(dzdxb, [h2, w2, ch2])
```

- 2.  $y = vl_nnsqrt(x, param, varargin)$ 
  - Feed forward (element-wise operation):

$$y = sign(x) . * \sqrt{abs(x)}$$

Note that y is with the same size as x.

• Back propagation (element-wise operation):

$$rac{dy}{dx} = 0.5 \cdot * rac{1}{\sqrt{abs(x) \cdot + param}}$$
  $rac{dz}{dx} = rac{dy}{dx} \cdot * rac{dz}{dy}$ 

where  $rac{dy}{dx}=(rac{dy_1}{dx_1},\dots,rac{dy_n}{dx_n})^T$  , and param is used for numeric stability.

- 3. y = vl\_nnl2normalization(x, param, varargin)
  - Feed forward:

$$y = \frac{x}{||x||_2}$$

Note that y is with the same size as x.

Back propagation:

$$egin{aligned} rac{d}{dx_j} \left(rac{x}{||x||_2}
ight) &= rac{1}{||x||_2^3} \left(x_1^2 + \ldots + x_{j-1}^2 + x_{j+1}^2 + \ldots + x_n^2
ight) \ &= rac{1}{||x||_2} - rac{x_j^2}{||x||_2^3} \end{aligned}$$

Which gives the vectorize form:

$$\nabla(\frac{x}{||x||_2}) = \frac{1}{||x||_2} \cdot - \frac{x^2}{||x||_2^3}$$

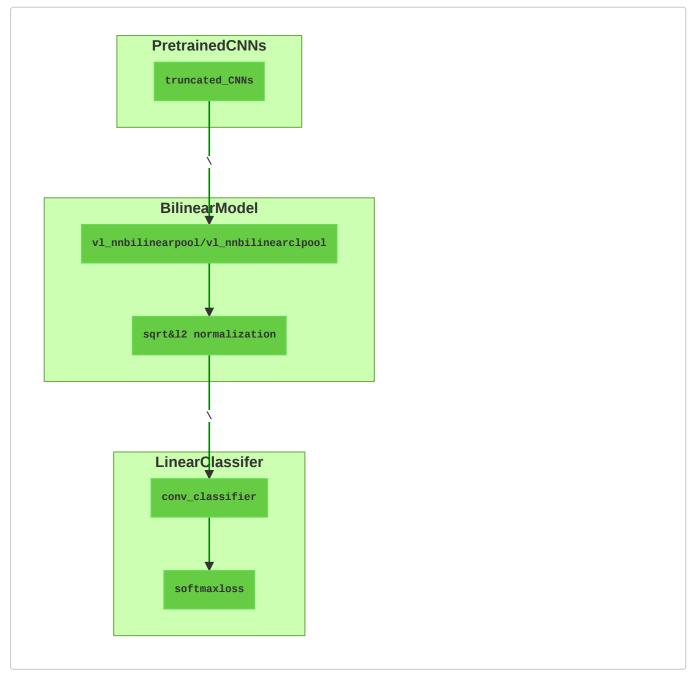
where 
$$x.^2=(x_1^2,\ldots,x_n^2)^T$$
 .

To prevent large values and ensure numeric stability, it is recommended to preprocess |x|| by adding a threshold:

$$||x||_2 = ||x||_2 + threshold$$

#### 1.5 Training Methodology

Build a B-CNN model:



Perform a two-step training:

- Step 1. Extract features using the PretrainedCNNs+BilinearModel , from the dataset. Train the LinearClassifier on the extracted features for the first step. It is a convex optimization problem. Using SGD algorithm with proper learning rate, the optima can be found quickly. For example, with lr=0.06, it quickly reaches the optima in less than 10 epochs.
- **Step 2**. Fine-tune the whole B-CNN model on the original dataset. That is, initialize the <code>conv\_classifier</code> with weights obtained from *step 1*.

After fine-tunning, remove conv\_classifier -> softmaxloss , combine training and validation set, and train a set of one-vs-all linear SVMs on the features extracted from 12\_normalization layer of the fine-tuned B-CNN model.

#### 2 MatConvNet

The B-CNN model is implemented based on MatConvNet.

**MatConvNet** is a MATLAB toolbox implementing *Convolutional Neural Networks* (CNNs) for computer vision applications. It is simple, efficient, and can run and lear state-of-the-art CNNs. Many pre-trained CNNs for image classification, segmentation, face recognition, and text detection are available.

Main functions provided:

```
vl_nnbilinearsampler
vl_nnconcat
vl_nnspnorm
vl_nnpdist
v1_nnconv
v1_nnconvt
vl_nncrop
vl_nndropout
vl_nnloss
vl_nnnoffset
vl_nnnormalize
vl_nnpool
vl_nnrelu
vl_nnroipool
vl_nnsigmoid
vl_nnsoftmax
vl_nnsoftmaxloss
DagNN wrapper
vl_simplenn
vl_simplenn_tidy
vl_simplenn_diagnose
vl_simplenn_display
vl_simplenn_move
vl_argparse
vl_compilenn
vl\_rootnn
vl_setupnn
vl_imreadjpeg
vl_taccum
```

#### Pretrained models:

- Fast R-CNN for object detection
- VGG-Face for face recognition
- Fully-Convolutional Networks (FCN), BVLC FCN and Torr Vision Group FCN-8s for semantic segmentation
- ResNet, GoogLeNet, VGG-VD, VGG-S/M/F, Caffe reference model, and AlexNet for ImageNet ILSVRC classification.

#### Documentation

- manual
- Function description
- CNN practical

# 3. Delving Into The Source Code

#### 3.1 Having an overview.

run\_experiments\_bcnn\_train.m under /path/to/bcnn/ is a top-level function that performs the **two-step** training of a B-CNN model. Having a look into this function can give us a quick overview of the source code.

• Overview of run\_experiments\_bcnn\_train.m :

| End

The first job of this function is to set the B-CNN model (B-CNN[M,M], B-CNN[D,D], or B-CNN[M,D]) and set the dataset via bcnnxx.opts, setupNameList, encoderList and datasetList:

```
% run_experiments_bcnn_train.m
 bcnnmm.name = 'bcnnmm' ;
 bcnnmm.opts = {...
  'type', 'bcnn', ...
  'modela', 'data/models/imagenet-vgg-m.mat', ...
                                                    % intialize network A with pre-trained mod
  'layera', 14,...
                                                      % specify the output of certain layer of n
etwork A to be bilinearly combined
  'modelb', 'data/models/imagenet-vgg-m.mat', ...
                                                      % intialize network B with pre-trained mod
el
  'layerb', 14,...
                                                      % specify the output of certain layer of n
etwork B to be bilinearly combined
  'shareWeight', true,...
                                                      % true: symmetric implementation where two
networks are identical
 } ;
 bcnnvdm.name = 'bcnnvdm' ;
 bcnnvdm.opts = {...
  'type', 'bcnn', ...
  'modela', 'data/models/imagenet-vgg-verydeep-16.mat', ...
  'layera', 30,...
  'modelb', 'data/models/imagenet-vgg-m.mat', ...
  'layerb', 14,...
  'shareWeight', false,...
                                                      % false: asymmetric implementation where t
wo networks are distinct
 } ;
 bcnnvdvd.name = 'bcnnvdvd' ;
 bcnnvdvd.opts = {...
  'type', 'bcnn', ...
  'modela', 'data/models/imagenet-vgg-verydeep-16.mat', ...
  'layera', 30,...
  'modelb', 'data/models/imagenet-vgg-verydeep-16.mat', ...
  'layerb', 30,...
  'shareWeight', true,...
 };
 setupNameList = {'bcnnmm'};
 encoderList = {{bcnnmm}};
 % setupNameList = {'bcnnvdvd'};
 % encoderList = {{bcnnvdvd}};
  datasetList = {{'cub', 1}}
```

Then it calls function <code>model\_setup</code> to set up hyper-parameters and prepare dataset. Finally it calls function <code>imdb\_bcnn\_train\_dag</code> to perform the *two-step* training.

• Overview of model\_setup(...):

End: save imdb

Hyper-parameters of training is set default inside the <code>model\_setup</code> function, and we can change it by passing a different value when it is called by <code>run\_experiments\_bcnn\_train</code> or directly inside <code>model\_setup</code>.

Then it loads the dataset specified in datasetList:

```
% /path/to/bcnn/model_setup.m
    switch opts.dataset
        case 'cubcrop'
           imdb = cub_get_database(opts.cubDir, true, false);
        case 'cub'
            imdb = cub_get_database(opts.cubDir, false, opts.useVal);
        case 'aircraft-variant'
            imdb = aircraft_get_database(opts.aircraftDir, 'variant');
        case 'cars'
            imdb = cars_get_database(opts.carsDir, false, opts.useVal);
        case 'imagenet'
            imdb = cnn_imagenet_setup_data('dataDir', opts.ilsvrcDir);
        case 'imagenet-224'
            imdb = cnn_imagenet_setup_data('dataDir', opts.ilsvrcDir_224);
        otherwise
            error('Unknown dataset %s', opts.dataset);
    end
```

• Overview of imdb\_bcnn\_train\_dag(imdb, opts)

```
Entry: `imdb_bcnn_train_dag(imdb, opts)`

|
Setup some training params: `opts.train....`
|
Build up and Initialize network:
   `initializeNetworkSharedWeights` or ` initializeNetworkTwoStreams`
|
Applying SGD algorithm to train the bcnn
|
End: save networks
```

The *two-step* training process is performed inside <code>imdb\_bcnn\_train\_dag.m</code> . It calls <code>initializeNetworkSharedWeights</code> or <code>initializeNetworkTwoStreams</code> to perform training step 1 and <code>bcnn\_train\_simplenn</code> or <code>bcnn\_train\_dag</code> to perform training step 2. Some hyper-parameters of step 1 are also set inside this function.

# 3.2 Analysizing some typical functions in bcnn-package which implementes layers of a B-CNN model.

• function y = vl\_nnbilinearpool(x, varargin)

```
%
        For each image with size `[height, width, channels]`, firstly
%
        reshape it into size `[height * width, channels]`, and then
        compute the output
                    $ = \frac{1}{height} * width} x^T x
        which gives $y$ the size `[channels, channels]`, reshape it again to a vector.
%
%
   backward pass:
        gradient of $y$ w.r.t $x$.
%
        $y$ is the same size as $x$, i.e., `[height, width, channels, batch_size]`.
%
        For each image, reshape $dzdy$ to size `[channels, channels]`
                        reshape $x$ to size `[height * width, channels]`.
        $dydx$ is caculated as:
                    $$y = \frac{1}{height * width} x * dzdy$$
        which gives $y$ the size `[height * width, channels]`,
        Reshape $y$ to `[height, width, channels]` as output.
% if the number of elements in `varargin` > 0 and the first element is not a string
backMode = numel(varargin) > 0 && ~isstr(varargin{1})
% if in backward mode, take out the `dzdy` in `varargin`
if backMode dzdy = varargin{1}; end
% if `x` is a `gpuArray`, it is in `gpuMode`
gpuMode = isa(x, 'gpuArray');
% = 10^{-6} winds the size of x into height, width, number of channel, and batch size
[h, w, ch, bs] = size(x);
% backward mode
if backMode
    if gpuMode
        y = gpuArray(zeros(size(x), 'single'));
        y = zeros(size(x), 'single'));
    end
    % for each image / for each feature map with `ch` channels
    for b = 1:bs
        dzdy_b = reshape(dzdy(1, 1, :, b), [ch, ch]);
        a = reshape (x(:, :, :, b), [h*w, ch]);
        % caculate dydx
        y(:, :, :, b) = reshape(a * dzdy_b, [h, w, ch]) / (h * w);
    end
else
    if gpuMode
        y = gpuArray(zeros([1, 1, ch * ch, bs], 'single'));
        y = zeros([1, 1, ch * ch, bs], 'single');
    for b = 1:bs
        a = reshape(x(:, :, :, b), [h * w, ch]);
        % caculate output
        y(1, 1, :, b) = reshape(a'*a, [1, ch*ch]) / (h * w);
    end
end
```

function y = vl\_nnbilinearclpool(x1, x2, varargin)

```
% $x$: input feature of size [height, width, channels, batch size].
% $varargin$: $dzdy$ when in backward pass.
% $y$:
  forward pass:
       Self outer product of $x$.
       For each image with size `[height, width, channels]`, firstly
%
       reshape it into size `[height * width, channels]`, and then
%
       compute the output
                   $ = \frac{1}{height} * width} x^T x
%
       which gives $y$ the size `[channels, channels]`, reshape it again to a vector.
  backward pass:
%
%
       gradient of $y$ w.r.t $x$.
       $y$ is the same size as $x$, i.e., `[height, width, channels, batch_size]`.
       For each image, reshape $dzdy$ to size `[channels, channels]
%
                      reshape $x$ to size `[height * width, channels]`.
%
%
       $dydx$ is caculated as:
                   $$y = \frac{1}{height * width} x * dzdy$$
       which gives $y$ the size `[height * width, channels]`,
       Reshape $y$ to `[height, width, channels]` as output.
% -----
% if the number of elements in `varargin` > 0 and the first element is not a string
backMode = numel(varargin) > 0 && ~isstr(varargin{1})
% if in backward mode, take out the `dzdy` in `varargin`
if backMode dzdy = varargin{1}; end
% if `x` is a `gpuArray`, it is in `gpuMode`
gpuMode = isa(x1, 'gpuArray');
% = 10^{-6} winds the size of x into height, width, number of channel, and batch size
[h1, w1, ch1, bs] = size(x1);
[h2, w2, ch2, \sim] = size(x2);
% resize the CNN output to the same size
if w1 * h1 <= w2 * h2
   % downsample feature 2
   x2 = array_resize(x2, w1, h1);
   % downsample feature 1
   x1 = array_resize(x1, w2, h2);
end
h = size(x1, 1); w = size(x1, 2);
% backward mode
if backMode
   if apuMode
       y = gpuArray(zeros(size(x), 'single'));
       y = zeros(size(x), 'single'));
    % for each image / for each feature map with `ch` channels
    for b = 1:bs
       dzdy_b = reshape(dzdy(1, 1, :, b), [ch1, ch2]);
       A = reshape (x1(:, :, :, b), [h*w, ch1]);
       B = reshape (x2(:, :, :, b), [h*w, ch2]);
       dB = reshape(A * dzdy_b, [h, w, ch2]);
       dA = reshape(B * dzdy_b', [h, w, ch1]); %'
       if w1 * h1 <= w2 * h2
           % B is downsampled
           % A is downsampled
    end
```

function y = vl\_nnsqrt(x, param, varagin)

```
% /path/to/bcnn/bcnn-package/vl_nnsqrt.m
function y = vl_nnsqrt(x, param, varagin)
% functionality: perform square root normalization for the input features
              at each location
% x: the input features of size [height, width, channels, batch_size]
\% param: the threshold to prevent large value when close to 0
% varargin: dzdy, only needed in backward pass
% y:
     forward pass:
        y = sign(x) \cdot * sqrt(|x|)
%
%
   backward pass:
        dydx = 0.5 ./ sqrt(|x| + param)
        y = dydx .* dzdy % the chain rule
% -----
```

function y = vl\_nnl2norm(x, param, varagin)

```
% /path/to/bcnn/bcnn-package/vl_nnl2norm.m
 function y = vl_nnl2norm(x, param, varagin)
 % functionality: perform square root normalization for the input features
                  at each location
 %
 % x: the input features of size [height, width, channels, batch_size]
 % param: the threshold to prevent large value when the norm is close to 0
 % varargin: dzdy, only needed in backward pass
 % y:
 %
       forward pass:
 %
           y = x . / ||x|| % note: ||x|| is 1-2 norm
       backward pass:
           \frac{d}{dx_j}(x./|x||) = \frac{1}{1}(x./|x||)^2 + \dots + x_{j-1}^2 + x_{j+1}^2 + \dots
... + x_n^2)
 %
           (d/dx_j)(x./||x||) = 1 / ||x|| - x_j^2 / ||x|| ^ 3
           gradient(x./||x||) = 1 / ||x|| - x.^2 / ||x|| ^ 3
```

#### 3.3 Looking into the code of preparing dataset.

To use the birds dataset cub , look into its function imdb = cub\_get\_database(cubDir, useCropped, useVal) :

```
% cub_get_database.m
% the directory where the real images reside
if useCropped
    imdb.imageDir = fullfile(cubDir, 'images_cropped') ;
else
    imdb.imageDir = fullfile(cubDir, 'images');
end
. . .
% read the class names, image names, bounding boxes, lables...
[~, classNames] = textread(fullfile(cubDir, 'classes.txt'), '%d %s');
imdb.classes.name = horzcat(classNames(:));
% Image names
[~, imageNames] = textread(fullfile(cubDir, 'images.txt'), '%d %s');
imdb.images.name = imageNames;
imdb.images.id = (1:numel(imdb.images.name));
% if use validation, set 1/3 to validation set
if useVal
   rng(0)
   trainSize = numel(find(imageSet==1));
   trainIdx = find(imageSet==1);
   % set 1/3 of train set to validation
   valIdx = trainIdx(randperm(trainSize, round(trainSize/3)));
    imdb.images.set(valIdx) = 2;
end
```

Download the CUB-200-2011 dataset and unzip and find that all the required files are contained in the package, all we need to do is put the directory under  $/path/to/bcnn_root/data$  with a new name cub.

- · Dataset details:
  - Birds: CUB-200-2011 dataset. Birds + box uses bounding-boxes at training and test time.
  - Aircrafts: FGVC aircraft dataset
  - · Cars: Stanford cars dataset
- · These results are with domain specific fine-tuning. For more details see the updated B-CNN tech report.

The job of  $cub\_get\_database.m$  is to build up a structure imdb:

```
imdb =

imageDir: 'data/cub/images'
  maskDir: 'data/cub/masks'
    sets: {'train' 'val' 'test'}
  classes: [1x1 struct]
  images: [1x1 struct]
  meta: [1x1 struct]
```

```
imdb.images =

name: {11788x1 cell}
    id: [1x11788 double]
    label: [1x11788 double]
    bounds: [4x11788 double]
    set: [1x11788 double]
    difficult: [1x11788 logical]
```

This structure seems quite clear. Only to note the member imdb.images.set, others are trivial.

```
% /path/to/bcnn_root/cub_get_database.m
...
imdb.images.set(imageSet == 1) = 1; % 1 for training
imdb.images.set(imageSet == 0) = 3; % 3 for test

if useVal
...
% set 1/3 of train set to validation
valIdx = trainIdx(randperm(trainSize, round(trainSize/3)));
imdb.images.set(valIdx) = 2; % 2 for validation
end
...
```

That imdb.images.set contains of a set of set-lables, one for each image. 1 lables the image for using in training, 2 for validation, and 3 for testing.

Let's trace the imdb.iamges.set to see how it is used in other files:

```
$ grep imdb.images.set ./*.m
```

```
./bcnn_train_dag.m:if isempty(opts.train), opts.train = find(imdb.images.set==1); end
./bcnn_train_dag.m:if isempty(opts.val), opts.val = find(imdb.images.set==2); end
./bcnn_train_simplenn.m:if isempty(opts.train), opts.train = find(imdb.images.set==1); end
./bcnn_train_simplenn.m:if isempty(opts.val), opts.val = find(imdb.images.set==2); end
./bird_demo.m:imageInd = find(imdb.images.label == classId & imdb.images.set == 1);
./imdb_bcnn_train_dag.m:train = find(imdb.images.set == 1) ;
                        train = find(imdb.images.set == 1) ;
./imdb_cnn_train.m:
./initializeNetworkSharedWeights.m:
                                      train = find(imdb.images.set==1|imdb.images.set==2);
./initializeNetworkTwoStreams.m:
                                       train = find(ismember(imdb.images.set, [1 2]));
./model_train.m:
                       train = find(ismember(imdb.images.set, [1 2])) ;
./model_train.m: train = ismember(imdb.images.set, [1 2]) ;
./model_train.m:
                  test = ismember(imdb.images.set, 3);
./print_dataset_info.m:train = ismember(imdb.images.set, [1 2]) ;
./print_dataset_info.m:test = ismember(imdb.images.set, [3]) ;
./run_experiments_bcnn_train.m:
                                        imdb.images.set(imdb.images.set==3) = 2;
```

The lines with ./bcnn\_train\_dag.m and ./bcnn\_train\_simplenn.m are doing the jobs of extracting images with label 1 as training set and images with 2 as validation set. But none of the lines are related to label 3, i.e., the test set, except three lines:

```
./model_train.m: test = ismember(imdb.images.set, 3) ;
./print_dataset_info.m:train = ismember(imdb.images.set, [1 2]) ;
./print_dataset_info.m:test = ismember(imdb.images.set, [3]) ;
./run_experiments_bcnn_train.m: imdb.images.set(imdb.images.set==3) = 2;
```

print\_dataset\_info.m prints out information about the dataset like:

```
>> print_dataset_info(imdb)
  dataset: classes: 200 in use. These are:
    1: 001.Black_footed_Albatross (train: 60, test: 0 total: 60)
    2: 002.Laysan_Albatross (train: 60, test: 0 total: 60)
    3: 003.Sooty_Albatross (train: 58, test: 0 total: 58)
    4: 004.Groove_billed_Ani (train: 60, test: 0 total: 60)
```

What left is the last line:

```
./run_experiments_bcnn_train.m: imdb.images.set(imdb.images.set==3) = 2;
```

which sets the test set to validation set!

Therefore, in order to separate a test set, simply set useval to true via params list in model\_setup is not enough. It is also required to comment this line for leaving out a test set.

#### 3.4 Inspecting the code of building up a B-CNN model.

The code of building up the actual B-CNN model lies in file initializeNetworkSharedWeights.m or initializeNetworkTwoStreams.m . Have a look into initializeNetworkSharedWeights.m :

```
% /path/to/bcnn/initializeNetworkSharedWeights.m
% . . .
% Load the model
net = load(encoderOpts.modela);
net.meta.normalization.keepAspect = opts.keepAspect;
% truncate the network
maxLayer = max(encoderOpts.layera, encoderOpts.layerb);
net.layers = net.layers(1:maxLayer);
% ...
% stack bilinearpool layer
if(encoderOpts.layera==encoderOpts.layerb)
    net.layers{end+1} = struct('type', 'bilinearpool', 'name', 'blp');
    net.layers{end+1} = struct('type', 'bilinearclpool', 'layer1', encoderOpts.layera, 'layer2', encoder
erOpts.layerb, 'name', 'blcp');
end
% stack normalization
net.layers{end+1} = struct('type', 'sqrt', 'name', 'sqrt_norm');
net.layers{end+1} = struct('type', 'l2norm', 'name', 'l2_norm');
net.layers{end+1} = struct('type', 'relu', 'name', 'relu_wbcnn');
% build a linear classifier netc
initialW = 0.001/scal * randn(1,1,mapSize1*mapSize2,numClass,'single');
initialBias = init_bias.*ones(1, numClass, 'single');
netc.layers = {};
netc.layers{end+1} = struct('type', 'conv', 'name', 'classifier', ...
    'weights', {{initialW, initialBias}}, ...
    'stride', 1, ...
    'pad', 0, ...
```

```
'learningRate', [1000 1000], ...
'weightDecay', [0 0]);
netc.layers{end+1} = struct('type', 'softmaxloss', 'name', 'loss');
netc = vl_simplenn_tidy(netc);
% ...
```

In this code block, the pretrained CNN is loaded from path <code>encoderOpts.modela</code> and truncated at layer <code>encoderOpts.layera</code>. Then a <code>bilinearpool</code> layer followed by a <code>sqrt</code> normalization and <code>l2norm</code> normalization layers are stacked upon the truncated CNN building up a <code>B-CNN</code> extractor <code>net</code>.

A linear classifier netc is also created for classification. The classifier consists in a full-connected layer of size [mapSize1\*mapSize2, numClass] followed by a softmaxloss layer.

The training step 1 is to train this classifier <code>netc</code> . Once the training completes, <code>netc</code> will be stacked upon <code>net</code> building up a complete B-CNN model available for training step 2.

#### 3.5 Analysizing the code of training step 1.

The traning step 1 is performed by initializeNetworkSharedWeights.m.

```
% initializeNetworkSharedWeights.m
    % get bcnn feature for train and val sets
    train = find(imdb.images.set==1|imdb.images.set==2);
        . . .
        % compute and cache the bilinear cnn features
        for t=1:batchSize:numel(train)
            batch = train(t:min(numel(train), t+batchSize-1));
            [im, labels] = getBatchFn(imdb, batch) ;
            netInit = net;
            net.layers{end}.class = labels ;
            res = [] ;
            res = vl_bilinearnn(netInit, im, [], res, ...
                'accumulate', false, ...
                'mode', 'test', ...
                'conserveMemory', true, ...
                'sync', true, ...
                'cudnn', opts.cudnn);
            codeb = squeeze(gather(res(end).x));
            for i=1:numel(batch)
                code = codeb(:,i);
                savefast(fullfile(opts.nonftbcnnDir, ['bcnn_nonft_', num2str(batch(i), '%05d')]), 'cod
e');
            end
        end
    end
```

```
bcnndb = imdb;
tempStr = sprintf('%05d\t', train);
tempStr = textscan(tempStr, '%s', 'delimiter', '\t');
bcnndb.images.name = strcat('bcnn_nonft_', tempStr{1}');
bcnndb.images.id = bcnndb.images.id(train);
bcnndb.images.label = bcnndb.images.label(train);
bcnndb.images.set = bcnndb.images.set(train);
bcnndb.imageDir = opts.nonftbcnnDir;

%train logistic regression
[netc, info] = cnn_train(netc, bcnndb, @getBatch_bcnn_fromdisk, opts.inittrain, ...
'conserveMemory', true);
end
...
```

For each image in training and validation set, this code block extracts a bilinear feature from it using network net . Given a batch of images, the v1\_bilinearnn here computes a bilinear feature for each of the images repectively.

The dataset boundb used for training network neto is then built up from these bilinear features. The training is performed by function cnn\_train .

#### 3.6 The code of training step 2.

Training step 2 is performed by bcnn\_train\_simplenn or bcnn\_train\_dag as indicated by the following code block:

```
% /path/to/bcnn/imdb_bcnn_train_dag.m
if simplenn
    fn_train = getBatchSimpleNNWrapper(train_bopts) ;
    fn_val = getBatchSimpleNNWrapper(val_bopts) ;
    [net,info] = bcnn_train_simplenn(net, imdb, fn_train, fn_val, opts.train, 'conserveMemory', true)
   net = net_deploy(net) ;
    saveNetwork(fullfile(opts.expDir, 'fine-tuned-model', 'final-model.mat'), net, info);
else
    fn_train = getBatchDagNNWrapper(train_bopts, useGpu) ;
    fn_val = getBatchDagNNWrapper(val_bopts, useGpu) ;
    opts.train = rmfield(opts.train, {'sync', 'cudnn'}) ;
    [net, info] = bcnn_train_dag(net, imdb, fn_train, fn_val, opts.train) ;
    net = net_deploy(net) ;
    save(fullfile(opts.expDir, 'fine-tuned-model', 'final-model.mat'), 'net', 'info', '-v7.3');
end
. . .
```

The function bcnn\_train\_simplenn is modified from cnn\_train of **MatConvNet**, which implementes the SGD algorithm for training a simple network.

The function bcnn\_train\_dag is modified from cnn\_train\_dag of **MatConvNet**, which implementes the SGD algorithm for training a complex network.

#### 3.7 Additional training step.

Once training step 2 is done, the fine-tuning is said to be done. However, there should be one additional training step to train the whole network combining the training and validation dataset.

In this step, authors of the paper chop off the softmax classifier, i.e., netc in initializeNetworkSharedWeights, and replace it with a set of linear SVMs. After this additional training step, the test set had been left out is used for evaluating the accuracy of the final model.

Note that training SVMs in this additional step consumes more than 32GB main memory of CPU.

#### 3.8 Miscellaneous

- v1\_bilinearnn is modified from v1\_simplenn of MatConvNet and implementes both the forward pass and backward pass of a network.
- imdb\_get\_batch is used for fetching a batch of examples along with labels from dataset \*.imdb . The output batch is ready to be passed to v1\_bilinearnn for training or validation.
- run\_experiments is used for training SVMs after training step 2.

# 4. [Paper] Separating Style and Content with Bilinear Models

Joshua B. Tenenbaum et al, Neural Computation 2000

# 5. Revised B-CNN model — Weighted Bilinear-CNN (WB-CNN) model.

#### 5.1 Intuitions on the bilinear model.

#### 5.2 Revised bilinear model.

$$Y = X_a^T W X_b,$$

where

$$X_a \in R^{P_a \times CH_a}, \ X_b \in R^{P_b \times CH_b}, \ W \in R^{P_a \times P_b}, \ Y \in R^{CH_a \times CH_b}$$

The derivatives w.r.t  $X_a$ ,  $X_b$ , and W are

$$\begin{array}{ll} \bullet & \nabla_{X_a}Z = WX_b \cdot (\nabla_YZ)^T \;, & \text{(size: } P_a \times P_b \cdot P_b \times CH_b \cdot CH_b \times CH_a = P_a \times CH_a \quad ) \\ \bullet & \nabla_{X_b}Z = W^TX_a \cdot (\nabla_YZ) \;, & \text{(size: } P_b \times P_a \cdot P_a \times CH_a \cdot CH_a \times CH_b = P_b \times CH_b \quad ) \\ \bullet & \nabla_WZ = X_a \cdot (\nabla_YZ) \cdot X_b^T \;, & \text{(size: } P_a \times CH_a \cdot CH_a \times CH_b \cdot CH_b \times P_b = P_a \times P_b \quad ) \end{array}$$

#### 5.3 Application

Considering two sets of feature maps output from some CNNs with sizes  $W_a \times H_a \times CH_a$  and  $W_b \times H_b \times CH_b$  respectively. The model can be applied easily by reshaping them to  $(W_a * H_a) \times CH_a$  and  $(W_b * H_b) \times CH_b$ .

#### 5.4 Add a self-defined layer vl\_weightedbilinearpool to matconvnet

1. Define the layer vl\_weightedbilinearpool.m

The first step to add a self-defined layer to matconvnet is to define a function implementing the layer's functionalities of 'feed forward' and 'back propagation' with given inputs. '

The following is what the vl\_weightedbilinearpool.m may look like.

```
function [y, varargout] = vl_weightedbilinearpool(x1, x2, W, varargin)
   % VL_WEIGHTEDBILINEARPOOL implementes the revised bilinear model with a weights matrix
   % Copyright (C) 2016 Jincheng Su @ Hikvision.
    % All rights reserved.
   % * **Feed forward**
   %
               * Input: `x1` and `x2`, with shapes `[h1, w1, ch1, bs]` and `[h2, w2, ch2, bs]`.
    %
                                                    `W`, the weights
              * Output: `y`, with shape `[ch1*ch2, bs]`.
   %
   % * **Back propagation**
    %
               * Input: `x1`, `x2` and `W` are the same as in forward pass,
   %
                                                   dzdy = varargin\{1\}, is the derivative of loss `z` w.r.t `y`.
                 * Output: y, the derivative of loss `z` w.r.t `x1`, i.e., dzdx1.
   %
    %
                                                       varargout\{1\} = y2, the derivative of loss `z` w.r.t `x2`, i.e., dzdx2.
                                                       varargout{2} = dw, the derivative of loss `z` w.r.t `W`, i.e., dzdW.
    % The revised B-CNN model
   %
  % $$ Y = X_a^TWX_b,$$
  %
  % where $I$ is an identity matrix and
                      x_a \in R^{P_a \times P_b}, x_b \in R^{P_b \times P_b}, x_b \in R^{P_b \times P_b}, x_b \in R^{P_a \times P_b}, x_b \in R^{P_b \times P_b}
in R^{CH_a\times CH_b}$$
  % The derivatives w.r.t $X_a$, $X_b$, and $W$ are
   % * \Lambda_{Z} = WX_b \cdot (\lambda_YZ)^T, $---$(size: $P_a\times P_b \cdot P_b\times CH_b\
cdot CH_b \times CH_a = P_a \times CH_a
 % * \alpha_{X_b}Z = W^TX_a \cdot (nabla_YZ) , $$\sim (size: $P_b \times P_a \cdot Ch_a)
\cdot CH_a \times CH_b = P_b \times CH_b
  % * \hat{X} = X_a \cdot (\lambda_y) \cdot X_b^T. $~~~$(size: $P_a\times CH_a \cdot CH_a\times CH_a\times CH_a\times CH_a\times CH_a\times CH_a\times CH_a\times CH_a\times CH_a\times CH_a\tim
es CH_b \cdot CH_b
 -----
   % flag for doing backward pass
    isBackward = numel(varargin) > 0 && ~isstr(varargin{1});
    if isBackward
                  dzdy = vararqin{1};
    end
    % if GPU is used
    gpuMode = isa(x1, 'gpuArray');
    % [height, widht, channels, batchsize]
    [h1, w1, ch1, bs] = size(x1);
    [h2, w2, ch2, \sim] = size(x2);
    if ~isBackward
                  % forward pass
                  if gpuMode
                                y = gpuArray(zeros([1, 1, ch1 * ch2, bs], 'single'));
                                y = zeros([1, 1, ch1 * ch2, bs], 'single');
                   end
                  for b = 1: bs
                                Xa = reshape(x1(:,:,:,b), [h1 * w1, ch1]);
                                 Xb = reshape(x2(:,:,:,b), [h2 * w2, ch2]);
```

```
y(1, 1, :, b) = reshape(Xa'*W*Xb, [1, ch1 * ch2]); %'
    end
else
    % backward pass
    if gpuMode
        y1 = gpuArray(zeros(h1, w1, ch1, bs, 'single'));
        y2 = gpuArray(zeros(h2, w2, ch2, bs, 'single'));
        dw = gpuArray(zeros(h1*w1, h2*w2, 'single'));
    else
       y1 = (zeros(h1, w1, ch1, bs, 'single'));
        y2 = (zeros(h2, w2, ch2, bs, 'single'));
        dw = (zeros(h1*w1, h2*w2, 'single'));
    end
    for b = 1: bs
        dZdY = reshape(dzdy(1, 1, :, b), [ch1, ch2]);
       Xa = reshape(x1(:,:,:,b), [h1 * w1, ch1]);
       Xb = reshape(x2(:,:,:,b), [h2 * w2, ch2]);
        dZdXa = reshape(W*Xb*dZdY', [h1, w1, ch1]);
        dZdXb = reshape(W'*Xa*dZdY, [h2, w2, ch2]);
        dZdW = Xa*dZdY*Xb'; %'
       y1(:, :, ;, b) = dZdXa;
       y2(:, :, :, b) = dZdXb;
        dw = dw + dZdW;
    end
    y = y1;
    varargout{1} = y2;
    varargout{2} = dw / bs;
end
```

2. Register the layer to vl\_simplenn.m .

Since I always hold the belief of never changing the source code easily, I would leave  $vl\_simplenn.m$  untouched but rather revise its alternative  $vl\_bilinearnn.m$ .

\$ cp /path/to/bcnn/bcnn-package/vl\_bilinearnn.m /path/to/bcnn/bcnn-package/vl\_bilinearnn.m\_bak \$ gvim /path/to/bcnn/bcnn-package/vl\_bilinearnn.m

```
% vl_bilinearnn.m
    % forward pass
        case 'pdist'
          res(i+1) = vl_nnpdist(res(i).x, 1.p, 'noRoot', 1.noRoot, 'epsilon', 1.epsilon);
        case 'bilinearpool'
          res(i+1).x = vl_nnbilinearpool(res(i).x);
        case 'bilinearclpool'
         x1 = res(1.layer1+1).x;
         x2 = res(1.layer2+1).x;
          res(i+1).x = vl_nnbilinearclpool(x1, x2);
        \% this is my layer. As a first try, I simply assume the input `x1` and `x2` are the sam
        case 'weightedbilinearpool'
          res(i+1).x = vl_weightedbilinearpool(res(i).x, res(i).x, l.weights{1});
        case 'sqrt'
          res(i+1).x = vl_nnsqrt(res(i).x, 1e-8);
        case '12norm'
          res(i+1).x = vl_nnl2norm(res(i).x, 1e-10);
```

```
case 'custom'
     % backward pass
         case 'bilinearclpool'
             x1 = res(1.layer1+1).x;
             x2 = res(1.layer2+1).x;
             [y1, y2] = vl_nnbilinearclpool(x1, x2, res(i+1).dzdx);
             res(1.layer1+1).dzdx = updateGradient(res(1.layer1+1).dzdx, y1);
             res(1.layer2+1).dzdx = updateGradient(res(1.layer2+1).dzdx, y2);
         % this is my layer. As a first try, I simply assume the input `x1` and `x2` are the sam
         case 'weightedbilinearpool'
             [y1, y2, dzdw{1}] = v1_weightedbilinearpool(res(i).x, res(i).x, 1.weights{1}, res(i).x
+1).dzdx);
             res(i).dzdx = updateGradient(res(i).dzdx, y1 + y2);
             clear y1 y2
         case 'sqrt'
             backprop = vl_nnsqrt(res(i).x, 1e-8, res(i+1).dzdx);
             res(i).dzdx = updateGradient(res(i).dzdx, backprop);
             clear backprop
     . . .
     % Add our type.
     switch 1.type
         case {'conv', 'convt', 'bnorm', 'weightedbilinearpool'}
             if ~opts.accumulate
                 res(i).dzdw = dzdw ;
             else
                 for j=1:numel(dzdw)
                     res(i).dzdw{j} = res(i).dzdw{j} + dzdw{j} ;
             end
         end
         dzdw = [];
     end
```

3. Our work of adding a layer to matconvnet is almost done. However, one another small revision is indispensable for enabling our layer run on a GPU unbuggly when using v1\_bilinearnn.m . That is, add our layer to the v1 simplenn move.m .

```
% /path/to/bcnn/matconvnet/matlab/simplenn/vl_simplenn_move.m
for l=1:numel(net.layers)
    switch net.layers{1}.type
        case {'conv', 'convt', 'bnorm', 'weightedbilinearpool'}
        for f = {'filters', 'biases', 'filtersMomentum', 'biasesMomentum'}
```

#### 5.5 Build our WB-CNN model for training.

Now that we have added a self-defined layer with type <code>weightedbilinearpool</code> to <code>matconvnet</code> , we need to build a network to test if it works correct or if it ever works. I'll do it by revised the <code>B-CNN</code> model.

As a first try, let's implementes a simple symmetric wb-cnn , which can be built easily by replace the bilinearpool layer of a symmetric b-cnn with our weightedbilinearpool layer.

1. Modify initializeNetworkSharedWeights.m

```
$ cp /path/to/bcnn/initializeNetworkSharedWeights.m /path/to/bcnn/initializeNetworkWeightedBcnn
.m
$ gvim /path/to/bcnn/initializeNetworkWeightedBcnn.m
```

```
% initializeNetworkWeightedBcnn.m
     % build a linear classifier netc
     netc.layers = {};
     h1 = 27;
     w1 = 27;
     bilinearW = 0.001/scal * randn(h1*w1, h1*w1, 'single');
     % stack weighted bilinearpool layer
     netc.layers{end+1} = struct('type', 'weightedbilinearpool', 'name', 'wblp', ...
         'weights',{{bilinearW}} , ...
         'learningRate', [1000], ...
         'weightDecay', [0.9]);
     % stack a dropout layer, `rate` is defined as a probability of a varaiable not to be zeroed
     netc.layers{end+1} = struct('type', 'dropout', 'name', 'dropout_wbcnn',...
         'rate', 0.3);
     % stack a relu layer
     netc.layers{end+1} = struct('type', 'relu', 'name', 'relu6');
     % stack normalization
     netc.layers{end+1} = struct('type', 'sqrt', 'name', 'sqrt_norm');
     netc.layers{end+1} = struct('type', 'l2norm', 'name', 'l2_norm');
     % stack classifier layer
     initialW = 0.001/scal * randn(1,1,ch1*ch2,numClass,'single');
     initialBias = init_bias.*ones(1, numClass, 'single');
     netc.layers{end+1} = struct('type', 'conv', 'name', 'classifier', ...
         'weights', {{initialW, initialBias}}, ...
         'stride', 1, ...
         'pad', 0, ...
         'learningRate', [1000 1000], ...
         'weightDecay', [0 0]);
     netc.layers{end+1} = struct('type', 'softmaxloss', 'name', 'loss') ;
     netc = vl_simplenn_tidy(netc) ;
                 codeb = squeeze(gather(res(end).x));
                 for i=1:numel(batch)
                      code = codeb(:, :, :, i);
     %
                      code = reshape(codeb(:, :, :, i), size(codeb, 1)*size(codeb, 2), size(code
b, 3));
                     savefast(fullfile(opts.nonftbcnnDir, ['bcnn_nonft_', num2str(batch(i), '%05
d')]), 'code');
                 end
             end
         end
     . . .
     function [im,labels] = getBatch_bcnn_fromdisk(imdb, batch)
     imtmp = cell(1, numel(batch));
     for i=1:numel(batch)
         load(fullfile(imdb.imageDir, imdb.images.name{batch(i)}));
         imtmp{i} = code;
```

```
end
h = size(imtmp{1}, 1);
w = size(imtmp{1}, 2);
ch = size(imtmp{1}, 3);
im = zeros(h, w, ch, numel(batch));
for i = 1:numel(batch)
    im(:, :, :, i) = imtmp{i};
end
clear imtmp
%im = cat(2, im{:});
%im = reshape(im, size(im, 1), size(im, 2), size(im, 3), size(im, 4));
labels = imdb.images.label(batch);
```

```
res = vl_simplenn(net, im, dzdy, res, ...
%
%
                         'accumulate', s \sim= 1, ...
%
                         'mode', evalMode, ...
%
                         'conserveMemory', params.conserveMemory, ...
                         'backPropDepth', params.backPropDepth, ...
%
                         'sync', params.sync, ...
%
%
                         'cudnn', params.cudnn, ...
%
                         'parameterServer', parserv, ...
%
                         'holdOn', s < params.numSubBatches) ;
     res = vl_bilinearnn(net, im, dzdy, res, ...
                      'accumulate', s ~= 1, ...
                       'mode', evalMode, ...
                       'conserveMemory', params.conserveMemory, ...
                       'backPropDepth', params.backPropDepth, ...
                       'sync', params.sync, ...
                       'cudnn', params.cudnn) ;
```