

2.1

9.

$$5A = 5 \begin{bmatrix} 1 & -2 & 5 \\ 4 & 4 & 8 \\ -3 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 5 & -10 & 25 \\ 20 & 20 & 40 \\ -15 & 5 & 0 \end{bmatrix}$$

$$0.25B = 0.25 \begin{bmatrix} 5 & 2 & 0 \\ -5 & 3 & -4 \\ -4 & 2 & -4 \end{bmatrix} = \begin{bmatrix} 1.25 & 0.5 & 0 \\ -1.25 & 0.75 & -1 \\ -1 & 0.5 & -1 \end{bmatrix}$$

$$5A + 0.25B = \begin{bmatrix} 5 & -10 & 25 \\ 20 & 20 & 40 \\ -15 & 5 & 0 \end{bmatrix} + \begin{bmatrix} 1.25 & 0.5 & 0 \\ -1.25 & 0.75 & -1 \\ -1 & 0.5 & -1 \end{bmatrix} = \begin{bmatrix} 6.25 & -9.5 & 25 \\ 18.75 & 20.75 & 39 \\ -16 & 5.5 & -1 \end{bmatrix}$$

$$\downarrow$$

$$5A + 0.25B + C = \begin{bmatrix} 6.25 & -9.5 & 25 \\ 18.75 & 20.75 & 39 \\ -16 & 5.5 & -1 \end{bmatrix} + \begin{bmatrix} 6 & -2 \\ 2 & -4 \\ 0 & -1 \end{bmatrix} \quad \begin{array}{l} \text{행과 열의 값이 일치하기} \\ \text{않아 연산이 불가능.} \end{array}$$

11.

$$6C + 8D = 6 \begin{bmatrix} 6 & -2 \\ 2 & -4 \\ 0 & -1 \end{bmatrix} + 8 \begin{bmatrix} -3 & 1 \\ 2 & 0 \\ -1 & 2 \end{bmatrix} = \begin{bmatrix} 36-24 & -12+8 \\ 12+16 & -24+0 \\ 0-8 & -6+16 \end{bmatrix}$$

$$= \begin{bmatrix} 12 & -4 \\ 28 & -24 \\ -8 & 10 \end{bmatrix}$$

$$2(3C + 4D) = 6C + 8D = \begin{bmatrix} 12 & -4 \\ 28 & -24 \\ -8 & 10 \end{bmatrix}$$

$$0.4C - 0.4D = 0.4 \begin{bmatrix} 6 & -2 \\ 2 & -4 \\ 0 & -1 \end{bmatrix} - 0.4 \begin{bmatrix} -3 & 1 \\ 2 & 0 \\ -1 & 2 \end{bmatrix} = \begin{bmatrix} 2.4+1.2 & -0.8-0.4 \\ 0.8-0.8 & -1.6-0 \\ 0+0.4 & -0.4-0.8 \end{bmatrix}$$

$$\swarrow$$

$$0.4(C-D) = 0.4C - 0.4D = \begin{bmatrix} 3.6 & -1.2 \\ 0 & -1.6 \\ 0.4 & -1.2 \end{bmatrix} = \leftarrow$$

13.

$$(3 \cdot 5)C = 15 \begin{bmatrix} 6 & -2 \\ 2 & -4 \\ 0 & -1 \end{bmatrix} = \begin{bmatrix} 90 & -30 \\ 15 & -60 \\ 0 & -15 \end{bmatrix}$$

$$3(5C) = 15C = \begin{bmatrix} 90 & -30 \\ 15 & -60 \\ 0 & -15 \end{bmatrix}$$

$$-D + 0 \cdot E = - \begin{bmatrix} -3 & 1 \\ 2 & 0 \\ -1 & 2 \end{bmatrix} + 0 \cdot \begin{bmatrix} 2 & 0 \\ -4 & 3 \\ -3 & 1 \end{bmatrix} = \begin{bmatrix} 3 & -1 \\ -2 & 0 \\ 1 & -2 \end{bmatrix}$$

$E - D + C + U =$ U는 C, D, E와 다르게 행과 열의 수가 달라 연산을 할 수 없다.

15.

$$(U+V)-W = \begin{bmatrix} 1.2 \\ 0 \\ -2.5 \end{bmatrix} + \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix} - \begin{bmatrix} -4 \\ -10 \\ 8 \end{bmatrix} = \begin{bmatrix} (1.2+2)+4 \\ (0-1)+10 \\ (-2.5+3)-8 \end{bmatrix} = \begin{bmatrix} 7.2 \\ 9 \\ -7.5 \end{bmatrix}$$

$$U + (V - W) = \begin{bmatrix} 7.2 \\ 9 \\ -7.5 \end{bmatrix} \rightarrow \text{괄호는 이 연산에서 영향을 주지 못해 위와 같다.}$$

$$C + 0W = \begin{bmatrix} 6 & -2 \\ 2 & -4 \\ 0 & -1 \end{bmatrix} + 0 \cdot \begin{bmatrix} -4 \\ -10 \\ 8 \end{bmatrix} = \begin{bmatrix} 6 & -2 \\ 2 & -4 \\ 0 & -1 \end{bmatrix} \text{ 정의를 따라 않는다.}$$

$$0 \cdot E + U - V = 0 \cdot \begin{bmatrix} 2 & 0 \\ -4 & 3 \\ -3 & 1 \end{bmatrix} + \begin{bmatrix} 1.2 \\ 0 \\ -2.5 \end{bmatrix} - \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix} = \begin{bmatrix} 1.2-2 \\ 0-(-1) \\ -2.5-3 \end{bmatrix} = \begin{bmatrix} -0.8 \\ 1 \\ -5.5 \end{bmatrix} \text{ 정의를 따라 않는다.}$$

\rightarrow 0을 곱하는 단계. 해당 값이 0이 되는 거지 행과 열이 사라지는 건 아니네.

7.3.

3

$$\begin{aligned}
 8y + 6z &= -4 \\
 -2x + 4y - 6z &= 18 \\
 x + y - z &= 2
 \end{aligned}
 \Rightarrow
 \begin{bmatrix}
 0 & 8 & 6 & -4 \\
 -2 & 4 & -6 & 18 \\
 1 & 1 & -1 & 2
 \end{bmatrix}$$

$$\rightarrow
 \begin{bmatrix}
 1 & 1 & -1 & 2 \\
 0 & 8 & 6 & -4 \\
 -2 & 4 & -6 & 18
 \end{bmatrix}
 \begin{array}{l}
 \text{--- ①} \\
 \text{--- ②}
 \end{array}
 \xrightarrow{\text{①} \times 2 + \text{②}}
 \begin{bmatrix}
 1 & 1 & -1 & 2 \\
 0 & 8 & 6 & -4 \\
 0 & 6 & -8 & 22
 \end{bmatrix}
 \begin{array}{l}
 \text{--- ③} \\
 \text{--- ④}
 \end{array}$$

← 이차리치 대입

$$\begin{aligned}
 \text{③} \times 3 + \text{④} \times 4 &\rightarrow \begin{array}{r} 0 \quad 24 \quad 18 \quad -12 \\ -20 \quad 24 \quad -32 \quad 88 \\ \hline 0 \quad 0 \quad 50 \quad -100 \end{array} \times \frac{1}{50} \\
 &= (0 \quad 0 \quad 50 \quad -100)
 \end{aligned}$$

$$\rightarrow
 \begin{bmatrix}
 1 & 1 & -1 & 2 \\
 0 & 8 & 6 & -4 \\
 0 & 0 & 1 & -2
 \end{bmatrix}
 \begin{array}{l}
 -1z = -2, \quad 8y + 6z = -4, \quad x + y - z = 2. \\
 \boxed{z = -2, \quad y = 1, \quad x = -1}
 \end{array}$$