

$$\underbrace{f(\theta)}_{\text{obj}} = \begin{cases} ab \left[ \frac{\theta}{2} \right] & \|v\| \geq 1 \\ \int_{\mathcal{M}} r \, d\theta & \text{else} \end{cases}$$