

# Assignment 1

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## Exercise 4: recursive estimation and optimization of $\lambda$

Write the update equations for  $R_\epsilon$  and  $\hat{\Theta}_\epsilon$ !

$$R_0 = 0.1 \cdot I_2 \quad \Theta = 0 \in \mathbb{R}^2 \quad X_1^T = (1 \quad 2018)$$

$$X_2^T \approx (1 \quad 2018.84) \quad y_1 = 2930483 \quad y_2 = 2934044$$

~~~~~ without forgetting / (exponential) weight matrix

$$\hat{\Theta}_\epsilon = (X_\epsilon^T X_\epsilon)^{-1} X_\epsilon^T y_\epsilon = R_\epsilon^{-1} h_\epsilon$$

$$R_t = R_{t-1} + X_t X_t^T$$

$$\Rightarrow R_1 = R_0 + X_1 X_1^T = 0.1 I_2 + \begin{pmatrix} 1 \\ 2018 \end{pmatrix} (1 \quad 2018) = \begin{pmatrix} 1.1 & 2018.1 \\ 2018.1 & 4072324 \end{pmatrix}$$

$$\Rightarrow R_2 = R_1 + X_2 X_2^T = \begin{pmatrix} 1.1 & 2018.1 \\ 2018.1 & 4072324 \end{pmatrix} + \begin{pmatrix} 1 \\ 2018.84 \end{pmatrix} (1 \quad 2018.84)$$

$$\approx \begin{pmatrix} 2.1 & 4036.94 \\ 4036.94 & 8144384.3403 \end{pmatrix}$$