

1.

$$A = \{1, 2, 4, 8, 15, 31, 46\}$$

$$B = \{6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16$$

$$17, 18, 19, 20, 21, 22, 23, 24, 25\}$$

$$C = \{-3, 0, 3, 6, 9, 12, 15, 18, 21, 24, 27, 30\}$$

$$D = \{7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47\}$$

Solution

$$\bullet (B \cap C) = \{6, 9, 12, 15, 18, 21, 24\}$$

$$(A \oplus D) = \{1, 2, 4, 7, 8, 11, 13, 15, 17, 19, 23, 29, 37, 41, 43, 46, 47\}$$

$$(B \cap C) \cup (A \oplus D) = \{1, 2, 4, 6, 7, 8, 9, 11, 12, 13, 15, 17, 18, 19, 21, 23, 24, 37, 41, 43, 46, 47\}$$

$$\bullet (B \oplus C) = \{-3, 0, 3, 7, 8, 10, 11, 13, 14, 16, 17, 19, 20, 22, 23, 25, 27, 30\}$$

$$(B - C) = \{7, 8, 10, 11, 13, 14, 16, 17, 19, 20, 22, 23, 25\}$$

$$(A \cup (B - C)) = \{1, 2, 4, 7, 8, 10, 11, 13, 14, 15, 16, 17, 19, 20, 22, 23, 25, 31, 46\}$$

$$(B \oplus C) \oplus (A \cup (B - C)) = \{-3, 0, 1, 2, 3, 4, 15, 27, 30, 31, 46\}$$

$$(C-B) = \{-3, 0, 3, 27, 30\}$$

$$(A \cap D) = \{31\}$$

$$((C-B) \oplus (A \cap D)) = \{-3, 0, 3, 27, 30, 31\}$$

$$(A \cup B \cup C) = \{-3, 0, 1, 2, 3, 4, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 27, 30, 31, 46\}$$

$$((C-B) \oplus (A \cap D)) \cap (A \cup B \cup C) =$$

$$\{-3, 0, 3, 27, 30\}$$

2. $(S, +, \cdot, ', 0, 2)$

$$+ \rightarrow (x+y) \% 4$$

$$\cdot \rightarrow (x * y) / 4$$

$$x' = 2 - x$$

Ley de idempotencia

$$\cdot x + x = x$$

$$(0+0) \% 4 = 0 \quad \checkmark$$

$$(2+2) \% 4 = 0 \quad \times \quad 0 \neq 2$$

3.

3.

• Primera iteración

$$\sinh(\pi/3) = \pi/3 = 1.047197551$$

• Segunda iteración

$$\sinh(\pi/3) = \pi/3 + \frac{(\pi/3)^3}{3!} = 1.238594321$$

$$\text{Error}_a = \left| \frac{1.238594321 - 1.047197551}{1.238594321} \right| = \frac{19.1\%}{15.45\%}$$

• Tercera iteración

$$\sinh(\pi/3) = \pi/3 + \frac{(\pi/3)^3}{3!} + \frac{(\pi/3)^5}{5!} = 1.24908823$$

$$\text{Error}_a = 0.84\%$$

• Cuarta iteración

$$\sinh(\pi/3) = \pi/3 + \frac{(\pi/3)^3}{3!} + \frac{(\pi/3)^5}{5!} + \frac{(\pi/3)^7}{7!} = 1.2493628$$

$$\text{Error}_a = 0.0219\%$$

✓