Master Thesis Experiment Report III : Inlet Architecture

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Abstract

Assessment of different input structures in the Lattice-Boltzmann system array.

1 Context

In this experiment, we will try different architectures for the inlet section of the system. As a recall from previous Experiment reports the inlet missing values (input into the system) are calculated following Zu-He method.

2 Problem

We have different possible architectures for the corners of the inlet border : either make the corners inlets or leave them as bounceback nodes.

3 Experiments

To assess the corner cases, we constructed a small 7x5 system with bounceback nodes on the top and bottom borders, an obstacle in the middle, the inlet on the right border and the inlet on the left border. Both cases are illustrated in Figures 1 and 2. The input velocity is a parabola (which corresponds to the expected velocity profile for a tube LB system). We will be running the simulation through 100 iterations.

We will monitor the PDFs of the whole system throughout the simulation, as well as the horizontal and vertical velocity of each lattice site for the following experiments. All the results have been compiled into two separate text files. The structure of the file for the second case is illustrated in figure 3

3.1 Experiment 1

3.1.1 Description

The first experiment follows the system illustrated in figure 1. Only the 3 centered leftmost nodes are defined as inlets. The execution is as in previous tests following the Zu-he method.

3.1.2 Results

The results have been compiled in a provided file.

3.2 Experiment 2

3.2.1 Description

The second experiment follows the system illustrated in figure 2. For this case, the corners have to be treated separately from the rest. The directions of the PDFs incoming for each lattice site are illustrated in Figure 4. The two corners have five missing directions: for the top left corner, we are missing the incoming PDfs of directions 0,1,2,5,8, and for the bottom left corner, we are missing the

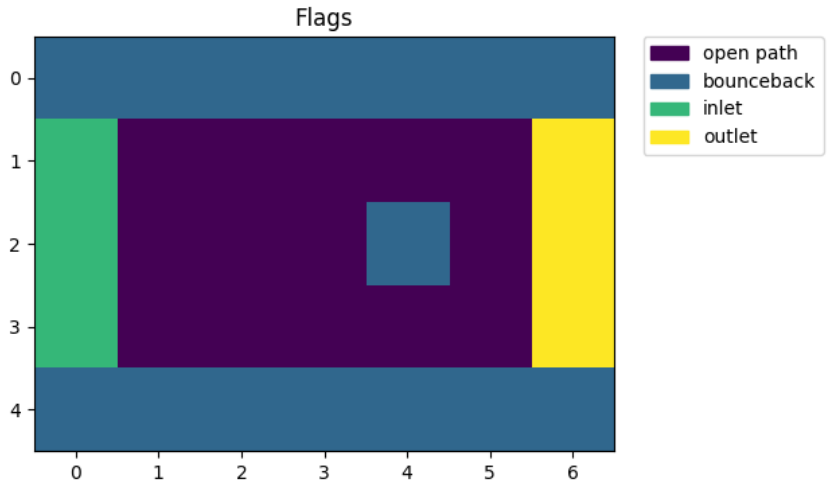

Figure 1: Corners as bounceback nodes

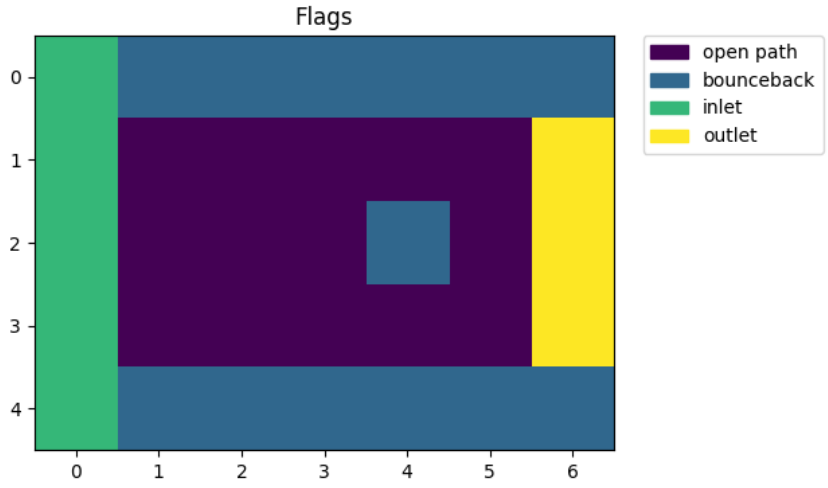

Figure 2: Corners as inlet nodes

PDFs of directions 0,1,2,3,6.

The issue with the Zu-he method here is that we can only compute 3 missing directions of incoming PDFs. Instead, we artificially defined the missing directions for the corners. For example, for the upper corner, as illustrated in Figure 5, we compute the missing PDfs for the lattice site (0;1). We then take the values obtained and paste them in the missing directions of site (0;0). Figure 5 shows where the direction has been copied. To recall, $fin(i, x, y)$ is the PDFs input for a lattice site of coordinate (x;y) at direction i. The filled arrows show the PDFs calculated with Zu-He, and the dotted arrows show where the values have been copied. The colors indicate where every copied direction has been taken.

3.2.2 Results

4 Results

The results have been compiled in a provided file.

```
MaxIter : 100, system size : [7x5]

System :

[[2. 1. 1. 1. 1. 1. 1.]
 [2. 0. 0. 0. 0. 0. 3.]
 [2. 0. 0. 0. 1. 0. 3.]
 [2. 0. 0. 0. 0. 0. 3.]
 [2. 1. 1. 1. 1. 1. 1.]]

0 = open path, 1 = BB, 2 = inlet, 3 = outlet

Directions for respectively fin & fout :

2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   |  6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0
1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   |  7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1
0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   |  8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2

2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   |  6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0
1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   |  7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1
0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   |  8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2

2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   |  6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0
1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   |  7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1
0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   |  8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2

2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   |  6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0
1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   |  7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1
0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   |  8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2

2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   2 5 8   |  6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0   6 3 0
1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   1 4 7   |  7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1   7 4 1
0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   0 3 6   |  8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2   8 5 2

Horizontal Velocity                                                    | Vertical Velocity

u[0,0,0]  u[0,1,0]  u[0,2,0]  u[0,3,0]  u[0,4,0]  u[0,5,0]  u[0,6,0]   |  u[1,0,0]  u[1,1,0]  u[1,2,0]  u[1,3,0]  u[1,4,0]  u[1,5,0]  u[1,6,0]

u[0,0,1]  u[0,1,1]  u[0,2,1]  u[0,3,1]  u[0,4,1]  u[0,5,1]  u[0,6,1]   |  u[1,0,1]  u[1,1,1]  u[1,2,1]  u[1,3,1]  u[1,4,1]  u[1,5,1]  u[1,6,1]

u[0,0,2]  u[0,1,2]  u[0,2,2]  u[0,3,2]  u[0,4,2]  u[0,5,2]  u[0,6,2]   |  u[1,0,2]  u[1,1,2]  u[1,2,2]  u[1,3,2]  u[1,4,2]  u[1,5,2]  u[1,6,2]

u[0,0,3]  u[0,1,3]  u[0,2,3]  u[0,3,3]  u[0,4,3]  u[0,5,3]  u[0,6,3]   |  u[1,0,3]  u[1,1,3]  u[1,2,3]  u[1,3,3]  u[1,4,3]  u[1,5,3]  u[1,6,3]

u[0,0,4]  u[0,1,4]  u[0,2,4]  u[0,3,4]  u[0,4,4]  u[0,5,4]  u[0,6,4]   |  u[1,0,4]  u[1,1,4]  u[1,2,4]  u[1,3,4]  u[1,4,4]  u[1,5,4]  u[1,6,4]
```

Figure 3: File structure for corners as inlet

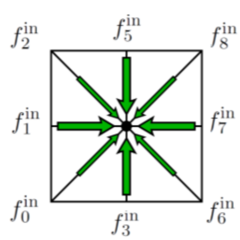

Figure 4: Directional PDFs input in a D2Q9 lattice, **Source :** [1]

5 Conclusion

6 References

[1] Jonas Lätt. "La méthode de Boltzmann sur réseau pour la simulation des fluides". In: ().

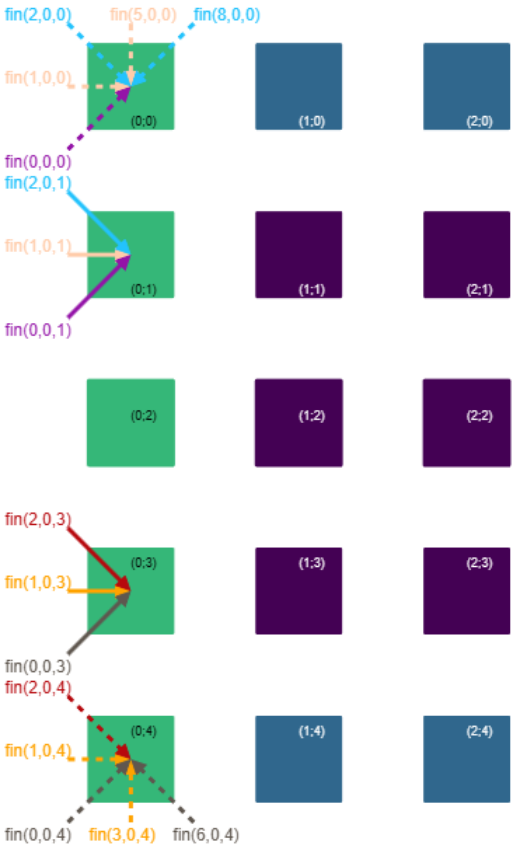

Figure 5: PDfs for the missing corners