DATA 624 PROJECT 2: Regression modeling - PH prediction

DATA 624 - Predictive Analytics Group 2

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Introduction

The goal of this project is to predict PH, a measure of acidity/alkalinity, using train data set from a beverage company which consists of 2571 rows of data and 33 variables. After creating models based on training data, we will test on scoring set of 267 rows with 32 variables (excluding target variable which is PH in our training set)

As a group project, each member of the group is responsible for creating their own models of choice. For instance, my own selections were PLS and Bagged Tree. However, the choice of models can be altered after careful review of data exploration it may require different type of model in case data suffers from outliers or any other data related issues.

Explaining why some necessary steps were applied before modeling and model A was preferred to Model B is often a topic in academic papers which is a meaningful topic that helps audience learn the concept of bagged regression and least square method better

The final version of report will contain all of our approaches with results of MAPE for each model with detailed explanation of why/what/how each model of choice was constructed.

1 Data Exploration

Data dictionary

The table below describes the variables in the train data set.

Table 1.1: Data dictionary

| Name | Туре | MD code | Length | Measurement Type | Excluded |
|-------------------|--------|------------|--------|-------------------|-------------|
| Test Time | Double | -9999 | 8 | m/d/yy h:mm Am/Pm | Auto |
| Brand Code | Double | -9999 | 8 | General | Categorical |
| Carb Volume | Double | -9999 | 8 | General | Auto |
| Fill Ounces | Double | -9999 | 8 | General | Auto |
| PC Volume | Double | -9999 | 8 | General | Auto |
| Carb Pressure | Double | -9999 | 8 | General | Auto |
| Carb Temp | Double | -9999 | 8 | General | Auto |
| PSC | Double | -9999 | 8 | General | Auto |
| PSC Fill | Double | -9999 | 8 | General | Auto |
| PSC CO2 | Double | -9999 | 8 | General | Auto |
| Mnf Flow | Double | -9999 | 8 | General | Auto |
| Carb Pressure1 | Double | -9999 | 8 | General | Auto |
| Fill Pressure | Double | -9999 | 8 | General | Auto |
| Hyd Pressure1 | Double | -9999 | 8 | General | Auto |
| Hyd Pressure2 | Double | -9999 | 8 | General | Auto |
| Hyd Pressure3 | Double | -9999 | 8 | General | Auto |
| Hyd Pressure4 | Double | -9999 | 8 | General | Auto |
| Filler Level | Double | -9999 | 8 | General | Auto |
| Filler Speed | Double | -9999 | 8 | General | Auto |
| Temperature | Double | -9999 | 8 | General | Auto |
| Usage cont | Double | -9999 | 8 | General | Auto |
| Carb Flow | Double | -9999 | 8 | General | Auto |
| Density | Double | -9999 | 8 | General | Auto |
| MFR | Double | -9999 | 8 | General | Auto |
| Balling | Double | -9999 | 8 | General | Auto |
| Pressure Vacuum | Double | -9999 | 8 | General | Auto |
| PH | Double | -9999 | 8 | General | Auto |
| Oxygen Filler | Double | -9999 | 8 | General | Auto |
| Bowl Setpoint | Double | -9999 | 8 | General | Auto |
| Pressure Setpoint | Double | -9999 | 8 | General | Auto |
| Air Pressurer | Double | -9999 | 8 | General | Auto |
| Alch Rel | Double | -9999 | 8 | General | Auto |
| Carb Rel | Double | -9999 | 8 | General | Auto |
| Balling Lvl | Double | -9999 | 8 | General | Auto |
| sample | Double | -999999998 | 8 | General | Auto |

Summary statistics

Since we are implementing models which do not require hard assumptions of joint distribution of variables, normality assumption is not required. We will focus on how to handle missing values only.

It is apparent, from below, that we have variables that are missing values - we will impute NULLs with MICE later on.

Table 1.2: Summary statistics

| metric | missing | min | Q1 | mean | median | Q3 | max | sd |
|------------------|---------|--------------|--------------|--------------|--------------|-------------|----------|--------------|
| AirPressurer | 0 | 140.8000000 | 142.2000000 | 142.8339946 | 142.6000000 | 143.000000 | 148.200 | 1.2119170 |
| AlchRel | 9 | 5.2800000 | 6.5400000 | 6.8974161 | 6.5600000 | 7.240000 | 8.620 | 0.5052753 |
| Balling | 1 | -0.1700000 | 1.4960000 | 2.1977696 | 1.6480000 | 3.292000 | 4.012 | 0.9310914 |
| BallingLvl | 1 | 0.0000000 | 1.3800000 | 2.0500078 | 1.4800000 | 3.140000 | 3.660 | 0.8703089 |
| BowlSetpoint | 2 | 70.0000000 | 100.0000000 | 109.3265862 | 120.0000000 | 120.000000 | 140.000 | 15.3031541 |
| CarbFlow | 2 | 26.0000000 | 1144.0000000 | 2468.3542234 | 3028.0000000 | 3186.000000 | 5104.000 | 1073.6964743 |
| CarbPressure | 27 | 57.0000000 | 65.6000000 | 68.1895755 | 68.2000000 | 70.600000 | 79.400 | 3.5382039 |
| CarbPressure1 | 32 | 105.6000000 | 119.0000000 | 122.5863726 | 123.2000000 | 125.400000 | 140.200 | 4.7428819 |
| CarbRel | 10 | 4.9600000 | 5.3400000 | 5.4367825 | 5.4000000 | 5.540000 | 6.060 | 0.1287183 |
| CarbTemp | 26 | 128.6000000 | 138.4000000 | 141.0949234 | 140.8000000 | 143.800000 | 154.000 | 4.0373861 |
| CarbVolume | 10 | 5.0400000 | 5.2933333 | 5.3701978 | 5.3466667 | 5.453333 | 5.700 | 0.1063852 |
| Density | 1 | 0.2400000 | 0.9000000 | 1.1736498 | 0.9800000 | 1.620000 | 1.920 | 0.3775269 |
| FillerLevel | 20 | 55.8000000 | 98.3000000 | 109.2523716 | 118.4000000 | 120.000000 | 161.200 | 15.6984241 |
| FillerSpeed | 57 | 998.0000000 | 3888.0000000 | 3687.1988862 | 3982.0000000 | 3998.000000 | 4030.000 | 770.8200208 |
| FillOunces | 38 | 23.6333333 | 23.9200000 | 23.9747546 | 23.9733333 | 24.026667 | 24.320 | 0.0875299 |
| FillPressure | 22 | 34.6000000 | 46.0000000 | 47.9221656 | 46.4000000 | 50.000000 | 60.400 | 3.1775457 |
| HydPressure1 | 11 | -0.8000000 | 0.0000000 | 12.4375781 | 11.4000000 | 20.200000 | 58.000 | 12.4332538 |
| HydPressure2 | 15 | 0.0000000 | 0.0000000 | 20.9610329 | 28.6000000 | 34.600000 | 59.400 | 16.3863066 |
| HydPressure3 | 15 | -1.2000000 | 0.0000000 | 20.4584507 | 27.6000000 | 33.400000 | 50.000 | 15.9757236 |
| HydPressure4 | 30 | 52.0000000 | 86.0000000 | 96.2888627 | 96.0000000 | 102.000000 | 142.000 | 13.1225594 |
| MFR | 212 | 31.4000000 | 706.3000000 | 704.0492582 | 724.0000000 | 731.000000 | 868.600 | 73.8983094 |
| MnfFlow | 2 | -100.2000000 | -100.0000000 | 24.5689373 | 65.2000000 | 140.800000 | 229.400 | 119.4811263 |
| OxygenFiller | 12 | 0.0024000 | 0.0220000 | 0.0468426 | 0.0334000 | 0.060000 | 0.400 | 0.0466436 |
| PCVolume | 39 | 0.0793333 | 0.2391667 | 0.2771187 | 0.2713333 | 0.312000 | 0.478 | 0.0606953 |
| PH | 4 | 7.8800000 | 8.4400000 | 8.5456486 | 8.5400000 | 8.680000 | 9.360 | 0.1725162 |
| PressureSetpoint | 12 | 44.0000000 | 46.0000000 | 47.6153966 | 46.0000000 | 50.000000 | 52.000 | 2.0390474 |
| PressureVacuum | 0 | -6.6000000 | -5.6000000 | -5.2161027 | -5.4000000 | -5.000000 | -3.600 | 0.5699933 |
| PSC | 33 | 0.0020000 | 0.0480000 | 0.0845737 | 0.0760000 | 0.112000 | 0.270 | 0.0492690 |
| PSCCO2 | 39 | 0.0000000 | 0.0200000 | 0.0564139 | 0.0400000 | 0.080000 | 0.240 | 0.0430387 |
| PSCFill | 23 | 0.0000000 | 0.1000000 | 0.1953689 | 0.1800000 | 0.260000 | 0.620 | 0.1177817 |
| Temperature | 14 | 63.6000000 | 65.2000000 | 65.9675401 | 65.6000000 | 66.400000 | 76.200 | 1.3827783 |
| Usagecont | 5 | 12.0800000 | 18.3600000 | 20.9929618 | 21.7900000 | 23.755000 | 25.900 | 2.9779364 |

Since Brand code is categorical, creating summary statistics was not possible. Instead, we implemented table summary of the distribution of each value. Note that we are missing 120 values.

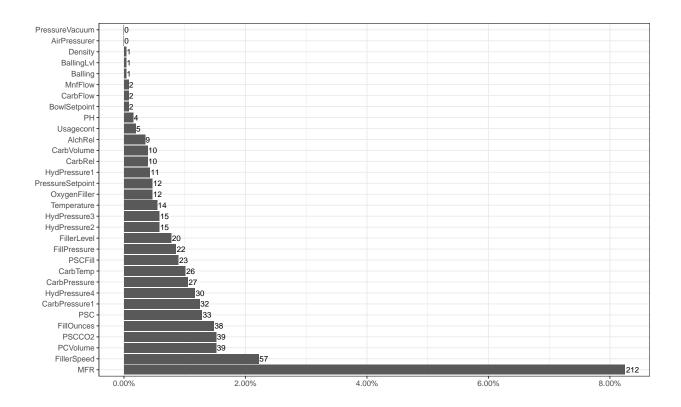
Table 1.3: Frequency distribution of BrandCode

| Var1 | Freq |
|------|------|
| Α | 293 |
| В | 1239 |
| С | 304 |
| D | 615 |
| NA | 120 |

Visualizations

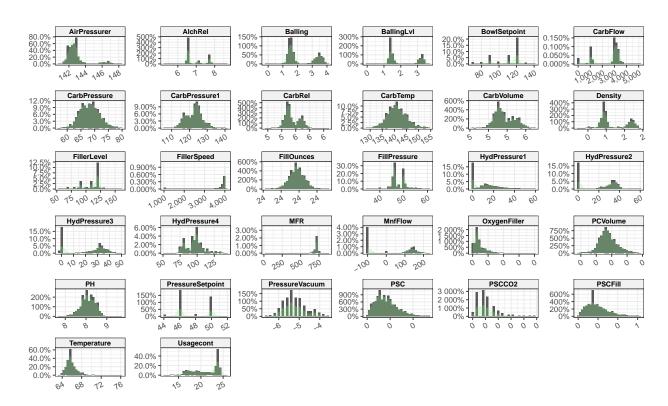
Missing data

With the help of visualization, it is easier to navigate how much each variable is missing. Note that MFR is the most missing variable.



Univariate distributions

We notice that there are some variables such as Temperature and Oxygen Filler that are highly positively skewed. There are potentials of presence of outliers for skewed variables.



As we expected, there are many outliers in Temperature and Oxygen Filler. Note that MFR greatly suffers from the presence of outliers.

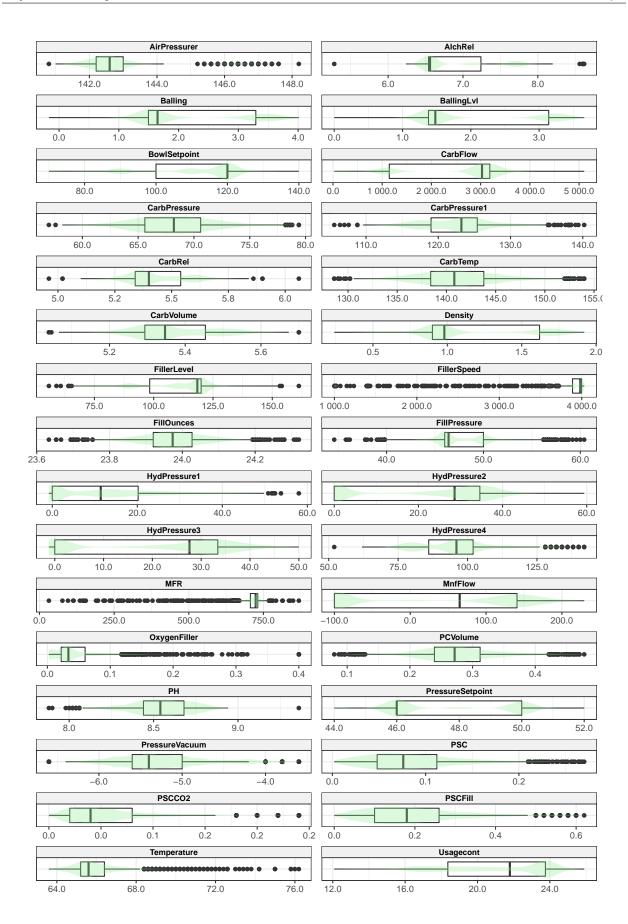
From the presence of multiple outliers, we then have to explain why/what/how we revise our initial model choice of Bagged Tree and apply necessary adjustment before applying PLS.

Ensembled model such as Random Forest is robust to outliers since only a subset of features are selected at random out of the total and the best split feature from the subset is used to split each node in a tree, unlike in bagging where all features are considered for splitting a node and this makes Random Forest a good altrenative for Bagged Tree.

Partial least squares regression (PLS regression) is used as an alternative for ordinary least squares regression in the presence of multicollinearity. This does not mean, however, PLS is robust to outliers. Thus, we will use Blocked Adaptive Computationally-Efficient Outlier Nominators (BACON) to eliminate outliers and then apply PLS.

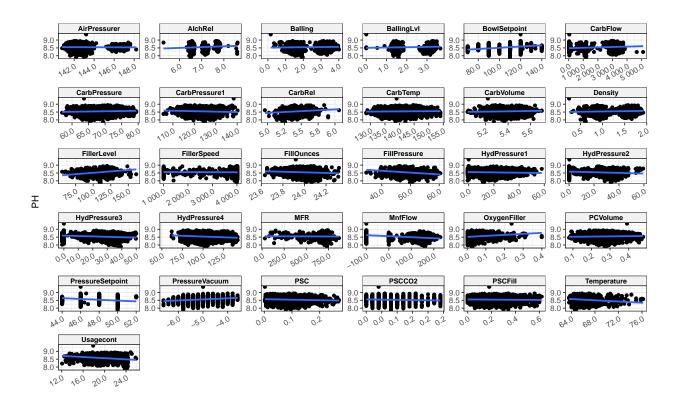
Reference:

(https://www.hindawi.com/journals/jam/2018/7696302/ - "PLS regression is sensitive to outliers and leverages. Thus several robust versions have been proposed in the literature, but only for linear PLS. Hubert [7] proposed two robust versions of the SIMPLS algorithm by using a robust estimation for the variance-covariance matrix. Kondylis and Hadi [8] used the BACON algorithm to eliminate outliers, resulting in a robust linear PLS.")



Bivariate relationships

Note that when Oxygen Filler has fairly positive relationship with PH, Temparature has negative relationship. We confirmed the relationships between predictors and target variable.

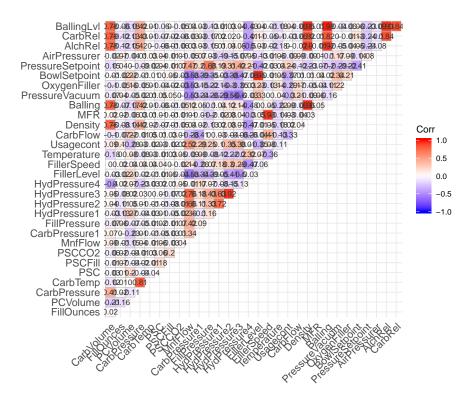


Correlation Matrix

We confirmed that there are several highly correlated predictors. This is another reason why Random Forest would be more preferred to Bagged Tree model. In fact, Random Forest is more robust to strong correlation than Bagged Tree. Although multicollinearity is not a big problem for for PLS and Random Forest, it can cause some problem when it comes to inferring the importance of certain predictors in tree model. Multicollinearity means that some predictors are shown as highly correlated with other combinications of predictors in variable importance. According to the reference, it may mislead business audience to think that some features are not more important than others vice-versa. However, we really do not know whether the reader of this paper would still treat highly correlated variable such as HydPressure3 different from HydPressure2 or not. Thus, we will just keep the variables as they are.

Reference:

("For example, the two surface area predictors have an extremely high correlation (0.96) and each is used in the tree shown in Fig. 8.4. It is possible that the small difference between these predictors is strongly driving the choice between the two, but it is more likely to be due to small, random differences in the variables. Because of this, more predictors may be selected than actually needed. In addition, the variable importance values are affected. If the solubility data only contained one of the surface area predictors, then this predictor would have likely been used twice in the tree, therefore inflating its importance value. Instead, including both surface area predictors in the data causes their importance to have only moderate values." Page 181 of Applied Predictive Modeling - Max KJ)



2 Data preparation

Before modeling can be done, the issues identified during the data exploration, namely, zero variance predictors, outliers and missing data need to be addressed. For BACON (outlier handling method) approach, categorical variable needs to be converted to numeric.

Imputation

After reviewing a few methods of multiple imputation techniques, Multiple Imputation Chained Equations (MICE) was selected for its strength in handling imputation for observations with more than one predictor missing. For categorical variable such as Brand Code will be imputed by mode. For BACON to work, we will also convert Brand Code to numeric.

We will also remove zero variance Predictors using nearZeroVar. It diagnoses predictors that have one unique value (i.e. are zero variance predictors) or predictors that are have both of the following characteristics: they have very few unique values relative to the number of samples and the ratio of the frequency of the most common value to the frequency of the second most common value is large.

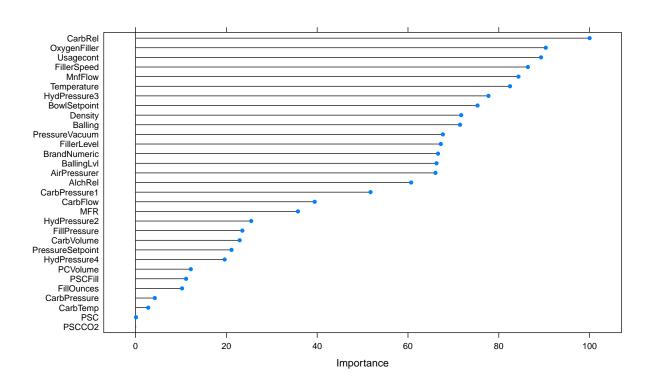
For outlier handling, BACON is used. BACON, short for 'Blocked Adaptive Computationally-Efficient Outlier Nominators', is a somewhat robust algorithm (set), with an implementation for regression or multivariate covariance estimation. The function produces index with TRUE or FALSE to identify rows with outliers. This index will be used as subset to train outlier free train set in the process of hyper-parameter tuning in train function and train the final model using full train set without removing outliers after being applied with best hyper-parameters.

3 Modeling

Model 1: Bagged Tree with BACON

Table 3.1: Model Summary - Bagged Tree with BACON

| RMSE | Rsquared | MAPE |
|-----------|-----------|-----------|
| 0.1198618 | 0.4922456 | 0.0106783 |

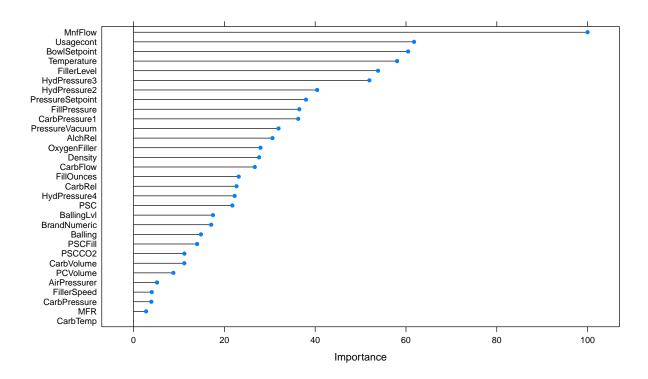


MAPE is 0.0106783 where as top 3 important predictors are CarbRel, OxygenFiler and Usuagecont. Since Bagged Tree uses all features for splitting a node Unlike Random Forest which uses only a subset of features at random out of the total for splitting each node in a tree, the order of feature importances between two models can be quite different.

Model 2: PLS with BACON

Table 3.2: Model Summary - PLS with BACON

| | RMSE | Rsquared | MAPE |
|----|-----------|-----------|-----------|
| 10 | 0.1327207 | 0.3740444 | 0.0123968 |



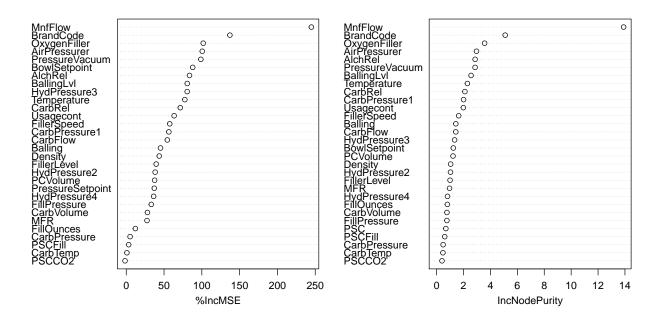
The final value used for the model was ncomp = 10. MAPE is 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968, 0.0123968 where as top 3 important predictors are MnfFlow, Usuagecont and BowlSetpoint. The order of variable importance, again, is quite different from Bagged Tree as PLS is not a tree-based model. Note that PLS is a dimension reduction technique with some similarity to principal component analysis. The predictor variables are mapped to a smaller set of variables and within that smaller space we perform a regression against the outcome variable. In contrast to principal component analysis where the dimension reduction ignores the outcome variable, the PLS procedure aims to choose new mapped variables that maximally explain the outcome variable.

Model 3: Random Forest with original data set

Table 3.3: Model Summary - RF with original data set

| RMSE | Rsquared | MAPE |
|-----------|-----------|-----------|
| 0.0969916 | 0.6909936 | 0.0081279 |

rf_model2



The final value used for the model was ncomp = 10. MAPE is 0.0081279 where as top 3 important predictors are MnfFlow, BrandCode and PressureVacuum for %incMSE and MnfFlow, BrandCode and OxygenFiller for IncNodePurity. Unlike PLS, Random Forest can produce 2 different variable importance plots.

The first graph shows that if a variable is assigned values by random permutation by how much will the MSE increase. The second plot is based on node purity which is measured by Gini Index and it is the the difference between RSS before and after the split on that variable. In short, each graph shows how much MSE or Impurity increases when each variable is randomly permuted.

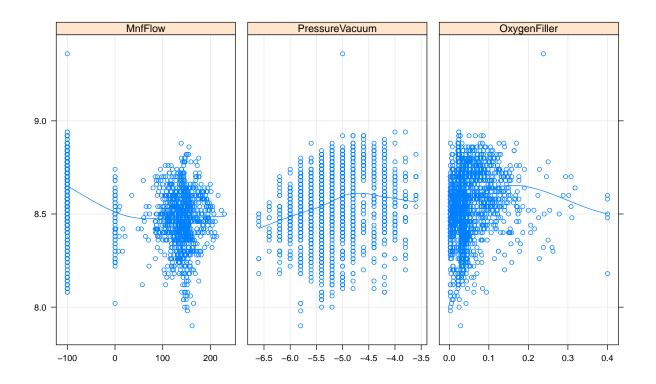
4 Evaluation

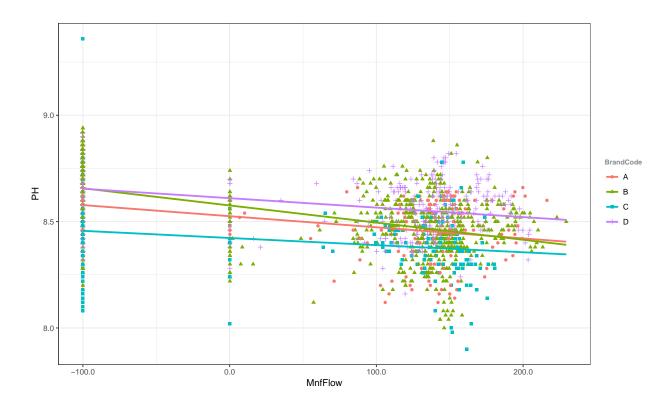
Table 4.1: Evaluation Summary on test set

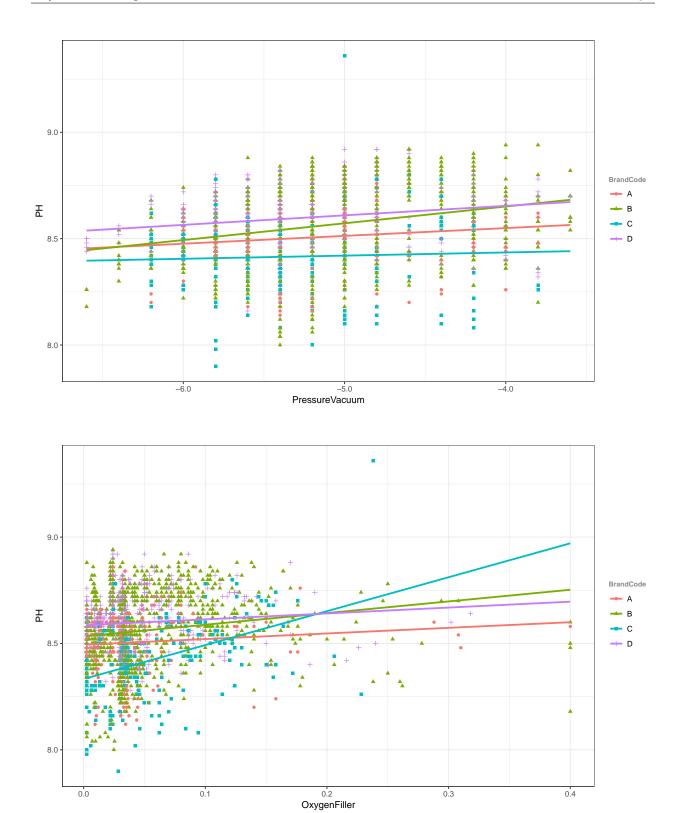
| MODEL | RMSE | Rsquare | MAPE |
|-------------|-----------|-----------|-----------|
| Bagged Tree | 0.1235554 | 0.5047507 | 0.0111408 |
| PLS - BACON | 0.1358493 | 0.3862047 | 0.0122273 |
| RF | 0.0883145 | 0.7449339 | 0.0075050 |

From the table, we confirmed that Random Forest is a clear winner with the lowest MAPE on test set.

Insight & Conclusion







We graphed top 4 most important variables from varImp of MSE and NodePurity. Given that Brand Code is categorical, we grouped 3 continous variables into Brand Code.

The first feature plot shows that 3 continous variables have very weak relationship with PH. MnfFlow has slight negative relation-

ship where as PressureVacuum and OxygenFiller have slight positive relationship.

From grouping by Brand Code, we see that for PH vs MnfFlow and PH vs PressureVacuum, it seems like predictors have the most negative relationship with PH with code = B. For PH vs OxygenFiller, code = C seems to have the most negative relationship with PH.

We can recommend business users to put more attention on increasing MnfFlow or decreasing PressureVacuum (especially code = B for both) and OxygenFiller (especially code = C) than any other predictors if their goal is to decrease PH.

Prediction

Let's export the prediction values of Random Forest (the best model) on StudentEvaluation as CSV file.

Appendix

```
library(tidyverse)
library(readxl)
library(psych)
library(ggplot2)
library(mice)
library(xtable)
library(GGally)
library(ggstance)
library(grid)
library(gridExtra)
library(ggpubr)
library(caret)
library(data.table)
library(recipes)
library(Metrics)
library(randomForest)
library(robustX)
                         # BACON
library(ggcorrplot)
                        # Vis corr matrix
library(e1071)
                         # Misc stats functions
df <- read_excel('C:/Users/ahwang/Desktop/Cuny/DATA624/project2/data/StudentData.xlsx')</pre>
df_eval <- read_excel('C:/Users/ahwang/Desktop/Cuny/DATA624/project2/data/StudentEvaluation.xlsx')</pre>
dict <- read excel('C:/Users/ahwang/Desktop/Cuny/DATA624/project2/data/DataDictionary.xlsx')</pre>
# remove space in-between variable names
colnames(df) <- gsub(" ","",colnames(df))</pre>
# Introduction {-#intro}
# Data Exploration
## Data dictionary
kable(dict, caption="Data dictionary", booktabs=T)%>%kable_styling()%>%row_spec()
## Summary statistics
# Create a table summarizing the training data
```

```
# create lists of desired summary stats for calculation
statFuns <-
  funs(missing = sum(is.na(.))
       , min = min(., na.rm = TRUE)
       , Q1 = quantile(., .25, na.rm = TRUE)
       , mean = mean(., na.rm = TRUE)
       , median = median(., na.rm = TRUE)
       , Q3 = quantile(., .75, na.rm = TRUE)
       , max = max(., na.rm = TRUE)
       , sd = sd(., na.rm = TRUE)
       , mad = mad(., na.rm = TRUE)
       , skewness = skewness(., na.rm = TRUE)
       , kurtosis = kurtosis(., na.rm = TRUE)
  )
# Create data frame of basic summary stats
dfSumTrain <-
  df %>%
  # union(dfEval %>% mutate(TARGET_WINS = as.numeric(NA))) %>%
  dplyr::select(-`BrandCode`) %>%
  summarise_all(statFuns) %>%
  gather() %>%
  separate(key, c('metric', 'stat'), sep = '(_)(?!.*_)') %>%
  spread(stat, value) %>%
  dplyr::select(metric, names(statFuns))
dfSumTrain %>% kable(caption="Summary statistics", booktabs=T)%>%kable styling()%>%row spec()
table(df$`BrandCode`, useNA = "ifany")%>%kable(caption="Frequency distribution of BrandCode", booktabs=
## Visualizations
### Missing data
dfSumTrain %>%
  group_by(metric) %>%
  mutate(miss_perc = missing / !!nrow(df)) %>%
  dplyr::select(metric, missing, miss_perc) %>%
  ggplot(data = ., aes(x = reorder(metric, -miss_perc) , y = miss_perc)) +
  geom_bar(stat = 'identity') +
  coord_flip() +
  geom_text(aes(label = missing), hjust = -0.1, size = 3) +
  labs(x = NULL, y = NULL, Title = '% Missing') +
  theme bw() +
 theme(legend.position = 'none') +
  scale_y_continuous(labels = scales::percent)
### Univariate distributions
df %>%
  # union(dfEval %>% mutate(TARGET_WINS = as.numeric(NA))) %>%
  dplyr::select(-BrandCode) %>%
  gather() %>%
```

```
group_by(key) %>%
  ggplot(data = ., aes(value)) +
  geom_histogram(bins = 30, aes(y = ..density..)) +
  geom_density(alpha = 0.3, color = NA, fill = 'lightgreen') +
  scale_x_continuous(labels = scales::comma) +
  scale_y_continuous(labels = scales::percent) +
  facet_wrap(~key, scales = 'free') +
  labs(x = NULL, y = NULL) +
  theme bw() +
  theme(axis.text.x = element_text(angle = 30, hjust = 1))
df %>%
  # union(dfEval %>% mutate(TARGET_WINS = as.numeric(NA))) %>%
  dplyr::select(-BrandCode) %>%
  gather() %>%
  group_by(key) %>%
  ggplot(data = ., aes(x = '', y = value)) +
  geom_boxplot() +
  geom_violin(alpha = 0.3, color = NA, fill = 'lightgreen') +
  labs(x = NULL, y = NULL) +
  theme_bw() +
  theme(axis.ticks.y=element_blank()) +
  facet_wrap(~key, scales = 'free', ncol = 2) +
  coord_flip()
### Bivariate relationships
df %>%
  dplyr::select(-BrandCode) %>%
  gather(key, value, -PH) %>%
  group_by(key) %>%
  ggplot(data = ., aes(x = value, y = PH)) +
  geom_point() +
  geom_smooth(method = 'gam') +
  facet_wrap(~key, scales = 'free') +
  labs(x = NULL) +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 30, hjust = 1))
### Correlation Matrix
# Calculate pairwise pearson correlation and display as upper matrix plot
df %>%
  # union(dfEval %>% mutate(TARGET WINS = as.numeric(NA))) %>%
 dplyr::select(-c('BrandCode','PH')) %>%
  cor(method = 'pearson', use = 'pairwise.complete.obs') %>%
  ggcorrplot(corr = ., method = 'square', type = 'upper'
             , lab = TRUE, lab_size = 3, lab_col = 'grey20')
# Data preparation
## Imputation
# set seed for split to allow for reproducibility
```

```
set.seed(58677)
# use mice w/ default settings to impute missing data
miceImput <- mice(df, printFlag = FALSE)</pre>
# add imputed data to original data set
df_mice <- complete(miceImput)</pre>
df mice$BrandCode[is.na(df mice$BrandCode)] <- 'B'</pre>
#table(df_mice$BrandCode, useNA = "ifany")
# Look for any features with no variance:
zero_cols <- nearZeroVar( df_mice )</pre>
df final <- df mice[,-zero cols] # drop these zero variance columns
df_final$BrandCode <- as.factor(df_final$BrandCode)</pre>
# convert categorical factor into numeric
M <- df_final
must_convert<-sapply(M,is.factor) # logical vector telling if a variable needs to be displayed as numer
BrandNumeric <- sapply(M[,must_convert],unclass) # data.frame of all categorical variables now displ
df_final2<-cbind(M[,!must_convert],BrandNumeric)</pre>
                                                           # complete data.frame with all variables put to
# split data train/test
# df for random forest
training <- df_final$PH %>%createDataPartition(p = 0.8, list = FALSE)
df_train <- df_final[training, ]</pre>
df_test <- df_final[-training, ]</pre>
# df for PLS and Bagging
training2 <- df_final2$PH %>%createDataPartition(p = 0.8, list = FALSE)
df_train2 <- df_final2[training2, ]</pre>
df_test2 <- df_final2[-training2, ]</pre>
# X and y split for BACON fit
x <- subset(df_train2, select = -c(PH) )</pre>
x <- as.matrix(x)</pre>
y <- df_train2[, c('PH')]
bacon_fit \leftarrow BACON(x = x, y = y)
# Modeling
## Model 1: Bagged Tree with BACON
set.seed(58677)
bagged_model <- train( PH~., data = df_train2, method="treebag",</pre>
                        tuneLength=10,
                        subset = bacon_fit$subset,
                        trControl=trainControl(method="cv",number=5) )
# create MAPE table
train_bag_pred <- predict(bagged_model)</pre>
bagged_model$results$MAPE <- Metrics::mape(df_train2$PH, train_bag_pred)
```

```
bagged_model$results[,c(2,3,8)]%>%kable(caption="Model Summary - Bagged Tree with BACON", booktabs=T)%>
# plot varImp
plot(varImp(bagged_model))
## Model 2: PLS with BACON
set.seed(58677)
df_final2$BrandNumeric <- as.factor(df_final2$BrandNumeric)</pre>
pls_model <- train( PH~., data = df_train2, method="pls",</pre>
                    tuneLength=10,
                    subset = bacon fit$subset,
                    preProcess=c("center","scale"), trControl=trainControl(method="cv",number=5) )
# create MAPE table
train_pls_pred <- predict(pls_model)</pre>
pls_model$results$MAPE <- Metrics::mape(df_train2$PH, train_pls_pred)</pre>
pls_model$results[10,c(2,3,8)]%>%kable(caption="Model Summary - PLS with BACON", booktabs=T)%>%kable_st
# plot varImp
plot(varImp(pls_model))
## Model 3-1: Random Forest with BACON
# set.seed(58677)
# rf_model <- train( PH~., data = df_train2, method="rf",
                      tuneLength=10,
#
                      subset = bacon_fit$subset,
#
                      importance = TRUE,
#
                      trControl=trainControl(method="cv", number=5) )
# # create MAPE table
# train_rf_pred <- predict(rf_model)</pre>
# rf_model$results$MAPE <- Metrics::mape(df_train2$PH, train_rf_pred)</pre>
# rf_model$results%>%kable(caption="Model Summary - RF with BACON", booktabs=T)%>%kable_styling()%>%row
# # plot varImp
# plot(varImp(rf_model))
# Although `BACON` is not needed for `Random Forest`, it would not bother using it anyway. We will expe
## Model 3: Random Forest with original data set
set.seed(58677)
# Algorithm Tune (tuneRF)
\#bestmtry \leftarrow tuneRF(df\_train[, -25], df\_train[, 25], stepFactor=1.5, improve=1e-5, ntree=2500)
##mtry <- ( (ncol(df_train) -1) / 3 ) or sqrt(ncol(df_train) - 1) # By default, # of predictors / 3 for
```

```
# from above result, we got mtry= 27 and ntree=2500 as optimal parameters
rf_model2 <- randomForest(PH~., data=df_train, method="rf", mtry= 31, importance = TRUE, ntree = 2500)
# create MAPE table
train_rf_pred2 <- predict(rf_model2)</pre>
s <- data.frame(
 RMSE = Metrics::rmse(df_train$PH, train_rf_pred2),
 Rsquared = caret::R2(df_train$PH, train_rf_pred2),
 MAPE = Metrics::mape(df train$PH, train rf pred2) )
s%>%kable(caption="Model Summary - RF with original data set", booktabs=T)%>%kable_styling()%>%row_spec
# plot varImp
varImpPlot(rf_model2)
# Evaluation
# Make predictions
p1 <- bagged_model %>% predict(df_test2)
p2 <- pls_model %>% predict(df_test2)
p3 <- rf_model2 %>% predict(df_test)
# Model performance metrics
sum_t <- data.frame(</pre>
 MODEL = c('Bagged Tree',
            'PLS - BACON',
            'RF'),
  RMSE = c(caret::RMSE(p1, df_test2$PH),
           caret::RMSE(p2, df_test2$PH),
           caret::RMSE(p3, df test$PH) ),
  Rsquare = c(caret::R2(p1, df_test2$PH),
              caret::R2(p2, df_test2$PH),
              caret::R2(p3, df_test$PH)),
 MAPE = c(Metrics::mape(p1, df_test2$PH),
           Metrics::mape(p2, df_test2$PH),
           Metrics::mape(p3, df_test$PH))
)
sum_t%>%kable(caption="Evaluation Summary on test set", booktabs=T)%>%kable_styling()%>%row_spec()
## Insight & Conclusion
# code
top_var <- c('MnfFlow','PressureVacuum', 'OxygenFiller')</pre>
featurePlot(df_train[, top_var],
            df_train$PH,
            plot = "scatter",
            between = list(x = 1, y = 1),
            type = c("g", "p", "smooth"),
            layout = c(3,1),
            labels = rep("", 2))
```

```
\# ggplot(df\_train[df\_train\$BrandCode == 'B',], aes(x=MnfFlow, y=PH, shape=BrandCode, color=BrandCode))
   geom_point()
#
# qqplot(df train[df train$BrandCode == 'A',], aes(x=MnfFlow, y=PH, shape=BrandCode, color=BrandCode))
   geom_point()
\# ggplot(df\_train[df\_train\$BrandCode == 'C',], aes(x=MnfFlow, y=PH, shape=BrandCode, color=BrandCode))
   geom point()
\# qqplot(df\_train[df\_train\$BrandCode == 'D',], aes(x=MnfFlow, y=PH, shape=BrandCode, color=BrandCode))
   geom_point()
ggplot(df_train, aes(x=MnfFlow, y=PH, color=BrandCode, shape=BrandCode)) +
  geom_point() +
  geom_smooth(method=lm, se=FALSE, fullrange=TRUE) +
  theme_bw()+theme()
ggplot(df_train, aes(x=PressureVacuum, y=PH, color=BrandCode, shape=BrandCode)) +
  geom_point() +
  geom_smooth(method=lm, se=FALSE, fullrange=TRUE) +
 theme bw()+theme()
ggplot(df_train, aes(x=0xygenFiller, y=PH, color=BrandCode, shape=BrandCode)) +
  geom point() +
  geom_smooth(method=lm, se=FALSE, fullrange=TRUE) +
  theme bw()+theme()
## Prediction
# remove space in-between variable names
colnames(df_eval) <- gsub(" ","",colnames(df_eval))</pre>
# remove column with zero-variance
set.seed(58677)
# use mice w/ default settings to impute missing data
miceImput2 <- mice(df_eval, printFlag = FALSE)</pre>
# add imputed data to original data set
df mice2 <- complete(miceImput2)</pre>
#table(df_eval$BrandCode, useNA = 'ifany')
df mice2$BrandCode[is.na(df mice2$BrandCode)] <- 'B'</pre>
#table(df_mice$BrandCode, useNA = "ifany")
# Look for any features with no variance:
#zero_cols <- nearZeroVar( df_mice2 )</pre>
df_final22 <- df_mice2[,-zero_cols] # drop these zero variance columns
df_final22$BrandCode <- as.factor(df_final22$BrandCode)</pre>
df_eval2 <- subset(df_eval, select = -PH)</pre>
pred_eval <- predict(rf_model2, subset(df_final22))</pre>
write.csv(pred_eval, 'prediction.csv')
```