

DATA 624 PROJECT 2: Regression modeling - PH prediction

DATA 624 - Predictive Analytics
Group 2

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Introduction

The goal of this project is to predict PH, a measure of acidity/alkalinity, using train data set from a beverage company which consists of 2571 rows of data and 33 variables. After creating models based on training data, we will test on scoring set of 267 rows with 32 variables (excluding target variable which is PH in our training set)

As a group project, each member of the group is responsible for creating their own models of choice. For instance, my own selections were PLS and Bagged Tree. However, the choice of models can be altered after careful review of data exploration - it may require different type of model in case data suffers from outliers or any other data related issues.

Explaining why some necessary steps were applied before modeling and model A was preferred to Model B is often a topic in academic papers which is a meaningful topic that helps audience learn the concept of bagged regression and least square method better.

The final version of report will contain all of our approaches with results of MAPE for each model with detailed explanation of why/what/how each model of choice was chosen.

1 Data Exploration

Data dictionary

The table below describes the variables in the train data set.

Table 1.1: Data dictionary

Name	Type	MD code	Length	Measurement Type	Excluded
Test Time	Double	-9999	8	m/d/yy h:mm Am/Pm	Auto
Brand Code	Double	-9999	8	General	Categorical
Carb Volume	Double	-9999	8	General	Auto
Fill Ounces	Double	-9999	8	General	Auto
PC Volume	Double	-9999	8	General	Auto
Carb Pressure	Double	-9999	8	General	Auto
Carb Temp	Double	-9999	8	General	Auto
PSC	Double	-9999	8	General	Auto
PSC Fill	Double	-9999	8	General	Auto
PSC CO2	Double	-9999	8	General	Auto
Mnf Flow	Double	-9999	8	General	Auto
Carb Pressure1	Double	-9999	8	General	Auto
Fill Pressure	Double	-9999	8	General	Auto
Hyd Pressure1	Double	-9999	8	General	Auto
Hyd Pressure2	Double	-9999	8	General	Auto
Hyd Pressure3	Double	-9999	8	General	Auto
Hyd Pressure4	Double	-9999	8	General	Auto
Filler Level	Double	-9999	8	General	Auto
Filler Speed	Double	-9999	8	General	Auto
Temperature	Double	-9999	8	General	Auto
Usage cont	Double	-9999	8	General	Auto
Carb Flow	Double	-9999	8	General	Auto
Density	Double	-9999	8	General	Auto
MFR	Double	-9999	8	General	Auto
Balling	Double	-9999	8	General	Auto
Pressure Vacuum	Double	-9999	8	General	Auto
PH	Double	-9999	8	General	Auto
Oxygen Filler	Double	-9999	8	General	Auto
Bowl Setpoint	Double	-9999	8	General	Auto
Pressure Setpoint	Double	-9999	8	General	Auto
Air Pressurer	Double	-9999	8	General	Auto
Alch Rel	Double	-9999	8	General	Auto
Carb Rel	Double	-9999	8	General	Auto
Balling Lvl	Double	-9999	8	General	Auto
sample	Double	-999999998	8	General	Auto

Summary statistics

Since we are implementing models which do not require hard assumptions of joint distribution of variables, normality assumption is not required. We will focus on how to handle missing values only.

It is apparent, from below, that we have variables that are missing values - we will impute NULLs with MICE later on.

Table 1.2: Summary statistics

metric	missing	min	Q1	mean	median	Q3	max	sd
AirPressurer	0	140.8000000	142.2000000	142.8339946	142.6000000	143.0000000	148.200	1.2119170
AlchRel	9	5.2800000	6.5400000	6.8974161	6.5600000	7.2400000	8.620	0.5052753
Balling	1	-0.1700000	1.4960000	2.1977696	1.6480000	3.292000	4.012	0.9310914
BallingLvl	1	0.0000000	1.3800000	2.0500078	1.4800000	3.140000	3.660	0.8703089
BowlSetpoint	2	70.0000000	100.0000000	109.3265862	120.0000000	120.0000000	140.000	15.3031541
CarbFlow	2	26.0000000	1144.0000000	2468.3542234	3028.0000000	3186.0000000	5104.000	1073.6964743
CarbPressure	27	57.0000000	65.6000000	68.1895755	68.2000000	70.6000000	79.400	3.5382039
CarbPressure1	32	105.6000000	119.0000000	122.5863726	123.2000000	125.4000000	140.200	4.7428819
CarbRel	10	4.9600000	5.3400000	5.4367825	5.4000000	5.5400000	6.060	0.1287183
CarbTemp	26	128.6000000	138.4000000	141.0949234	140.8000000	143.8000000	154.000	4.0373861
CarbVolume	10	5.0400000	5.2933333	5.3701978	5.3466667	5.4533333	5.700	0.1063852
Density	1	0.2400000	0.9000000	1.1736498	0.9800000	1.6200000	1.920	0.3775269
FillerLevel	20	55.8000000	98.3000000	109.2523716	118.4000000	120.0000000	161.200	15.6984241
FillerSpeed	57	998.0000000	3888.0000000	3687.1988862	3982.0000000	3998.0000000	4030.000	770.8200208
FillOunces	38	23.6333333	23.9200000	23.9747546	23.9733333	24.0266667	24.320	0.0875299
FillPressure	22	34.6000000	46.0000000	47.9221656	46.4000000	50.0000000	60.400	3.1775457
HydPressure1	11	-0.8000000	0.0000000	12.4375781	11.4000000	20.2000000	58.000	12.4332538
HydPressure2	15	0.0000000	0.0000000	20.9610329	28.6000000	34.6000000	59.400	16.3863066
HydPressure3	15	-1.2000000	0.0000000	20.4584507	27.6000000	33.4000000	50.000	15.9757236
HydPressure4	30	52.0000000	86.0000000	96.2888627	96.0000000	102.0000000	142.000	13.1225594
MFR	212	31.4000000	706.3000000	704.0492582	724.0000000	731.0000000	868.600	73.8983094
MnfFlow	2	-100.2000000	-100.0000000	24.5689373	65.2000000	140.8000000	229.400	119.4811263
OxygenFiller	12	0.0024000	0.0220000	0.0468426	0.0334000	0.0600000	0.400	0.0466436
PCVolume	39	0.0793333	0.2391667	0.2771187	0.2713333	0.3120000	0.478	0.0606953
PH	4	7.8800000	8.4400000	8.5456486	8.5400000	8.6800000	9.360	0.1725162
PressureSetpoint	12	44.0000000	46.0000000	47.6153966	46.0000000	50.0000000	52.000	2.0390474
PressureVacuum	0	-6.6000000	-5.6000000	-5.2161027	-5.4000000	-5.0000000	-3.600	0.5699933
PSC	33	0.0020000	0.0480000	0.0845737	0.0760000	0.1120000	0.270	0.0492690
PSCCO2	39	0.0000000	0.0200000	0.0564139	0.0400000	0.0800000	0.240	0.0430387
PSCFill	23	0.0000000	0.1000000	0.1953689	0.1800000	0.2600000	0.620	0.1177817
Temperature	14	63.6000000	65.2000000	65.9675401	65.6000000	66.4000000	76.200	1.3827783
Usagecont	5	12.0800000	18.3600000	20.9929618	21.7900000	23.7550000	25.900	2.9779364

Since Brand code is categorical, creating summary statistics was not possible. Instead, we implemented table summary of the distribution of each value. Note that we are missing 120 values.

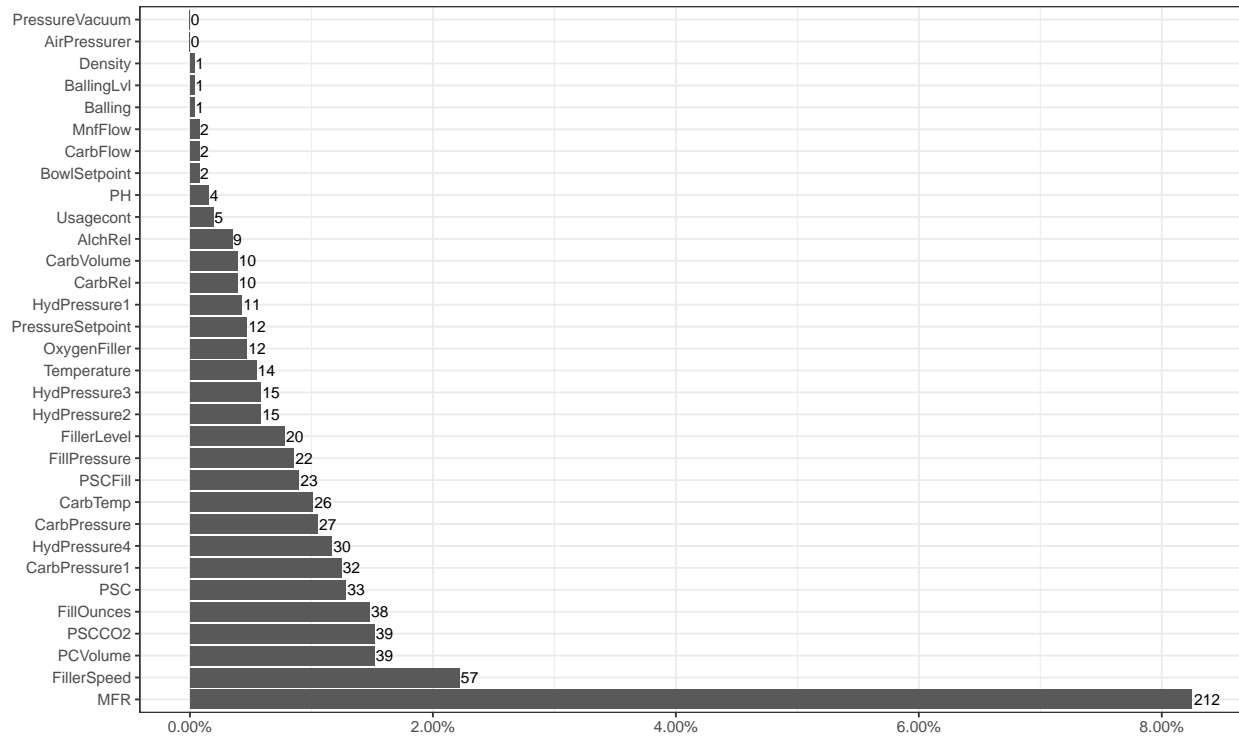
Table 1.3: Frequency distribution of BrandCode

Var1	Freq
A	293
B	1239
C	304
D	615
NA	120

Visualizations

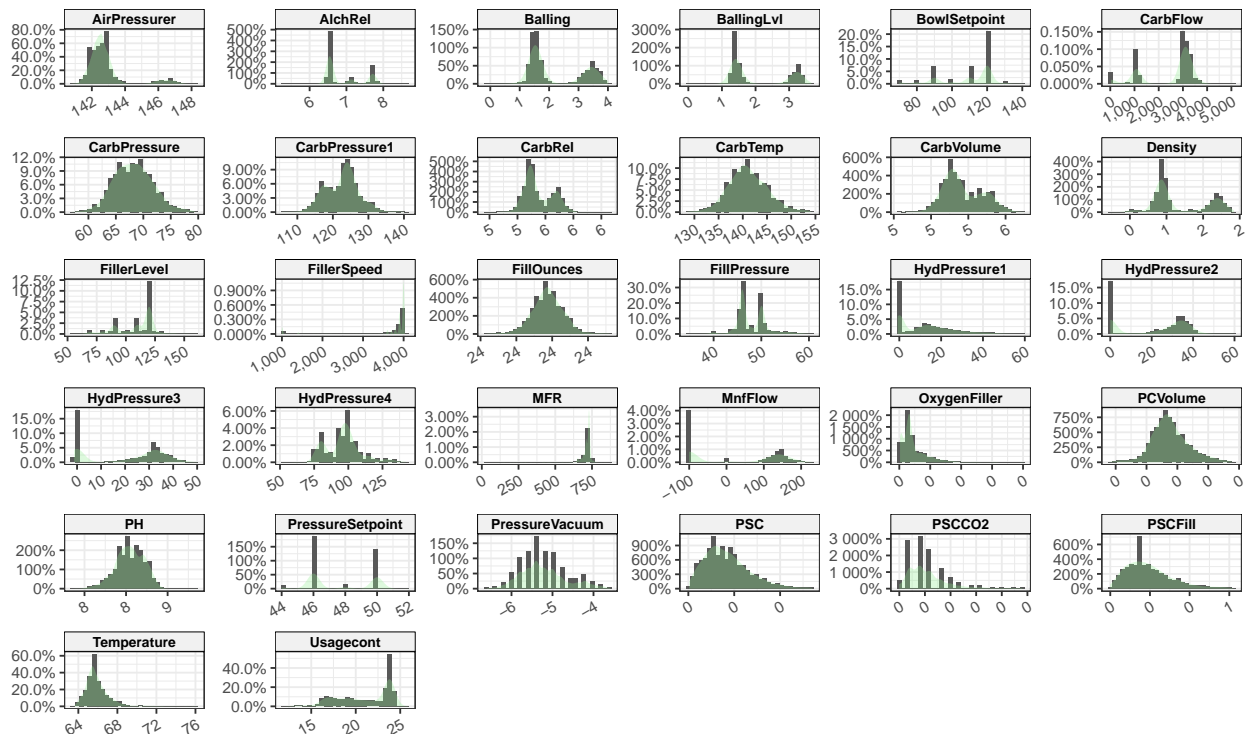
Missing data

With the help of visualization, it is easier to navigate how much each variable is missing. Note that MFR has the most number of missing values.



Univariate distributions

We notice that there are some variables such as Temperature and Oxygen Filler that are highly positively skewed. There are potentials of presence of outliers for skewed variables.



As we expected, there are many outliers in Temperature and Oxygen Filler. Note that MFR greatly suffers from the presence of outliers.

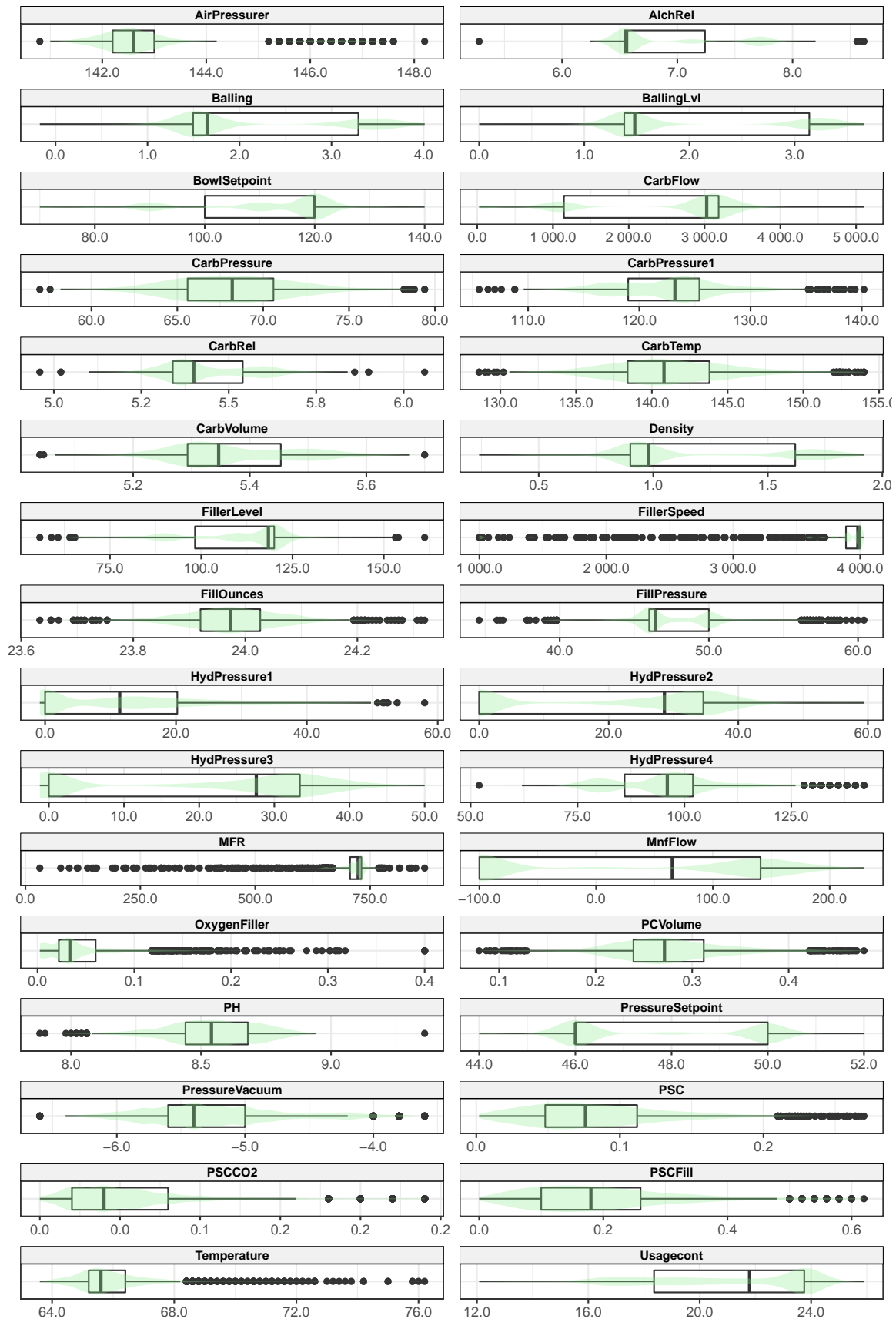
From the presence of multiple outliers, we then have to explain why/what/how we decided to add Random Forest as an additional model and apply necessary pre-processing before modeling PLS and Bagged Tree, if needed. If number of outlier

Although tree-based models, including Bagged Tree, are generally robust to outliers and multicollinearity, it does not necessarily mean Model A in tree-based is always equally good as another model in tree-based. Ensembled model such as Random Forest is potentially even more robust to outliers and multicollinearity than Bagged Tree since only a subset of features are selected at random out of the total and the best split feature from the subset is used to split each node in a tree, unlike in bagging where all features are considered for splitting a node. This makes Random Forest a potentially good alternative for Bagged Tree.

Partial least squares regression (PLS regression) is used as an alternative for ordinary least squares regression in the presence of multicollinearity. Although PLS is quite sensitive to outliers, like in OLS, small number of outliers will not necessarily worsen the predictive ability. In fact, depending on the situations, removing outlier will rather decrease MAPE on test set. Since the benefit of removing outlier cannot be predicted in our case, we will compare MAPE on test set between PLS model without outliers and PLS model without handling outliers to select the best model.

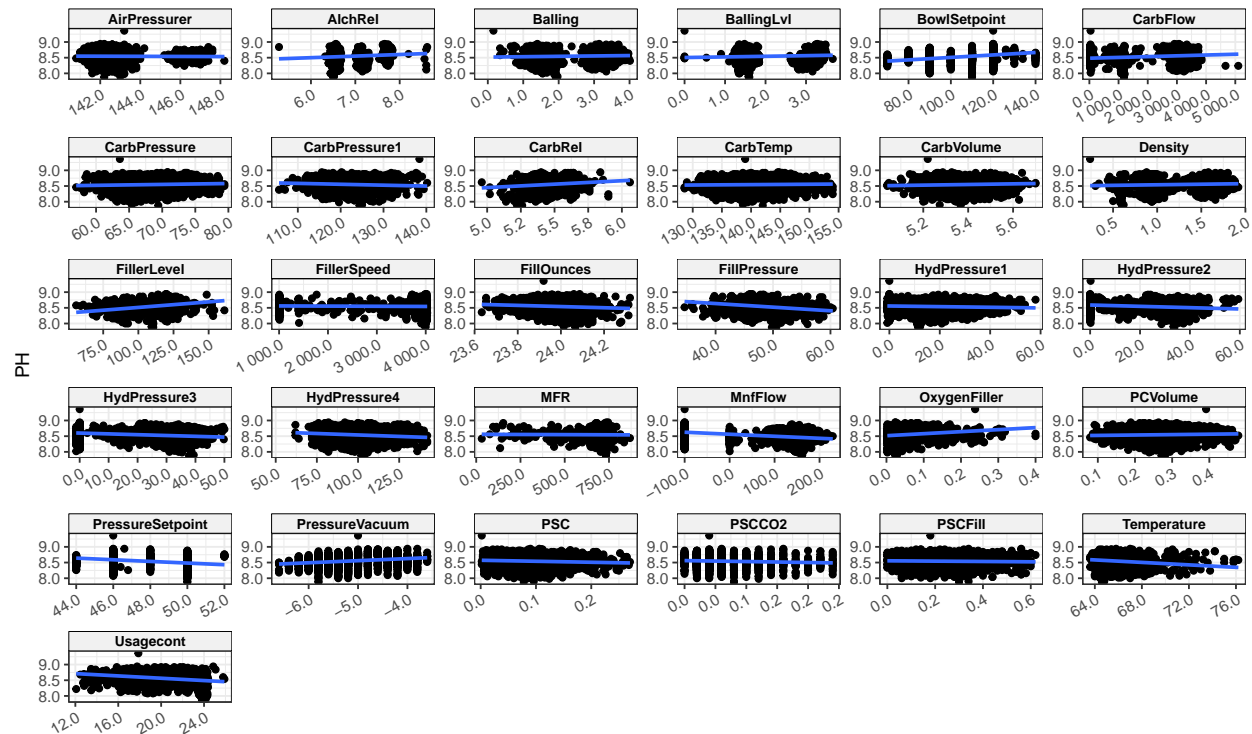
Reference:

(<https://www.hindawi.com/journals/jam/2018/7696302/> - "PLS regression is sensitive to outliers and leverages. Thus several robust versions have been proposed in the literature, but only for linear PLS. Hubert [7] proposed two robust versions of the SIMPLS algorithm by using a robust estimation for the variance-covariance matrix. Kondylis and Hadi [8] used the BACON algorithm to eliminate outliers, resulting in a robust linear PLS.")



Bivariate relationships

Note that Oxygen Filler has weak positive relationship with PH. On the other hand, we know that Temperature has weak negative relationship with PH. All of the predictors have really weak relationship with PH suggesting that linear models might not work well.

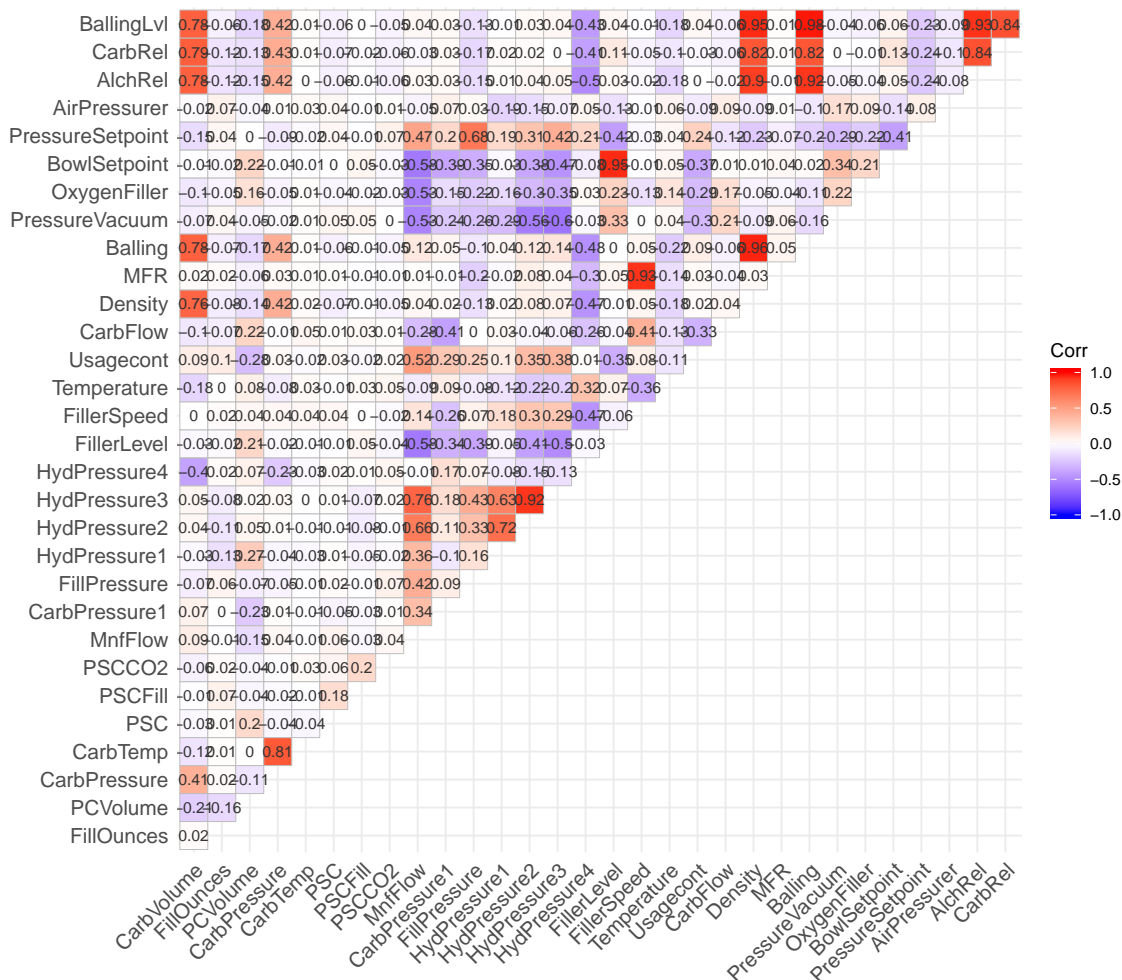


Correlation Matrix

We confirmed that there are several highly correlated predictors. This is another reason why Random Forest would be more preferred to Bagged Tree model. In fact, Random Forest is more robust to strong correlation than Bagged Tree. Although multicollinearity is not a big problem for tree-based models and PLS, it can cause some problem when it comes to inferring the importance of certain predictors in tree model. Multicollinearity means that some predictors are shown as highly correlated with other combinations of predictors in variable importance. According to the reference, it may mislead business audience to think that some features are not more important than others vice-versa. However, we really do not know whether the reader of this paper would treat highly correlated variable such as HydPressure3 and HydPressure2 differently or not. Therefore, we will just keep the variables as they are.

Reference:

(“For example, the two surface area predictors have an extremely high correlation (0.96) and each is used in the tree shown in Fig. 8.4. It is possible that the small difference between these predictors is strongly driving the choice between the two, but it is more likely to be due to small, random differences in the variables. Because of this, more predictors may be selected than actually needed. In addition, the variable importance values are affected. If the solubility data only contained one of the surface area predictors, then this predictor would have likely been used twice in the tree, therefore inflating its importance value. Instead, including both surface area predictors in the data causes their importance to have only moderate values.” Page 181 of Applied Predictive Modeling - Max KJ)



2 Data preparation

Before modeling can be done, the issues identified during the data exploration, namely, zero variance predictors, outliers and missing data need to be addressed.

Imputation

After reviewing a few methods of multiple imputation techniques, Multiple Imputation Chained Equations (MICE) was selected for its strength in handling imputation for observations with more than one predictor missing. For categorical variable such as Brand Code will be imputed by mode. For BACON to work, we will also convert Brand Code to numeric.

We will also remove zero variance Predictors using `nearZeroVar`. It diagnoses predictors that have one unique value or predictors that have both of the following characteristics: 1. they have very few unique values relative to the number of samples and 2. the ratio of the frequency of the most common value to the frequency of the second most common value is large. We confirmed that `HydPressure1` is dropped as a result.

For outlier handling, we will use BACON, short for 'Blocked Adaptive Computationally-Efficient Outlier Nominators'. It is a robust algorithm (set), with an implementation for regression or multivariate covariance estimation. The function produces index with `FALSE` to identify rows with outliers. This index will be used as subset to fit outlier-free train subset in the process of hyperparameter tuning in `train` function and re-train the final model with best tuned hyperparameters. The result of BACON confirmed

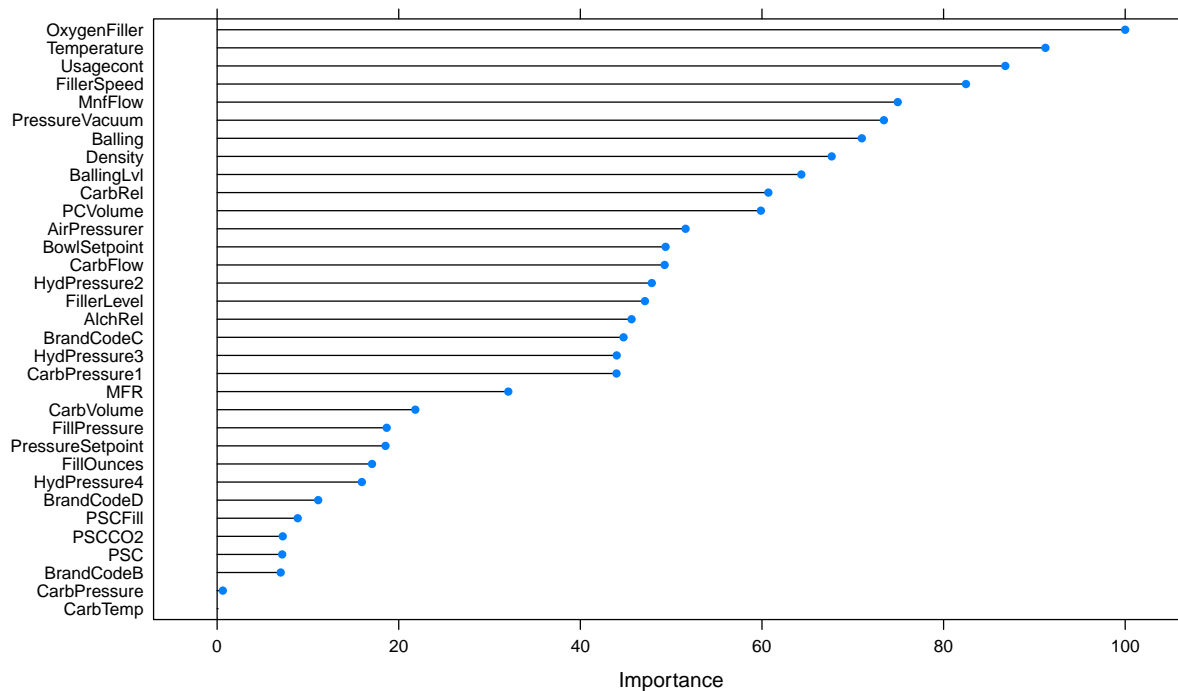
that only about 0.9% or 19 of train set are detected as outliers. Note that we have total 2058 of rows in tran set.

3 Modeling

Model 1: Bagged Tree

Table 3.1: Model Summary - Bagged Tree

RMSE	Rsquared	MAPE
0.1206346	0.5193537	0.010415

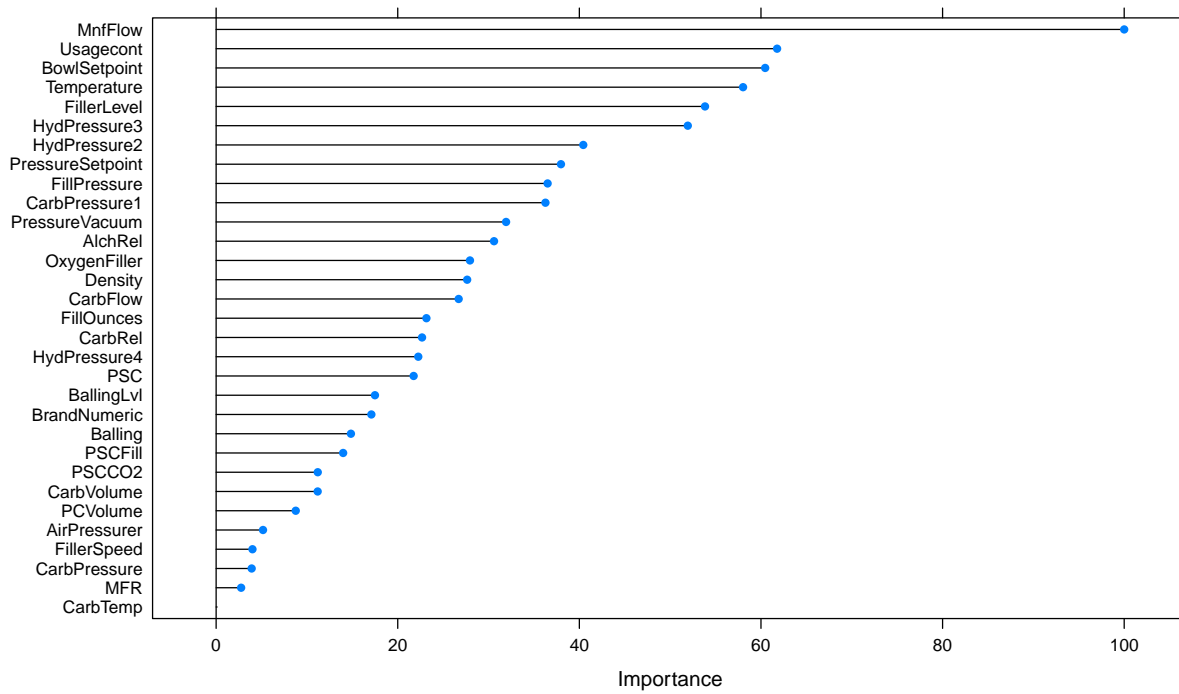


MAPE is 0.010415 where as top 3 important predictors are CarbRel, OxygenFiler and Usagecont. Since Bagged Tree uses all features for splitting a node unlike Random Forest which uses only a subset of features at random out of the total for splitting each node in a tree, the order of feature importances between two models can be quite different.

Model 2: PLS with BACON

Table 3.2: Model Summary - PLS with BACON

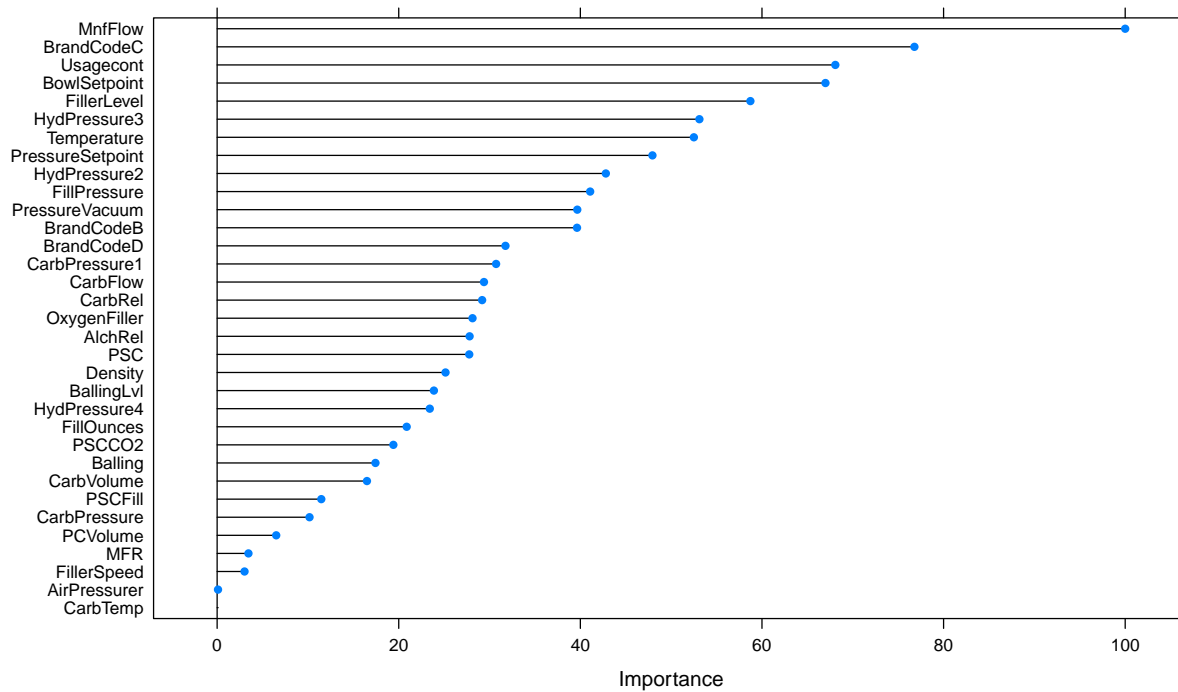
	RMSE	Rsquared	MAPE
10	0.1327207	0.3740444	0.0123968



Model 2-2: PLS

Table 3.3: Model Summary - PLS

	RMSE	Rsquared	MAPE
10	0.1351874	0.3869645	0.0121429



The final value used for both was $ncomp = 10$. MAPE for PLS-BACON is 0.0123968 and for PLS it is 0.0121429. Top 3 important predictors for PLS-BACON are MnFlow, Usagecont and BowlSetpoint and for PLS they are MnFlow, BrandCodeC and Usagecont. The order of variable importance, again, is quite different from Bagged Tree as PLS model is not a tree-based model.

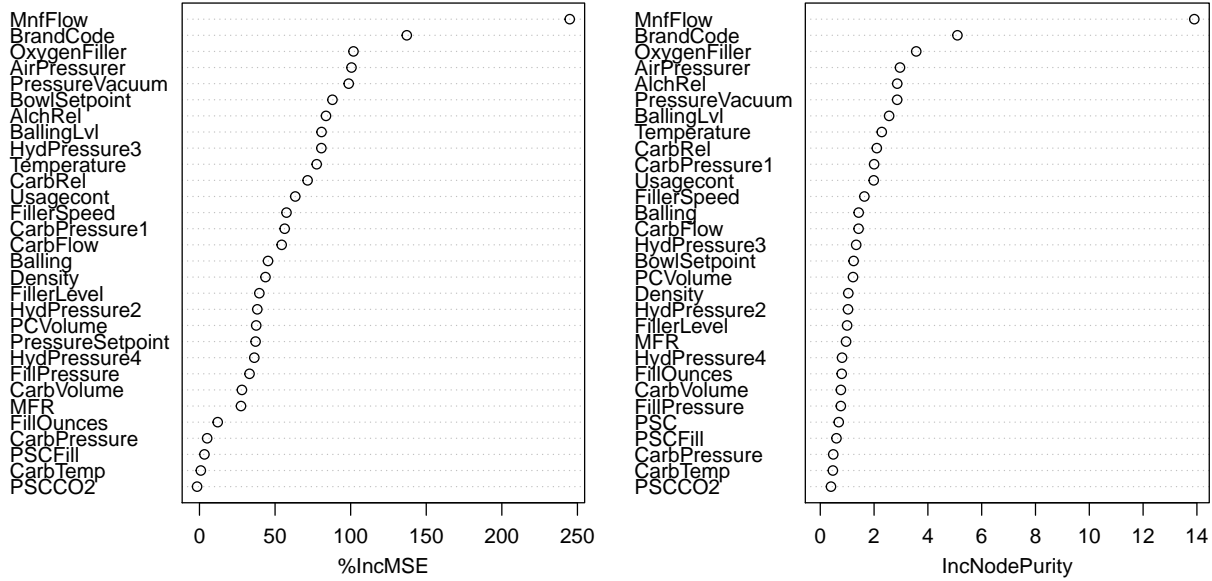
Note that PLS is a dimension reduction technique with some similarity to principal component analysis. The predictor variables are mapped to a smaller set of variables and within that smaller space we perform a regression against the outcome variable. In contrast to principal component analysis where the dimension reduction ignores the outcome variable, the PLS procedure aims to choose new mapped variables that maximally explain the outcome variable.

Model 3: Random Forest

Table 3.4: Model Summary - RF with original data set

RMSE	Rsquared	MAPE
0.0969916	0.6909936	0.0081279

Random_Forest_Variance_Importance



The optimal parameters for model was $mtry = 31$ and $ntree = 2500$. MAPE is 0.0081279 where as top 3 important predictors are MnFFlow, BrandCode and PressureVacuum for %incMSE and MnFFlow, BrandCode and OxygenFiller for IncNodePurity. Unlike PLS, Random Forest can produce 2 different variable importance plots.

The first graph shows how much MSE would increase if a variable is assigned with values by random permutation. The second plot is based on node purity which is measured by the difference between RSS before and after the split on that variable (Gini Index). In short, each graph shows how much MSE or Impurity increases when each variable is randomly permuted.

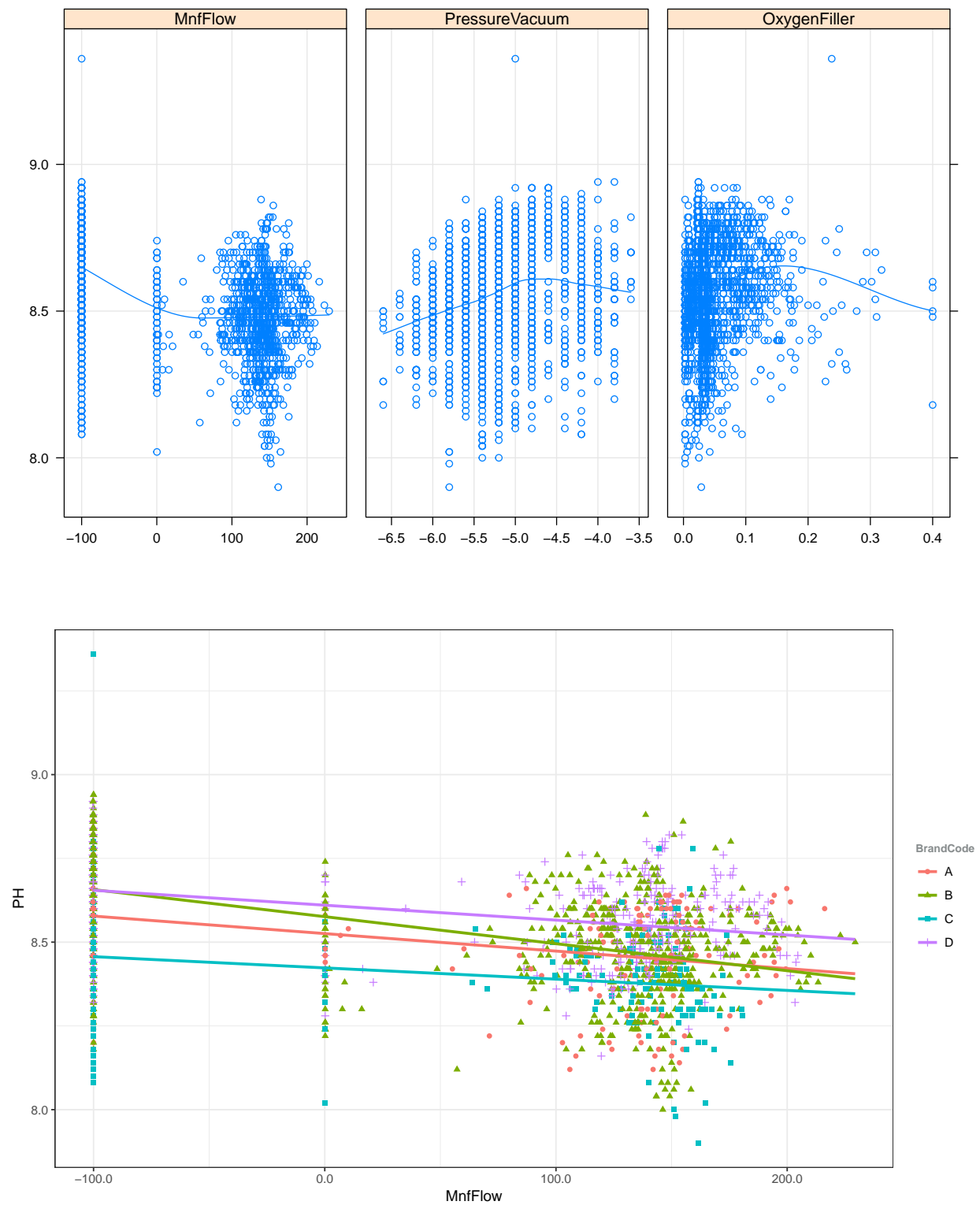
4 Evaluation

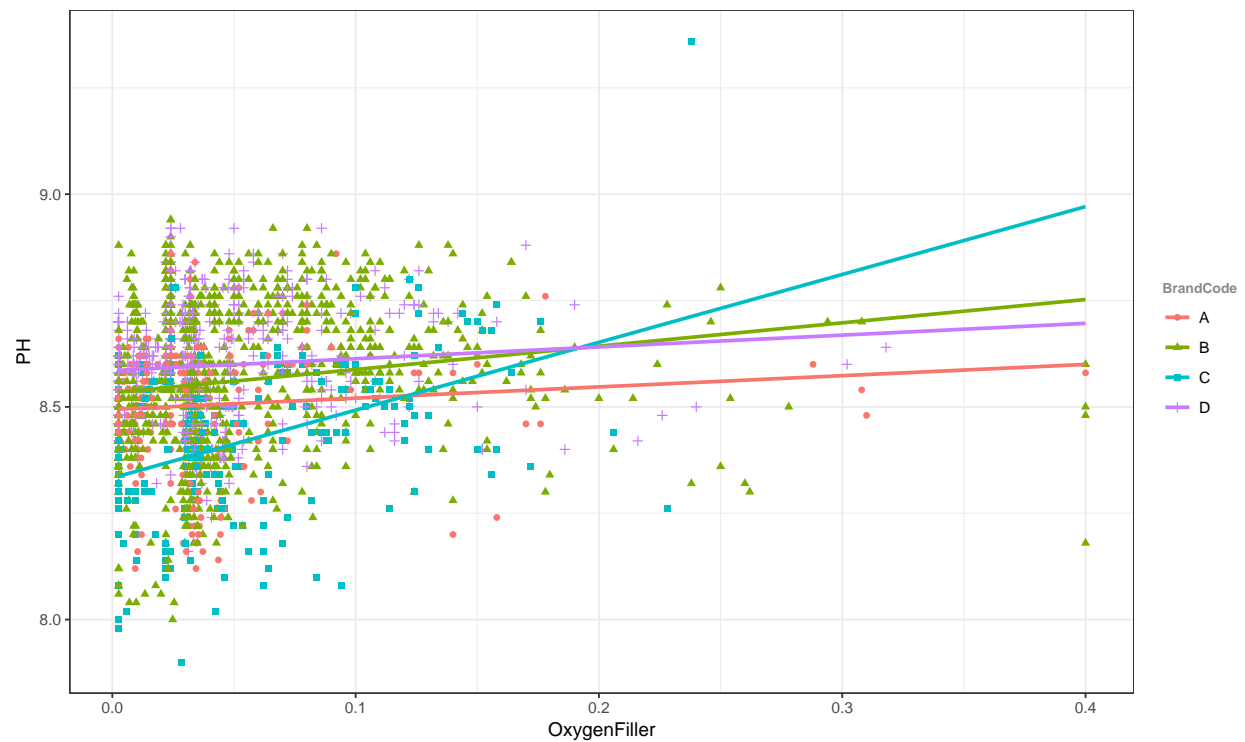
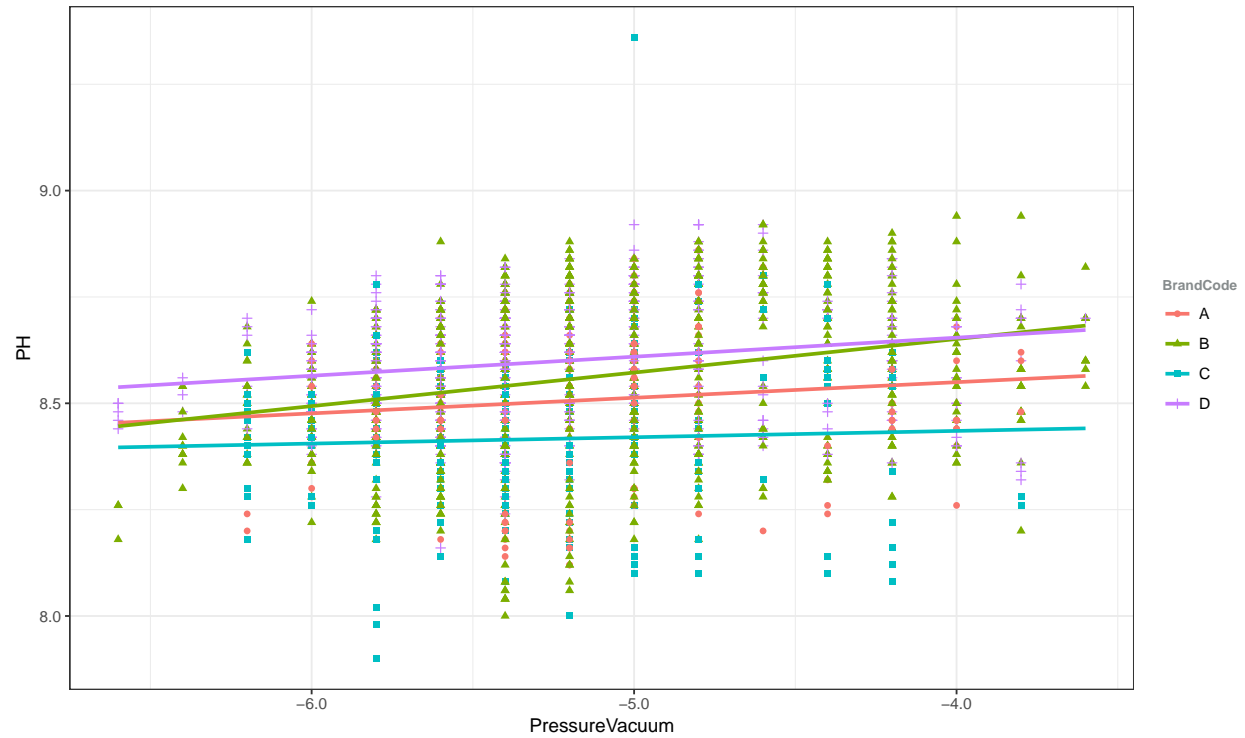
Table 4.1: Evaluation Summary on test set

MODEL	RMSE	Rsquare	MAPE
Bagged Tree	0.1117219	0.5921901	0.0100767
PLS - BACON	0.1358493	0.3862047	0.0122273
PLS	0.1302540	0.4322064	0.0119971
RF	0.0883145	0.7449339	0.0075050

From the table, we confirmed that Random Forest is a clear winner with the lowest MAPE on test set. Also, note that PLS without removing outlier is better model than PLS-BACON. This is not a surprising result since the number of outliers was very small (19 out of 2058) and hence removing outlier is unnecessary process for our case.

Insight & Conclusion





We graphed top 4 most important variables from Random Forest's varImp of MSE and NodePurity. Given that Brand Code is categorical, we grouped 3 continuous variables into Brand Code.

The first feature plot shows that 3 continuous variables have very weak relationship with PH. MnFlow has slight negative relation-

ship where as PressureVacuum and OxygenFiller have slight positive relationship.

From grouping by Brand Code, we see that for PH vs MnfFlow and PH vs PressureVacuum, it seems like predictors have the most negative relationship with PH with code = B. For PH vs OxygenFiller, code = C seems to have the most negative relationship with PH.

We can recommend business users to put more attention on increasing MnfFlow or decreasing PressureVacuum (especially code = B for both) and OxygenFiller (especially code = C) than any other predictors if their goal is to decrease PH.

Prediction

Let's export the prediction values of Random Forest (the best model) on StudentEvaluation as CSV file.

Appendix

```
library(tidyverse)
library(readxl)
library(psych)
library(ggplot2)
library(mice)
library(xtable)
library(GGally)
library(ggstance)
library(grid)
library(gridExtra)
library(ggpubr)
library(caret)
library(data.table)
library(recipes)
library(Metrics)
library(randomForest)
library(robustX)      # BACON
library(ggcorrplot)   # Vis corr matrix
library(e1071)        # Misc stats functions

df <- read_excel('~\\GitHub\\CUNY_DATA_624\\Project_Two\\data\\StudentData.xlsx')
df_eval <- read_excel('~\\GitHub\\CUNY_DATA_624\\Project_Two\\data\\StudentEvaluation.xlsx')
dict <- read_excel('~\\GitHub\\CUNY_DATA_624\\Project_Two\\data\\DataDictionary.xlsx')

# remove space in-between variable names
colnames(df) <- gsub(" ", "", colnames(df))

# Data Exploration
## Data dictionary

kable(dict, caption="Data dictionary", booktabs=T)%>%kable_styling()%>%row_spec()

## Summary statistics

# Create a table summarizing the training data
# create lists of desired summary stats for calculation
statFuns <-
```

```

funs(missing = sum(is.na(.))
     , min = min(., na.rm = TRUE)
     , Q1 = quantile(., .25, na.rm = TRUE)
     , mean = mean(., na.rm = TRUE)
     , median = median(., na.rm = TRUE)
     , Q3 = quantile(., .75, na.rm = TRUE)
     , max = max(., na.rm = TRUE)
     , sd = sd(., na.rm = TRUE)
     , mad = mad(., na.rm = TRUE)
     , skewness = skewness(., na.rm = TRUE)
     , kurtosis = kurtosis(., na.rm = TRUE)
)

# Create data frame of basic summary stats
dfSumTrain <-
  df %>%
  # union(dfEval %>% mutate(TARGET_WINS = as.numeric(NA))) %>%
  dplyr::select(-`BrandCode`) %>%
  summarise_all(statFuns) %>%
  gather() %>%
  separate(key, c('metric', 'stat'), sep = '_(?!.*_)') %>%
  spread(stat, value) %>%
  dplyr::select(metric, names(statFuns))

dfSumTrain %>% kable(caption="Summary statistics", booktabs=T)%>%kable_styling()%>%row_spec()

table(df$`BrandCode`, useNA = "ifany")%>%kable(caption="Frequency distribution of BrandCode", booktabs=T)

## Visualizations

### Missing data

dfSumTrain %>%
  group_by(metric) %>%
  mutate(miss_perc = missing / (!nrow(df))) %>%
  dplyr::select(metric, missing, miss_perc) %>%
  ggplot(data = ., aes(x = reorder(metric, -miss_perc), y = miss_perc)) +
  geom_bar(stat = 'identity') +
  coord_flip() +
  geom_text(aes(label = missing), hjust = -0.1, size = 3) +
  labs(x = NULL, y = NULL, Title = '% Missing') +
  theme_bw() +
  theme(legend.position = 'none') +
  scale_y_continuous(labels = scales::percent)

### Univariate distributions

df %>%
  # union(dfEval %>% mutate(TARGET_WINS = as.numeric(NA))) %>%
  dplyr::select(-BrandCode) %>%
  gather() %>%
  group_by(key) %>%
  ggplot(data = ., aes(value)) +

```

```

geom_histogram(bins = 30, aes(y = ..density..)) +
geom_density(alpha = 0.3, color = NA, fill = 'lightgreen') +
scale_x_continuous(labels = scales::comma) +
scale_y_continuous(labels = scales::percent) +
facet_wrap(~key, scales = 'free') +
labs(x = NULL, y = NULL) +
theme_bw() +
theme(axis.text.x = element_text(angle = 30, hjust = 1))

df %>%
  # union(dfEval %>% mutate(TARGET_WINS = as.numeric(NA))) %>%
  dplyr::select(-BrandCode) %>%
  gather() %>%
  group_by(key) %>%
  ggplot(data = ., aes(x = '', y = value)) +
  geom_boxplot() +
  geom_violin(alpha = 0.3, color = NA, fill = 'lightgreen') +
  labs(x = NULL, y = NULL) +
  theme_bw() +
  theme(axis.ticks.y=element_blank()) +
  facet_wrap(~key, scales = 'free', ncol = 2) +
  coord_flip()

### Bivariate relationships

df %>%
  dplyr::select(-BrandCode) %>%
  gather(key, value, -PH) %>%
  group_by(key) %>%
  ggplot(data = ., aes(x = value, y = PH)) +
  geom_point() +
  geom_smooth(method = 'gam') +
  facet_wrap(~key, scales = 'free') +
  labs(x = NULL) +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 30, hjust = 1))

### Correlation Matrix

# Calculate pairwise pearson correlation and display as upper matrix plot
df %>%
  # union(dfEval %>% mutate(TARGET_WINS = as.numeric(NA))) %>%
  dplyr::select(-c('BrandCode', 'PH')) %>%
  cor(method = 'pearson', use = 'pairwise.complete.obs') %>%
  ggcorrplot(corr = ., method = 'square', type = 'upper'
    , lab = TRUE, lab_size = 3, lab_col = 'grey20')

# Data preparation
## Imputation

# set seed for split to allow for reproducibility
set.seed(58677)

```

```

# use mice w/ default settings to impute missing data
miceInput <- mice(df, printFlag = FALSE)

# add imputed data to original data set
df_mice <- complete(miceInput)
df_mice$BrandCode[is.na(df_mice$BrandCode)] <- 'B'
#table(df_mice$BrandCode, useNA = "ifany")

# Look for any features with no variance:
zero_cols <- nearZeroVar( df_mice )
df_final <- df_mice[, -zero_cols] # drop these zero variance columns
df_final$BrandCode <- as.factor(df_final$BrandCode)

# convert categorical factor into numeric
M <- df_final
must_convert <- sapply(M, is.factor) # logical vector telling if a variable needs to be displayed as numeric
BrandNumeric <- sapply(M[, must_convert], unclass) # data.frame of all categorical variables now displayed as numeric
df_final2 <- cbind(M[, !must_convert], BrandNumeric) # complete data.frame with all variables put together

# split data train/test
# df for random forest
training <- df_final$PH %>% createDataPartition(p = 0.8, list = FALSE)
df_train <- df_final[training, ]
df_test <- df_final[-training, ]

# df for PLS and Bagging
training2 <- df_final2$PH %>% createDataPartition(p = 0.8, list = FALSE)
df_train2 <- df_final2[training2, ]
df_test2 <- df_final2[-training2, ]

# X and y split for BACON fit
x <- subset(df_train2, select = -c(PH) )
x <- as.matrix(x)
y <- df_train2[, c('PH')]

bacon_fit <- BACON(x = x, y = y)

# Modeling

## Model 1: Bagged Tree

set.seed(58677)
bagged_model <- train( PH ~ ., data = df_train, method = "treebag",
  tuneLength = 10,
  # subset = bacon_fit$subset,
  trControl = trainControl(method = "cv", number = 5) )

# create MAPE table
train_bag_pred <- predict(bagged_model)
bagged_model$results$MAPE <- Metrics::mape(df_train$PH, train_bag_pred)

bagged_model$results[, c(2, 3, 8)] %>% kable(caption = "Model Summary - Bagged Tree", booktabs = T) %>% kable_styl

```

```

# plot varImp
plot(varImp(bagged_model))

## Model 2: PLS with BACON

set.seed(58677)
df_final2$BrandNumeric <- as.factor(df_final2$BrandNumeric)

pls_model <- train( PH~., data = df_train2, method="pls",
                    tuneLength=10,
                    subset = bacon_fit$subset,
                    preProcess=c("center","scale"), trControl=trainControl(method="cv",number=5) )

# create MAPE table
train_pls_pred <- predict(pls_model)
pls_model$results$MAPE <- Metrics::mape(df_train2$PH, train_pls_pred)

pls_model$results[10,c(2,3,8)]%>%kable(caption="Model Summary - PLS with BACON", booktabs=T)%>%kable_sty

# plot varImp
plot(varImp(pls_model))

## Model 2-2: PLS
set.seed(58677)
#df_final2$BrandNumeric <- as.factor(df_final2$BrandNumeric)

pls_model2 <- train( PH~., data = df_train, method="pls",
                    tuneLength=10,
                    # subset = bacon_fit$subset,
                    preProcess=c("center","scale"), trControl=trainControl(method="cv",number=5) )

# create MAPE table
train_pls_pred2 <- predict(pls_model2)
pls_model2$results$MAPE <- Metrics::mape(df_train$PH, train_pls_pred2)

pls_model2$results[10,c(2,3,8)]%>%kable(caption="Model Summary - PLS", booktabs=T)%>%kable_styling()%>%

# plot varImp
plot(varImp(pls_model2))

## Model 3-1: Random Forest with BACON

# set.seed(58677)
# rf_model <- train( PH~., data = df_train2, method="rf",
#                   tuneLength=10,
#                   subset = bacon_fit$subset,
#                   importance = TRUE,
#                   trControl=trainControl(method="cv",number=5) )
#
# # create MAPE table
# train_rf_pred <- predict(rf_model)
# rf_model$results$MAPE <- Metrics::mape(df_train2$PH, train_rf_pred)
#

```

```

# rf_model$results%>%kable(caption="Model Summary - RF with BACON", booktabs=T)%>%kable_styling()%>%row_
#
# # plot varImp
# plot(varImp(rf_model))
#
# Although `BACON` is not needed for `Random Forest`, it would not bother using it anyway. We will expect

## Model 3: Random Forest

set.seed(58677)

# Algorithm Tune (tuneRF)
#bestmtry <- tuneRF(df_train[, -25], df_train[,25], stepFactor=1.5, improve=1e-5, ntree=2500)

##mtry <- ( (ncol(df_train) -1) / 3 ) or sqrt(ncol(df_train) - 1) # By default, # of predictors / 3 for

# from above result, we got mtry= 31 and ntree=2500 as optimal parameters
rf_model2 <- randomForest(PH~., data=df_train, method="rf", mtry= 31, importance = TRUE, ntree = 2500)

# create MAPE table
train_rf_pred2 <- predict(rf_model2)

s <- data.frame(
  RMSE = Metrics::rmse(df_train$PH, train_rf_pred2),
  Rsquared = caret::R2(df_train$PH, train_rf_pred2),
  MAPE = Metrics::mape(df_train$PH, train_rf_pred2) )

s%>%kable(caption="Model Summary - RF with original data set", booktabs=T)%>%kable_styling()%>%row_spec

# plot varImp
Random_Forest_Variance_Importance <- rf_model2
varImpPlot(Random_Forest_Variance_Importance)

# Evaluation

# Make predictions
p1 <- bagged_model %>% predict(df_test)
p2 <- pls_model %>% predict(df_test2)
p22 <- pls_model %>% predict(df_test)
p3 <- rf_model2 %>% predict(df_test)

# Model performance metrics
sum_t <- data.frame(
  MODEL = c('Bagged Tree',
            'PLS - BACON',
            'PLS',
            'RF'),
  RMSE = c(caret::RMSE(p1, df_test$PH),
            caret::RMSE(p2, df_test2$PH),
            caret::RMSE(p22, df_test$PH),
            caret::RMSE(p3, df_test$PH) ),
  Rsquare = c(caret::R2(p1, df_test$PH),
              caret::R2(p2, df_test2$PH),

```

```

      caret::R2(p22, df_test$PH),
      caret::R2(p3, df_test$PH)),
  MAPE = c(Metrics::mape(p1, df_test$PH),
           Metrics::mape(p2, df_test2$PH),
           Metrics::mape(p22, df_test$PH),
           Metrics::mape(p3, df_test$PH))
)

sum_t%>%kable(caption="Evaluation Summary on test set", booktabs=T)%>%kable_styling()%>%row_spec()

## Insight & Conclusion

# code
top_var <- c('MnfFlow', 'PressureVacuum', 'OxygenFiller')

featurePlot(df_train[, top_var],
            df_train$PH,
            plot = "scatter",
            between = list(x = 1, y = 1),
            type = c("g", "p", "smooth"),
            layout = c(3,1),
            labels = rep("", 2))

# ggplot(df_train[df_train$BrandCode == 'B',], aes(x=MnfFlow, y=PH, shape=BrandCode, color=BrandCode))
#   geom_point()
#
# ggplot(df_train[df_train$BrandCode == 'A',], aes(x=MnfFlow, y=PH, shape=BrandCode, color=BrandCode))
#   geom_point()
#
# ggplot(df_train[df_train$BrandCode == 'C',], aes(x=MnfFlow, y=PH, shape=BrandCode, color=BrandCode))
#   geom_point()
#
# ggplot(df_train[df_train$BrandCode == 'D',], aes(x=MnfFlow, y=PH, shape=BrandCode, color=BrandCode))
#   geom_point()
ggplot(df_train, aes(x=MnfFlow, y=PH, color=BrandCode, shape=BrandCode)) +
  geom_point() +
  geom_smooth(method=lm, se=FALSE, fullrange=TRUE) +
  theme_bw()+theme()

ggplot(df_train, aes(x=PressureVacuum, y=PH, color=BrandCode, shape=BrandCode)) +
  geom_point() +
  geom_smooth(method=lm, se=FALSE, fullrange=TRUE) +
  theme_bw()+theme()

ggplot(df_train, aes(x=OxygenFiller, y=PH, color=BrandCode, shape=BrandCode)) +
  geom_point() +
  geom_smooth(method=lm, se=FALSE, fullrange=TRUE) +
  theme_bw()+theme()

## Prediction

# remove space in-between variable names
colnames(df_eval) <- gsub(" ", "", colnames(df_eval))

```

```
# remove column with zero-variance
set.seed(58677)

# use mice w/ default settings to impute missing data
miceInput2 <- mice(df_eval, printFlag = FALSE)

# add imputed data to original data set
df_mice2 <- complete(miceInput2)
#table(df_eval$BrandCode, useNA = 'ifany')
df_mice2$BrandCode[is.na(df_mice2$BrandCode)] <- 'B'
#table(df_mice$BrandCode, useNA = "ifany")

# Look for any features with no variance:
#zero_cols <- nearZeroVar( df_mice2 )
df_final22 <- df_mice2[, -zero_cols] # drop these zero variance columns
df_final22$BrandCode <- as.factor(df_final22$BrandCode)

df_eval2 <- subset(df_eval, select = -PH)

pred_eval <- predict(rf_model2, subset(df_final22))
write.csv(pred_eval, 'prediction.csv')
```