

# Team 2 - Homework Two

Assignment 2: KJ 7.2; KJ 7.5

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## Dependencies

```
# predictive modeling
libraries('mlbench', 'caret', 'AppliedPredictiveModeling')

# Formatting Libraries
libraries('default', 'knitr', 'kableExtra')

# Plotting Libraries
libraries('ggplot2', 'grid', 'ggfortify')
```

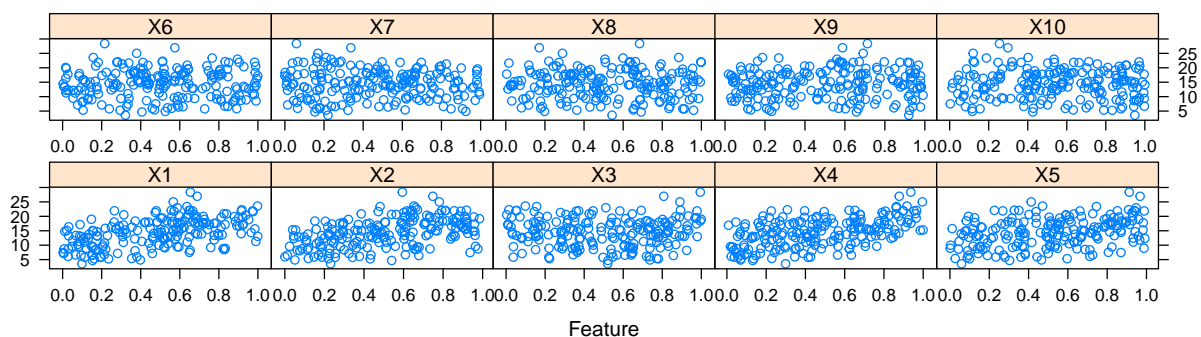
## (1) Kuhn & Johnson 7.2

Friedman (1991) introduced several benchmark data sets create by simulation. One of these simulations used the following nonlinear equation to create data:  $y = 10\sin(\pi x_1 x_2)20(x_3 - 0.5)^2 10x_4 5x_5 N(0, \sigma^2)$ ; where the  $x$  values are random variables uniformly distributed between  $[0, 1]$  (there are also 5 other non-informative variables also created in the simulation).

**\*\*The package `mlbench` contains a function called `mlbench.friedman1` that simulates these data:\*\***

```
set.seed(200)
trainingData <- mlbench.friedman1(200, sd = 1)
trainingData$x <- data.frame(trainingData$x)

featurePlot(trainingData$x, trainingData$y)
```



```
testData <- mlbench.friedman1(5000, sd = 1)
testData$x <- data.frame(testData$x)
```

(a) Tune several models on these data. For example:

**Model 1: KNN model with hyperparameter tuning**

**Train set CV performance - Hyperparameter tuning:**

k-Nearest Neighbors

200 samples  
10 predictor

Pre-processing: centered (10), scaled (10)

Resampling: Cross-Validated (10 fold)

Summary of sample sizes: 180, 180, 180, 180, 180, 180, ...

Resampling results across tuning parameters:

k	RMSE	Rsquared	MAE
1	4.218081	0.4124441	3.500924
2	3.546791	0.5197988	2.941632
3	3.460792	0.5170308	2.841547
4	3.304737	0.5584950	2.697459
5	3.281638	0.5736341	2.695889
6	3.201700	0.6056758	2.651120
7	3.212544	0.6083203	2.677007
8	3.175321	0.6293337	2.589611
9	3.117499	0.6632514	2.555966
10	3.118730	0.6619864	2.542520
11	3.059105	0.6860779	2.486276
12	3.110398	0.6794240	2.539603
13	3.107626	0.6909955	2.504201
14	3.098502	0.6981615	2.503473
15	3.107763	0.7020139	2.517724
16	3.092651	0.7141572	2.499280
17	3.094870	0.7184612	2.502765
18	3.106069	0.7205098	2.512843
19	3.110156	0.7223952	2.522663
20	3.129738	0.7248629	2.544792
21	3.125325	0.7282228	2.555344
22	3.152564	0.7265154	2.583124
23	3.156426	0.7299184	2.590130
24	3.156312	0.7315798	2.583509
25	3.168639	0.7320840	2.600023
26	3.192311	0.7301789	2.615933
27	3.191953	0.7359772	2.626247
28	3.236432	0.7229397	2.667947
29	3.266908	0.7199837	2.696586
30	3.264200	0.7279598	2.695916
31	3.273003	0.7273885	2.702978
32	3.282489	0.7276198	2.702930
33	3.289932	0.7284479	2.707697
34	3.303444	0.7281557	2.717839
35	3.320845	0.7249744	2.727184
36	3.331038	0.7257760	2.729478
37	3.342847	0.7296750	2.740671
38	3.353494	0.7305494	2.745450
39	3.363513	0.7335993	2.748193
40	3.369217	0.7349916	2.752439
41	3.394484	0.7291182	2.779272
42	3.404124	0.7292558	2.783362
43	3.403433	0.7342789	2.780712
44	3.418392	0.7341581	2.794006

45	3.420892	0.7410895	2.790850
46	3.421315	0.7485185	2.801475
47	3.434838	0.7498270	2.816174
48	3.449996	0.7487060	2.831474
49	3.451778	0.7525105	2.833605
50	3.467105	0.7471964	2.844317

RMSE was used to select the optimal model using the smallest value.  
The final value used for the model was  $k = 11$ .

**Test set performance values:**

	RMSE	Rsquared	MAE
	3.1222641	0.6690472	2.4963650

Unlike above approach where `tuneLength = 10` to find 10 odd numbered  $K$ s starting from 5, we will set `tuneGrid` running from  $k = 1$  to 50 after CV process. RMSE on validation set was used to select the optimal model using the smallest value. The final value used for the model was  $k = 11$  with RMSE on test set of 3.1222641.

## Model 2: Neural Networks

`integer(0)`

**Train set CV performance - Hyperparameter tuning:**

Neural Network

200 samples  
10 predictor

Pre-processing: centered (10), scaled (10)

Resampling: Cross-Validated (10 fold)

Summary of sample sizes: 180, 180, 180, 180, 180, 180, ...

Resampling results across tuning parameters:

size	decay	RMSE	Rsquared	MAE
1	0.00	2.803056	0.6666327	2.258691
1	0.01	2.427596	0.7621743	1.887808
1	0.10	2.435471	0.7608686	1.890066
2	0.00	2.489139	0.7430098	1.959395
2	0.01	2.580965	0.7303017	2.026386
2	0.10	2.697160	0.7081857	2.145994
3	0.00	2.175481	0.8114073	1.736758
3	0.01	2.247174	0.7923587	1.847530
3	0.10	2.574029	0.7395256	2.056691
4	0.00	2.338196	0.7863493	1.857565
4	0.01	2.382258	0.7789730	1.875869
4	0.10	2.441937	0.7640421	1.906016
5	0.00	4.095639	0.6461716	2.815675
5	0.01	2.611351	0.7275315	2.058338
5	0.10	2.527299	0.7479751	2.043740
6	0.00	4.360771	0.5655777	2.776134
6	0.01	2.740151	0.7334422	2.120769
6	0.10	2.723467	0.7037555	2.191856
7	0.00	8.107456	0.6013541	3.614263
7	0.01	2.634878	0.7306846	2.082135

7	0.10	2.634554	0.7272090	2.034430
8	0.00	9.294033	0.4764955	3.995120
8	0.01	3.239373	0.6734412	2.543492
8	0.10	2.857949	0.7043441	2.285976
9	0.00	7.318398	0.5467571	3.670600
9	0.01	3.541729	0.5379448	2.671080
9	0.10	3.187206	0.6050659	2.544700
10	0.00	4.083062	0.5181907	2.838082
10	0.01	3.525950	0.5879990	2.836265
10	0.10	3.010387	0.6719106	2.387353

RMSE was used to select the optimal model using the smallest value.  
The final values used for the model were size = 3 and decay = 0.

#### Test set performance values:

RMSE	Rsquared	MAE
2.3950120	0.7740742	1.7970761

We removed highly correlated predictors to ensure that the maximum absolute pairwise correlation between the predictors is less than 0.75. we did not have any highly correlated predictors so let's keep the features as they are.

We found nnet with size = 3 (number of units in the hidden layer) and decay = 0 (parameter for weight decay) is the optimal model based on RMSE on validating set. RMSE on test set was 2.395012.

#### Model 3: Neural Networks Using Model Averaging

##### Train set CV performance - Hyperparameter tuning:

Model Averaged Neural Network

200 samples  
10 predictor

Pre-processing: centered (10), scaled (10)

Resampling: Cross-Validated (10 fold)

Summary of sample sizes: 180, 180, 180, 180, 180, 180, ...

Resampling results across tuning parameters:

size	decay	RMSE	Rsquared	MAE
1	0.00	2.451722	0.7625351	1.896021
1	0.01	2.427658	0.7621763	1.887707
1	0.10	2.435387	0.7608838	1.890037
2	0.00	2.458303	0.7556215	1.947825
2	0.01	2.447743	0.7533484	1.884509
2	0.10	2.483261	0.7506467	1.924237
3	0.00	2.086103	0.8297667	1.625836
3	0.01	2.155718	0.8096710	1.676070
3	0.10	2.227768	0.8003473	1.734663
4	0.00	2.036944	0.8294847	1.636994
4	0.01	2.102926	0.8232439	1.623997
4	0.10	2.032960	0.8301759	1.604834
5	0.00	2.314361	0.7871277	1.717315
5	0.01	2.131569	0.8131597	1.670786
5	0.10	2.192707	0.8054839	1.778156
6	0.00	2.593804	0.7448382	1.966474

6	0.01	2.167612	0.8108275	1.674682
6	0.10	2.042238	0.8227937	1.645410
7	0.00	4.989121	0.5232150	3.110796
7	0.01	2.238776	0.7948069	1.754542
7	0.10	2.202599	0.7926956	1.751645
8	0.00	5.839958	0.5788055	3.266803
8	0.01	2.392621	0.7727856	1.893142
8	0.10	2.271702	0.7860966	1.790783
9	0.00	5.138515	0.4191673	3.248740
9	0.01	2.463813	0.7534985	1.927194
9	0.10	2.250755	0.7930757	1.820346
10	0.00	3.400511	0.6426513	2.428742
10	0.01	2.456849	0.7404324	1.988814
10	0.10	2.437919	0.7608963	1.971687

Tuning parameter 'bag' was held constant at a value of FALSE  
 RMSE was used to select the optimal model using the smallest value.  
 The final values used for the model were size = 4, decay = 0.1 and bag  
 = FALSE.

**Test set performance values:**

	RMSE	Rsquared	MAE
	2.1306481	0.8202697	1.5982639

We found nnet with size = 4 (number of units in the hidden layer) and decay = 0.1 (parameter for weight decay) is the optimal model based on RMSE on validating set. RMSE on test set was 2.1306481.

#### Model 4: Multivariate Adaptive Regression Splines (MARS)

**Train set CV performance - Hyperparameter tuning:**

Call: earth(x=data.frame[200,10], y=c(18.46,16.1,17...), keepxy=TRUE,  
 degree=2, nprune=17)

	coefficients
(Intercept)	20.378441
h(0.621722-X1)	-15.512132
h(X1-0.621722)	9.177132
h(0.601063-X2)	-17.940676
h(X2-0.601063)	10.064356
h(X3-0.281766)	11.590022
h(0.447442-X3)	14.641640
h(X3-0.447442)	-12.924806
h(X3-0.606015)	13.416764
h(0.734892-X4)	-10.074386
h(X4-0.734892)	9.687149
h(0.850094-X5)	-5.385762
h(0.218266-X1) * h(X2-0.601063)	-55.372637
h(X1-0.218266) * h(X2-0.601063)	-27.542831
h(X1-0.621722) * h(X2-0.295997)	-26.527403
h(0.649253-X1) * h(0.601063-X2)	26.129827

Selected 16 of 18 terms, and 5 of 10 predictors

Termination condition: Reached nk 21

Importance: X1, X4, X2, X5, X3, X6-unused, X7-unused, X8-unused, ...

Number of terms at each degree of interaction: 1 11 4

GCV 1.61518      RSS 210.6377      GRSq 0.934423      RSq 0.9568093

**Test set performance values:**

	RMSE	Rsquared	MAE
	1.1492504	0.9471145	0.9158382

We found MARS with `degree = 2` (Maximum degree of interaction (Friedman's `mi`)) and `nprune = 17` (aximum number of terms (including intercept) in the pruned model) is the optimal model based on RMSE on validating set. RMSE on test set was 1.1492504.

**Model 5: Support Vector regression**

**Train set CV performance - Hyperparameter tuning:**

Support Vector Machines with Radial Basis Function Kernel

200 samples  
10 predictor

Pre-processing: centered (10), scaled (10)

Resampling: Cross-Validated (10 fold)

Summary of sample sizes: 180, 180, 180, 180, 180, 180, ...

Resampling results across tuning parameters:

C	RMSE	Rsquared	MAE
0.25	2.534788	0.7882081	2.034824
0.50	2.292127	0.8029516	1.819981
1.00	2.091598	0.8284381	1.657402
2.00	1.967193	0.8457471	1.546737
4.00	1.883133	0.8561761	1.482054
8.00	1.863807	0.8588797	1.468328
16.00	1.834215	0.8633819	1.456738
32.00	1.836471	0.8632508	1.459909
64.00	1.836471	0.8632508	1.459909
128.00	1.836471	0.8632508	1.459909
256.00	1.836471	0.8632508	1.459909
512.00	1.836471	0.8632508	1.459909
1024.00	1.836471	0.8632508	1.459909
2048.00	1.836471	0.8632508	1.459909

Tuning parameter 'sigma' was held constant at a value of 0.0552698

RMSE was used to select the optimal model using the smallest value.

The final values used for the model were sigma = 0.0552698 and C = 16.

**Test set performance values:**

	RMSE	Rsquared	MAE
	2.0490047	0.8297577	1.5586106

Since the nature of the equation of the data is non-linear, we will use `svmRadial` as kernal function for regression. The final values used for the model were sigma = 0.0552698 and C = 16 with RMSE on test set of 2.0490047.

- (b) Which models appear to give the best performance? Does MARS select the informative predictors (those named X1-X5)?

MARS appears to give the best performance based on RMSE, R squared and MAE on test set. The summary out put of `mars_model` gives us that **Importance:** X1, X4, X2, X5, X3, X6-unused, X7-unused,

X8-unused, X9-unused, .... MARS does select the informative predictors X1-X5 only.

	knn_pv	nnet_pv	avnnet_pv	mars_pv	svm_pv
RMSE	3.1222641	2.3950120	2.1306481	1.1492504	2.0490047
Rsquared	0.6690472	0.7740742	0.8202697	0.9471145	0.8297577
MAE	2.4963650	1.7970761	1.5982639	0.9158382	1.5586106

Call: earth(x=data.frame[200,10], y=c(18.46,16.1,17...), keepxy=TRUE,  
degree=2, nprune=17)

	coefficients
(Intercept)	20.378441
h(0.621722-X1)	-15.512132
h(X1-0.621722)	9.177132
h(0.601063-X2)	-17.940676
h(X2-0.601063)	10.064356
h(X3-0.281766)	11.590022
h(0.447442-X3)	14.641640
h(X3-0.447442)	-12.924806
h(X3-0.606015)	13.416764
h(0.734892-X4)	-10.074386
h(X4-0.734892)	9.687149
h(0.850094-X5)	-5.385762
h(0.218266-X1) * h(X2-0.601063)	-55.372637
h(X1-0.218266) * h(X2-0.601063)	-27.542831
h(X1-0.621722) * h(X2-0.295997)	-26.527403
h(0.649253-X1) * h(0.601063-X2)	26.129827

Selected 16 of 18 terms, and 5 of 10 predictors

Termination condition: Reached nk 21

Importance: X1, X4, X2, X5, X3, X6-unused, X7-unused, X8-unused, ...

Number of terms at each degree of interaction: 1 11 4

GCV	1.61518	RSS	210.6377	GRSq	0.934423	RSq	0.9568093
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## (2) Kuhn & Johnson 7.5

Exercise 6.3 describes data for a chemical manufacturing process. Use the same data imputation, data splitting, and pre-processing steps as before and train several nonlinear regression models.

- (a) Which nonlinear regression model gives the optimal resampling and test set performance?

**Test set performance values:**

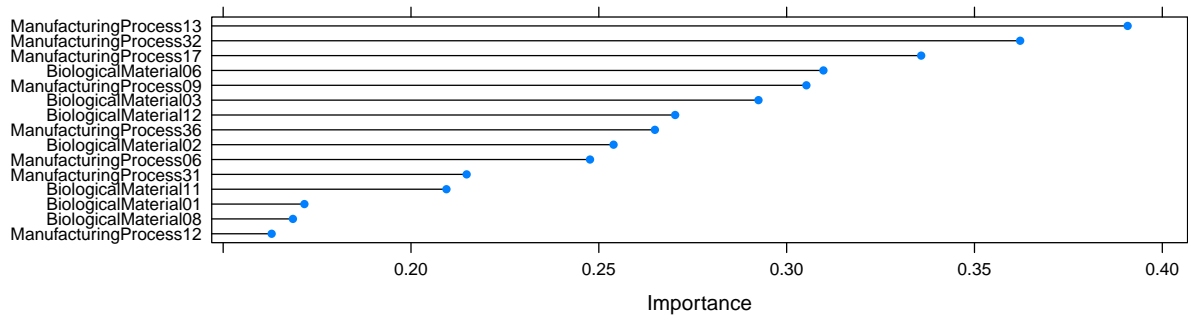
	knn_pv2	nnet_pv2	avnnet_pv2	mars_pv2	svm_pv2
RMSE	1.4986649	1.6189836	1.6190778	1.4131453	1.2756876
Rsquared	0.3302198	0.3159727	0.3159386	0.3911259	0.5011139
MAE	1.2035764	1.3311308	1.3312383	1.0797807	1.0200509

SVM regression gives the optimal performance based on RMSE, Rsquared and MAE on test set.

- (b) Which predictors are most important in the optimal nonlinear regression model? Do either the biological or process variables dominate the list? How do the top ten important predictors compare to the top ten predictors from the optimal linear model?

In linear model, `ManufacturingProcess32` was the most important predictor but in non-linear model, it is 2nd most important predictor - the most important predictor is `ManufacturingProcess13`.

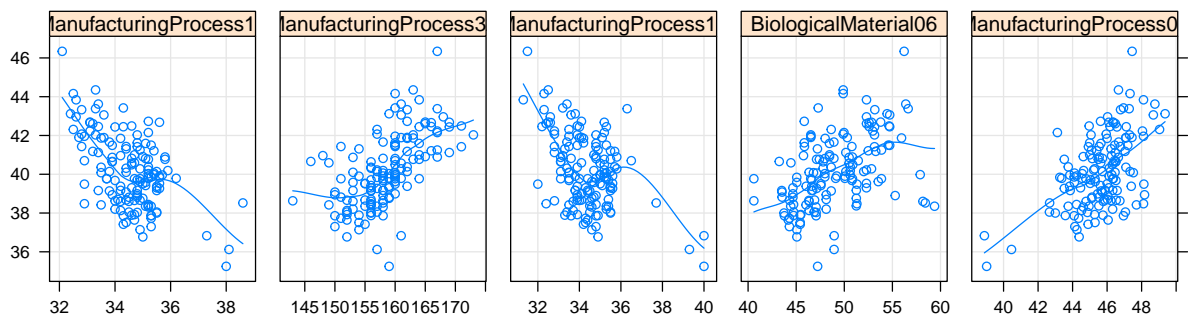
In linear model, only 2 of top 10 were Biological where as in non-linear, 4 of them were.



- (c) Explore the relationships between the top predictors and the response for the predictors that are unique to the optimal nonlinear regression model. Do these plots reveal intuition about the biological or process predictors and their relationship with yield?

From Bivariate plot and correlation matrix, we know that **ManufacturingProcess32** has fairly positive relationship with **Yield** where as other 2 variables have fairly negative relationship. Among biological predictors, we know **BiologicalMaterial06** is the most important with fairly strong positive relationship with **Yield**.

This information can help researchers to focus more on **ManufacturingProcess32** and **BiologicalMaterial06** if their goal is to increase **Yield**.



```
corr_top5
ManufacturingProcess13 -0.5645290
ManufacturingProcess32  0.6017957
ManufacturingProcess17 -0.4666781
BiologicalMaterial06    0.4673292
ManufacturingProcess09  0.5423679
```

## R Code

```
#insert all code here
# (7.2a)
##Model 1: KNN model with hyperparameter tuning##

set.seed(100)
knn_model <- train(trainingData$x,
                    trainingData$y,
```



```

        method = "knn",
        # Center and scaling will occur for new predictions too
        preProc = c("center", "scale"),
        tuneGrid = data.frame(.k = 1:50),
        trControl = trainControl(method = "cv"))

##Test set performance values:##
knn_Pred <- predict(knn_model, newdata = testData$x)
knn_pv <- postResample(pred = knn_Pred, obs = testData$y)

##Model 2: Neural Networks##

#findCorrelation(cor(trainingData$x), cutoff = .75)

# hyperparameter tuning for nnet
nnetGrid <- expand.grid(.size = c(1:10), .decay = c(0, 0.01, .1))

set.seed(100)
nnet_model <- train(trainingData$x, trainingData$y,
                    method = "nnet",
                    tuneGrid = nnetGrid,
                    trControl = trainControl(method="cv"),
                    ## Automatically standardize data prior to modeling and prediction
                    preProc = c("center", "scale"),
                    linout = TRUE,
                    trace = FALSE,
                    MaxNWts = 10 # (ncol(trainingData$x) + 1) + 10 + 1,
                    maxit = 500)

##Test set performance values:##
nnet_Pred <- predict(nnet_model, newdata = testData$x)
nnet_pv <- postResample(pred = nnet_Pred, obs = testData$y)

##Model 3: Neural Networks Using Model Averaging##
nnetGrid2 <- expand.grid(.size = c(1:10), .decay = c(0, 0.01, .1), .bag = FALSE)

set.seed(100)
avnnnet_model <- train(trainingData$x, trainingData$y,
                      method = "avNNet",
                      tuneGrid = nnetGrid2,
                      trControl = trainControl(method="cv"),
                      preProc = c("center", "scale"),
                      linout = TRUE,
                      trace = FALSE,
                      MaxNWts = 10 # (ncol(trainingData$x) + 1) + 10 + 1,
                      maxit = 500)

##Test set performance values:##
avnnnet_Pred <- predict(avnnnet_model, newdata = testData$x)
avnnnet_pv <- postResample(pred = avnnnet_Pred, obs = testData$y)

##Model 4: Multivariate Adaptive Regression Splines (MARS)##
marsGrid <- expand.grid(.degree = 1:3, .nprune = 2:38)

```

```

set.seed(100)
mars_model <- train(trainingData$x, trainingData$y,
method = "earth",
tuneGrid = marsGrid,
trControl = trainControl(method="cv"))

##Test set performance values:##
mars_Pred <- predict(mars_model, newdata = testData$x)
mars_pv <- postResample(pred = mars_Pred, obs = testData$y)

##Model 5: Support Vector regression##
set.seed(100)
svm_model <- train(trainingData$x, trainingData$y,
method = "svmRadial",
preProc = c("center", "scale"),
tuneLength = 14,
trControl = trainControl(method="cv"))

##Test set performance values:##
svm_Pred <- predict(svm_model, newdata = testData$x)
svm_pv <- postResample(pred = svm_Pred, obs = testData$y)

# (7.2b)
sum_t <- data.frame(
  knn_pv,
  nnet_pv,
  avnnet_pv,
  mars_pv,
  svm_pv
)

# (7.5a)
# Call code from 6.3
data("ChemicalManufacturingProcess")

# save df
df <- ChemicalManufacturingProcess

# set seed for split to allow for reproducibility
set.seed(20190227L)

# use mice w/ default settings to impute missing data
miceInput <- mice::mice(df, printFlag = FALSE)

# add imputed data to original data set
df_mice <- mice::complete(miceInput)

# Look for any features with no variance:
zero_cols <- nearZeroVar( df_mice )
df_final <- df_mice[,-zero_cols] # drop these zero variance columns

# split data train/test
training <- df_final$Yield %%

```

```

createDataPartition(p = 0.8, list = FALSE)

df_train <- df_final[training, ]
df_test <- df_final[-training, ]

# model1 - KNN
set.seed(100)
knn_model2 <- train(Yield~., data = df_train,
  method = "knn",
  # Center and scaling will occur for new predictions too
  preProc = c("center", "scale"),
  tuneGrid = data.frame(.k = 1:50),
  trControl = trainControl(method = "cv"))

knn_Pred2 <- predict(knn_model2, newdata = df_test)

## The function 'postResample' can be used to get the test set performance values
knn_pv2 <- postResample(pred = knn_Pred2, obs = df_test$Yield)

# model2 - nnet
# remove highly correlated predictors to ensure that the maximum absolute pairwise correlation between
df_train_x <- df_train[-1]
df_train_y <- df_train[,1]
df_test_x <- df_test[-1]
df_test_y <- df_test[,1]

tooHigh <- findCorrelation(cor(df_train_x), cutoff = .75)

trainx_nn <- df_train_x[, -tooHigh]
testx_nn <- df_test_x[, -tooHigh]

# hyperparameter tuning for nnet
nnetGrid12 <- expand.grid(.size = c(1:10), .decay = c(0, 0.01, .1))

set.seed(100)
nnet_model2 <- train(trainx_nn, df_train_y,
  method = "nnet",
  tuneGrid = nnetGrid12,
  trControl = trainControl(method="cv"),
  ## Automatically standardize data prior to modeling and prediction
  preProc = c("center", "scale"),
  linout = TRUE,
  trace = FALSE,
  MaxNWts = 10 # (ncol(trainx_nn) + 1) + 10 + 1,
  maxit = 500)

nnet_Pred2 <- predict(nnet_model2, newdata = testx_nn)

## The function 'postResample' can be used to get the test set performance values
nnet_pv2 <- postResample(pred = nnet_Pred2, obs = df_test_y)

# model 3 - avNNet
# hyperparameter tuning for avnnet

```

```

nnetGrid22 <- expand.grid(.size = c(1:10), .decay = c(0, 0.01, .1), .bag = FALSE)

set.seed(100)
avnnnet_model2 <- train(trainx_nn, df_train_y,
                        method = "avNNet",
                        tuneGrid = nnetGrid22,
                        trControl = trainControl(method="cv"),
                        ## Automatically standardize data prior to modeling and prediction
                        preProc = c("center", "scale"),
                        linout = TRUE,
                        trace = FALSE,
                        MaxNWts = 10 # (ncol(trainx_nn) + 1) + 10 + 1,
                        maxit = 500)

avnnnet_Pred2 <- predict(avnnnet_model2, newdata = testx_nn)

## The function 'postResample' can be used to get the test set performance values
avnnnet_pv2 <- postResample(pred = avnnnet_Pred2, obs = df_test_y)

# model 4 - MARS
# hyperparameter tuning for MARS
marsGrid2 <- expand.grid(.degree = 1:3, .nprune = 2:38)

set.seed(100)
mars_model2 <- train(Yield~., data = df_train,
                    method = "earth",
                    tuneGrid = marsGrid2,
                    trControl = trainControl(method="cv"))

mars_Pred2 <- predict(mars_model2, newdata = df_test)

## The function 'postResample' can be used to get the test set performance values
mars_pv2 <- postResample(pred = mars_Pred2, obs = df_test$Yield)

# model 5 - SVM - regression
set.seed(100)
svm_model2 <- train(Yield~., data = df_train,
                    method = "svmRadial",
                    preProc = c("center", "scale"),
                    tuneLength = 14,
                    trControl = trainControl(method="cv"))

svm_Pred2 <- predict(svm_model2, newdata = df_test)

## The function 'postResample' can be used to get the test set performance values
svm_pv2 <- postResample(pred = svm_Pred2, obs = df_test$Yield)

# Model performance metrics
sum_t2 <- data.frame(
  knn_pv2,
  nnet_pv2,
  avnnnet_pv2,
  mars_pv2,

```

```

    svm_pv2
)

# (7.5b)
varimp <- varImp(svm_model2,scale=F,useModel = T)
#plot(varimp, top=15, scales = list(y = list(cex = 0.8)))

# (7.5c)
viporder <- order(abs(varimp$importance),decreasing=TRUE)
topVIP <- rownames(varimp$importance)[viporder[c(1:5)]]

#featurePlot(df_train[, topVIP],
#            df_train$Yield,
#            plot = "scatter",
#            between = list(x = 1, y = 1),
#            type = c("g", "p", "smooth"),
#            layout = c(5,1),
#            labels = rep("", 2))
corr_top5 <- cor(df_train[, topVIP], df_train$Yield, method = 'pearson', use = 'pairwise.complete.obs')

```