

CHEME 465 Fall 2020; HW3; Question 3 3) You have a liquid-phase, irreversible chemical reaction occurring in a series of equally sized CSTRs. From your extensive Googling of this particular reaction, you know that $k(T = 450 \text{ K}) = 3.98 \times 10^{-3} \text{ hr}^{-1}$ and that the energy barrier for the reaction is $E_a = 7 \text{ kcal/mol}$. You are also given the following conversion data as a function of the Damköhler number (Da) from the series of CSTRs. You can assume that the volume of each reactor is 4000 L , $CA_0 = 1.8 \text{ mol/L}$, $u_0 = 20 \text{ L/hr}$, and $T = 450 \text{ K}$. Da : 0.00, 0.30, 0.60, 0.91, 1.21, 1.51, 1.82, 2.12, 2.42, 2.73, 3.00. X : 0.000, 0.545, 0.756, 0.854, 0.906, 0.936, 0.954, 0.966, 0.975, 0.980, 0.984. Instead of counting the number of CSTRs in series, you assume that it would be much easier to compute it based off of the provided data. Assuming that the reaction is first order, plot the experimental data along with analytical curves for X vs. Da with the number of tanks varying to find curve which matches in Python. (Note: Da should be plotted along the x-axis) b. Given the provided operating and kinetic parameters, what is the conversion achieved in this system? c. Now that you know the number of CSTRs there are in series, if the temperature of the system is increased to 500 K and everything else stays the same, what would the conversion be? d. If the initial concentration is doubled, how would this change the volume? e. If you wanted to increase the conversion of this reaction, how would you change the parameters for the CSTRs in series (e.g., reactor volumes, flow rates, number of reactors)?

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In [64]: import numpy as np
import matplotlib.pyplot as plt
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In [70]: #Given Information from Problem 3
k_450 = 3.98*10**(-3)    #unit: 1/hr (T = 450K)
Ea     = 7               #unit: kcal/mol
V      = 4000            #unit: L - Volume of each reactor
C_A0   = 1.8             #unit: mol/L
v_0    = 20              #unit: L/hr
T_450  = 450             #unit: K
R      = 1.987*10**(-3)  #unit: kcal/(mol*K)
Da_exp = np.array([0.0, 0.3, 0.6, 0.9, 1.2, 1.5, 1.8, 2.1, 2.4, 2.7, 3.0])
X      = np.array([0.00, 0.545, 0.756, 0.854, 0.906, 0.936, 0.954, 0.966, 0.975, 0.980, 0.984])
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In [76]: #Part A

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X_calc1 = 1 - 1/(1+Da_exp)**(1)
X_calc2 = 1 - 1/(1+Da_exp)**(2)
X_calc3 = 1 - 1/(1+Da_exp)**(3)
X_calc4 = 1 - 1/(1+Da_exp)**(4)

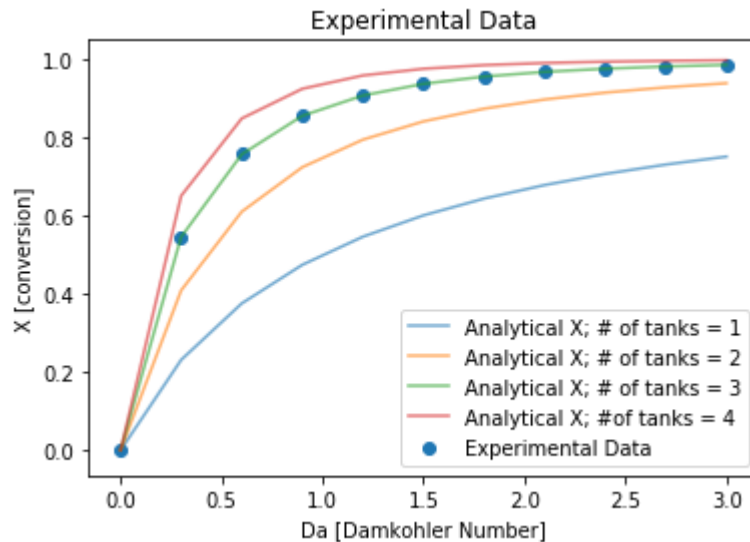
plt.title("Experimental Data")
plt.xlabel("Da [Damkohler Number]" )
plt.ylabel("X [conversion]")

plt.scatter(Da_exp, X, alpha = 1, label = "Experimental Data")
plt.plot(Da_exp, X_calc1, alpha = 0.6, label = "Analytical X; # of tanks = 1")
plt.plot(Da_exp, X_calc2, alpha = 0.6, label = "Analytical X; # of tanks = 2")
plt.plot(Da_exp, X_calc3, alpha = 0.6, label = "Analytical X; # of tanks = 3")
plt.plot(Da_exp, X_calc4, alpha = 0.6, label = "Analytical X; #of tanks = 4")
plt.legend(loc='best')

print('From the plot, we see the # of CSTRs in series =3')

```

From the plot, we see the # of CSTRs in series =3



In [72]: #Part B

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# Assume reaction is first order so -r_A = k*C_A
Da1_b = k_450*C_A0*V/(v_0*C_A0)
# from part a n = 3
Xf_b = 1 - 1/(1+Da1_b)**(3)
# Conclusion:
print('Part B will have a conversion = {:.3f}'.format(Xf_b))

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Given operating/kinetic parameters, conversion = 0.827

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In [79]: #Part C

#If temperature=500K

# Equation to use for k based on temperature  $k = A \cdot \exp(-E_a/(R \cdot T))$ 
#at k=450 K
A = k_450/(np.exp(-Ea/(R*T_450)))
#at k 500K:
k_500 = A*np.exp(-Ea/(R*500))

#Assume reaction is first order so  $-r_A = k \cdot C_A$ 
Da1_c = k_500*C_A0*V/(v_0*C_A0)

#We know from part A  $n = 3$ :
Xf_c = 1 - 1/(1+Da1_c)**(3)

print('For Part C conversion = {:.3f}'.format(Xf_c))
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For Part C conversion = 0.951

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In [81]: #Part D

#Initial concentration doubled; how would this affect volume?

C_A0_d = 2*C_A0

# Volume of tank #3;  $V = v_0 \cdot C_{A0} \cdot (X_3 - X_2) / (-r_{A\_exit})$ 
# At  $T = 450$  K:
X_2 = 1 - 1/(1+Da1_b)**(2)
X_3 = 1 - 1/(1+Da1_b)**(3)
V_d = v_0*C_A0_d*(X_3-X_2)/(k_450*C_A0_d*(1-X_3))

print('Original Volume = {:.2f} L'.format(V))

print('Volume If we double intial concentration volume = {:.2f} L'.format(V_d))

print('Volume is the same if initial concentration is doubled.')
```

Original Volume = 4000.00 L

Volume If we double intial concentration volume = 4000.00 L

Volume is the same if initial concentration is doubled.

```

In [75]: #Part E

#To increase conversion, what parameters should be adjusted?
#I will use the value from part b to compare

print('Compare to the Conversion from part b = {:.3f} \n'.format(Xf_b))

#Doubling flow rate of reactors

#Assume reaction is first order so  $-r_A = k \cdot C_A$ 
Da1_e = k_450 * C_A0 * V / ((v_0 * 2) * C_A0)

#Part a; n = 3:
Xf_e = 1 - 1 / (1 + Da1_e) ** (3)

print('doubling flow rate conversion = {:.3f}'.format(Xf_e))

#If we cut in half flow rate of reactors

#Assume reaction is first order so  $-r_A = k \cdot C_A$ 
Da1_e = k_450 * C_A0 * V / ((v_0 / 2) * C_A0)

#Part a; n = 3:
Xf_e = 1 - 1 / (1 + Da1_e) ** (3)

print('Halving flow rate conversion = {:.3f}'.format(Xf_e))

#Doubling volume of reactors

#Assume reaction is first order so  $-r_A = k \cdot C_A$ 
Da1_e = k_450 * C_A0 * (V * 2) / (v_0 * C_A0)

#from part A n = 3:
Xf_e = 1 - 1 / (1 + Da1_e) ** (3)

print('Doubling volume of reactors conversion = {:.3f}'.format(Xf_e))

#doubling number of reactors
#Assume reaction is first order so  $-r_A = k \cdot C_A$ 
Da1_e = k_450 * C_A0 * V / (v_0 * C_A0)
Xf_e = 1 - 1 / (1 + Da1_e) ** (3 * 2)

print('doubling number of reactors conversion = {:.3f} \n'.format(Xf_e))

print('To increase the conversion for this problem')
print('Decrease flow rate. Increase volume. Increase # of reactors.')

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Compare to the Conversion from part b = 0.827

doubling flow rate conversion = 0.634

Halving flow rate conversion = 0.943

Doubling volume of reactors conversion = 0.943

doubling number of reactors conversion = 0.970

To increase the conversion for this problem

Decrease flow rate. Increase volume. Increase # of reactors.

In []:

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