

Ques-1: How does Shor's Algorithm threaten the security of RSA and Elliptic Curve cryptography (ECC), and what are the potential consequences for current digital infrastructure?

IT-21031

Ans:

Shor's Algorithm threatens the security of RSA and Elliptic curve cryptography (ECC) because it can efficiently solve the hard mathematical problems - integer factorization (for RSA) and elliptic curve discrete logarithm (for ECC) on which these cryptographic systems are based. While classical computers take an impractically long time to solve these problems, a quantum computer running Shor's algorithm could break RSA and ECC in polynomial time, making them vulnerable. The potential consequences for current digital infrastructure include:

- Decryption of secure communications (HTTPS, VPN)
- Forgery of digital signatures used in authentication.

- Exposure of sensitive data in banking, government, and healthcare.
- Long-term risk from data harvested now and decrypted later when quantum computers are ready.

IT-21031

This creates an urgent need to adopt quantum-resistant (post-quantum) cryptographic systems.

Ques - 2 : Discuss the role of quantum key distribution (QKD) in future cryptographic systems. How does it differ from classical public-key encryption?

Ans:

Quantum key distribution (QKD) allows two parties to securely share a cryptographic key using the principles of quantum mechanics. The most well-known QKD protocol is BB84, which uses quantum bits (qubits) to detect any

eavesdropping attempts.

Differences from Classical Public-key Encryption:

- * Classical encryption (RSA) relies on hard mathematical problems for security, while QKD relies on the laws of physics. IT-21031
- * QKD can detect eavesdropping (due to quantum no-cloning and measurement disturbance) but classical methods cannot.
- * QKD is used for key distribution, not for encrypting data itself.

Ques-3: What are the main differences between lattice-based cryptography and traditional number-theoretic approaches like RSA, particularly in the context of quantum resistance?

* Lattice-based

Ans:

- * Lattice-based cryptography is based on geometric problems in high-dimensional

space (shortest vector problem) which are believed to be hard even for quantum computers.

* RSA and ECC rely on integer factorization and discrete logarithms, which are vulnerable to Shor's algorithm.

IT-21031

* Lattice cryptography is quantum-resistant and it's a strong candidate for post-quantum cryptography.

Ques-4: Develop a python based PRNG that uses the current system time and a custom seed value. Write complete program and corresponding output.

Ans:

```
import time
```

```
def prng(seed):
```

```
    current_time = int(time.time() * 1000)
```

```
    combined = seed ^ current_time
```

```
    combined = (combined * 1103515245 + 12345)
                & 0xFFFFFFFF
```

```
    return combined
```

```
seed-value = 12395
```

```
random-number = prng (seed-value)
```

```
print ("Generated pseudo-random number;"  
       random-number)
```

Sample output:

Generated pseudo-random number: 1620932541

IT-21031

Ques - 5: Explain the Sieve of Eratosthenes algorithm and use it to find all prime numbers less than 50. How does its time complexity compare to trial version?

Ans:

Sieve of Eratosthenes: An efficient algorithm to find all primes $\leq n$. It works by iteratively marking the multiples of each prime number starting from 2.

Algorithm:

1. Create a boolean list for numbers upto n .
2. Start from $p=2$ mark all multiples of p as

False

3. Repeat until $p^2 > n$.Python code for $n = 50$:

def sieve(n):

IT-21031

prime = [True for _ in range(n)]

prime[0] = prime[1] = False

p=2

while $p \cdot p < n$:

if prime[p]:

for i in range($p \cdot p, n, p$):

prime[i] = False

p+=1

return [i for i in range(n) if prime[i]]

print(sieve(50))

Output: [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47]Time complexity:* sieve: $O(n \log \log n)$ * Trial Division: $O(n\sqrt{n})$ (slower)

Ques-6: State and explain the necessary and sufficient conditions for a composite number to be a Carmichael number. Then verify whether $n = 561, 1105, 1729$ are Carmichael numbers.

Ans:

IT-21031

A Carmichael number is a composite number n such that for all integers a coprime to n ,

$$a^{n-1} \equiv 1 \pmod{n} \text{ (Fermat-like property)}$$

Necessary and sufficient condition:

A composite number n is a Carmichael number if and only if :

- * n is square-free
- * For every prime p dividing n , $(p-1)$ divides $(n-1)$

Check for :

$$* 561 = 3 \times 11 \times 17 \checkmark$$

$$* 1105 = 5 \times 13 \times 17 \checkmark$$

$$* 1729 = 7 \times 13 \times 9 \checkmark$$

In all cases :

- * Composite
- * Square-free
- * $p-1$ divides $(n-1)$

Ques-7: Determine whether the following are valid algebraic structures and justify your answer :

Is the set \mathbb{Z} with operations + and \times a ring?

Yes, \mathbb{Z} is a commutative ring with identity.

IT-21031

Are the sets $(\mathbb{R}, +)$ and $(\mathbb{Z}/n\mathbb{Z}, +)$ Abelian groups?

Yes, both are Abelian groups.

* \mathbb{R} under addition : associative, identity 0,

inverse -a, commutative.

* $\mathbb{Z}/n\mathbb{Z}$ under addition mod n: same properties hold.

Ques-8:

What is the remainder when $73 \times (-19)$ is reduced modulo 15?

Ans:

$$73 \times (-19) = -1022 \equiv -1022$$

$-1022 \text{ mod } 15 = \text{remainder when divided by 15}$

$$-1022 \equiv 8 \pmod{15}$$

Answer: 8

Ques-9: Determine the multiplicative inverse of 23 modulo 66 using Extended Euclidean Algorithm

Ans: Apply Extended Euclidean Algorithm:

$$\text{gcd}(66, 23) = 1$$

IT-21031

$$23^{-1} \bmod 66 = x \text{ such that } 23x \equiv 1 \pmod{66}$$

using EEA:

$$66 = 2 \times 23 + 20$$

$$23 = 1 \times 20 + 3$$

$$20 = 6 \times 3 + 2$$

$$3 = 1 \times 2 + 1$$

$$2 = 2 \times 1 + 0$$

Back - substitute:

$$1 = 3 - 1 \times 2$$

$$= 3 - 1 \times (20 - 6 \times 3)$$

$$= 7 \times 3 - 1 \times 20$$

$$= 7 \times (23 - 1 \times 20) - 1 \times 20 = 7 \times 23 - 8 \times 20$$

$$= 7 \times 23 - 8(66 - 2 \times 23) = 7 \times 23 - 8 \times 66 + 16 \times 23$$

$$= 23 \times (7 + 16) - 8 \times 66 = 23 \times 23 - 8 \times 66$$

So, inverse $\approx 23 \approx$

Multiplicative inverse of $23 \bmod 66$ is 23.

Ques -10: State and prove Bezout's Theorem.
Use it to find the multiplicative inverse of
97 modulo 385.

IT-21031

Bezout's Theorem:

For integers a and b , there exist integers x and y such that : where, x and y are
 $ax + by = \gcd(a, b)$ Bezout's coefficients

if $\gcd(a, b) = 1$, then x is the modular inverse
of $a \pmod{b}$.

Proof: Using the Extended Euclidean Algorithm.

Step - 1: Apply the Euclidean Algorithm

Let a and b be integers and assume $a > b \geq 0$.

We perform repeated division:

$$a = bq_1 + r_1$$

$$b = r_1 q_2 + r_2$$

$$r_1 = r_2 q_3 + r_3$$

$$\dots$$

$$r_{n-2} = r_{n-1} q_n + r_n$$

$$r_{n-1} = r_n q_{n+1} + 0$$

Then $\gcd(a, b) = r_n$

Step-2: Back-substitute to express $\gcd(a, b)$ as a linear combination of a and b .

Using the last few equations, we backtrack and express each remainder in terms of the previous remainders until we express $\gcd(a, b) = r_n$ as:

$$r_n = ax + by$$

IT-21031

for some integers x and y . Hence, Bezout's identity is proven.

Use Extended Euclidean Algorithm for 97 and 385:

$$385 = 3 \times 97 + 94$$

$$97 = 1 \times 94 + 3$$

$$94 = 31 \times 3 + 1$$

Back substitute:

$$1 = 94 - 31 \times 3$$

$$= 94 - 31 \times (97 - 1 \times 94) = 32 \times 94 - 31 \times 97$$

$$= 32 \times (385 - 3 \times 97) - 31 \times 97 = 32 \times 385 - 127 \times 97$$

So,

$$1 = 32 \times 385 - 127 \times 97$$

$$\Rightarrow -127 \times 97 \equiv 1 \pmod{385} \Rightarrow$$

\Rightarrow Inverse of 97 is 258 ($-127 \equiv 258 \pmod{385}$)

Ques: 11 - Use Bezout's identity to prove that the equation $385x + 97y = 1$ has integer solutions.

Find x, y .

From earlier solution, we get

$$1 = 32 \times 385 - 97 \times 127$$

IT-21031

$$\text{So, } x = 32 \text{ and } y = -127$$

Integer solution exists.

Ques - 12: Prove Fermat's Little Theorem and explain how it is used to test for primality.

Is 561 a prime number based on this test?

$$\text{Evaluate } 5^{20} \pmod{561}.$$

Ans:

Fermat's Little theorem:

If p is prime and a not divisible by p , then

$$a^{p-1} \equiv 1 \pmod{p}$$

Use in primality testing:

* If $a^{n-1} \not\equiv 1 \pmod{n} \rightarrow n$ is composite

* If $\phi = 1 \rightarrow$ possibly prime (but carmichael number like 561 pass it)

check for 561:

$$\gcd(5, 561) = 1$$

IT-21031

$$\text{compute } 5^{560} \bmod 561:$$

Since 561 is Carmichael, $5^{560} \equiv 1 \pmod{561}$

But 561 is **not prime**.

Ques-13: State and prove the Chinese Remainder Theorem. Then solve the following system:

CRT Ans:

CRT: For pairwise coprime modulo m_1, m_2, \dots, m_k and congruences:

$$x \equiv a_1 \pmod{m_1}$$

$$x \equiv a_2 \pmod{m_2}$$

...

There exists a unique solution modulo $M = m_1 \times m_2 \times \dots \times m_k$.

$$M = m_1 \times m_2 \times \dots \times m_k.$$

Example: Solve

$$x \equiv 2 \pmod{3}$$

$$x \equiv 3 \pmod{4}$$

$$x \equiv 1 \pmod{5}$$

Steps:

$$M = 3 \times 4 \times 5 = 60$$

IT-21031

$$* M_1 = 60/3 = 20, M_2 = 15, M_3 = 12$$

$$* \text{Inverse: } 20^{-1} \pmod{3} = 2, 15^{-1} \pmod{4} = 3$$

$$12^{-1} \pmod{5} = 3$$

$$x = (2 \times 20 \times 2) + (3 \times 15 \times 3) + (1 \times 12 \times 3) = 80 + 135 + 36 \\ = 251$$

$$x \equiv 251 \pmod{60} \Rightarrow x = 11$$

Answer: ~~$x \equiv 11 \pmod{60}$~~ $x = 11 \pmod{60}$

Ques-14: Briefly explain the CIA triad in information security.

Ans:

* Confidentiality: Protect data from Unauthorized access (encryption)

* Integrity: Ensure data is accurate and

and unaltered (hashing)

* Availability : Ensure systems / data are accessible when needed (backups, uptime)

Together, they form the foundation of a secure system.

IT-21031

15

Ques-15: How does steganography differ from cryptography, and what are common techniques used?

Ans: * Cryptography : Scrambles data to hide meaning.

* Steganography : Hides the existence of data (embedding in images / audio).

Techniques :

- * LSB (Least Significant Bit) insertion

- * Masking and filtering

- * Audio / Video embedding

Ques-16: key differences between phishing, malware and Dos attacks.

Attack Type	Method	Impact
Phishing	Social Engineering via emails or fake sites	Credential theft
Malware	Malicious Software	Data theft, Spying, damage
Dos	Overloading a system	Service unavailability

IT-21031

Ques-17: Explain GDPR and its role in cyber-security.

Ans: General Data Protection Regulation (GDPR) is an EU law that protects personal data and privacy.

Key Roles:

- * Enforces user consent
- * Grants data access and deletion rights
- * Imposes fines for data breaches
- * Promotes secure data handling practices.

Ques-18: Explain DES using a 64-bit plaintext and a 56-bit key.

Ans:

DES (Data Encryption standard):

■ Symmetric-key block cipher

■ Input: 64-bit block, 56-bit key

■ Steps:

1. Initial permutation (IP)

2. 16 rounds of Feistel function (expansion, substitution using S-boxes, permutation)

3. Final permutation (IP⁻¹)

Each round uses a subkey from the original key.

Ques-19: Evaluate $(-8 \times 5) \bmod 17$ and explain how to simplify negative modular multiplication

Ans: We have: $(-8 \times 5) \bmod 17$

First multiply: $-8 \times 5 = -40$

Step-2 Then reduce negative value modulo 17

We want: $-40 \bmod 17$

IT-21031

A remainder must be non-negative (in standard modular arithmetic).

To convert a negative number into positive equivalent:

IT-21031

If $r < 0$, add the modulus until it's positive.

$$-40 + 17 = -23 \text{ (still negative)}$$

$$-23 + 17 = -6 \text{ (still negative)}$$

$$-6 + 17 = 11 \text{ (positive)}$$

Final answer: $(-8 \times 5) \bmod 17 = 11$

Q1 How to simplify negative modular multiplication:

1. Reduce each operand mod n before multiplying:

2. or multiply first. then adjust the negative result by adding the modulus until you get a positive equivalent.

Ques-20:

In the DES algorithm

Given,

- $R_0 = 0x F0 F0 F0 F0$
- round key $K_1 = 0x D F0 F0 F0 F$ IT-21031
- first round function $f(R_0, K_1)$ assumed to be bitwise XOR (simplified)
- $L_0 = 0x A A A A A A A A$
- $L_1 = R_0 \text{ and } R_1 = L_0 \oplus f(R_0, K_1)$

Compute :

$$\begin{aligned} f(R_0, K_1) &= R_0 \oplus K_1 = 0x F0 F0 F0 F0 \oplus 0x D F0 F0 F0 F \\ &= 0x F F F F F F F F \end{aligned}$$

So, • $L_1 = R_0 = 0x F0 F0 F0 F0$

$$\begin{aligned} \bullet R_1 &= L_0 \oplus f(R_0, K_1) = 0x A A A A A A A A \oplus 0x F F F F F F F F \\ &= 0x 5 5 5 5 5 5 5 5 \end{aligned}$$

Ans: $f(R_0, K_1) = 0x F F F F F F F F$

$$L_1 = 0x F0 F0 F0 F0$$

$$R_1 = 0x 5 5 5 5 5 5 5 5$$

Ques-21: Use the partial AES S-box to perform Sub Bytes on [0x23, 0xA7, 0x4C, 0x19]

Ans: lookups use high nibble = row

low nibble = column

- 0x23 → row 2, col 3 = 0xD9

IT-21031

- 0xA7 → row A, col 7 = 0x63

- 0x4C → row 4, col C = 0x2E

- 0x19 → row 1, col 9 = 0xC6

Resulting output : [0xD9, 0x63, 0x2E, 0xC6]

Ques-22: In AES, apply the Add Round key step only. Given Input word [0x1A, 0x2B, 0x3C, 0x4D] and round key [0x55, 0x66, 0x77, 0x88] compute the XOR.

Ans: byte wise XOR :

- 0x1A ⊕ 0x55 = 0x4F

- 0x2B ⊕ 0x66 = 0x4D

- 0x3C ⊕ 0x77 = 0x4B

- 0x4D ⊕ 0x88 = 0xC5

Output word : [0x4F, 0x4D, 0x4B, 0xC5]

Ques-23: Show how MixColumns uses the fixed matrix over GF(2⁸) to transform column

[0x01, 0x02, 0x03, 0x04]

Matrix :

$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix}$$

IT-21031

Compute each output byte as gf-mul/xor

(multiplication by 0x02/0x03 done in Rijndael field with reduction poly 0x11B).

Step results (hex) :

- Row 1 = $02 \cdot 0x01 \oplus 03 \cdot 0x02 \oplus 01 \cdot 0x03 \oplus 01 \cdot 0x04$
 $= 0x02 \oplus 0x06 \oplus 0x03 \oplus 0x04 = 0x03$
- Row 2 = $0x01 \oplus 0x04 \oplus 0x05 \oplus 0x04 = 0x04$
- Row 3 = $0x01 \oplus 0x02 \oplus 0x06 \oplus 0x0C = 0x09$
- Row 4 = $0x03 \oplus 0x02 \oplus 0x03 \oplus 0x08 = 0x0A$

Output column : [0x03, 0x04, 0x09, 0x0A]

Ques-24: Describe AES-OFB mode and how it ensures synchronization.

Ans:

How it works: OFB (Output Feedback) turns the block cipher into a synchronous stream cipher. Starting from an IV:

IT-21031

$$o_0 = E(K, IV), o_1 = E(K, o_0), o_2 = (K, o_1), \dots$$

Ciphertext $c_i = p_i \oplus o_i$. Decryption uses the same o_i to recover p_i .

- **Synchronization:** Both sides must share the same IV and key and process blocks in the same order. OFB keystream depends only on IV and key (not plaintext/ciphertext), so as long as sender and receiver use the same IV and no blocks are lost/inserted, keystreams align and decryption succeeds. Loss or reordering of blocks breaks sync until a new IV or explicit resync is used.

Ques - 25: Which AES modes cause error propagation during decryption? Illustrate with CBC and CFB and explain integrity impact.

- CBC

IT-21031

Ans:

- CBC: A single-bit error in ciphertext block c_i causes p_i (after decryption of c_i) to be completely garbled (because $D(c_i)$ is wrong). The subsequent plaintext block p_{i+1} will have a single bit flip at the same bit positions (because $p_{i+1} = D(c_{i+1}) \oplus c_i$). So, corruption affects two plaintext blocks (one fully garbled, the next with bit-flips). CBC is malleable: attackers can flip bits in ciphertext to cause predictable changes in decrypted plaintext \rightarrow integrity is not guaranteed without authentication.

- CFB: Error propagation depends on segment size; a bit error in c_i will directly flip corresponding bits in decrypted p_i , and because of feedback, a limited number of

subsequent bits/blocks may be affected until the error shifts out of the feedback register. So, CFB has limited error propagation.

Integrity implication: Neither mode provides integrity by itself, both need MAC/AE (HMAC or AES-GCM) to detect tampering.

IT-21031

Ques-26: Which AES mode for encrypting large files with parallel processing: ECB-CBC or CTR ? Justify

Recommendation : CTR (counter) mode

Why :

- Keystream blocks are $E(k, \text{nonce} || \text{counter})$ so, each block encryption / decryption is independent and fully parallelizable.

- No block-pattern leakage like ECB (which is insecure).

- No sequential dependency like CBC (which prevents parallel encryption)

- Error effect is local (no long propagation).

Caveat: use unique / counter per key to avoid reuse.

Ques - 27: RSA example : Given message $M=1$
 public key $e=5$, $n=14$. Encrypt and decrypt
 with private $d=11$.

IT-21031

Ans:

$$\text{Encrypt : } c = M^e \bmod n = 1^5 \bmod 14 = 1$$

$$\text{Decrypt : } m = c^d \bmod n = 1^{11} \bmod 14 = 1$$

ciphertext = 1 (Note : $n=14$ is not secure - small/ composite - this is purely illustrative.)

Ques - 28: RSA signature : Given $H(M)=5$

private key $d=3$, $n=33$. Generate signature.

Ans:

$$\begin{aligned}\text{Signature } s &= H(M)^d \bmod n = 5^3 \bmod 33 \\ &= 125 \bmod 33 = 26\end{aligned}$$

Signature = 26.

Ques :- 29 : Diffie - Hellman example : $p=17$
 $g=3$, $a=9$ (Aleya), $b=5$ (Badol). Compute
 public keys and shared secret.

• Aleya public $A = g^a \text{ mod } p = 3^4 \text{ mod } 17$
 $= 81 \text{ mod } 17$
 $= 13$

• Badol public $B = g^b \text{ mod } p = 3^5 \text{ mod } 17$
 $= 243 \text{ mod } 17 = 5$

• Shared secret $K = B^a \text{ mod } p = 5^4 \text{ mod } 17$
 $= 625 \text{ mod } 17$
 $= 13$ (or $A^b \text{ mod } p$ yields same)

public keys : Aleya = 13, Badol = 5

Shared secret = 13

IT-21031

Ques - 30 : Hash $H(n) = (\text{Sum ASCII chars}) \text{ mod } 100$. compute $H("A")$ and $H("BA")$
 what does this imply about collision resistance?

Ans:

• ASCII ('A') = 65, ASCII ('B') = 66, sum = 66 + 65
 $= 131$

• $H("A") = 131 \text{ mod } 100 = 31$

• $H("BA") = 66 + 65 = 131 \text{ mod } 100 = 31$

Both produce same hash (collision).

Implication : The function is not collision resistant.

many different inputs map to the same short output. A cryptographic hash must make finding collisions computationally infeasible.

Ques: $\text{Mac} = (\text{Message} + \text{Secret key}) \bmod 17$.

Given message = 15, key = 7, compute MAC.

If attacker changes message to 10 without key, can they forge MAC?

IT-21031

Ans: $\text{MAC} = (15+7) \bmod 17 = 22 \bmod 17 = 5$

- For message 10, correct MAC would be $(10+7) \bmod 17 = 17 \bmod 17 = 0$.

Attacker without key cannot compute the correct MAC unless they guess the key, or brute-force (small modulus makes brute-force trivial). Thus conceptually secure if key secret and large enough, but this construction is insecure in practice (too simple, no cryptographic strength). Use HMAC or other secure MACs.

Ques-32: Explain TLS handshake steps and how symmetric keys are established using asymmetric cryptography.

IT-21031

Ans:

- ClientHello : client sends supported versions chiphersuites, client random R_c .
- ServerHello : Server picks ciphersuits, sends Server Random R_s .
- Server Certificate : Server proves identity by sending certificate containing its public key.
- (Optional) Serverkey Exchange ; for ephemeral DH/ECDH server sends params signed by server key .
- ClientkeyExchange : either client encrypts peramaster secret with server public key (RSA key-exchange) or sends client DH public value ($DHE/ECDHE$).
- Both compute premaster \rightarrow master secret:

$$\text{master} = \text{PRF}(\text{premaster}, R_c, R_s)$$

derive symmetric keys from master secret.

- Change Cipher Spec & Finished : both sides switch to negotiated symmetric ciphers and verify handshake integrity.

IT-21031

Symmetric keys come from the shared premaster secret produced by asymmetric operations (RSA encryption of premaster or Diffie-Hellman shared secret) combined with nonces and a PRF to derive final session keys.

Ques - 33:

Explain SSH layered architecture (protocol stack) and roles of each layer.

Ans :

- Transport layer (SSH-TRANSPORT) : establishes encrypted, authenticated channel, negotiates algorithms, provides confidentiality integrity optional compression.
- User Authentication Layer (SSH-USERAUTH)

authenticates the user over the secure transport (password, public-key, host-based).

- Connection Layer (SSH-CONNECTION): multiplexes channels (shells, exec, port forwarding, subsystems like SFTP) over the authenticated transport.

IT-21031

Each layer builds on the lower: transport secures, userauth authenticates, connection carries application sessions.

Ques - 3G :

Explain the steps involved in the TLS handshake process.

Ans: (Concise stepwise recap)

- ClientHello (version, ciphers)
- ServerHello (chosen ciphers)
- Server sends certificate (and ServerKeyExchange if needed).
- ServerHello Done.

- Client key Exchange (premaster via RSA or client DH value)
 - (optional) Client certificate + certificateVerify
 - Both compute master secret from premaster and derive session keys.
- IT-21031
- Client sends ChangeCipherSpec and Finished
 - Server sends ChangeCipherSpec and Finished.
 - Secure application traffic begins under negotiated symmetric keys.

Ques - 35 :

General form of elliptic curve equation over a finite field and Why used in cryptography

Ans :

- Over a prime field F_p : $y^2 \equiv x^3 + ax + b \pmod{p}$, with discriminant $4a^3 + 27b^2 \neq 0 \pmod{p}$ to avoid singularities.
- Points on the curve plus a point at infinity form an abelian group (point addition/doubling).

Why used: The Elliptic Curve Discrete Logarithm Problem (ECDLP) - given p and $Q = kp$, find k is believed hard. Ecc gives strong security per bit, enabling smaller keys and faster operations than equivalent RSA schemes.

IT-21031

Ques-36:

How does ECC achieve same level of security as RSA with much smaller keys?

Ans:

- Different hard problems: RSA security rests on integer factorization (sub-exponential GNFS algorithms), while ECC security rests on ECDLP (best general attacks like Pollard's rho run in roughly $\mathcal{O}(\sqrt{n})$ exponential time).
- Consequence: For equivalent security, Ecc needs much smaller key sizes (256-bit Ecc \approx 3072-bit RSA).
- Practical benefits: smaller keys / certificates,

faster key generation /signing - lower storage / communication overhead - useful for constrained devices.

IT-21031

Ques-37:

Given the elliptic curve $y^2 = x^3 + 2x + 3 \pmod{97}$
determine whether the point $P = (3, 6)$ lies on the curve.

Ans:

Compute both sides modulo 97:

- Left: $y^2 = 6^2 = 36 \pmod{97}$
- Right: $x^3 + 2x + 3 = 3^3 + 2 \cdot 3 + 3 = 27 + 6 + 3 = 36 \pmod{97}$

Since $36 \equiv 36 \pmod{97}$, the equality holds.

Yes. $P = (3, 6)$ lies on the curve.

Ques-38: Given public key ($P=23, g=5, h=8$)
and message $m=10$, compute the ElGamal ciphertext using random $k=6$.

Ans: ElGamal encryption (mod p)

- $C_1 = g^k \text{ mod } p$
- $C_2 = m \cdot h^k \text{ mod } p$

Compute:

$$\bullet C_1 = 5^6 \text{ mod } 23 = 15625 \text{ mod } 23 = 8.$$

$$\bullet h^k = 8^6 \text{ mod } 23 = \text{compute } \equiv (\text{gives})?$$

$$\rightarrow 8^2 = 64 \equiv 18, 8^4 \equiv 18^2 = 324 \equiv 2,$$

$$\text{then } 8^2 \equiv 2 \cdot 18 = 36 \equiv 13. \text{ so, } h^6 \equiv 13.$$

$$\bullet C_2 = 10 \cdot 13 \text{ mod } 23 = 130 \text{ mod } 23 = 15.$$

$$\therefore \text{ciphertext: } (C_1, C_2) = (8, 15).$$

IT-21031

Ques - 39:

Explain why lightweight cryptography matters for IoT, and give one example of a lightweight algorithm used in IoT.

Ans:

why it matters:

IoT devices often have severe constraints -

low CPU, little RAM, limited energy, small

Storage - so full-scale conventional crypto (large-block ciphers, heavyweight authenticated protocols) may be too slow, power-hungry, or memory-intensive. Lightweight cryptography provides secure primitives tailored to those constraints: lower computational cost, smaller code size, and lower memory use while still offering adequate security for the device's threat model.

IT-21031

Example algorithm:

Ascon (an authenticated encryption and hashing family) - winner in the NIST lightweight cryptography project - is designed for constrained devices and offers AEAD functionality with small footprint and good performance on low-end microcontrollers. (other examples often used historically:

lightweight AES variants, chacha20-based constructions for low-cost devices and

and specialized ciphers like Simon/Speck
note that Simon/Speck are controversial and
not widely recommended for new standardized
deployments.)

IT-21031

Ques - 40:

List and briefly explain three common
IoT-specific attacks and mitigation strategies

Ans:

1. Firmware hijacking / malicious firmware updates.
 - What: Attacker replaces legitimate firmware with malicious firmware (backdoors, botnet clients).
 - Mitigations: Secure boot, digitally signed firmware updates, code-signature verification, Strict update channels, rollback protection, and regular signed update audits.

2. Physical tampering / device compromise

- What: Attacker with physical access extracts keys · modifies hardware , or installs implants.
- Mitigations : Use tamper-evident / tamper-resistant enclosures , secure elements or TPMs to protect keys , disable debug ports in production hardware-based key storage (root of trust) and device attestation.

3. Botnets / mass compromises

IT-21031

- What: Default / weak credentials or vulnerable services are exploited at scale to enslave devices into DDoS botnets.
- Mitigations: Enforce strong unique credentials · disable unused services / ports , network segmentation , rate-limiting automated patching use of device identity + certificate-based authentication and monitoring / IDS to detect

unusual outbound traffic.

Additional general strategies: least privilege, encrypted communications (TLS with proper cert / nonce handling), periodic security audits, supply-chain security and incident response planning.

IT-21031