CS 106B, Lecture 27 Hashing

小结:

hashing的idea和概念

collision(不同value的hash value相同)及其解决方案: separate chaining

rehashing: 当前储存容器过密(load factor过高):增长hash table, 打散separate chain

好的hash function特征

Plan for Today

- Implementing the last data structure of CS106B: a HashMap/HashSet
 - What is hashing?
 - How can we achieve the O(1) add, remove, contains of a HashSet?

Implementing a set

- Consider implementing a set as an unfilled array.
 - What would make a good ordering for the elements?
- If we store them in the **next available index**, as in a vector, ...

```
set.add(9);
set.add(23);
set.add(8);
...
```

index	0	1	2	3	4	5	6	7	8	9
value	9	23	8	-3	49	12	0	0	0	0
size	6	capacity			10					

- How efficient is add? contains? remove?
 - O(1), O(N), O(N)

Sorted array set

• Suppose we store the elements in an unfilled array, but in **sorted** order rather than order of insertion.

```
set.add(9);
set.add(23);
set.add(8);
set.add(-3);
set.add(49);
set.add(12);
```

```
      index
      0
      1
      2
      3
      4
      5
      6
      7
      8
      9

      value
      -3
      8
      9
      12
      23
      49
      0
      0
      0
      0

      size
      6
      capacity
      10
```

- How efficient is add? contains? remove?
 - O(N), O(log N), O(N)

A strange idea

- Silly idea: When client adds value i, store it at index i in the array.
 - Would this work?
 - Problems / drawbacks of this approach? How to work around them?

```
set.add(9);
...
set.add(18);
set.add(12);
```

set.add(7);

set.add(1);

```
    index
    0
    1
    2
    3
    4
    5
    6
    7
    8
    9

    value
    0
    1
    0
    0
    0
    0
    0
    7
    0
    9

    size
    3
    capacity
    10
```

```
    index
    0
    1
    2
    3
    4
    5
    6
    7
    8
    9
    0
    1
    2
    3
    4
    5
    6
    7
    8
    9

    value
    0
    1
    0
    0
    0
    0
    0
    7
    0
    9
    0
    0
    12
    0
    0
    0
    0
    0
    18
    0

    size
    5
    capacity
    20
```

Hash Functions

• hash function: function of the form

int hashFunc(Type arg);

- must be deterministic (same input produces the same output)
- should be well-distributed (the numbers produced are as spread out



- Idea: Store any given element value in the index given by the hash function (why hash functions must be consistent)
 - In previous slide, our (bad) "hash function" was: $hashCode(i) \rightarrow i$.
 - Drawbacks?
 - Potentially requires a large array (array capacity > i).
 - Array could be very sparse, mostly empty (memory waste).

Improving Space Efficiency

- If any number is equally possible, we'll need a huge array, even if we only have a couple of buckets
- Idea: use a hash function, but modify the result to be within a much smaller range (the size of the array)
- We can then think of the array as a sequence of buckets storing elements

```
int getIndex(Type value) {
    return hashCode(value) % capacity;
}
```

Efficiency of hashing

```
int getIndex(int i) {
    return hashCode(i) % capacity;
}

- add:    elements[getIndex(i)] = i;
- contains:    if (elements[getIndex(i)] == i) { ... }
- remove:    elements[getIndex(i)] = 0;

• Q: What is the runtime of add, contains, and remove?
```

A. O(1) **B.** O(log N) **C.** O(N) **D.** O(N log N) **E.** O(N^2)

Are there any problems with this approach?

Collisions

• collision: When a hash function maps 2 values to same index.

```
// hashCode = abs(i)
```

```
set.add(11);
set.add(49);
set.add(24);
set.add(37);
set.add(54);
// collides with 24 :-(
```

- collision resolution: An algorithm for fixing collisions.
- A hash function should be well-distributed to minimize collisions.

Probing

- **probing**: Resolving a collision by moving to another index.
 - linear probing: Moves to the next available index (wraps if needed).

```
set.add(11);
set.add(49);
set.add(24);
set.add(37);
set.add(54); // collides with 24; must probe
```

- quadratic probing: a variation that moves increasingly far away:
 - index +1, +4, +9, ...
- Drawbacks of probing? How does this change add, contains, etc.?

Clustering

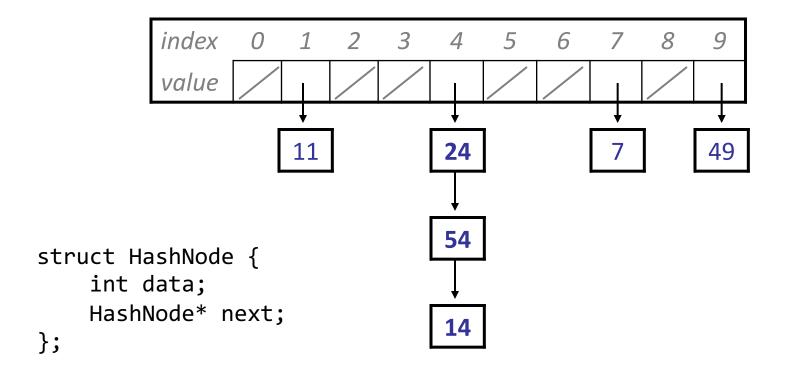
- clustering: Clumps of elements at neighboring indexes.
 - slows down the hash table lookup; you must loop through them.

```
index
set.add(11);
                           11
                                       54
                                           14
                  value
                                    24
                                                    49
set.add(49);
                           capacity
                                    10
                   size
set.add(24);
set.add(37);
set.add(54); // collides with 24
set.add(14); // collides with 24, then 54
set.add(86); // collides with 14, then 37
```

- A lookup for 94 must look at 7 out of 10 total indexes.
- Must have a special value for removed elements (tombstones).

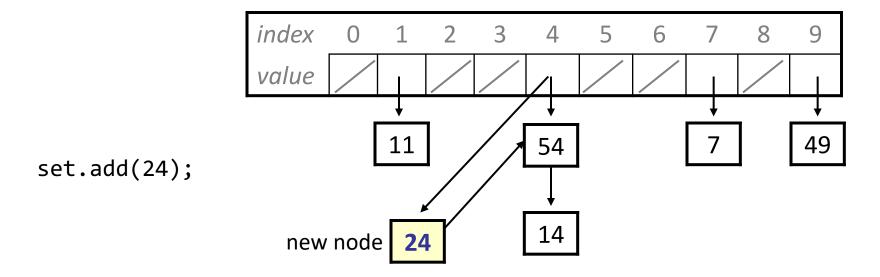
Separate chaining

- separate chaining: Solving collisions by storing a list at each index.
 - add/search/remove must traverse lists, but the lists are short
 - impossible to "run out" of indexes, unlike with probing



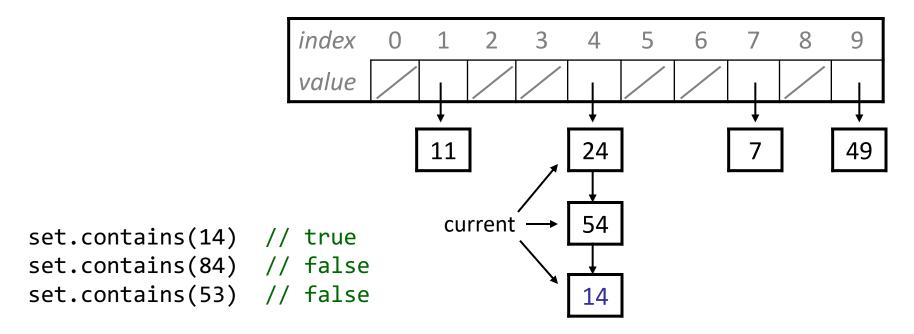
The add operation

- How do we add an element to the hash table?
 - Recall: To modify a linked list, you must either change the list's front reference, or the next field of a node in the list.
 - Where in the list should we add the new element?
 - Must make sure to avoid duplicates.



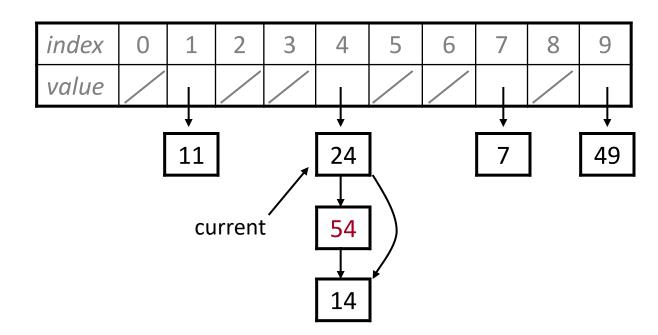
The contains operation

- How do we search for an element in the hash table?
 - Must loop through the linked list for the appropriate hash index, looking for the desired value.
 - Recall: Traverse a linked list with a "current" node pointer.



The remove operation

- How do we remove an element from the hash table?
 - Cases to consider: front (24), non-front (14), not found (94), null (32)
 - To remove a node from a linked list, you must either change the list's front, or the next field of the *previous* node in the list.



set.remove(54);

Announcements

- Assn. 7 is due Thursday
- Please fill out the survey for this class! We really appreciate it.
- Thursday class is optional.
- Final is Friday, at 12:15PM, in Hewlett
 - More information:
 https://web.stanford.edu/class/cs106b/exams/final.html

Exercise: HashSet

- Implement a HashSet class that represents a set of integers using a hash table.
 - Include the following public members:

```
HashSet()
add(int value)
clear()
contains(int value)
remove(int value)
```

HashSet.h

```
struct HashNode {
    int data;
    HashNode* next;
};
class HashSet {
public:
    HashSet();
    ~HashSet();
    void add(int value);
    void clear();
    bool isEmpty() const;
    bool contains(int value) const;
    void remove(int value);
    int size() const;
private:
    HashNode** elements;
    int mysize;
    int capacity;
    int getIndex(int value) const;
};
```

HashSet.cpp

```
#include "HashSet.h"
HashSet::HashSet() {
    capacity = 10;
    mysize = 0;
    elements = new HashNode*[capacity](); // all are null
}
void HashSet::add(int value) {
    if (!contains(value)) {
        int h = hashCode(value);  // insert at front of chain
        elements[h] = new HashNode(value, elements[h]);
        mysize++;
bool HashSet::contains(int value) const {
    HashNode* curr = elements[hashCode(value)];
    while (curr != nullptr) {
        if (curr->data == value) { return true; }
        curr = curr->next;
    return false;
```

HashSet.cpp 2

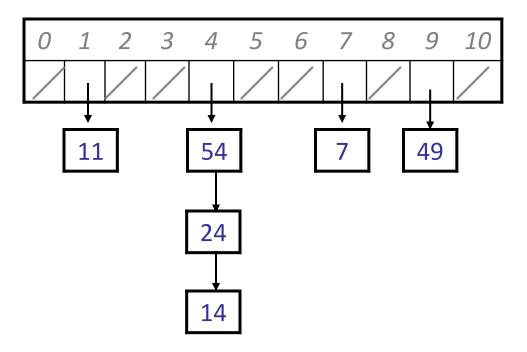
```
HashSet::~HashSet() {
    clear();
    delete[] elements;
}
void HashSet::clear() {
    for (int i = 0; i < capacity; i++) {
        while (elements[i] != nullptr) {    // free all chains
            HashNode* trash = elements[i];
            elements[i] = elements[i]->next;
            delete trash;
    mysize = 0;
}
int HashSet::getIndex(int value) const {
    return hash(value) % capacity;
}
```

HashSet.cpp 3

```
void HashSet::remove(int value) {
    int h = hashCode(value);
    if (elements[h] != nullptr) {
        if (elements[h]->data == value) {  // remove from front
            HashNode* trash = elements[h];
            elements[h] = elements[h]->next;
            mysize--;
            delete trash;
        } else {
            HashNode* curr = elements[h];
            while (curr->next != nullptr) { // from middle/end
                if (curr->next->data == value) {
                    HashNode* trash = curr->next; // found it
                    curr->next = curr->next->next;
                    mysize--;
                    delete trash;
                    break;
                curr = curr->next;
```

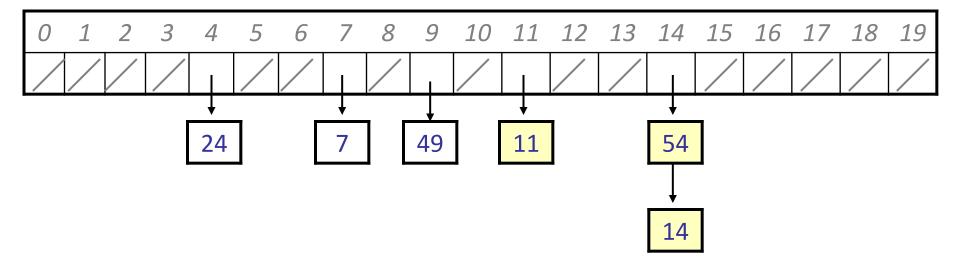
Rehashing

• rehash: Growing to a larger array when the table is too full.



Rehashing

- rehash: Growing to a larger array when the table is too full.
 - Cannot simply copy the old array to a new one. (Why not?)

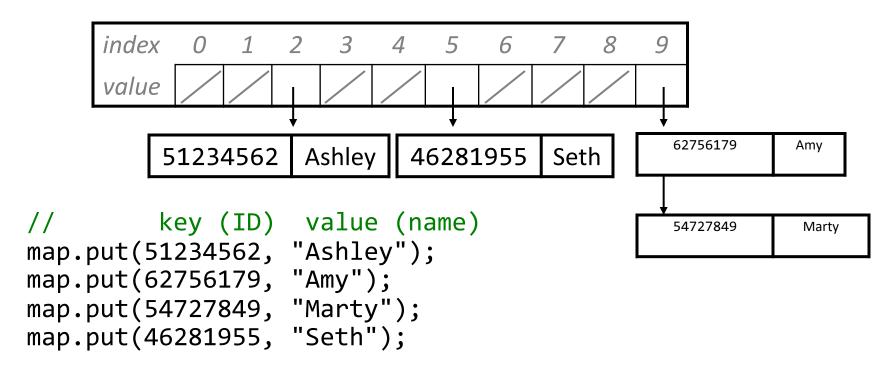


- load factor: ratio of (# of elements) / (hash table length)
 - many implementations rehash when load factor \cong .75

Overflow

Hash map

A hash map is like a set where the nodes store key/value pairs:



Must modify the HashNode class to store a key and a value

Hash map vs. hash set

- The hashing is always done on the keys, not the values.
- The contains function is now containsKey; there and in remove,
 you search for a node whose key matches a given key.
- The add method is now put; if the given key is already there, you must replace its old value with the new one.

```
map.put(54727849, "Chris"); // replace Marty with Chris
```

