

CS 106X, Lecture 18

Arrays and Trees

reading:

Programming Abstractions in C++, Chapters 11.3, 16.1

Plan For Today

- Arrays
- Announcements
- Trees

Learning Goals

- Understand the difference between Vectors and arrays
- Understand how trees use pointers to represent data in useful ways

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Arrays

2	12	15	6	-1	4
---	----	----	---	----	---

type name length

int myArray[6];

(on the stack)

Arrays

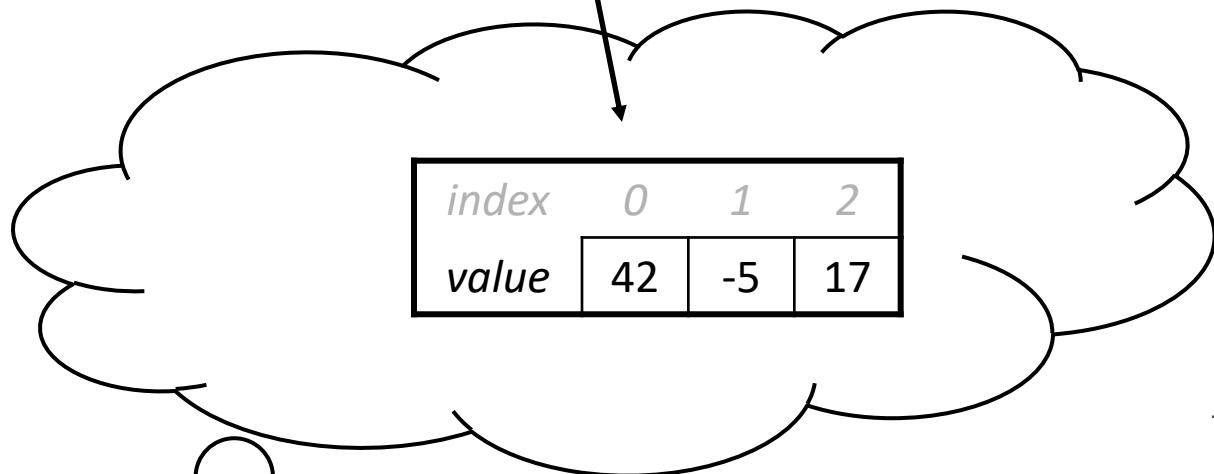
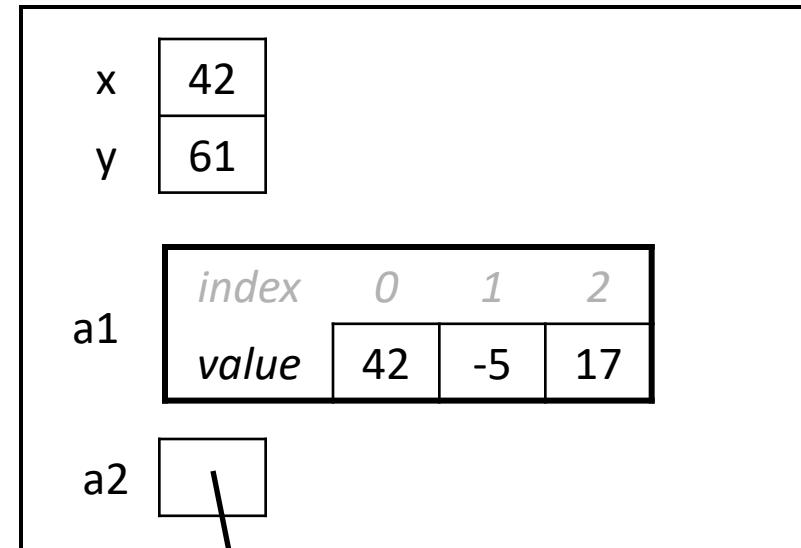
2	12	15	6	-1	4
---	----	----	---	----	---

```
type           name          type           length  
int *myArray = new int[6];
```

(on the heap)

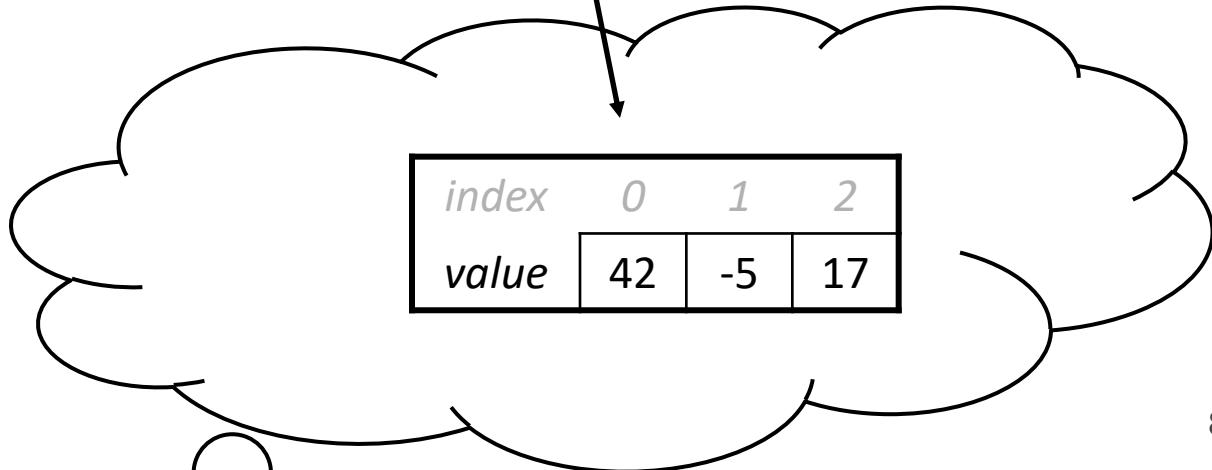
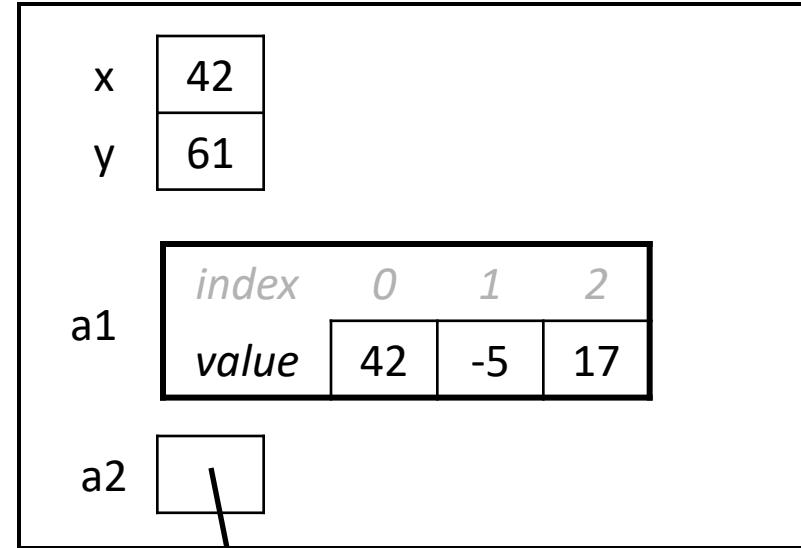
Stack and Heap

```
void makeArrays() {  
    int x = 42;  
    int y = 61;  
    int a1[3];  
    int* a2 = new int[3];  
    ...  
}
```

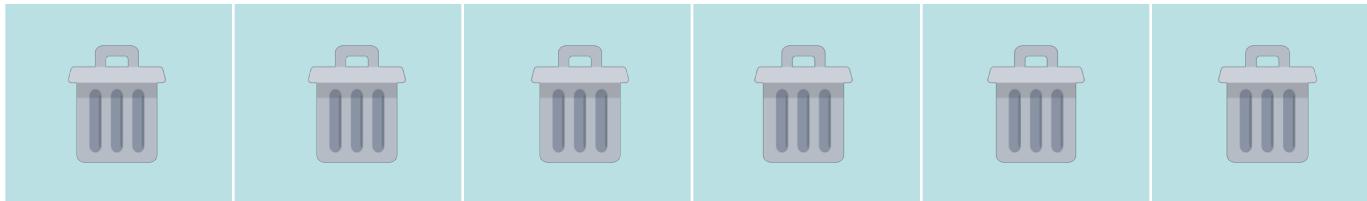


Stack and Heap

```
void makeArrays() {  
    int x = 42;  
    int y = 61;  
    int a1[3];  
    int* a2 = new int[3];  
delete[] a2;  
    ...  
}
```



Heap Initialization



*int *myArray = new int[6];*

Heap Initialization



*int *myArray = new int[6]();*

slower!

A red arrow points from the word "slower!" to the empty parentheses at the end of the code line, highlighting the performance impact of dynamically allocating an array and initializing it with a constructor.

Arrays As Parameters

```
void myFunction(int arr[]) {  
    ...  
}  
  
int main() {  
    int myArray[6];  
    myFunction(myArray);  
    return 0;  
}
```

Array Length

- C++ arrays have no members!
 - No `size` field
 - No helpful methods like `indexOf`

```
int arraySize = 6;
```

```
int myArray[arraySize];
```

```
for int i = 0; i < arraySize; i++) {  
    myArray[i] = ...  
}
```

Array Length

- C++ arrays have no members!
 - No **size** field
 - No helpful methods like **indexOf**

```
void myFunction(int arr[], int size) {  
    ...  
}  
  
int main() {  
    int arraySize = ...  
    int myArray[arraySize];  
    myFunction(myArray, arraySize);  
}
```

How Vector/Stack works

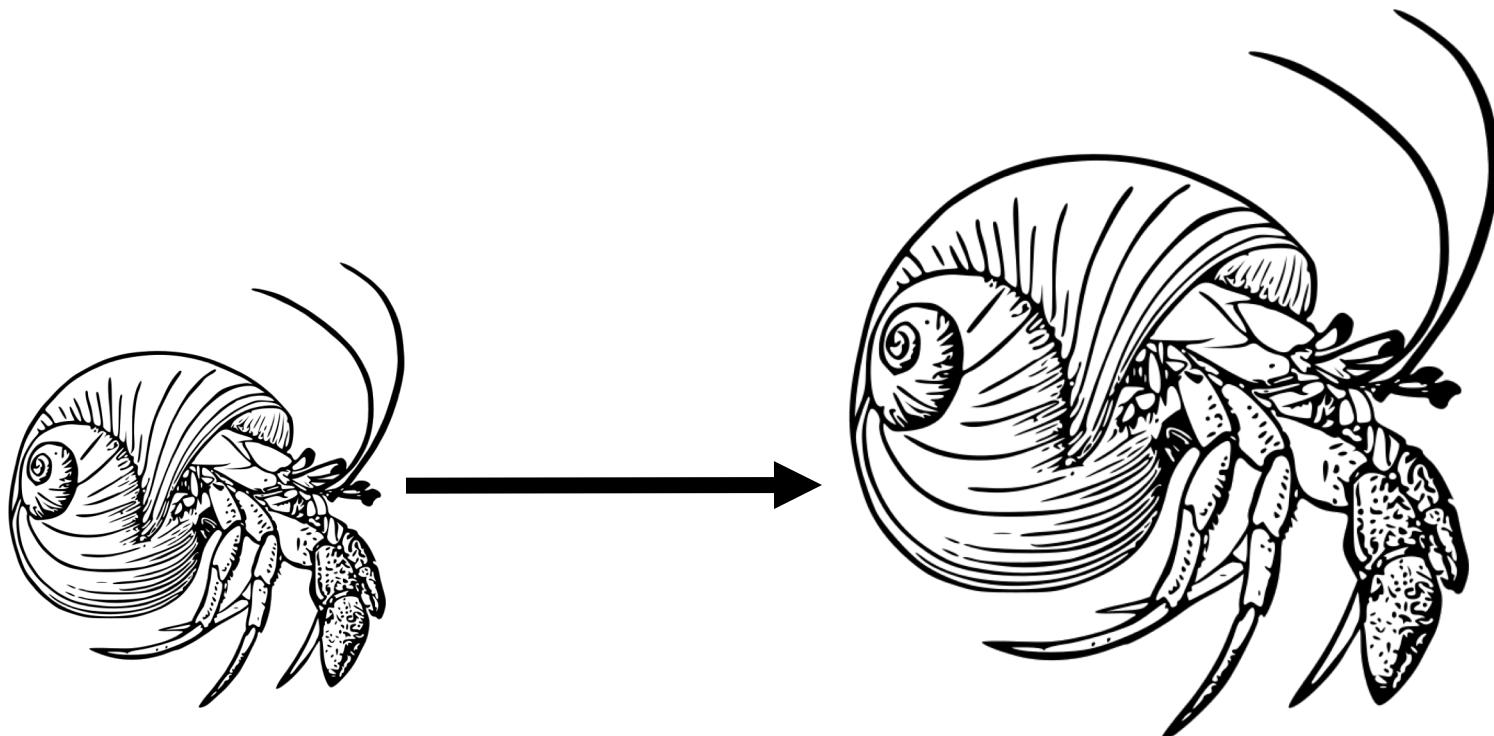
- Vectors and Stacks contain internal **arrays** to store elements.
- The array is created with some extra space (it is an “unfilled array”), and is replaced with a larger array when space runs out.

```
Vector<int> v;  
v.add(42);  
v.add(-5);  
v.add(17);
```

index	0	1	2	3	4	5	6	7	8	9
value	42	-5	17	0	0	0	0	0	0	0
size	3	capacity	10							

```
Stack<int> s;  
s.push(42);  
s.push(-5);  
s.push(17);
```

Outgrowing Our Shell



Exercise

- Let's implement a **stack** using an unfilled array.
 - We'll call it **ArrayStack**. It will be very similar to the C++ Stack.
 - its behavior:
 - `push(value)`
 - `pop()`
 - `peek()`
 - `isEmpty()`
 - `toString()`
 - `operator <<`
 - The stack's *size* will be the number of elements added to it so far.
 - The actual array length ("capacity") in the object may be larger. We'll start with an array of **length 10** by default.

ArrayStack.h

```
class ArrayStack {  
public:  
    ...  
  
private:  
    int elements[INITIAL_CAPACITY];  
    ...  
};
```

ArrayStack.h

```
class ArrayStack {  
public:  
    ...  
  
private:  
    int *elements;  
    ...  
};
```

ArrayStack.cpp

```
ArrayStack::ArrayStack() {  
    elements = new int[INITIAL_CAPACITY]();  
    ...  
}
```

Plan For Today

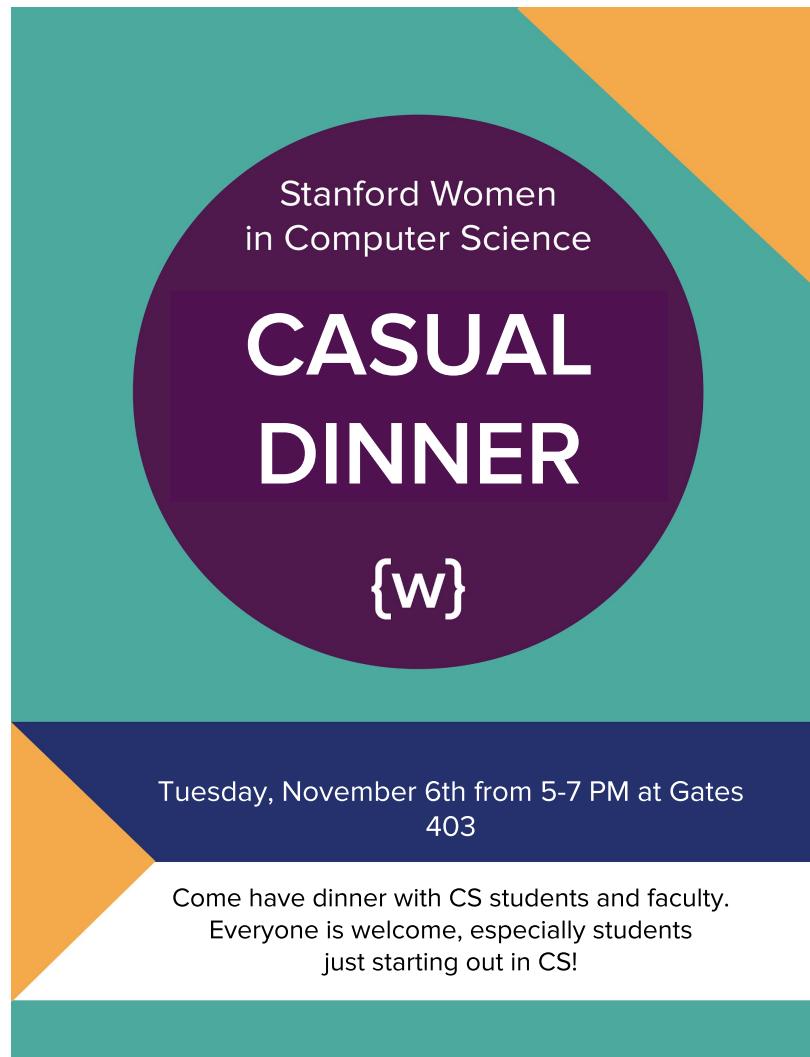
- Arrays
- Announcements
- Trees

Announcements

- Congratulations on finishing the midterm!
- Midterms will be graded and handed back by Monday
- Section Leading Application due tonight at midnight! See cs198.stanford.edu

Announcements

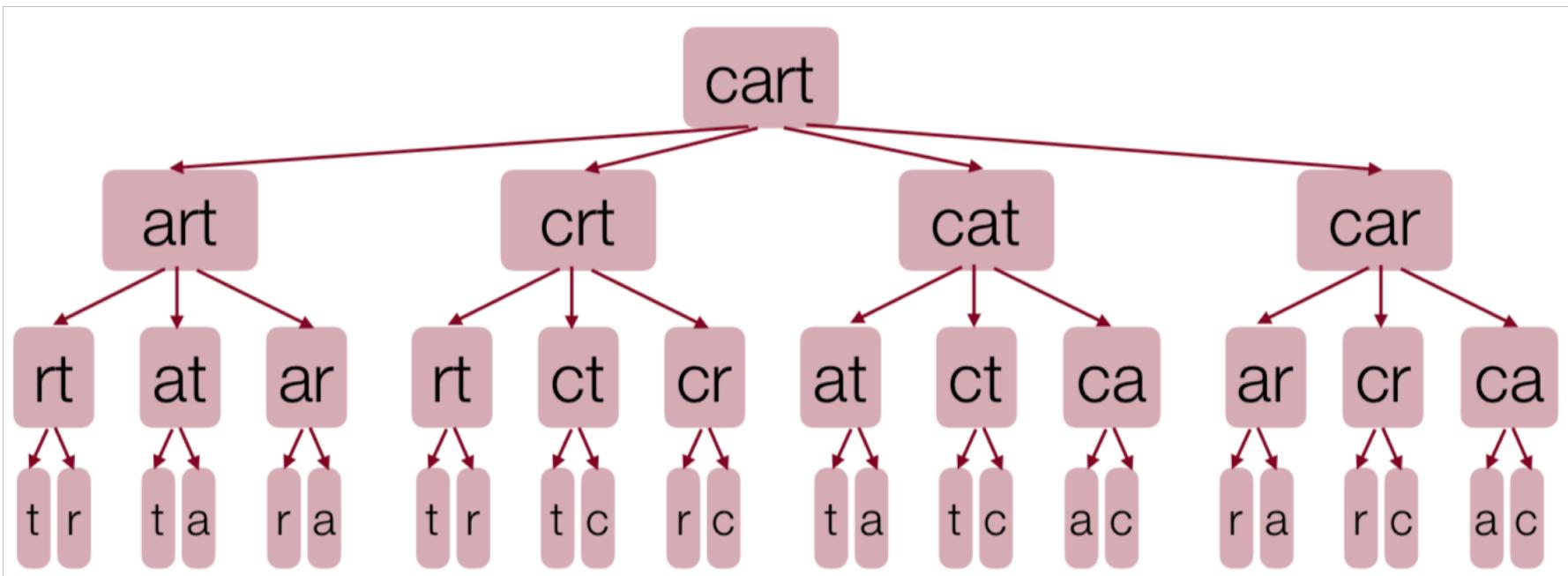
- WiCS Casual Dinner **Tues. 11/6 5-7 in Gates 403!** Join me!



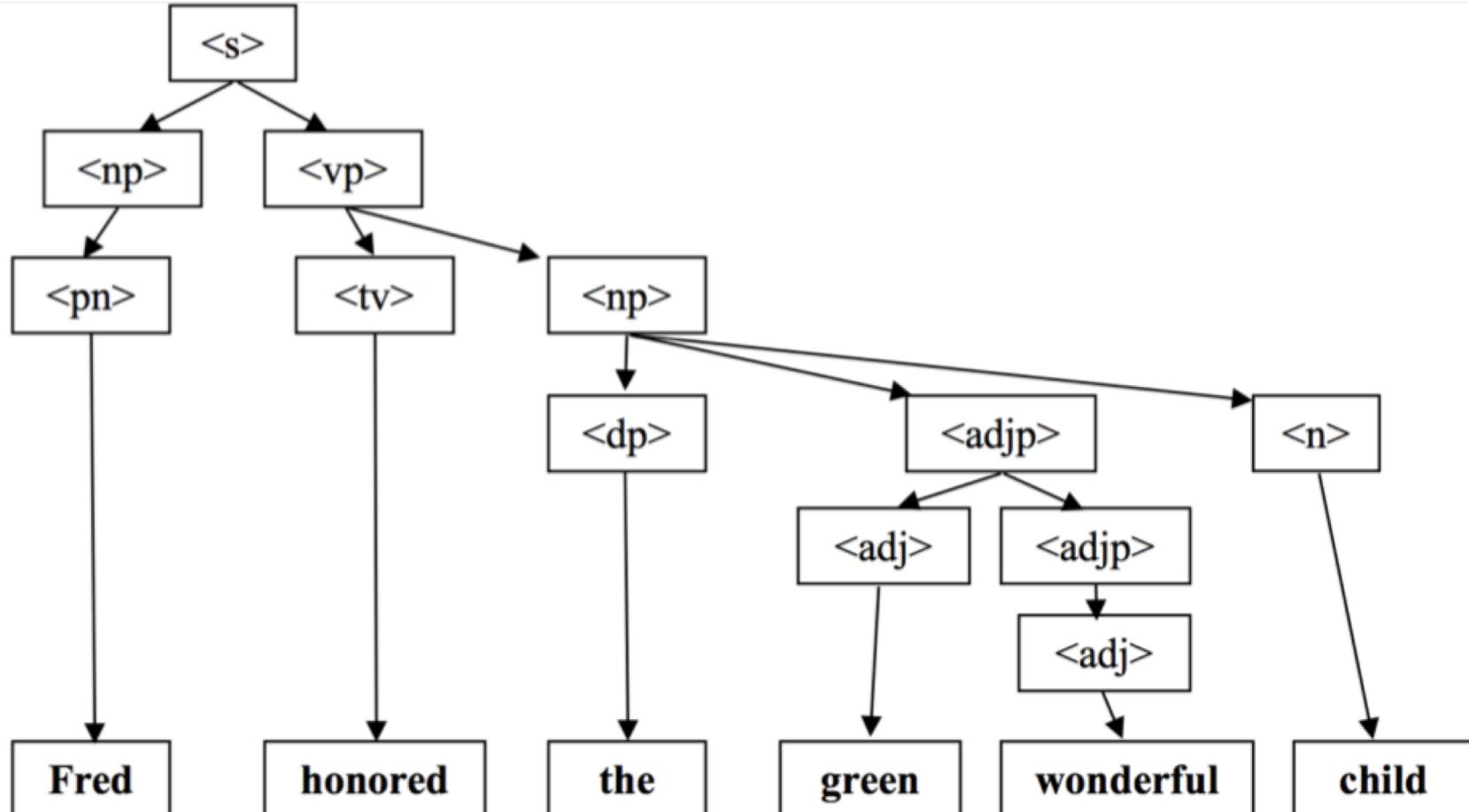
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Trees

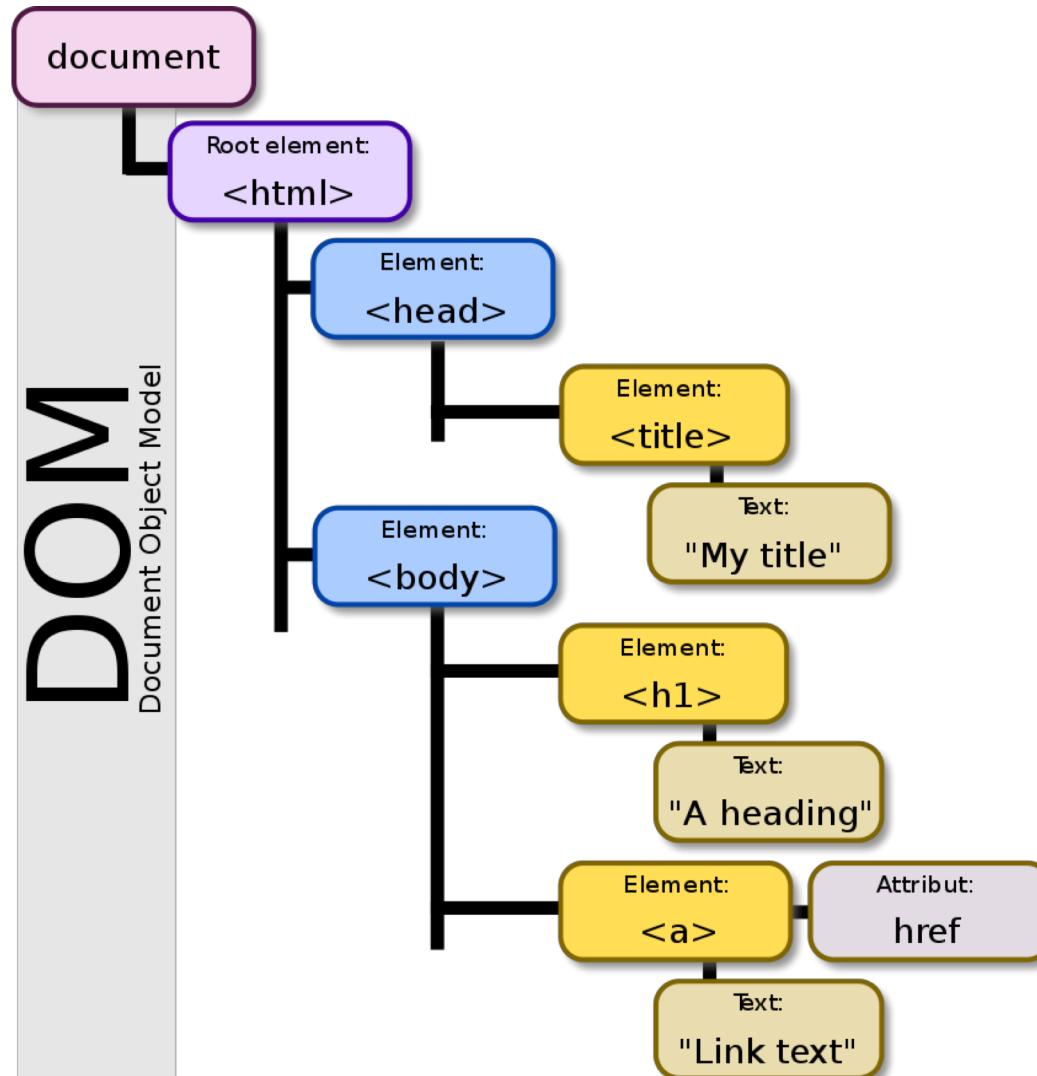


Trees

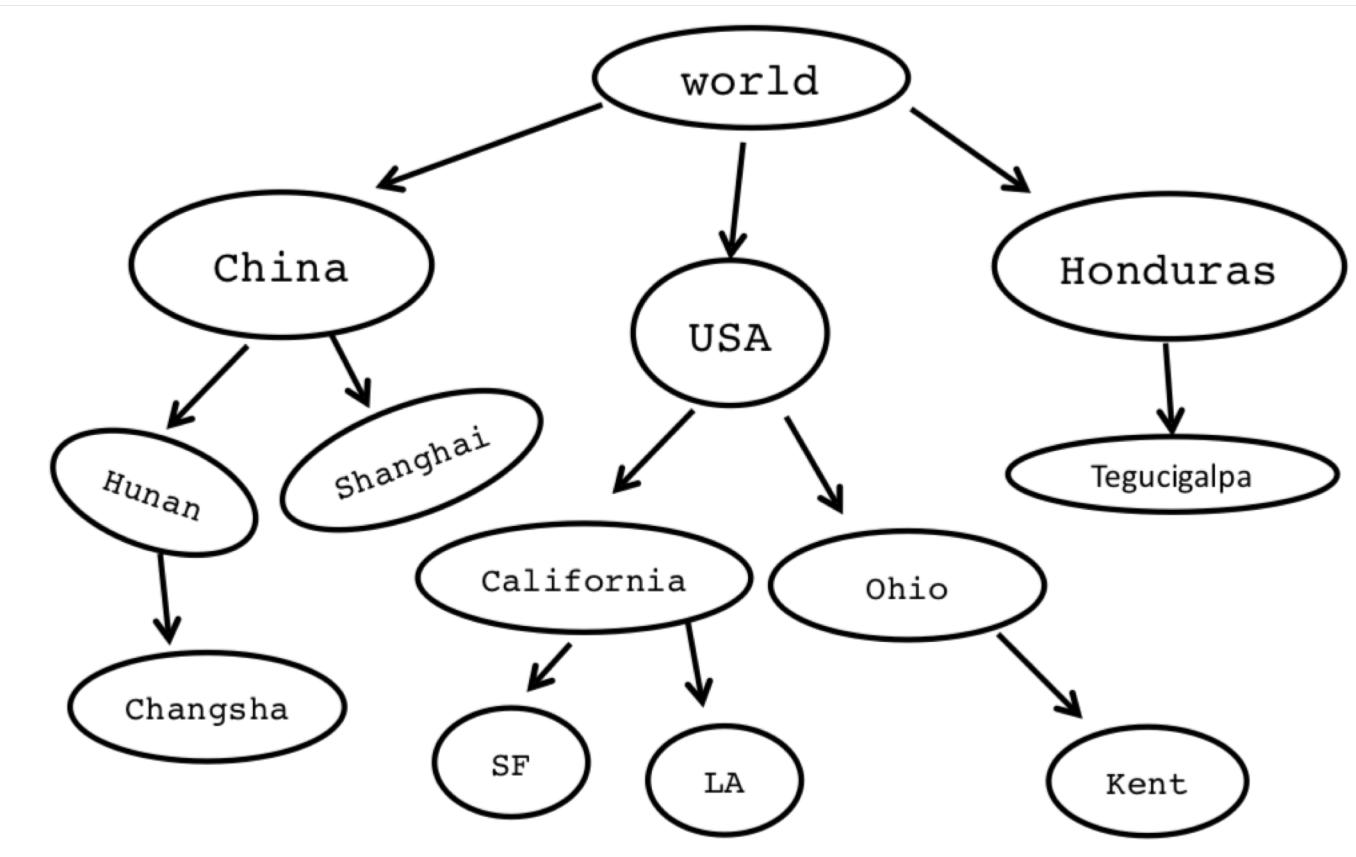


Random expansion from sentence.txt grammar for symbol "<s>"

Trees

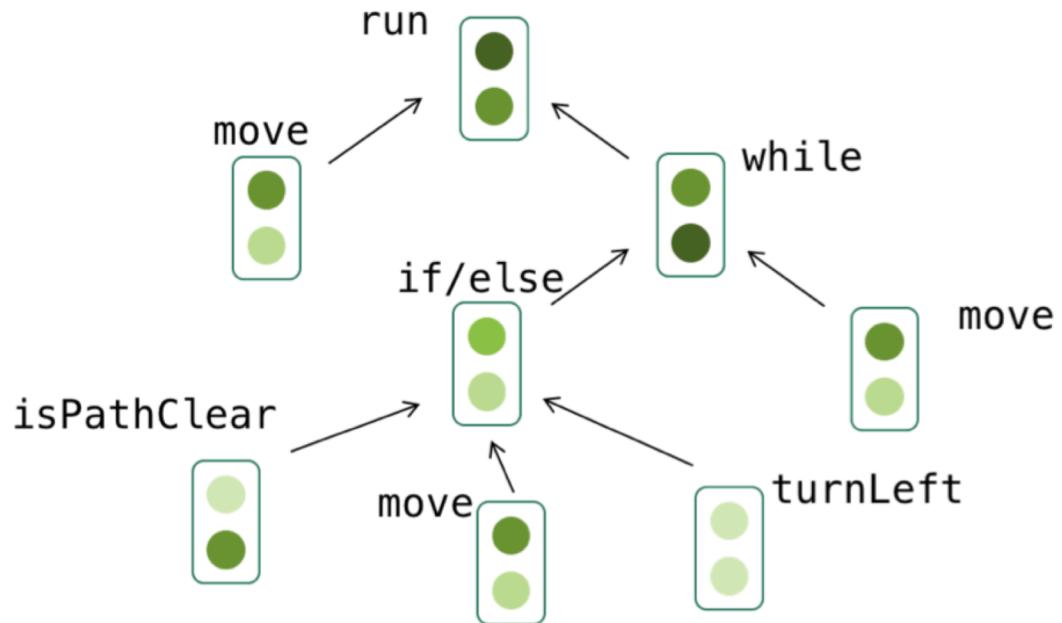


Trees



Trees

```
// Example student solution
function run() {
    // move then loop
    move();
    // the condition is fixed
    while (notFinished()) {
        if (isPathClear()) {
            move();
        } else {
            turnLeft();
        }
        // redundant
        move();
    }
}
```

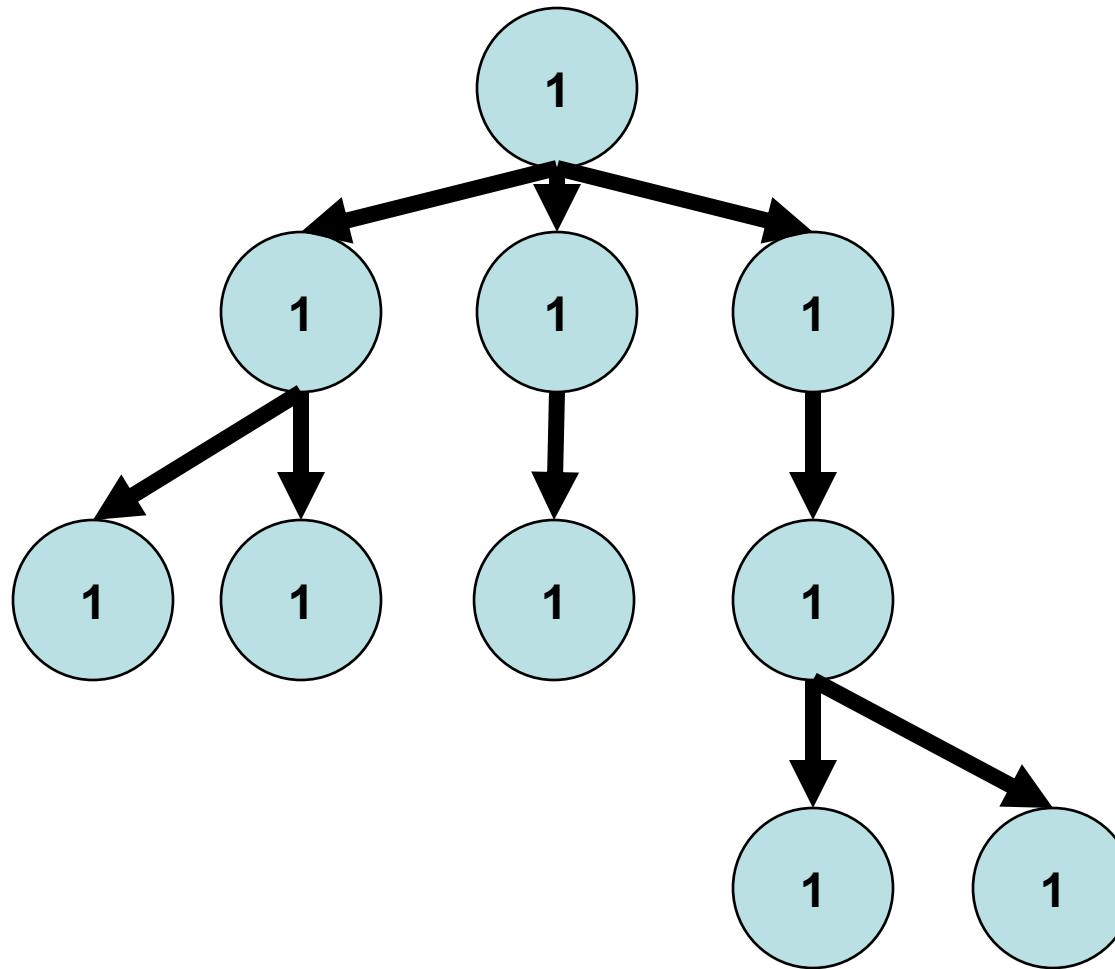


This is a figure in an academic paper written by a recent CS106 student!

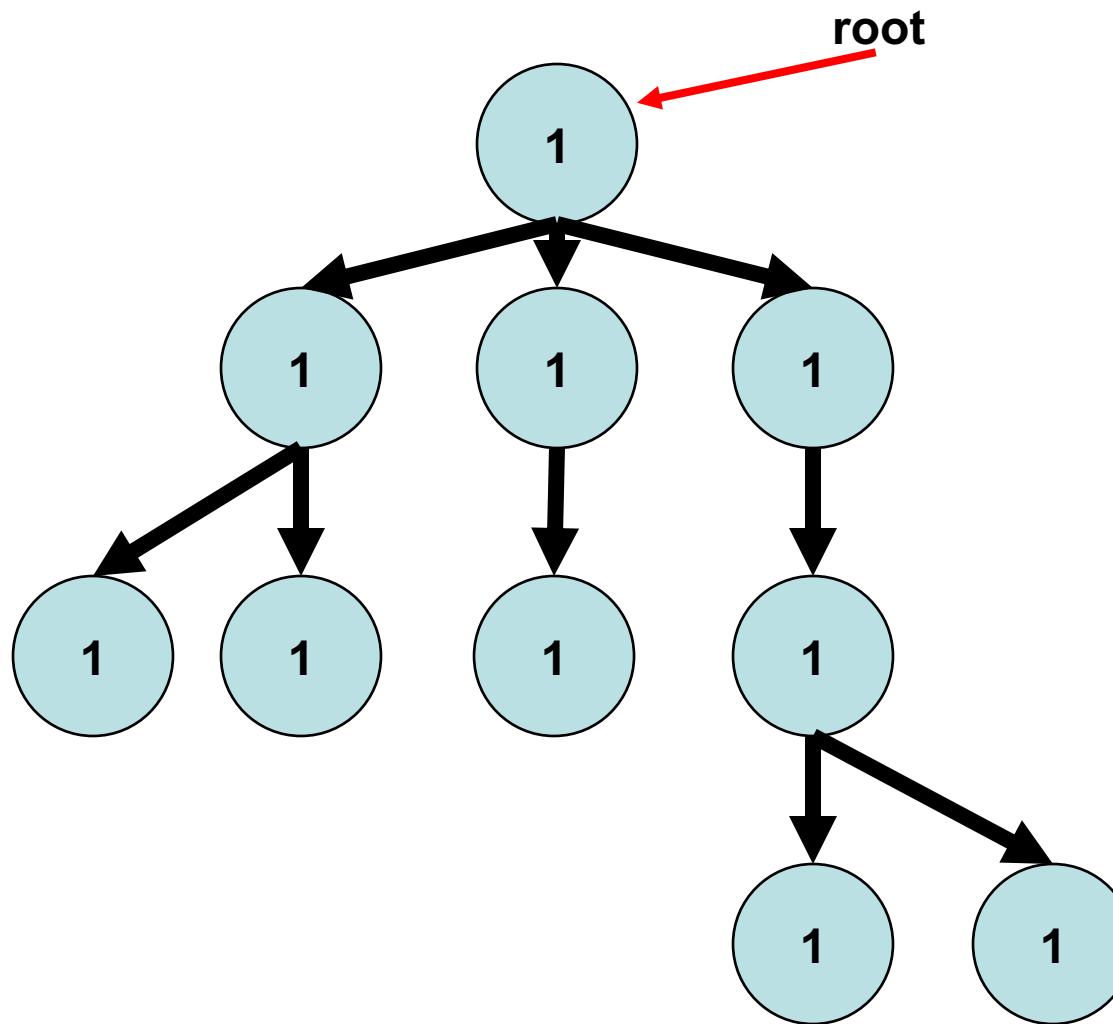
Trees

- **Tree:** a directed, acyclic structure of linked nodes
 - **Directed:** has one-way links between nodes
 - **Acyclic:** No path wraps back around to the same node twice (aka only one unique path from a node to any other node).
- Recursive!
 - A tree is either empty, or
 - A root node that contains **data** and zero or more **subtrees**.

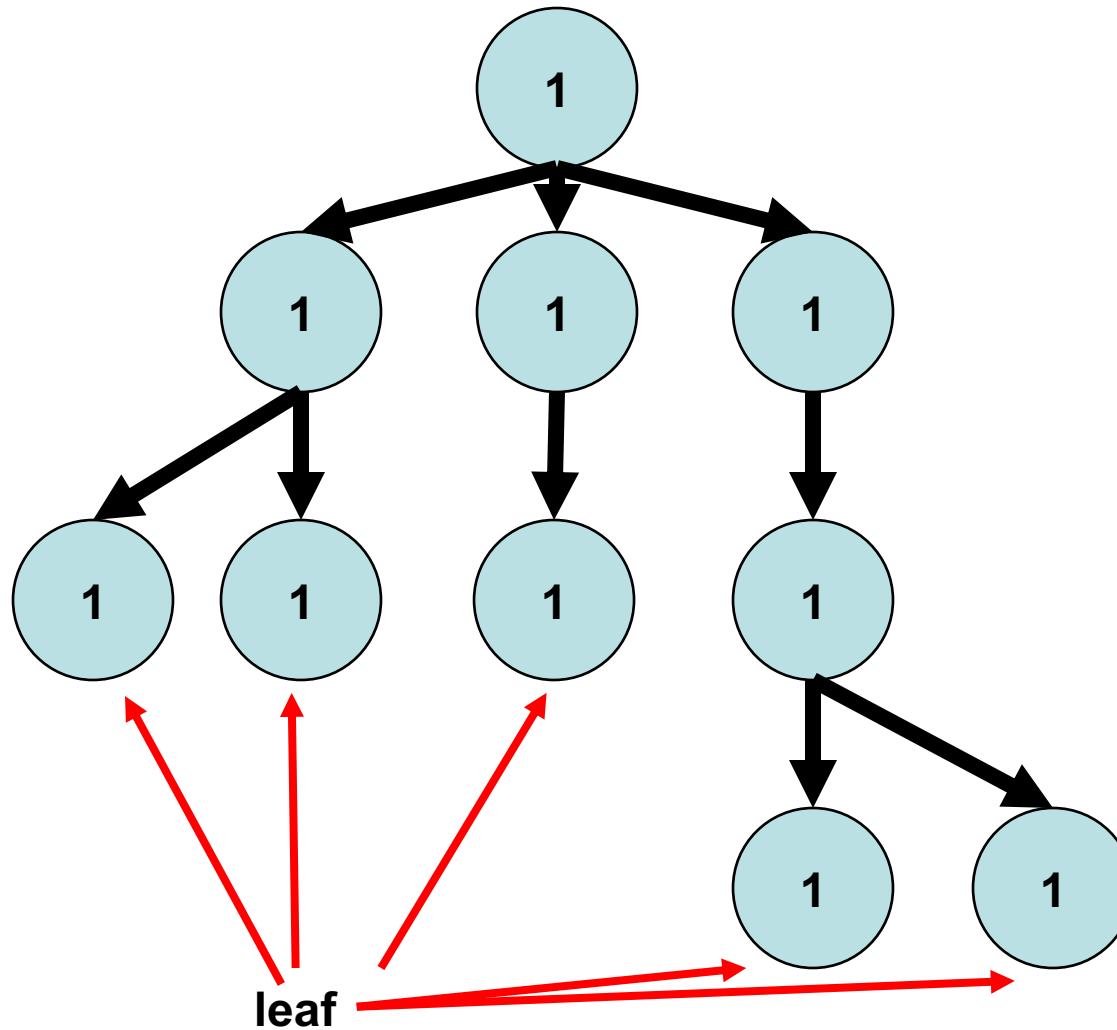
Trees



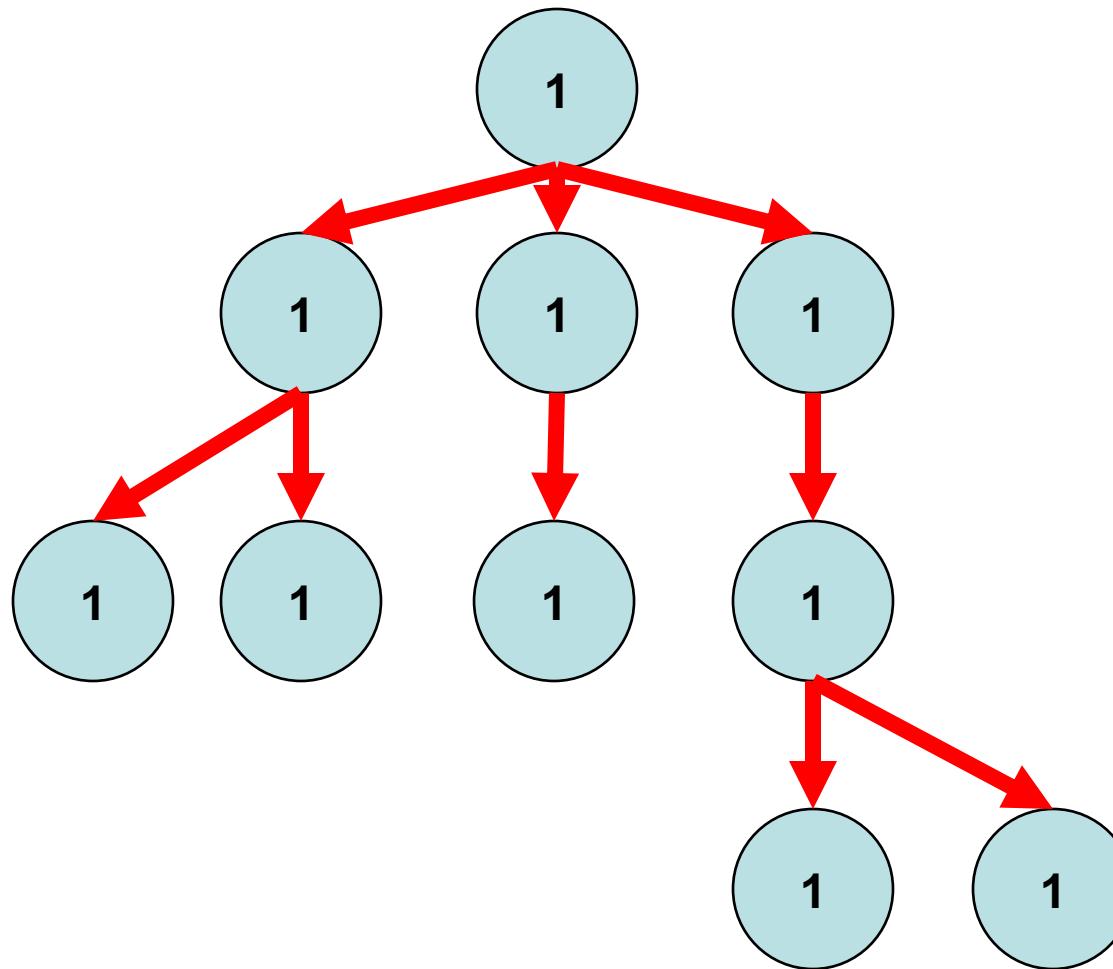
Trees



Trees

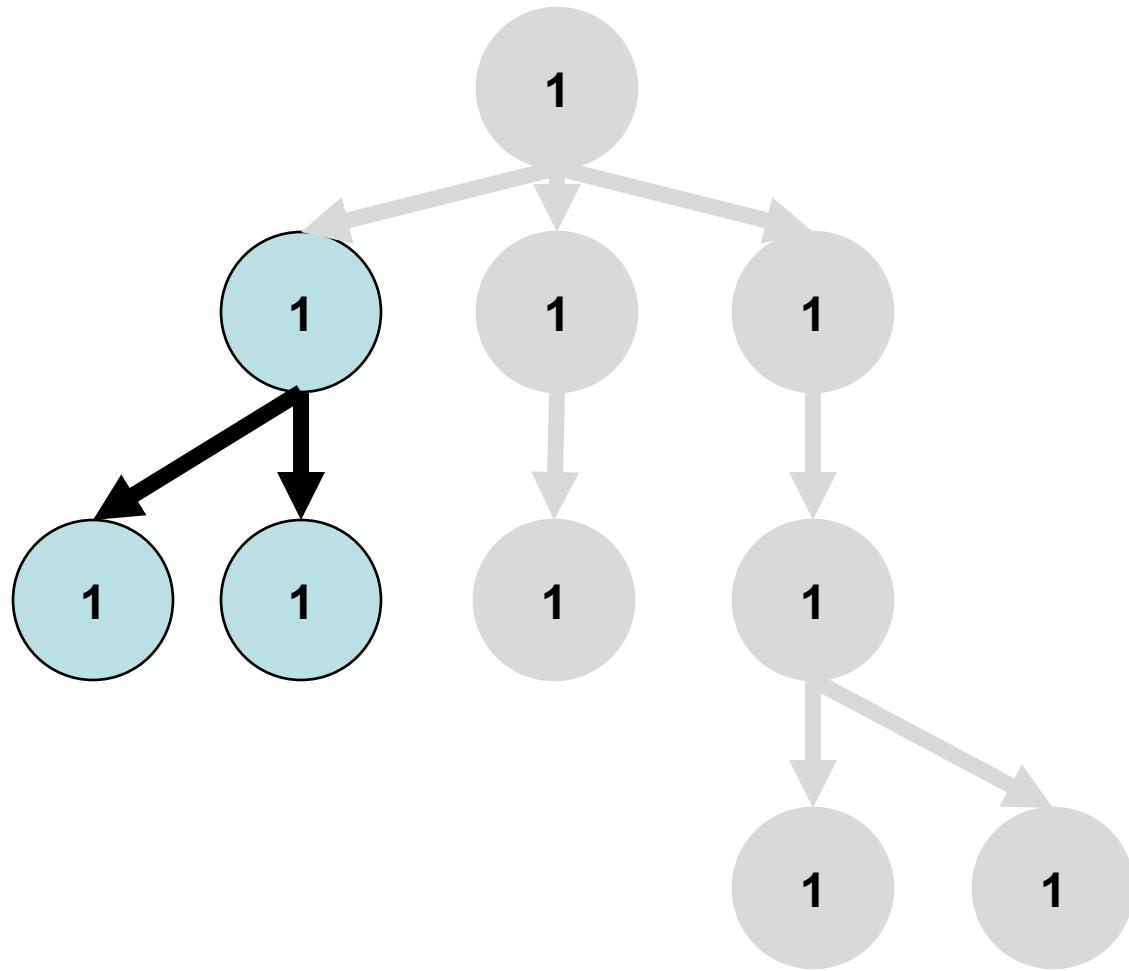


Trees

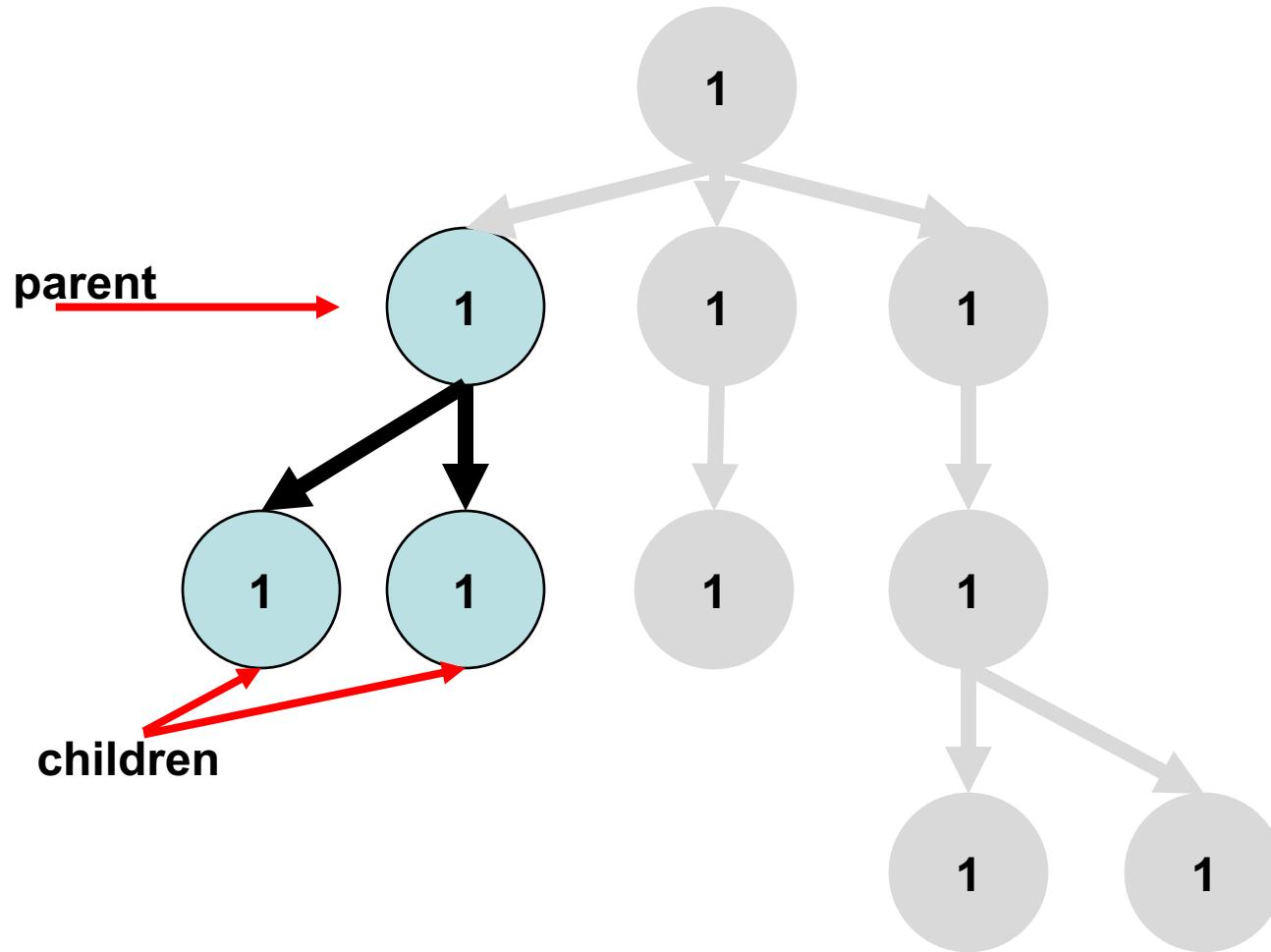


branches

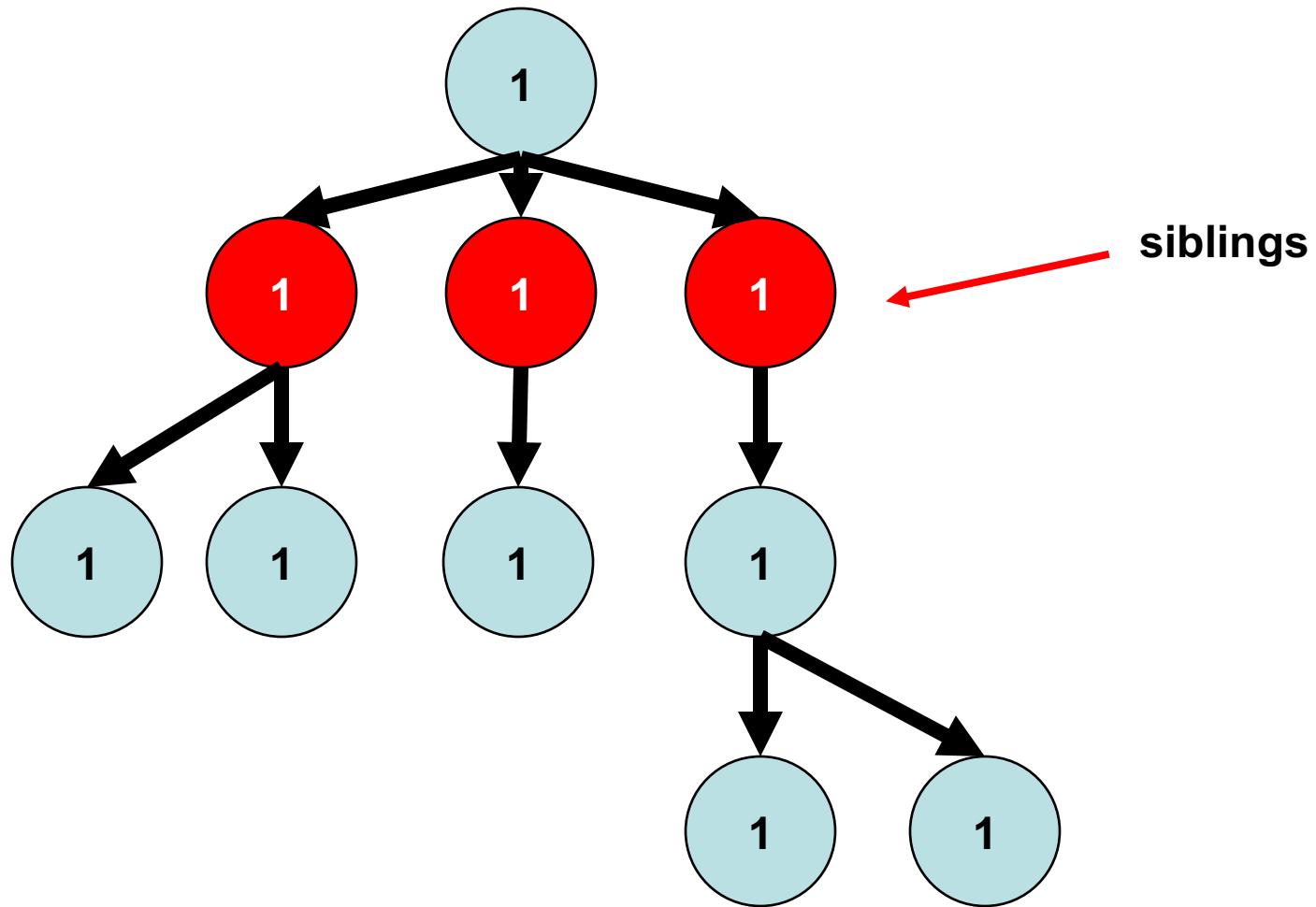
Trees



Trees



Trees



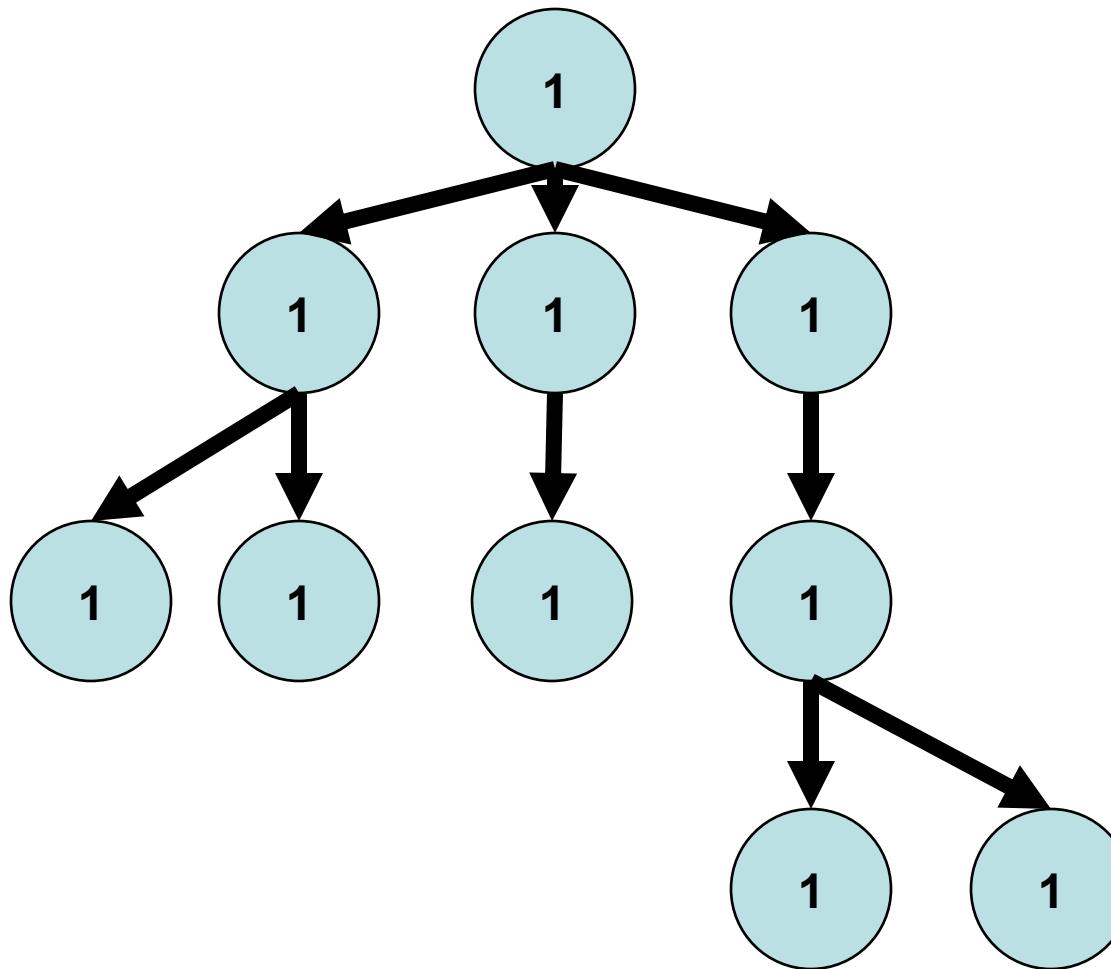
Trees

Level 1

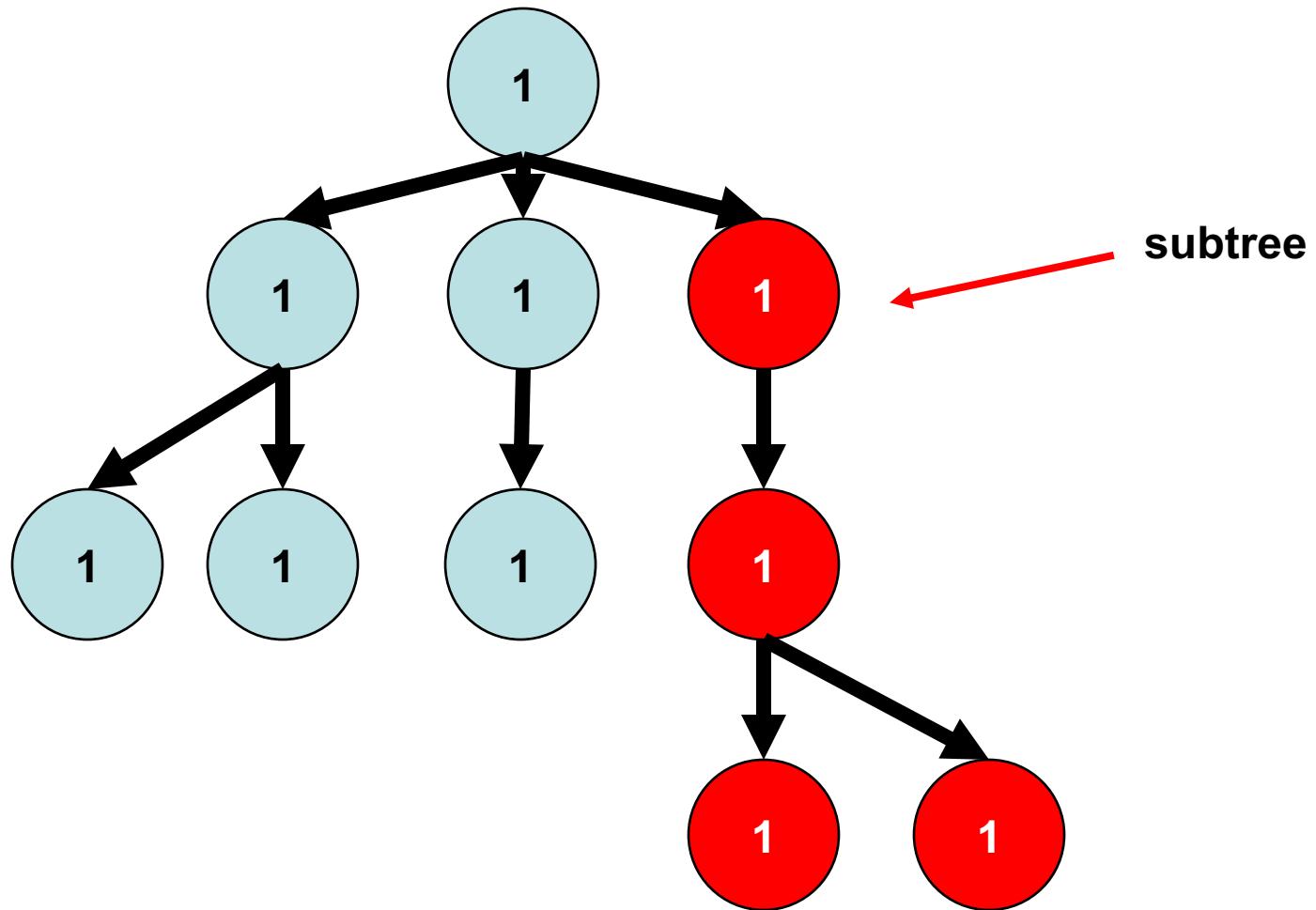
Level 2

Level 3

Level 4

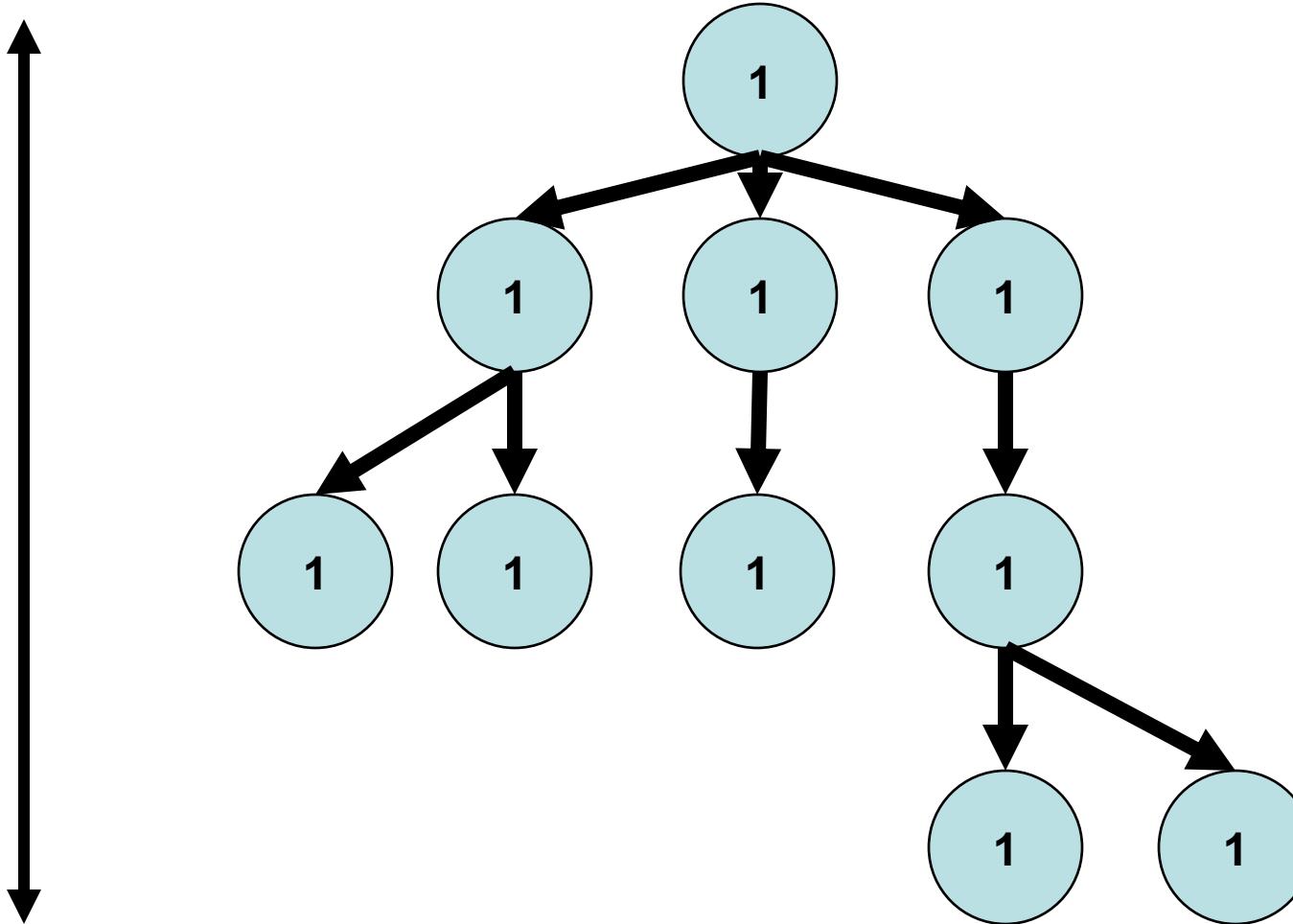


Trees



Trees

Height = 4 \rightarrow longest path from the root to any node, in # nodes



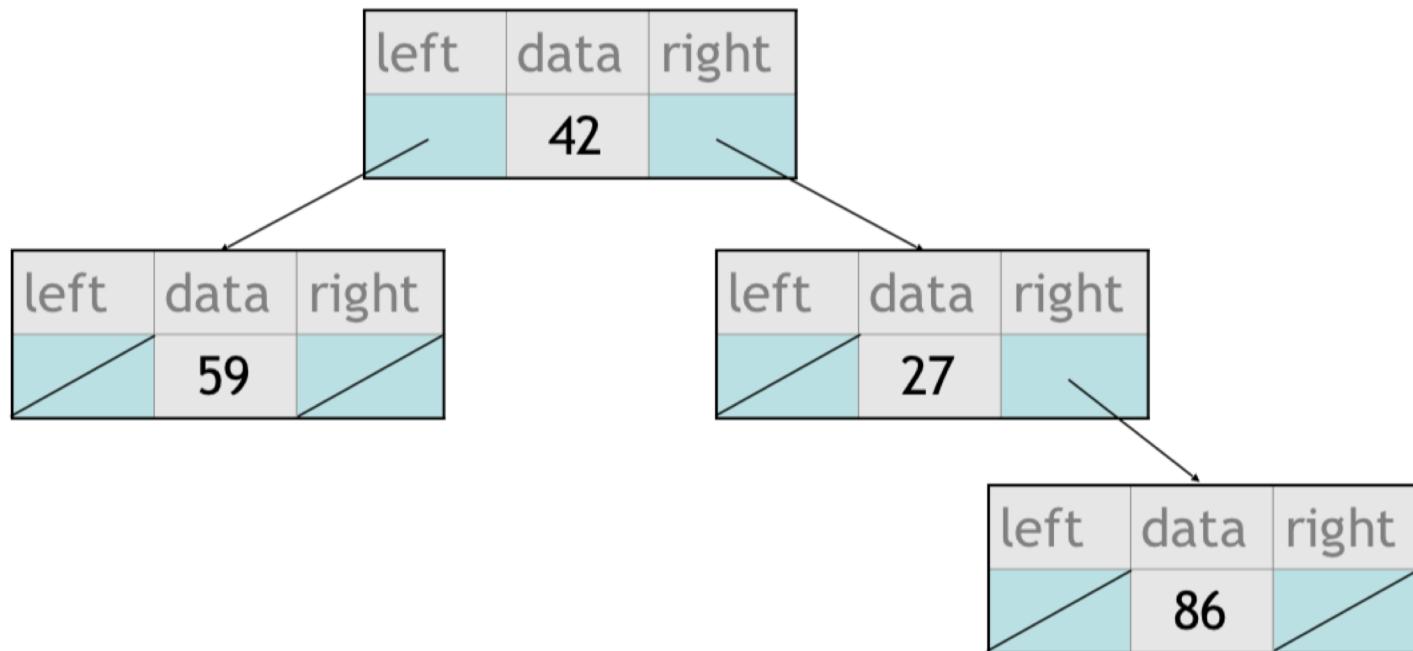
TreeNode

```
// A TreeNode is one node in a binary tree of integers.  
struct TreeNode {  
    int data;          // data stored at this node  
    TreeNode* left;    // pointer to left subtree  
    TreeNode* right;   // pointer to right subtree  
  
    // Constructs a node with the given data and links.  
TreeNode(int data, TreeNode* left, TreeNode* right) {  
    this->data = data;  
    this->left = left;  
    this->right = right;  
}  
  
bool isLeaf() const {  
    return left == nullptr && right == nullptr;  
}  
};
```

left	data	right

TreeNode

- A basic **tree node object** stores data and pointers to left/right
 - Multiple nodes can be linked together into a larger tree



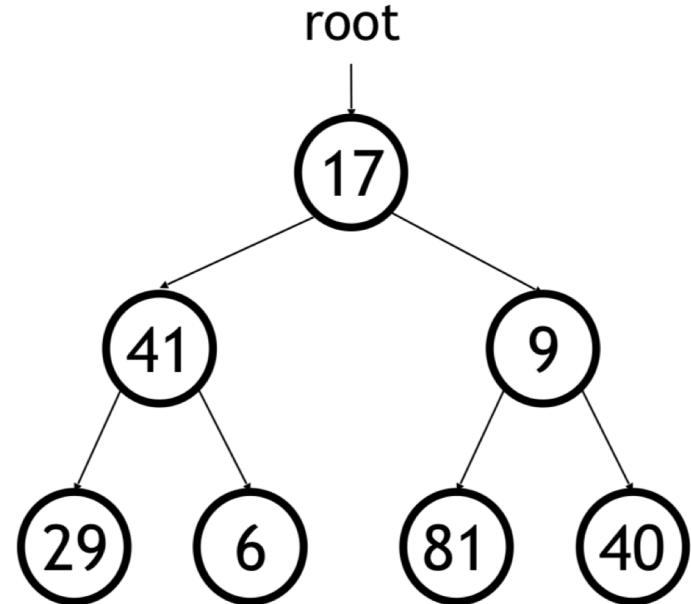
Common Tree Operations

- print
- height
- size
- contains
- deleteTree

print

- Write a function named **print** that accepts a tree node pointer as its parameter and prints the elements of that tree, one per line.
 - A node's left subtree should be printed before it, and its right subtree should be printed after it.
 - Example: `print(root);`

29
41
6
17
81
9
40

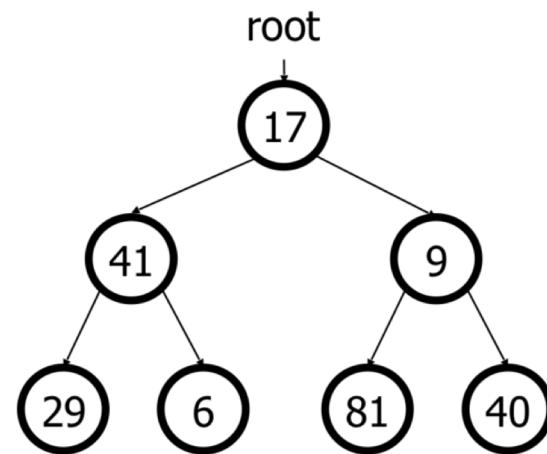


print

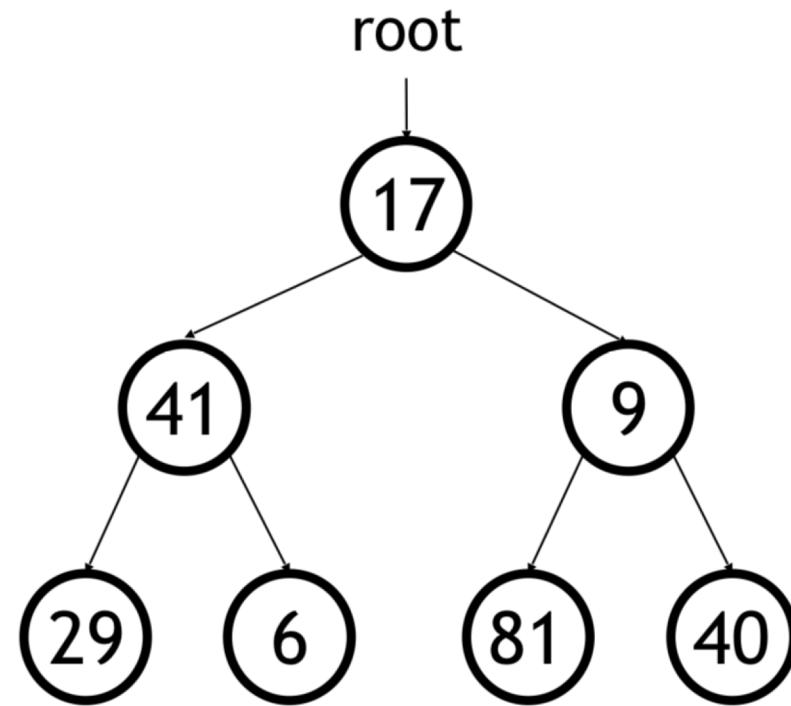
```
void print(TreeNode* node) {
    // (base case is implicitly to do nothing on NULL)
    if (node != nullptr) {
        // recursive case: print left, center, right
        print(node->left);
        cout << node->data << endl;
        print(node->right);
    }
}
```

Traversal

- **traversal:** An examination of the elements of a tree.
 - A pattern used in many tree algorithms and methods
- Common orderings for traversals:
 - **pre-order:** process root node, then its left/right subtrees
 - **in-order:** process left subtree, then root node, then right
 - **post-order:** process left/right subtrees, then root node



Traversal



- pre-order: 17 41 29 6 9 81 40
- in-order: 29 41 6 17 81 9 40
- post-order: 29 6 41 81 40 9 17

Recap

- Arrays
- Announcements
- Trees

Next time: more trees!