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1  /* Avl.c */
2  #include <stdlib.h>
3  #include <malloc.h>
4  #include <assert.h>
5  #include <string.h>
6  #include "Avl.h"
7  #include "LinkStack.h"
8  #include "LinkQueue.h"
9
10 /* x表示值, p表示指针 */
11 #define IsRoot(x)      (!((x).parent))
12 #define IsLChild(x)    (!IsRoot(x) && (&(x) == (x).parent->lc))
13 #define IsRChild(x)    (!IsRoot(x) && (&(x) == (x).parent->rc))
14 #define HasParent(x)   (!IsRoot(x))
15 #define HasLChild(x)   ((x).lc)
16 #define HasRChild(x)   ((x).rc)
17 #define HasChild(x)    (HasLChild(x) || HasRChild(x))
18 #define HasBothChild(x) (HasLChild(x) && HasRChild(x))
19 #define IsLeaf(x)      (!HasChild(x))
20 //获取x的兄弟节点
21 #define Sibling(x)      (IsLChild(x) ? (x).parent->rc : (x).parent->lc)
22 //获取x的叔叔节点
23 #define Uncle(x)        (IsLChild(*(x).parent)) ? (x).parent->parent->rc :
(x).parent->parent->lc)
24 //节点高度, 空树高度为-1
25 #define stature(p)      ((p) ? (p)->height : -1)
26 //理想平衡条件
27 #define Balanced(x)     (stature((x).lc) == stature((x).rc))
28 //平衡因子
29 #define BalFac(x)       (stature((x).lc) - stature((x).rc))
30 //AVL平衡条件
31 #define AvlBalanced(x)  ((-2 < BalFac(x)) && (BalFac(x) < 2))
32 //在左、右孩子中取更高者, 在AVL平衡调整前, 借此确定重构方案
33 #define tallerChild(p)  ( \
34     stature((p)->lc) > stature((p)->rc) ? (p)->lc : ( /*左高*/ \
35     stature((p)->lc) < stature((p)->rc) ? (p)->rc : ( /*右高*/ \
36     IsLChild(*(p)) ? (p)->lc : (p)->rc /*等高: 与父亲p同侧者(zig-zig或zag-zag)优先*/ \
37     ) \
38     ) \
39 )
40
41 static AVLNODE *nodeNew(int keySize, const void *e)
42 {
43     AVLNODE *newNode = (AVLNODE *)malloc(sizeof(AVLNODE) + keySize);
44     if (NULL == newNode)
45     {
46         return NULL;
47     }
48     newNode->parent = NULL;
49     newNode->lc = NULL;
50     newNode->rc = NULL;
51     newNode->height = 0;
52     memcpy(newNode->key, e, keySize);
53     return newNode;
54 }
55
56 static void nodeDispose(AVLNODE *node, AvlFree *freeFn)
57 {
58     if (NULL != freeFn)
59     {
60         freeFn(node->key);
61     }
62     free(node);
63 }
64
65 //Avl初始化
66 void AvlNew(AVLTREE *avlTree, int keySize, AvlCmp *cmpFn, AvlFree *freeFn)
67 {
68     assert(keySize > 0);
69     assert(NULL != cmpFn);
70     avlTree->root = NULL;
71     avlTree->hot = NULL;
72     avlTree->size = 0;

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73     avlTree->keySize = keySize;
74     avlTree->cmpFn = cmpFn;
75     avlTree->freeFn = freeFn;
76 }
77
78 //Avl判空
79 int AvlEmpty(AVLTREE *avlTree)
80 {
81     return (avlTree->size == 0);
82 }
83
84 //Avl规模
85 int AvlSize(AVLTREE *avlTree)
86 {
87     return avlTree->size;
88 }
89
90 //Avl树高度
91 int AvlHeight(AVLTREE *avlTree)
92 {
93     return avlTree->root->height;
94 }
95
96 //将当前节点及其左侧分支入栈
97 static goAlongLeftBranch(AVLNODE *node, STACK *s)
98 {
99     AVLNODE *cur = node;
100     while (NULL != cur)
101     {
102         StackPush(s, &cur);
103         cur = cur->lc;
104     }
105 }
106
107 //Avl销毁
108 void AvlDispose(AVLTREE *avlTree)
109 {
110     if (AvlEmpty(avlTree))
111     {
112         return ;
113     }
114     STACK avlNodeStack;
115     //栈中存放avl节点指针
116     StackNew(&avlNodeStack, sizeof(AVLNODE *), NULL);
117     AVLNODE *node = avlTree->root, *cur;
118     while (1)
119     {
120         //从当前节点出发，逐批入栈
121         goAlongLeftBranch(node, &avlNodeStack);
122         //所有节点处理完毕
123         if (StackEmpty(&avlNodeStack))
124         {
125             break;
126         }
127         //弹出栈顶节点并访问之
128         StackPop(&avlNodeStack, &node);
129         cur = node;
130         node = node->rc; //转向右子树
131         nodeDispose(cur, avlTree->freeFn);
132     }
133     StackDispose(&avlNodeStack);
134     avlTree->root = NULL;
135     avlTree->hot = NULL;
136     avlTree->size = 0;
137 }
138
139 static void visitAlongLeftBranch(AVLNODE *node, STACK *s, AvlTraverseOp *traverseOpFn)
140 {
141     AVLNODE *x = node;
142     while (NULL != x)
143     {
144         traverseOpFn(x->key);
145         StackPush(s, &(x->rc));

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146         x = x->lc;
147     }
148 }
149
150 //Avl先序遍历（非递归）
151 void AvlTravPre(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
152 {
153     if (NULL == traverseOpFn || AvlEmpty(avlTree))
154     {
155         return ;
156     }
157     STACK avlNodeStack;
158     StackNew(&avlNodeStack, sizeof(AVLNODE *), NULL);
159     AVLNODE *node = avlTree->root;
160     while (1)
161     {
162         visitAlongLeftBranch(node, &avlNodeStack, traverseOpFn);
163         if (StackEmpty(&avlNodeStack))
164         {
165             break;
166         }
167         StackPop(&avlNodeStack, &node);
168     }
169     StackDispose(&avlNodeStack);
170 }
171
172 static void travPreRecAt(AVLNODE *node, AvlTraverseOp *traverseOpFn)
173 {
174     if (NULL == node)
175     {
176         return ;
177     }
178     traverseOpFn(node->key);
179     travPreRecAt(node->lc, traverseOpFn);
180     travPreRecAt(node->rc, traverseOpFn);
181 }
182
183 //Avl先序遍历（递归）
184 void AvlTravPreRec(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
185 {
186     if (NULL == traverseOpFn || AvlEmpty(avlTree))
187     {
188         return ;
189     }
190     travPreRecAt(avlTree->root, traverseOpFn);
191 }
192
193 //二叉树中序遍历算法（迭代版#1）
194 static void travIn_V1(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
195 {
196     STACK avlNodeStack;
197     //栈中存放avl节点指针
198     StackNew(&avlNodeStack, sizeof(AVLNODE *), NULL);
199     AVLNODE *node = avlTree->root;
200     while (1)
201     {
202         //从当前节点出发，逐批入栈
203         goAlongLeftBranch(node, &avlNodeStack);
204         //所有节点处理完毕
205         if (StackEmpty(&avlNodeStack))
206         {
207             break;
208         }
209         //弹出栈顶节点并访问之
210         StackPop(&avlNodeStack, &node);
211         traverseOpFn(node->key);
212         node = node->rc; //转向右子树
213     }
214     StackDispose(&avlNodeStack);
215 }
216
217 //二叉树中序遍历算法（迭代版#2，版本#1的等价形式）
218 static void travIn_V2(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)

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219 {
220     STACK avlNodeStack;
221     //栈中存放avl节点指针
222     StackNew(&avlNodeStack, sizeof(AVLNODE *), NULL);
223     AVLNODE *node = avlTree->root;
224     while (1)
225     {
226         if (NULL != node)
227         {
228             StackPush(&avlNodeStack, &node);
229             node = node->lc;
230         }
231         else if (!StackEmpty(&avlNodeStack))
232         {
233             StackPop(&avlNodeStack, &node);
234             traverseOpFn(node->key);
235             node = node->rc;
236         }
237         else
238         {
239             break;
240         }
241     }
242     StackDispose(&avlNodeStack);
243 }
244
245 //定位节点node在中序遍历中的直接后继
246 static AVLNODE *succ(AVLNODE *node)
247 {
248     AVLNODE *s = node;
249     if (NULL != s->rc) //若有右孩子，则直接后继必在右子树中
250     {
251         s = s->rc;
252         while (HasLChild(*s))
253         {
254             s = s->lc;
255         }
256     }
257     else
258     {
259         while (IsRChild(*s))
260         {
261             s = s->parent;
262         }
263         s = s->parent;
264     }
265     return s;
266 }
267
268 //二叉树中序遍历算法（迭代版#3）
269 static void travIn_V3(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
270 {
271     //前一步是否刚从右子树回溯--省去栈，仅O(1)辅助空间
272     int backtrack = 0;
273     AVLNODE *node = avlTree->root;
274     while (1)
275     {
276         //若有左子树且不是刚刚回溯，则深入遍历左子树
277         if (!backtrack && HasLChild(*node))
278         {
279             node = node->lc;
280         } //否则无左子树或刚刚回溯
281         else
282         {
283             traverseOpFn(node->key);
284             //右子树非空，深入右子树继续遍历，并关闭回溯标志
285             if (HasRChild(*node))
286             {
287                 node = node->rc;
288                 backtrack = 0;
289             }
290             else //右子树为空则回溯并设置回溯标志
291             {

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292         node = succ(node);
293         if (NULL == node)
294         {
295             break;
296         }
297         backtrack = 1;
298     }
299 }
300 }
301 }
302
303 //Avl中序遍历（非递归）
304 void AvlTravIn(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
305 {
306     if (NULL == traverseOpFn || AvlEmpty(avlTree))
307     {
308         return ;
309     }
310     travIn_Vl(avlTree, traverseOpFn);
311 }
312
313 static void travInRecAt(AVLNODE *node, AvlTraverseOp *traverseOpFn)
314 {
315     if (NULL == node)
316     {
317         return ;
318     }
319     travInRecAt(node->lc, traverseOpFn);
320     traverseOpFn(node->key);
321     travInRecAt(node->rc, traverseOpFn);
322 }
323
324 //Avl中序遍历（递归）
325 void AvlTravInRec(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
326 {
327     if (NULL == traverseOpFn || AvlEmpty(avlTree))
328     {
329         return ;
330     }
331     travInRecAt(avlTree->root, traverseOpFn);
332 }
333
334 //在以s栈顶节点为根的子树中，
335 //找到最高左侧可见叶节点（highest leaf visible from left）
336 static void gotoHLVFL(STACK *s)
337 {
338     AVLNODE *x;
339     StackTop(s, &x);
340     while (NULL !=x)
341     {
342         if (HasLChild(*x)) //尽可能向左
343         {
344             if (HasRChild(*x)) //若有右孩子，优先入栈
345             {
346                 StackPush(s, &(x->rc));
347             }
348             StackPush(s, &(x->lc));
349         }
350         else
351         {
352             //此处x->rc可能为空，
353             //左、右孩子都不存在时，将NULL入栈，便于while退出
354             StackPush(s, &(x->rc));
355         }
356         StackTop(s, &x);
357     }
358     StackPop(s, NULL); //返回之前，弹出栈顶空节点
359 }
360
361 //Avl后序遍历（非递归）
362 void AvlTravPost(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
363 {
364     if (NULL == traverseOpFn || AvlEmpty(avlTree))

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365     {
366         return ;
367     }
368     STACK avlNodeStack;
369     StackNew(&avlNodeStack, sizeof(AVLNODE *), NULL);
370     AVLNODE *x = avlTree->root;
371     StackPush(&avlNodeStack, &x);
372     while (!StackEmpty(&avlNodeStack))
373     {
374         AVLNODE *nodeTop;
375         StackTop(&avlNodeStack, &nodeTop);
376         //若栈顶非当前节点之父, 则必为其右兄
377         if (nodeTop != x->parent)
378         {
379             gotoHLVFL(&avlNodeStack);
380         }
381         StackPop(&avlNodeStack, &x);
382         traverseOpFn(x->key);
383     }
384     StackDispose(&avlNodeStack);
385 }
386
387 static void travPostRecAt(AVLNODE *node, AvlTraverseOp *traverseOpFn)
388 {
389     if (NULL == node)
390     {
391         return ;
392     }
393     travInRecAt(node->lc, traverseOpFn);
394     travInRecAt(node->rc, traverseOpFn);
395     traverseOpFn(node->key);
396 }
397
398 //Avl后序遍历(递归)
399 void AvlTravPostRec(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
400 {
401     if (NULL == traverseOpFn || AvlEmpty(avlTree))
402     {
403         return ;
404     }
405     travPostRecAt(avlTree->root, traverseOpFn);
406 }
407
408 //Avl层序遍历
409 void AvlTravLevel(AVLTREE *avlTree, AvlTraverseOp *traverseOpFn)
410 {
411     if (NULL == traverseOpFn || AvlEmpty(avlTree))
412     {
413         return ;
414     }
415     QUEUE avlNodeQueue;
416     QueueNew(&avlNodeQueue, sizeof(AVLNODE *), NULL);
417     AVLNODE *node = avlTree->root;
418     QueueEn(&avlNodeQueue, &node);
419     while (!QueueEmpty(&avlNodeQueue))
420     {
421         QueueDe(&avlNodeQueue, &node);
422         traverseOpFn(node->key);
423         if (HasLChild(*node))
424         {
425             QueueEn(&avlNodeQueue, &(node->lc));
426         }
427         if (HasRChild(*node))
428         {
429             QueueEn(&avlNodeQueue, &(node->rc));
430         }
431     }
432     QueueDispose(&avlNodeQueue);
433 }
434
435 //Avl中查找关键码所在节点, hot指向当前节点的父节点
436 AVLNODE *AvlSearch(AVLTREE *avlTree, const void *e)
437 {

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438     AVLNODE *node = avlTree->root;
439     avlTree->hot = NULL;
440     while (NULL != node)
441     {
442         if (0 == avlTree->cmpFn(e, node->key))
443         {
444             break ;
445         }
446         avlTree->hot = node;
447         if (0 < avlTree->cmpFn(e, node->key))
448         {
449             node = node->rc;
450         }
451         else
452         {
453             node = node->lc;
454         }
455     }
456     return node;
457 }
458
459 int max(int a, int b)
460 {
461     return (a > b ? a : b);
462 }
463
464 //更新节点node的高度
465 static int updateHeight(AVLNODE *node)
466 {
467     return node->height = 1 + max(stature(node->lc), stature(node->rc));
468 }
469
470 //更新节点node及其祖先的高度
471 static void updateHeightAbove(AVLNODE *node)
472 {
473     AVLNODE *cur = node;
474     while (NULL != cur)
475     {
476         updateHeight(cur);
477         cur = cur->parent;
478     }
479 }
480
481 //按照“3+4”结构联接3个节点及四颗子树，返回重组后的局部子树根节点的位置（即b）
482 //子树根节点与上层节点之间的双向联接，均须由上层调用者完成
483 static AVLNODE *connect34(AVLNODE *a, AVLNODE *b, AVLNODE *c, AVLNODE *T0, AVLNODE
484 *T1, AVLNODE *T2, AVLNODE *T3)
485 {
486     a->lc = T0;
487     if (T0)
488     {
489         T0->parent = a;
490     }
491     a->rc = T1;
492     if (T1)
493     {
494         T1->parent = a;
495     }
496     updateHeight(a);
497
498     c->lc = T2;
499     if (T2)
500     {
501         T2->parent = c;
502     }
503     c->rc = T3;
504     if (T3)
505     {
506         T3->parent = c;
507     }
508     updateHeight(c);
509     b->lc = a;

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510     a->parent = b;
511     b->rc = c;
512     c->parent = b;
513     updateHeight(b);
514     return b;
515 }
516
517 //BST节点旋转变换统一算法（3节点+4子树），返回调整后局部子树根节点的位置
518 //注意：尽管子树根会正确指向上层节点（如果存在），但反向的联接须由上层函数完成
519 static AVLNODE *rotateAt(AVLNODE *grandsonNode)
520 {
521     AVLNODE *p = grandsonNode->parent;
522     AVLNODE *g = p->parent;
523     if (IsLChild(*p)) //zig
524     {
525         if (IsLChild(*grandsonNode)) //zig-zig
526         {
527             p->parent = g->parent; //向上联接
528             return connect34(grandsonNode, p, g, grandsonNode->lc, grandsonNode->rc,
529                             p->rc, g->rc);
529         }
530         else //zig-zag
531         {
532             grandsonNode->parent = g->parent; //向上联接
533             return connect34(p, grandsonNode, g, p->lc, grandsonNode->lc,
534                             grandsonNode->rc, g->rc);
535         }
536     }
537     else //zag
538     {
539         if (IsLChild(*grandsonNode)) //zag-zig
540         {
541             grandsonNode->parent = g->parent; //向上联接
542             return connect34(g, grandsonNode, p, g->lc, grandsonNode->lc,
543                             grandsonNode->rc, p->rc);
544         }
545         else //zag-zag
546         {
547             p->parent = g->parent; //向上联接
548             return connect34(g, p, grandsonNode, g->lc, p->lc, grandsonNode->lc,
549                             grandsonNode->rc);
550         }
551     }
552 }
553
554 //Avl中插入关键码
555 AVLNODE *AvlInsert(AVLTREE *avlTree, const void *e)
556 {
557     AVLNODE *node = AvlSearch(avlTree, e);
558     if (NULL != node)
559     {
560         return node;
561     }
562     //新节点初始化
563     node = nodeNew(avlTree->keySize, e);
564     if (NULL == node)
565     {
566         return NULL;
567     }
568     node->parent = avlTree->hot;
569     //空树时指定根
570     if (NULL == node->parent)
571     {
572         avlTree->root = node;
573     }
574     else
575     {
576         if (0 < avlTree->cmpFn(e, avlTree->hot->key))
577         {
578             avlTree->hot->rc = node;
579         }
580         else
581         {
582             avlTree->hot->lc = node;
583         }
584     }
585 }

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579         avlTree->hot->lc = node;
580     }
581 }
582 avlTree->size ++;
583
584 AVLNODE *g = avlTree->hot;
585 for (; g; g = g->parent)
586 {
587     if (!AvlBalanced(*g))
588     {
589         //重新接入原树
590         if (IsRoot(*g))
591         {
592             avlTree->root = rotateAt(tallerChild(tallerChild(g)));
593         }
594         else if (IsLChild(*g))
595         {
596             AVLNODE *u = g->parent;
597             u->lc = rotateAt(tallerChild(tallerChild(g)));
598         }
599         else
600         {
601             AVLNODE *u = g->parent;
602             u->rc = rotateAt(tallerChild(tallerChild(g)));
603         }
604         break;
605     }
606     else
607     {
608         updateHeight(g);
609     }
610 }
611 return node;
612 }
613
614 static void swap(void *dataAddr1, void *dataAddr2, int dataSize)
615 {
616     char *tmp = (char *)malloc(dataSize);
617     memcpy(tmp, dataAddr1, dataSize);
618     memcpy(dataAddr1, dataAddr2, dataSize);
619     memcpy(dataAddr2, tmp, dataSize);
620     free(tmp);
621 }
622
623 //删除node所指节点
624 //返回值指向实际被删除节点的接替者，hot指向实际被删除节点的父亲，二者均可能是NULL
625 static AVLNODE *removeAt(AVLNODE **node, AVLNODE **hot, AvlFree *freeFn, int keySize)
626 {
627     AVLNODE *w = *node; //实际被删除的节点
628     AVLNODE *successor = NULL; //实际被删除节点的接替者
629
630     //若**node的左子树为空，则直接将**node替换为其右子树
631     if (!HasLChild(**node))
632     {
633         *node = (*node)->rc;
634         successor = *node;
635     }
636     else if (!HasRChild(**node)) //右子树为空，对称处理
637     {
638         *node = (*node)->lc;
639         successor = *node;
640     }
641     else //左、右子树均存在，则选择**node节点的直接后继作为实际被摘除节点
642     {
643         w = succ(w); //在右子树中找到直接后继
644         swap((*node)->key, w->key, keySize);
645         AVLNODE *u = w->parent;
646         successor = w->rc; //此时待删除节点不可能有左孩子
647         //隔离被删除节点w
648         if (*node == u)
649         {
650             u->rc = successor;
651         }

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652         else
653         {
654             u->lc = successor;
655         }
656     }
657     //记录实际被删除节点的父亲
658     *hot = w->parent;
659     if (successor)
660     {
661         successor->parent = *hot; //将被删除节点的接替者与hot相联
662     }
663     nodeDispose(w, freeFn);
664     return successor;
665 }
666
667 static int avlRemoveBase(AVLTREE *avlTree, void *e, AvlFree *freeFn)
668 {
669     AVLNODE *node = AvlSearch(avlTree, e);
670     //查不到要删除的节点，删除失败
671     if (NULL == node)
672     {
673         return -1;
674     }
675     AVLNODE *hot = NULL; //记录删除节点的父亲
676     removeAt(&node, &hot, freeFn, avlTree->keySize);
677     avlTree->size --;
678
679     AVLNODE *g = hot;
680     for (; g; g = g->parent)
681     {
682         if (!AvlBalanced(*g))
683         {
684             AVLNODE *localRoot;
685             if (IsRoot(*g))
686             {
687                 localRoot = rotateAt(tallerChild(tallerChild(g)));
688                 avlTree->root = localRoot;
689             }
690             else if (IsLChild(*g))
691             {
692                 AVLNODE *u = g->parent;
693                 localRoot = rotateAt(tallerChild(tallerChild(g)));
694                 u->lc = localRoot;
695             }
696             else
697             {
698                 AVLNODE *u = g->parent;
699                 localRoot = rotateAt(tallerChild(tallerChild(g)));
700                 u->rc = localRoot;
701             }
702             g = localRoot;
703         }
704         updateHeight(g); //即便g未失衡，其高度也可能降低
705     }
706     return 0;
707 }
708
709 //Avl中删除关键码所在节点，返回值：0成功，!0失败
710 int AvlRemove(AVLTREE *avlTree, void *e)
711 {
712     return avlRemoveBase(avlTree, e, avlTree->freeFn);
713 }
714
715 //Avl中删除关键码所在节点（无需深度删除关键码），返回值：0成功，!0失败
716 int AvlRemoveU(AVLTREE *avlTree, void *e)
717 {
718     return avlRemoveBase(avlTree, e, NULL);
719 }

```