NMF Final (Only nndsvd 5 component without ozone)

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```
# load the packages
library(NMF)
library(tidyverse)
library(grid)
library(gridExtra)
library(readxl)
library(circular)
library(lwgeom)
library(units)
```

Procedure

- 1. Remove hourly observation with missing observation for any chemical
- 2. Remove background noise level using min values (except for chemicals with minimum value < 2*LOD and maximum value > 100*LOD)
- 3. Zero values are converted to a random value between 0 and 0.5*LOD
- 4. Normalize using min and max
- 5. Remove Ozone (wouldn't affect # of obs.)

Reading the data

```
# retrieving the vocs, removing everything else except the vocs
hourly_vocs <- hourly_nona %>% select(any_of(vocs))

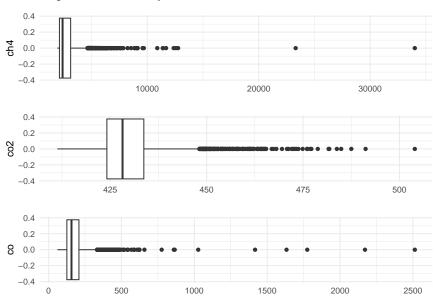
# retrieving the non-vocs: co2_ppm, nox, ch4, h2s, so2, o3
# double check this
hourly_non_vocs <- hourly_nona %>% select(any_of(non_vocs))

hourly_full_nona <- cbind(hourly_non_vocs, hourly_vocs)

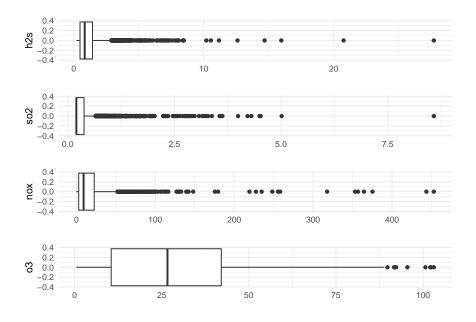
# retrive a vector of yearmonth
hourly_dates <- hourly_nona %>%
    mutate(yearmonth = substring(day, 0, 7)) %>%
    pull(yearmonth)
```

Data visualisation

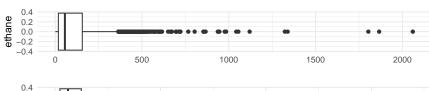
• Boxplots of the hourly concentrations non-voc

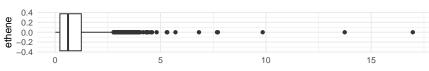


• Boxplots sulfur compounds, NOx, ozone

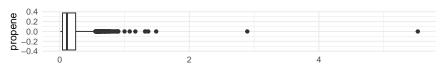


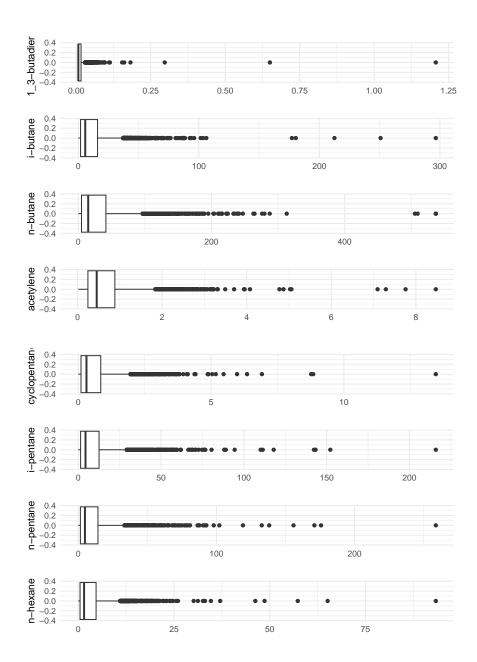
• Boxplots VOCs

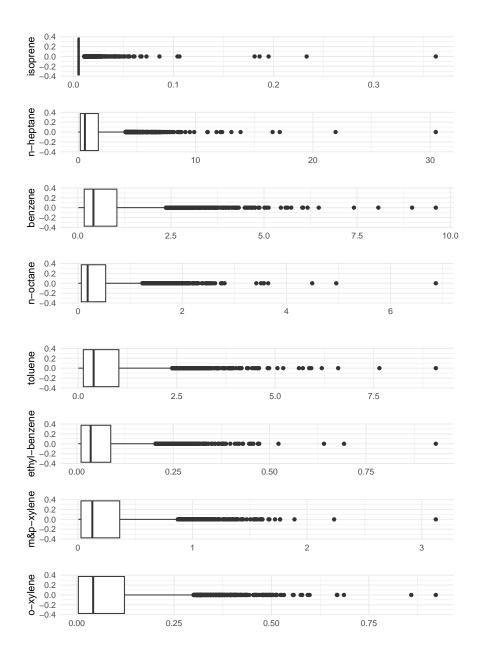












Data pre-processing

• STEP 1: Limits of detection

```
# # extract the yearmonth from date variables
# LOD_voc_monthly <- LOD_voc_monthly %>%
# mutate(yearmonth = strftime(as.POSIXct(start_date, format = '%Y-%m-%d %H:%M:%S',
# tz = 'UTC'), '%Y-%m'))
#
# LOD_voc_monthly <- LOD_voc_monthly %>%
# select(-c(start_date, end_date)) %>%
# select(!any_of(ends_with('half_ldl')))
#
# colnames(LOD_voc_monthly) <- str_replace_all(names(LOD_voc_monthly), '_ldl', '')

LOD_voc_avg <- read_xlsx('../data/LNM_VOC_Uncertainties.xlsx', skip = 1)
LOD_voc_avg <- LOD_voc_avg %>%
    select(1, 4) %>%
    rename('LOD' = 2, 'chemical' = 1) %>%
    head(20)
```

• STEP 2: Background correction

```
##
             ch4
                            co2
                                            СО
                                                          h2s
                                                                         so2
        1928.000
                                                                       0.200
##
                        411.300
                                        59.910
                                                        0.200
##
                                        ethane
                                                       ethene
             nox
                             о3
                                                                     propane
##
           0.025
                          0.500
                                         0.916
                                                        0.011
                                                                       0.224
##
         propene 1 3-butadiene
                                      i-butane
                                                     n-butane
                                                                   acetylene
##
           0.009
                          0.007
                                         0.035
                                                        0.090
                                                                       0.019
##
    cyclopentane
                      i-pentane
                                     n-pentane
                                                     n-hexane
                                                                    isoprene
           0.005
                                                        0.021
                                                                       0.005
##
                          0.038
                                         0.042
##
       n-heptane
                        benzene
                                      n-octane
                                                      toluene ethyl-benzene
##
           0.004
                          0.017
                                         0.004
                                                        0.004
                                                                       0.004
##
      m&p-xylene
                       o-xylene
                          0.004
##
           0.004
```

• Summary statistics of backgrounds and extremes

```
get_info <- function(column) {</pre>
  N <- length(column)
  background <- quantile(column, 0)</pre>
  quantile1 <- quantile(column, 0.01)</pre>
  quantile99 <- quantile(column, 0.99)
  n_background <- sum(column == background)</pre>
  max <- max(column)</pre>
  return(c(N, quantile1, quantile99, max, background, n_background))
}
info table <- hourly full nona %>%
 reframe(across(everything(), ~ get_info(.x)))
info_table <- info_table %>%
  mutate(rownames = c('N', '1st percentile', '99th percentile', 'Max',
                       'Background', '# Background')) %>%
  pivot_longer(-rownames) %>%
  pivot_wider(names_from = rownames, values_from = value)
knitr::kable(info_table)
```

						#
name	N	1st percentile	99th percentile	Max	Background	Background
ch4	4788	1962.98700	6286.12400	34010.900	1928.000	1
co2	4788	416.47870	460.62260	503.990	411.300	1
co	4788	84.23050	442.08860	2513.440	59.910	1
h2s	4788	0.20000	5.20986	27.700	0.200	829
so2	4788	0.20000	1.78686	8.578	0.200	3266
nox	4788	0.22974	89.72371	452.959	0.025	2
o3	4788	0.50000	76.02600	103.100	0.500	259
ethane	4788	1.84422	526.44700	2060.000	0.916	1
ethene	4788	0.01100	3.50826	16.970	0.011	163
propane	4788	0.84674	300.79000	1211.000	0.224	1
propene	4788	0.00900	0.69739	5.528	0.009	411
1_3-butadiene	4788	0.00700	0.05900	1.207	0.007	3357
i-butane	4788	0.15148	60.89400	296.600	0.035	1
n-butane	4788	0.37248	166.52100	536.900	0.090	1
acetylene	4788	0.04900	2.61304	8.471	0.019	2
cyclopentane	4788	0.00500	3.06899	13.460	0.005	96
i-pentane	4788	0.10987	49.60210	215.900	0.038	1
n-pentane	4788	0.10487	55.95980	258.800	0.042	1
n-hexane	4788	0.04300	18.17780	93.360	0.021	2
isoprene	4788	0.00500	0.03313	0.362	0.005	2816
n-heptane	4788	0.01500	6.57669	30.470	0.004	5
benzene	4788	0.02800	3.78693	9.610	0.017	3
n-octane	4788	0.00400	2.00839	6.867	0.004	100
toluene	4788	0.01300	3.52165	9.077	0.004	11
ethyl-benzene	4788	0.00400	0.31613	0.931	0.004	918
m&p-xylene	4788	0.00400	1.29156	3.123	0.004	851
o-xylene	4788	0.00400	0.45700	0.922	0.004	1330

- STEP 2 processing continued: background correction
- adjustments that were made according to paper: Gunnar's paper section 2.2 and Guha 3.3
- Check whether chemical has background noise level that needs to be removed
- NO ADJUSTMENT if minimum value < 2xLOD and maximum value > 100xLOD

```
adjusting_neg_bg_from_lod <- function(chemical, LOD, background, hourly_data){
    # get min and max
    min_value <- min(hourly_data[chemical], na.rm = TRUE)
    max_value <- max(hourly_data[chemical], na.rm = TRUE)
    # if min less than double LOD or max > 100 times LOD
    # adjust to -100 (for entire column???)
    if (min_value < 2 * LOD & max_value > 100 * LOD ){
        return (0)
    }
    return (background)
}
```

- Check if background is negligible for non voc
- merge background and LOD

```
rowwise() %>%
mutate(min = min(hourly_full_nona[chemical], na.rm = TRUE),
    LODx2 = 2 * LOD,
    criterion1 = min(hourly_full_nona[chemical], na.rm = TRUE) < 2 * LOD,
    max = max(hourly_full_nona[chemical], na.rm = TRUE),
    LODx100 = 100 * LOD,
    criterion2 = max(hourly_full_nona[chemical], na.rm = TRUE) > 100 * LOD,
    adjusted_background = adjusting_neg_bg_from_lod(chemical, LOD, background, hourly_full_nona))
```

- Check if background is negligible for voc
- merge background and LOD

• create dataset with background removed

• check number of 0 values per compound

```
# look at zero values
colSums(hourly_nona_bgrm == 0)
## ch4 co2 co h2s so2
```

```
##
##
                                                             829
                                                                            3266
                1
                                1
                                               1
##
                               о3
                                          ethane
                                                                        propane
              nox
                                                          ethene
##
                0
                                0
                                                1
##
         propene 1_3-butadiene
                                        i-butane
                                                       n-butane
                                                                      acetylene
##
                             3357
                                               1
                                                               1
                                                                               0
##
    cyclopentane
                       i-pentane
                                       n-pentane
                                                       n-hexane
                                                                       isoprene
##
                                                                            2816
##
       n-heptane
                                        n-octane
                                                         toluene ethyl-benzene
                         benzene
##
                                0
                                               0
                                                               0
##
      m&p-xylene
                        o-xylene
```

```
##
                     0
                                        0
```

• STEP 3: replace zero values with random values between 0 and 0.5xLOD

```
set.seed(123)
replace_zero_with_random <- function(column, name, LOD_df){</pre>
  LOD <- LOD_df$LOD[LOD_df$chemical == name]
  column <- if_else(column == 0, round(runif(length(column), 0, 0.5 * LOD), 3), column)</pre>
  return (column)
}
hourly_nona_bgrm_zerorepl <- hourly_nona_bgrm %>%
  mutate(across(adjusted_background_non_voc$chemical,
                ~ replace_zero_with_random(.x, cur_column(), adjusted_background_non_voc)))
hourly_nona_bgrm_zerorepl <- hourly_nona_bgrm_zerorepl %>%
  mutate(across(adjusted_background_voc$chemical,
                 ~ replace_zero_with_random(.x, cur_column(), adjusted_background_voc)))
```

• STEP 4: Normalize the non-vocs

```
#normalizing function
normalize_column <- function(column){</pre>
  background <- quantile(column, 0)</pre>
  max <- quantile(column, 1) # this could be adjusted
  return ((column - background)/(max - background))
}
```

• STEP 4: Normalize all

##

```
# normalize all
hourly_nona_bgrm_zerorepl_norm <- as_tibble(sapply(as.list(hourly_nona_bgrm_zerorepl),
                                                    normalize column))
#normalize the NON_VOC
summary(hourly_nona_bgrm_zerorepl_norm)
```

```
co2
                                                                 h2s
         ch4
                                               CO
           :0.00000
                              :0.0000
                                                :0.00000
                                                                   :0.00000
##
    Min.
                      Min.
                                        Min.
                                                           Min.
##
    1st Qu.:0.00579
                       1st Qu.:0.1384
                                         1st Qu.:0.02592
                                                           1st Qu.:0.01022
   Median :0.01460
                      Median :0.1823
                                        Median :0.03884
                                                           Median: 0.02335
##
           :0.02683
                              :0.2000
                                                :0.04761
    Mean
                       Mean
                                         Mean
                                                           Mean
                                                                   :0.03501
##
    3rd Qu.:0.03720
                       3rd Qu.:0.2418
                                         3rd Qu.:0.05970
                                                           3rd Qu.:0.04525
##
                      Max.
                                        Max.
    Max.
           :1.00000
                            :1.0000
                                                :1.00000
                                                           Max.
                                                                   :1.00000
##
         so2
                             nox
                                                  о3
                                                                   ethane
           :0.000000
                               :0.000000
                                                                      :0.000000
##
   Min.
                       \mathtt{Min}.
                                            Min.
                                                   :0.00000
                                                               \mathtt{Min}.
##
    1st Qu.:0.007878
                        1st Qu.:0.006534
                                            1st Qu.:0.09747
                                                               1st Qu.:0.008385
##
  Median :0.015994
                        Median :0.020262
                                            Median :0.25487
                                                               Median : 0.026671
  Mean
           :0.026287
                               :0.036440
                                                   :0.26676
                                                               Mean
                                                                      :0.050992
##
                        Mean
                                            Mean
##
    3rd Qu.:0.023633
                        3rd Qu.:0.049978
                                            3rd Qu.:0.40546
                                                               3rd Qu.:0.075375
           :1.000000
##
   Max.
                        Max.
                               :1.000000
                                           Max.
                                                   :1.00000
                                                              Max.
                                                                      :1.000000
##
        ethene
                          propane
                                              propene
                                                               1 3-butadiene
  Min.
           :0.00000
                      Min.
                              :0.000000
                                           Min.
                                                  :0.000000
                                                               Min.
                                                                      :0.000000
##
    1st Qu.:0.01268
                       1st Qu.:0.009283
                                           1st Qu.:0.005979
                                                               1st Qu.:0.002500
## Median :0.03547
                      Median :0.028409
                                           Median :0.018482
                                                               Median : 0.004167
## Mean
           :0.05042
                       Mean
                             :0.053803
                                           Mean
                                                  :0.028772
                                                               Mean
                                                                      :0.007371
## 3rd Qu.:0.07266
                       3rd Qu.:0.080130
                                           3rd Qu.:0.042761
                                                               3rd Qu.:0.007500
## Max.
           :1.00000
                      Max.
                              :1.000000
                                                                      :1.000000
                                           Max.
                                                  :1.000000
                                                               Max.
```

```
##
       i-butane
                          n-butane
                                             acetylene
                                                               cyclopentane
##
    Min.
           :0.00000
                              :0.000000
                                                   :0.00000
                                                                      :0.000000
                       Min.
                                           \mathtt{Min}.
                                                              Min.
                       1st Qu.:0.008777
    1st Qu.:0.00614
                                           1st Qu.:0.02674
                                                              1st Qu.:0.007432
    Median :0.01925
                       Median :0.027522
                                           Median :0.05135
                                                              Median :0.022668
##
##
    Mean
           :0.03837
                       Mean
                              :0.054900
                                           Mean
                                                   :0.07436
                                                              Mean
                                                                      :0.043730
##
    3rd Qu.:0.05369
                       3rd Qu.:0.077042
                                           3rd Qu.:0.10211
                                                              3rd Qu.:0.062653
##
    Max.
           :1.00000
                       Max.
                              :1.000000
                                           Max.
                                                   :1.00000
                                                              Max.
                                                                      :1.000000
##
      i-pentane
                          n-pentane
                                               n-hexane
                                                                   isoprene
##
    Min.
           :0.000000
                        Min.
                                :0.000000
                                            Min.
                                                    :0.000000
                                                                Min.
                                                                        :0.000000
##
    1st Qu.:0.006303
                        1st Qu.:0.005681
                                            1st Qu.:0.004703
                                                                1st Qu.:0.002801
    Median :0.019941
                        Median :0.018371
                                            Median :0.016039
                                                                Median :0.005602
##
    Mean
           :0.041094
                        Mean
                                :0.038859
                                            Mean
                                                    :0.034979
                                                                Mean
                                                                        :0.010315
##
    3rd Qu.:0.057857
                        3rd Qu.:0.054837
                                            3rd Qu.:0.049544
                                                                3rd Qu.:0.011204
                               :1.000000
                                                    :1.000000
                                                                        :1.000000
##
    Max.
           :1.000000
                        Max.
                                            Max.
                                                                Max.
##
      n-heptane
                           benzene
                                              n-octane
                                                                   toluene
##
           :0.000000
                                :0.00000
                                                   :0.000000
                                                                       :0.00000
    Min.
                        Min.
                                           Min.
                                                               Min.
##
    1st Qu.:0.005473
                        1st Qu.:0.01637
                                           1st Qu.:0.008269
                                                               1st Qu.:0.01389
    Median :0.018348
                        Median :0.04222
                                           Median :0.026009
                                                               Median : 0.04276
##
   Mean
           :0.039328
                        Mean
                               :0.07655
                                           Mean
                                                  :0.054341
                                                               Mean
                                                                       :0.07825
##
    3rd Qu.:0.055866
                        3rd Qu.:0.10779
                                           3rd Qu.:0.076497
                                                               3rd Qu.:0.11333
##
    Max.
           :1.000000
                        Max.
                               :1.00000
                                           Max.
                                                   :1.000000
                                                               Max.
                                                                       :1.00000
##
    ethyl-benzene
                          m&p-xylene
                                               o-xylene
##
  Min.
           :0.000000
                               :0.000000
                                                    :0.00000
                        \mathtt{Min}.
                                            \mathtt{Min}.
##
   1st Qu.:0.007551
                        1st Qu.:0.007374
                                            1st Qu.:0.00000
## Median :0.034520
                        Median :0.039115
                                            Median: 0.04139
## Mean
           :0.062378
                        Mean
                               :0.077508
                                            Mean
                                                    :0.08650
##
   3rd Qu.:0.090615
                        3rd Qu.:0.115742
                                            3rd Qu.:0.12881
  Max.
           :1.000000
                        Max.
                                :1.000000
                                            Max.
                                                    :1.00000
```

FINAL step: create matrix of processed and normalized concentrations for NMF

```
normalized_matrix <- as.matrix(hourly_nona_bgrm_zerorepl_norm)
#important: using the normalized VOCs for this file</pre>
```

NMF section

Preprocess

Global variables

```
components <- 4:10
```

Remove Ozone

```
normalized_matrix_less_o3 <- normalized_matrix[ ,setdiff(colnames(normalized_matrix), "o3")]
```

Compute error matrix

```
adjusted_background_voc$chemical),
                      LOD = c(adjusted_background_non_voc$LOD,
                              adjusted_background_voc$LOD))
LOD_merged <- tibble(chemical = names(hourly_nona_bgrm_zerorepl_norm)) %>%
  left_join(LOD_merged) %>%
  filter(chemical %in% colnames(normalized_matrix_less_o3))
## Joining with `by = join_by(chemical)`
# creating uncertainty Matrix
for (i in 1:dim(weight_matrix)[1]) {
  for (j in 1:dim(weight matrix)[2]) {
    chemical <- colnames(normalized_matrix_less_o3)[j]</pre>
    xij <- normalized matrix less o3[i, j]
    LOD <- LOD_merged$LOD[LOD_merged$chemical == chemical]
    # Get LOD value for this row
    if (j == 1) {
      # based on equation 6, we sqrt ch4 (at column = 1) and times by 1
      weight_matrix[i, j] <- sqrt(xij)</pre>
    } else if (j == 2) {
      # 0.25 for co2
      weight_matrix[i, j] <- 0.25 * sqrt(xij)</pre>
    } else if (j == 3) {
      # 0.5 for CO
      weight_matrix[i, j] <- 0.5 * sqrt(xij)</pre>
    } else if (xij <= LOD) {</pre>
      weight_matrix[i, j] <- 2 * LOD # equation 5a) in reference paper</pre>
    } else {
      weight matrix[i, j] \leftarrow sqrt(((0.1 * xij)**2 + LOD**2)) #equation 5c) in reference paper
    }
  }
}
```

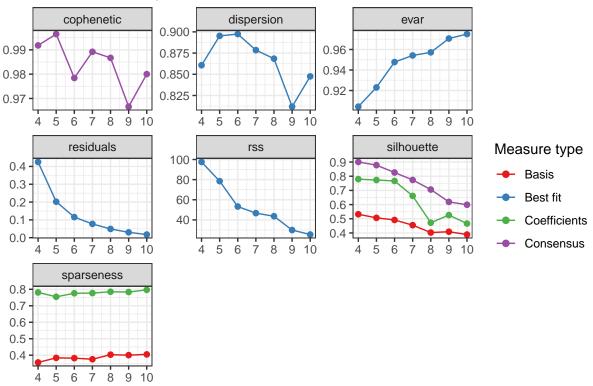
Helper for source contributions plots

LS-NMF + Random seed

```
# for each rank, run 30 models and find best one
# start time lsnmf rand <- Sys.time()</pre>
#
# lsnmf_random_less_o3 <- nmf(</pre>
# normalized_matrix_less_o3,
# components,
# method = "ls-nmf",
# weight = weight_matrix,
#
  30,
#
    seed = 123456
# )
#
# end_time_lsnmf_rand <- Sys.time()</pre>
# end_time_lsnmf_rand-start_time_lsnmf_rand
# # 19.25 minutes to run the above
```

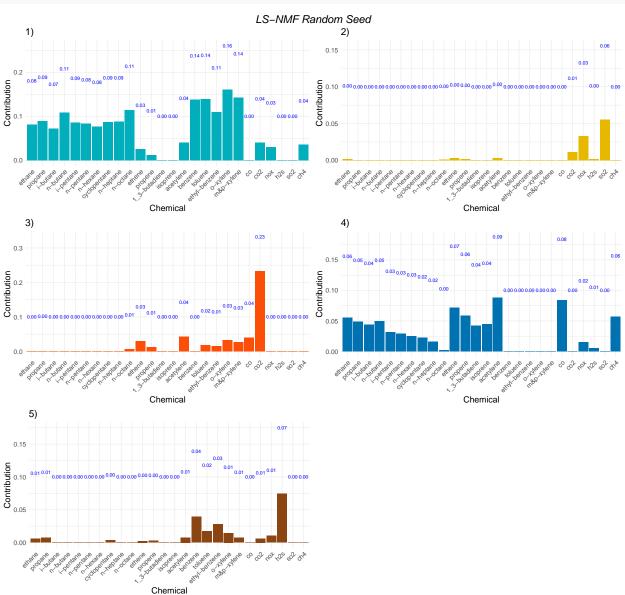
```
# saveRDS(lsnmf_random_less_o3,
# 'lsnmf_random_less_o3.rds')
lsnmf_random_less_o3 <- readRDS('lsnmf_random_less_o3.rds')
# plots the NMF rank survey
plot(lsnmf_random_less_o3)</pre>
```

NMF rank survey



Factorization rank

Look at 5 factors:



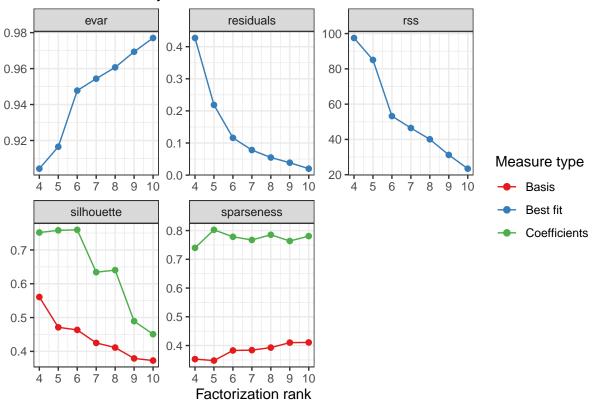
LS-NMF + nndsvd seed

```
#function below used to estimate the optimal rank and will be used in the nmf() function.
# start_time_lsnmf_nndsvd <- Sys.time()
#
# lsnmf_nndsvd_less_o3 <- nmf(</pre>
```

```
normalized_matrix_less_o3,
#
   rank = components,
   nrun = 1, # since using nndsvd
#
#
   method = "ls-nmf",
#
   weight = weight_matrix,
    seed = 'nndsvd'
#
# )
#
# end_time_lsnmf_nndsvd <- Sys.time()</pre>
# end_time_lsnmf_nndsvd-start_time_lsnmf_nndsvd
# # 1.34 minutes to run the above
# saveRDS(lsnmf_nndsvd_less_o3,
          'lsnmf_nndsvd_less_o3.rds')
lsnmf_nndsvd_less_o3 <- readRDS('lsnmf_nndsvd_less_o3.rds')</pre>
```

```
# plots the NMF rank survey
plot(lsnmf_nndsvd_less_o3)
```

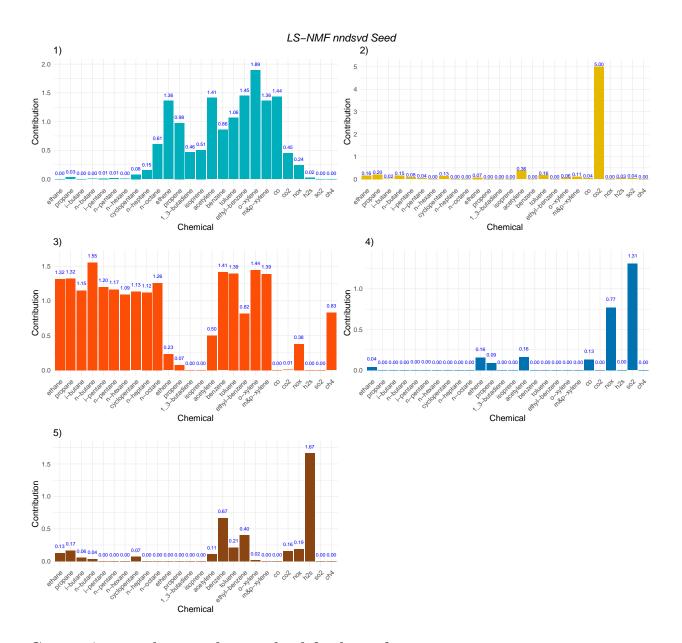
NMF rank survey



Look at 5 factors:

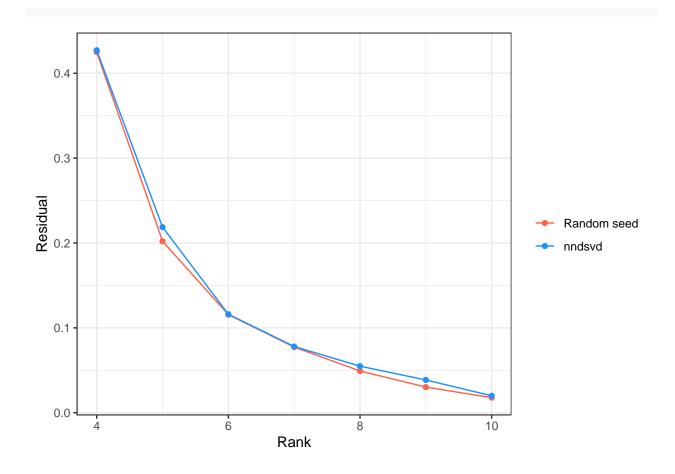
```
output <- lsnmf_nndsvd_less_o3$fit$`5`
W <- basis(output)
H <- coef(output)</pre>
```

```
# Convert H to a data frame for ggplot
H_df_5c_less_o3 <- as.data.frame(H)</pre>
# Add a column for chemicals
H_df_5c_less_o3$Component <- rownames(H_df_5c_less_o3)</pre>
# Reshape data to long format
H_long_5c_less_o3 <- pivot_longer(H_df_5c_less_o3, cols = -Component,</pre>
                                    names_to = "Chemical", values_to = "Contribution")
# Plot
nmfplt_1_lsnmf_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                              '1', '1)')
nmfplt_2_lsnmf_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                              '2', '2)')
nmfplt_3_lsnmf_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                              '3', '3)')
nmfplt_4_lsnmf_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                              '4', '4)')
nmfplt_5_lsnmf_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                              '5', '5)')
```



Comparing random seed vs nndsvd for ls-nmf

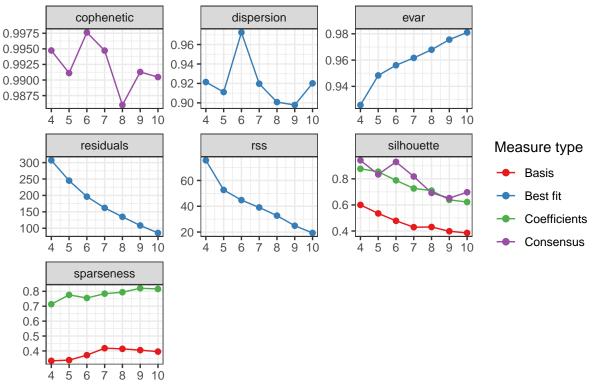
Residuals is defined as sum(((X - fitted(object)) * weight)^2)/2



KL + Random seed

```
\# start\_time\_kl\_random \leftarrow Sys.time()
# kl_random_less_o3 <- nmf(</pre>
# normalized_matrix_less_o3,
# rank = components,
  nrun = 30,
#
   method = "KL",
#
   seed = 123456
# )
# end_time_kl_random <- Sys.time()</pre>
{\it\#-end\_time\_kl\_random\_start\_time\_kl\_random}
# 14.27 minutes to run the above
# saveRDS(kl_random_less_o3, 'kl_random_less_o3.rds')
kl_random_less_o3 <- readRDS('kl_random_less_o3.rds')</pre>
# plots the NMF rank survey
plot(kl_random_less_o3)
```

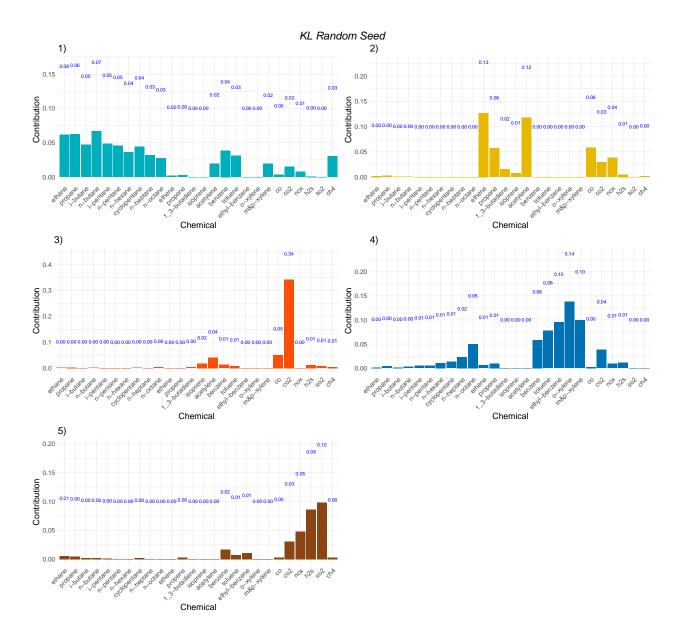
NMF rank survey



Factorization rank

```
\#\#\# Look at 5 factors:
```

```
output <- kl_random_less_o3$fit$`5`</pre>
W <- basis(output)</pre>
H <- coef(output)</pre>
# Convert H to a data frame for ggplot
H_df_5c_less_o3 <- as.data.frame(H)</pre>
# Add a column for chemicals
H_df_5c_less_o3$Component <- rownames(H_df_5c_less_o3)</pre>
# Reshape data to long format
H_long_5c_less_o3 <- pivot_longer(H_df_5c_less_o3, cols = -Component,</pre>
                                     names_to = "Chemical", values_to = "Contribution")
# Plot
nmfplt_1_kl_random_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                               '1', '1)')
nmfplt_2_kl_random_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                               '2', '2)')
nmfplt_3_kl_random_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                               '3', '3)')
nmfplt_4_kl_random_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                               '4', '4)')
nmfplt_5_kl_random_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre>
                                               '5', '5)')
```



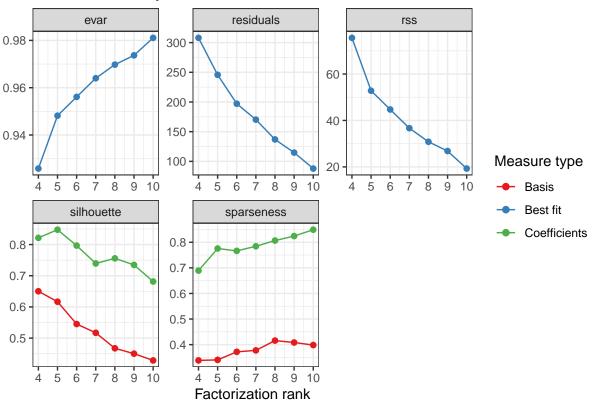
KL + nndsvd

```
# errors <- numeric(length(components) - 4)

# Loop over the number of components
# for (n in components) {
# nmf_result <- nmf(normalized_matrix_less_o3, rank = n, method = "KL", seed='nndsvd')
# reconstruction <- basis(nmf_result) %*% coef(nmf_result)
# error <- norm(normalized_matrix_less_o3 - reconstruction, type = "F")^2 # RSS
# errors[n-3] <- error
# print(pasteO('Completed ', n - 3, ' out of 7'))
# }
# # saveRDS(errors, 'errors_KL_nndsvd_less_o3.rds')
# errors <- readRDS('errors_KL_nndsvd_less_o3.rds')</pre>
```

```
\# start\_time\_kl\_nndsvd \leftarrow Sys.time()
#
# kl_nndsvd_less_o3 <- nmf(</pre>
   normalized_matrix_less_o3,
  rank = components,
#
#
   nrun = 1,
   method = "KL",
#
    seed = 'nndsvd'
# )
# end_time_kl_nndsvd <- Sys.time()</pre>
\# end_time_kl_nndsvd-start_time_kl_nndsvd
# 1 minute to run the above
# saveRDS(kl_nndsvd_less_o3, 'kl_nndsvd_less_o3.rds')
kl_nndsvd_less_o3 <- readRDS('kl_nndsvd_less_o3.rds')</pre>
# plots the NMF rank survey
plot(kl_nndsvd_less_o3)
```

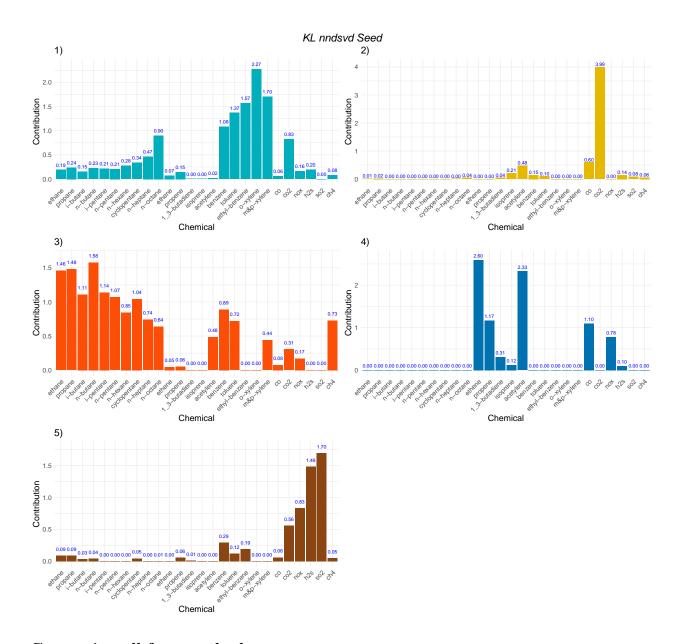
NMF rank survey



Look at 5 factors:

```
output <- kl_nndsvd_less_o3$fit$`5`
W <- basis(output)</pre>
```

H <- coef(output)</pre> # Convert H to a data frame for ggplot H_df_5c_less_o3 <- as.data.frame(H)</pre> # Add a column for chemicals H_df_5c_less_o3\$Component <- rownames(H_df_5c_less_o3)</pre> # Reshape data to long format H_long_5c_less_o3 <- pivot_longer(H_df_5c_less_o3, cols = -Component,</pre> names_to = "Chemical", values_to = "Contribution") # Plot nmfplt_1_kl_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre> '1', '1)') nmfplt_2_kl_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre> '2', '2)') nmfplt_3_kl_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre> '3', '3)') nmfplt_4_kl_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre> '4', '4)') nmfplt_5_kl_nndsvd_less_o3_5c <- get_component_plot(H_long_5c_less_o3,</pre> '5', '5)')

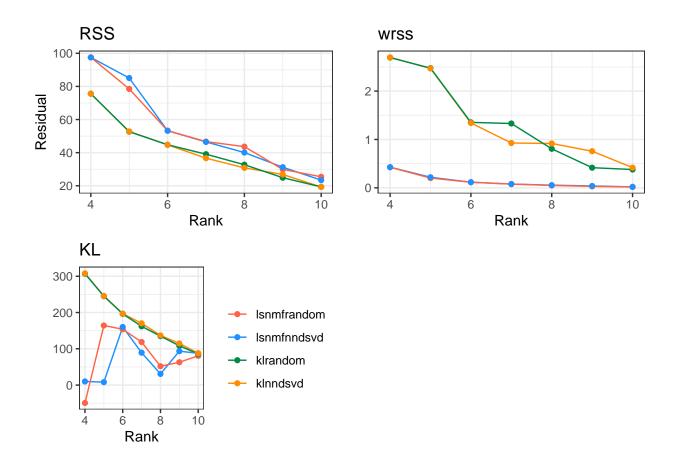


Comparing all four methods

Using RSS, WRSS, and KL

```
get_residual <- function(component, seed, method, objective) {
  fitted <- fitted(get(paste(method, seed, 'less_o3', sep = '_'))$fit[[component-3]])
  if (objective == 'wrss') {
    return(sum(((normalized_matrix_less_o3 - fitted) * weight_matrix)^2)/2)
  } else if (objective == 'kl') {
    log_term <- normalized_matrix_less_o3/fitted
    log_term[log_term<.Machine$double.eps] <- .Machine$double.eps
    return(sum(normalized_matrix_less_o3 * log(log_term) - fitted + normalized_matrix_less_o3))
  } else if (objective == 'rss') {
    return(norm(normalized_matrix_less_o3 - fitted, type = 'F')^2)
  }
}</pre>
```

```
df_plot <- expand_grid(</pre>
  component = components,
  seed = c('random', 'nndsvd'),
 method = c('lsnmf', 'kl'),
  objective = c('rss', 'wrss', 'kl')
) %>%
 rowwise() %>%
 mutate(residual = get residual(component, seed, method, objective)) %>%
  ungroup() %>%
  mutate(model = paste0(method, seed))
RSS_plot <- df_plot %>%
  filter(objective=='rss') %>%
  ggplot() +
  geom_line(aes(x = component, y = residual, group = model, color = model)) +
  geom_point(aes(x = component, y = residual, group = model, color = model)) +
  scale_colour_manual("",
                    breaks = c("lsnmfrandom", "lsnmfnndsvd",
                               "klrandom", "klnndsvd"),
                    values = c("tomato1", "dodgerblue",
                               "springgreen4", "darkorange")) +
  labs(x = 'Rank', y = 'Residual', title = 'RSS') +
  theme bw() +
  theme(legend.position="none")
WRSS_plot <- df_plot %>%
  filter(objective=='wrss') %>%
  ggplot() +
  geom_line(aes(x = component, y = residual, group = model, color = model)) +
  geom_point(aes(x = component, y = residual, group = model, color = model)) +
  scale_colour_manual("",
                  breaks = c("lsnmfrandom", "lsnmfnndsvd",
                             "klrandom", "klnndsvd"),
                  values = c("tomato1", "dodgerblue",
                             "springgreen4", "darkorange")) +
  labs(x = 'Rank', y = '', title = 'wrss') +
  theme_bw() +
  theme(legend.position="none")
KL_plot <- df_plot %>%
  filter(objective=='kl') %>%
  ggplot() +
  geom_line(aes(x = component, y = residual, group = model, color = model)) +
  geom_point(aes(x = component, y = residual, group = model, color = model)) +
  scale_colour_manual("",
                    breaks = c("lsnmfrandom", "lsnmfnndsvd",
                               "klrandom", "klnndsvd"),
                    values = c("tomato1", "dodgerblue",
                               "springgreen4", "darkorange")) +
  labs(x = 'Rank', y = '', title = 'KL') +
  theme_bw()
grid.arrange(RSS_plot, WRSS_plot, KL_plot, ncol=2)
```



NMF with 5 source factors without ozone

- remove ozone
- use KL divergence loss with svd seed
- Extract W (basis) and H (coefs) matrices
- Calculate variance explained in all 5 factors
- Calculate variance explained by each factor

```
nmf_result_5c_less_o3 <- kl_nndsvd_less_o3$fit$`5`

basis_matrix_5c_less_o3 <- basis(nmf_result_5c_less_o3) #W
coef_matrix_5c_less_o3 <- coef(nmf_result_5c_less_o3) #H

# get variance explained by the factors (total residuals)
reconstruct<-fitted(nmf_result_5c_less_o3)

tss <- sum((normalized_matrix_less_o3 - mean(normalized_matrix_less_o3))^2)
rss <- sum((normalized_matrix_less_o3 - reconstruct)^2)
variance_explained <- 1 - (rss / tss)
variance_explained</pre>
```

```
## [1] 0.9212864
```

```
# get variance explained by each factor separately
# Compute variance explained by each factor
# Initialize variance explained tracker
variance_explained_factors <- numeric(5)</pre>
```

```
# Incrementally add factors and calculate variance explained
reconstruction <- matrix(0, nrow = nrow(basis_matrix_5c_less_o3), ncol = ncol(coef_matrix_5c_less_o3))
for (i in 1:5) {
    # Add the i-th factor to the reconstruction
    reconstruction <- reconstruction + (basis_matrix_5c_less_o3[, i, drop=FALSE] %*% coef_matrix_5c_less_
    # Compute Residual Sum of Squares (RSS)
    rss_f <- sum((normalized_matrix_less_o3 - reconstruction)^2)

# Compute Variance Explained by adding this factor
    variance_explained_factors[i] <- 1 - (rss_f / tss)
}

# Print variance explained by each factor cumulatively
variance_explained_factors

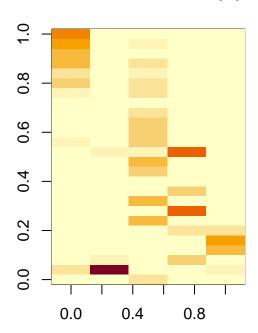
## [1] 0.2395401 0.5113683 0.8113445 0.8921360 0.9212864

par(mfrow = c(1, 2))
image(basis_matrix_5c_less_o3, main = "Basis Matrix (W)")
image(coef_matrix_5c_less_o3, main = "Coefficient Matrix (H)")</pre>
```

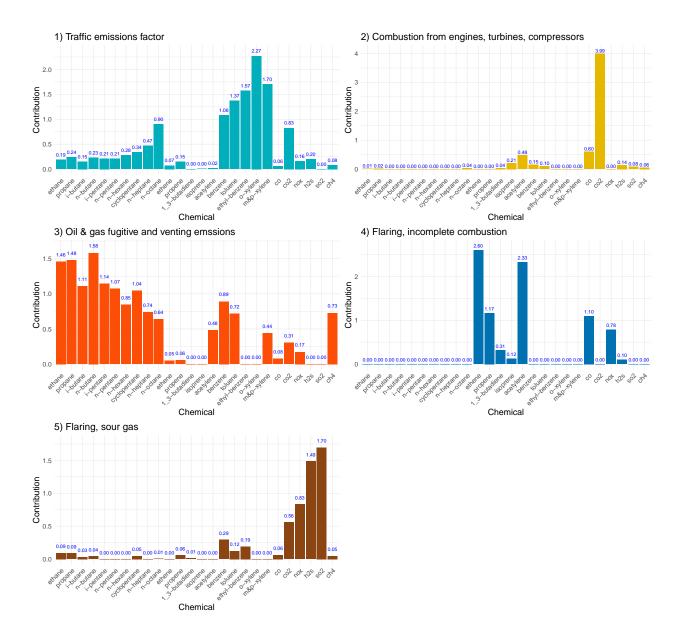
Basis Matrix (W)

0.0 0.2 0.4 0.6 0.8 1.0

Coefficient Matrix (H)

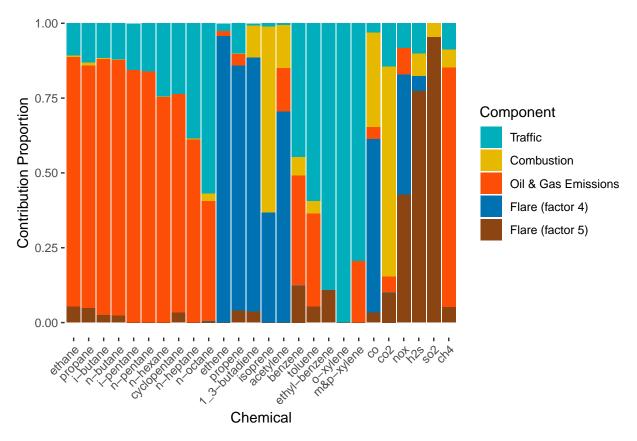


```
# Convert H to a data frame for ggplot
H_df_5c_less_o3 <- as.data.frame(coef_matrix_5c_less_o3)
# Add a column for chemicals</pre>
```



Fingerprint plot

```
'Combustion',
    'Oil & Gas Emissions',
    'Flare (factor 4)',
    'Flare (factor 5)'
  )
) %>%
mutate(Component = factor(
  Component,
  levels = c(
    'Traffic',
    'Combustion',
    'Oil & Gas Emissions',
    'Flare (factor 4)',
    'Flare (factor 5)'
  )
)) %>%
pivot_longer(cols = -Component,
             names_to = "Chemical",
             values_to = "Contribution_prop") %>%
mutate(Chemical = factor(Chemical, levels = desired_order)) %>%
ggplot(aes(fill = Component, y = Contribution_prop, x = Chemical)) +
geom_bar(position = "fill", stat = "identity") +
scale_fill_manual(values = custom_colors) +
theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
labs(x = "Chemical", y = "Contribution Proportion") +
theme(
 panel.grid.major = element_blank(),
 panel.grid.minor = element_blank(),
 panel.background = element_blank()
)
```



#ggsave("fingerprint.png", c)

Wind plots

```
hourly_wind_nona <- hourly_nona %>%
    select(wdr_deg, wsp_ms)

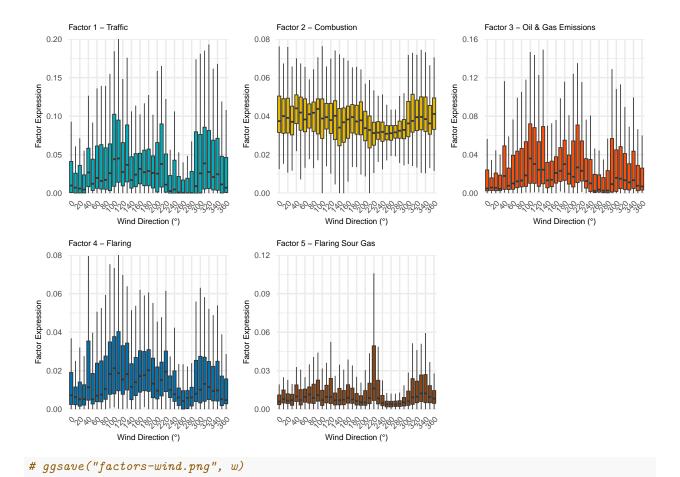
data_to_plot <- tibble(
    component1 = basis(nmf_result_5c_less_o3)[,1],
    component2 = basis(nmf_result_5c_less_o3)[,2],
    component3 = basis(nmf_result_5c_less_o3)[,3],
    component4 = basis(nmf_result_5c_less_o3)[,4],
    component5 = basis(nmf_result_5c_less_o3)[,5],
    wd = round(hourly_wind_nona$wdr_deg, -1)
)

color_pal <- c("#00AFBB", "#E7B800", "#FC4E07", "#0072B2", "#8B4513")

data_long <- data_to_plot %>%
    pivot_longer(cols = starts_with("component"), names_to = "Factor", values_to = "Expression")

factor_labels <- c(
    "component1" = "Factor 1 - Traffic",
    "component2" = "Factor 2 - Combustion",</pre>
```

```
"component3" = "Factor 3 - Oil & Gas Emissions",
 "component4" = "Factor 4 - Flaring",
  "component5" = "Factor 5 - Flaring Sour Gas"
)
data_long <- data_long %>%
 mutate(wd = factor(wd, levels = sort(unique(wd))))
# Select every second wind direction for labeling
every_second_label <- levels(data_long$wd)[seq(1, length(levels(data_long$wd)), by = 2)]
y_axis_limits <- list(</pre>
  "component1" = c(0, 0.2),
 "component2" = c(0, 0.08),
  "component3" = c(0, 0.16),
  "component4" = c(0, 0.08),
  "component5" = c(0, 0.12)
plots <- lapply(1:5, function(i) {</pre>
  factor_name <- paste0("component", i)</pre>
  ggplot(data_long %>% filter(Factor == factor_name),
         aes(x = wd, y = Expression, fill = as.factor(wd))) +
   geom_boxplot(outliers=F, size=0.3) +
    scale_fill_manual(values = rep(color_pal[i], length(unique(data_long$wd)))) +
   scale_x_discrete(breaks = every_second_label) +
    coord_cartesian(ylim = y_axis_limits[[factor_name]]) +
    scale_y_continuous(
      limits = c(0, NA),
     breaks = seq(0, y_axis_limits[[factor_name]][2], length.out = 5) ,
      expand=expansion(mult=c(0))
   ) +
   labs(title = factor_labels[factor_name],
         x = "Wind Direction (°)",
         y = "Factor Expression") +
   theme minimal() +
   theme(
      legend.position = "none",
      plot.title = element_text(size = 6), # Smaller title text
      axis.title = element_text(size = 6), # Smaller axis labels
      axis.text = element_text(size = 6), # Smaller x and y tick labels
      axis.text.x = element_text(angle = 45, hjust = 1)
   )
})
grid.arrange(grobs = plots, ncol = 3)
```



Factor analysis

generated.

merge in factors 1-5 to dataset (hourly)
 # First look at how well this approximates

This warning is displayed once every 8 hours.

```
fitted_5c_less_o3 <- fitted(nmf_result_5c_less_o3)
sum(abs(normalized_matrix_less_o3-fitted_5c_less_o3))

## [1] 1059.63

# NMF factorizes V = WH

# Store Basis matrix (W) and Coef Matrix (H)
saveRDS(basis_matrix_5c_less_o3, 'result_rfiles/nmf_norm_5c_less_o3_basis.rds')
saveRDS(coef_matrix_5c_less_o3, 'result_rfiles/nmf_norm_5c_less_o3_coef.rds')

# Merge basis matrix into hourly observations
basis_matrix_5c_less_o3 <- as_tibble(basis_matrix_5c_less_o3) %>%
setNames(c('Factor1', 'Factor2', 'Factor3', 'Factor4', 'Factor5'))

## Warning: The `x` argument of `as_tibble.matrix()` must have unique column names if
## `.name_repair` is omitted as of tibble 2.0.0.
## i Using compatibility `.name_repair`.
```

Call `lifecycle::last_lifecycle_warnings()` to see where this warning was

```
normalized_hourly_data_5c_less_o3 <- hourly_nona[,c('day', 'time_utc')] %>%
   cbind(normalized_matrix_less_o3) %>%
   cbind(basis_matrix_5c_less_o3) %>%
   right_join(hourly_data %>% select(-'day'), join_by(time_utc), suffix = c('_norm', ''))

# saveRDS(normalized_hourly_data_5c_less_o3,
# 'result_rfiles/normalized_hourly_data_5c_less_o3.rds')
normalized_hourly_data_5c_less_o3 <- readRDS('result_rfiles/normalized_hourly_data_5c_less_o3.rds')</pre>
```

- make daily dataset for VNF analysis
- compute wind directions from plots

- 1) number of flares in 100km of trailer associated with NMF
- 2) weighted count based on distance to trailer

```
# Check if relationship between # flares and flare factor (4 & 5)
# Linear model
flare_factor <- lm(n_flare_100 ~ Factor1 + Factor2 + Factor3 + Factor4 + Factor5,
                   data = normalized_daily_data_5c_less_o3)
summary(flare_factor)
##
## Call:
## lm(formula = n_flare_100 ~ Factor1 + Factor2 + Factor3 + Factor4 +
##
       Factor5, data = normalized_daily_data_5c_less_o3)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
                    4.205 18.488 76.270
## -54.638 -22.160
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                             7.455
                                     7.034 1.61e-11 ***
               52.438
## Factor1
               -27.402
                           106.172 -0.258
                                            0.7965
## Factor2
              -338.560
                           196.573 -1.722
                                             0.0861 .
## Factor3
               286.534
                           151.310
                                    1.894
                                             0.0593 .
## Factor4
              -287.536
                           244.717 -1.175
                                             0.2410
## Factor5
              231.978
                           212.510
                                    1.092
                                            0.2760
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 27.79 on 273 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.03877,
                                   Adjusted R-squared: 0.02117
## F-statistic: 2.202 on 5 and 273 DF, p-value: 0.05434
flare_factor45 <- lm(n_flare_100 ~ Factor4 + Factor5, data = normalized_daily_data_5c_less_o3)
summary(flare_factor45)
##
## lm(formula = n_flare_100 ~ Factor4 + Factor5, data = normalized_daily_data_5c_less_o3)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -53.409 -23.830
                   5.588 18.235 77.131
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                40.780
                            3.386 12.044
                                            <2e-16 ***
## Factor4
               -48.431
                          150.383 -0.322
                                            0.7477
               360.559
                          206.393
## Factor5
                                    1.747
                                            0.0818 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 28.02 on 276 degrees of freedom
    (1 observation deleted due to missingness)
## Multiple R-squared: 0.01171,
                                   Adjusted R-squared: 0.004548
## F-statistic: 1.635 on 2 and 276 DF, p-value: 0.1968
flare_factor_weighted <- lm(weighted.count ~ Factor1 + Factor2 + Factor3 + Factor4 + Factor5,
                           data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted)
##
## Call:
## lm(formula = weighted.count ~ Factor1 + Factor2 + Factor3 + Factor4 +
##
      Factor5, data = normalized_daily_data_5c_less_o3)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -2.3295 -0.2180 0.0546 0.3809 3.9848
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                           0.2278
                                    9.907
## (Intercept) 2.2572
                                            <2e-16 ***
                           3.2450
                                    0.038
                                           0.9694
## Factor1
                0.1244
## Factor2
               -4.7740
                           6.0080 - 0.795
                                            0.4275
## Factor3
                7.4339
                           4.6246
                                    1.607
                                            0.1091
## Factor4
              -12.9155
                           7.4794 - 1.727
                                            0.0853 .
## Factor5
                4.0762
                           6.4951
                                    0.628
                                           0.5308
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.8492 on 273 degrees of freedom
   (1 observation deleted due to missingness)
## Multiple R-squared: 0.02221,
                                    Adjusted R-squared:
## F-statistic: 1.24 on 5 and 273 DF, p-value: 0.2905
flare_factor_weighted45 <- lm(weighted.count ~ Factor4 + Factor5,</pre>
                              data = normalized_daily_data_5c_less_o3)
summary(flare factor weighted45)
##
## Call:
## lm(formula = weighted.count ~ Factor4 + Factor5, data = normalized_daily_data_5c_less_o3)
## Residuals:
##
      Min
                1Q Median
                                3Q
## -2.2558 -0.1821 0.0775 0.3622 3.9366
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.0910
                           0.1029 20.315
                                             <2e-16 ***
                            4.5712 -0.878
## Factor4
                -4.0144
                                              0.381
## Factor5
                7.3663
                            6.2738
                                    1.174
                                              0.241
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8518 on 276 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.005595, Adjusted R-squared: -0.001611
## F-statistic: 0.7765 on 2 and 276 DF, p-value: 0.461
# All factors + wind speed + wind direction + factor5:sw wind.
# Wind direction from 270 to 45 is left as reference group.
flare_factor_weighted_2 <- lm(weighted.count ~ Factor1 + Factor2 + Factor3 +</pre>
                                Factor4 + Factor5 + wsp_ms + wind_45_135 +
                                wind_135_180 + Factor5*wind_180_270,
                              data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_2)
##
## Call:
## lm(formula = weighted.count ~ Factor1 + Factor2 + Factor3 + Factor4 +
       Factor5 + wsp ms + wind 45 135 + wind 135 180 + Factor5 *
       wind_180_270, data = normalized_daily_data_5c_less_o3)
##
##
## Residuals:
                1Q Median
                                3Q
                                       Max
## -2.4382 -0.2036 0.0782 0.3578 3.9528
## Coefficients:
                             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                             2.14418
                                        0.33390
                                                   6.422 6.11e-10 ***
                                                          0.9825
## Factor1
                             0.07365
                                         3.35780
                                                   0.022
## Factor2
                             -4.92773
                                         6.19462 -0.795
                                                           0.4270
## Factor3
                             8.99603
                                         4.80767
                                                   1.871
                                                           0.0624 .
```

```
## Factor4
                           -10.66714
                                        7.82960 -1.362
                                                          0.1742
## Factor5
                             3.28556
                                        7.52447 0.437
                                                          0.6627
## wsp ms
                                                0.980
                                                         0.3282
                            0.04430
                                        0.04523
## wind_45_135TRUE
                                        0.17743 -0.877
                            -0.15557
                                                          0.3814
## wind_135_180TRUE
                            -0.15153
                                        0.13270 -1.142
                                                         0.2545
## wind 180 270TRUE
                            -0.21667
                                        0.22628 -0.958
                                                          0.3392
## Factor5:wind_180_270TRUE
                            2.51821
                                      13.08348
                                                0.192
                                                        0.8475
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8524 on 268 degrees of freedom
    (1 observation deleted due to missingness)
## Multiple R-squared: 0.03302,
                                   Adjusted R-squared: -0.003061
## F-statistic: 0.9152 on 10 and 268 DF, p-value: 0.5196
\# Same as above but only factor 4 and 5
flare_factor_weighted_3 <- lm(weighted.count ~ Factor4 + Factor5 + wsp_ms +</pre>
                               Factor5*wind_180_270,
                             data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_3)
##
## Call:
## lm(formula = weighted.count ~ Factor4 + Factor5 + wsp_ms + Factor5 *
      wind_180_270, data = normalized_daily_data_5c_less_o3)
##
## Residuals:
##
               1Q Median
                               3Q
      Min
                                      Max
## -2.2706 -0.1961 0.0714 0.3721 3.9358
##
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            2.057728
                                      0.222033 9.268 <2e-16 ***
## Factor4
                           -3.273445
                                       5.155494 -0.635
                                                           0.526
## Factor5
                            7.499668
                                       7.297235
                                                 1.028
                                                           0.305
## wsp_ms
                            0.009441
                                      0.040855
                                                 0.231
                                                           0.817
## wind_180_270TRUE
                           -0.059345
                                      0.215638 -0.275
                                                           0.783
## Factor5:wind_180_270TRUE -0.078349 12.897092 -0.006
                                                           0.995
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.856 on 273 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.006554, Adjusted R-squared: -0.01164
## F-statistic: 0.3602 on 5 and 273 DF, p-value: 0.8754
# Same as above but interaction between factor 4 and SW wind
flare_factor_weighted_3b <- lm(weighted.count ~ Factor4 + Factor5 + wsp_ms +
                                Factor4*wind_180_270,
                              data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_3b)
##
## Call:
## lm(formula = weighted.count ~ Factor4 + Factor5 + wsp ms + Factor4 *
      wind_180_270, data = normalized_daily_data_5c_less_o3)
##
```

```
##
## Residuals:
      Min
               1Q Median
## -2.3058 -0.2123  0.0650  0.3774  3.9523
## Coefficients:
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             2.030311
                                      0.215853
                                                 9.406
                                                           <2e-16 ***
## Factor4
                            -0.841684 5.604781 -0.150
                                                           0.881
## Factor5
                             7.401203 6.365967
                                                 1.163
                                                           0.246
## wsp_ms
                             0.005478 0.040870
                                                  0.134
                                                           0.893
## wind_180_270TRUE
                             0.143565
                                       0.224432
                                                  0.640
                                                           0.523
## Factor4:wind_180_270TRUE -10.510472
                                      9.618074 -1.093
                                                           0.275
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8541 on 273 degrees of freedom
    (1 observation deleted due to missingness)
## Multiple R-squared: 0.01088, Adjusted R-squared: -0.007235
## F-statistic: 0.6006 on 5 and 273 DF, p-value: 0.6995
# Same as above but with East wind
flare_factor_weighted_3c <- lm(weighted.count ~ Factor4 + Factor5 + wsp_ms +
                                Factor5*wind_45_135,
                              data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_3c)
##
## Call:
## lm(formula = weighted.count ~ Factor4 + Factor5 + wsp_ms + Factor5 *
##
      wind_45_135, data = normalized_daily_data_5c_less_o3)
##
## Residuals:
      Min
               1Q Median
                               3Q
## -2.2355 -0.1832 0.0761 0.3768 3.9129
##
## Coefficients:
                            Estimate Std. Error t value Pr(>|t|)
##
                           2.1177298 0.2207356 9.594
                                                        <2e-16 ***
## (Intercept)
## Factor4
                          -4.0986004 5.1120629 -0.802
                                                           0.423
## Factor5
                           6.1846170 6.5540446
                                                0.944
                                                           0.346
## wsp ms
                           0.0008777 0.0407876
                                                 0.022
                                                           0.983
                                                           0.255
## wind_45_135TRUE
                          -0.4275903 0.3752245 -1.140
## Factor5:wind_45_135TRUE 22.0187173 23.3341439
                                                 0.944
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8543 on 273 degrees of freedom
    (1 observation deleted due to missingness)
## Multiple R-squared: 0.01053,
                                   Adjusted R-squared: -0.007588
## F-statistic: 0.5813 on 5 and 273 DF, p-value: 0.7143
flare_factor_weighted_3d <- lm(weighted.count ~ Factor4 + Factor5 + wsp_ms +
                                Factor4*wind_45_135,
                              data = normalized_daily_data_5c_less_o3)
```

```
summary(flare_factor_weighted_3d)
##
## Call:
## lm(formula = weighted.count ~ Factor4 + Factor5 + wsp_ms + Factor4 *
       wind_45_135, data = normalized_daily_data_5c_less_o3)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -2.2680 -0.1822 0.0707 0.3665 3.9260
##
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                           2.09473
                                      0.21997
                                                9.523 <2e-16 ***
## Factor4
                          -4.50558
                                      5.36882 -0.839
                                                         0.402
## Factor5
                           7.78444
                                      6.38818
                                               1.219
                                                         0.224
## wsp_ms
                           0.00343
                                      0.04074
                                               0.084
                                                         0.933
## wind_45_135TRUE
                          -0.19324
                                      0.28449
                                               -0.679
                                                         0.498
## Factor4:wind_45_135TRUE 4.84677 13.38860
                                               0.362
                                                         0.718
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8555 on 273 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.007783,
                                   Adjusted R-squared: -0.01039
## F-statistic: 0.4283 on 5 and 273 DF, p-value: 0.8288
# Wind speed + factor 4 and interaction with East wind
flare_factor_weighted_4a <- lm(weighted.count ~ wsp_ms + Factor4*wind_45_135,
                              data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_4a)
##
## Call:
## lm(formula = weighted.count ~ wsp_ms + Factor4 * wind_45_135,
##
       data = normalized_daily_data_5c_less_o3)
##
## Residuals:
               1Q Median
##
      Min
                               3Q
                                      Max
## -2.1668 -0.1983  0.0661  0.3882  3.8663
##
## Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
##
                                      0.206642 10.585
## (Intercept)
                           2.187226
                                                         <2e-16 ***
                                      0.040343 -0.094
                                                          0.925
## wsp_ms
                          -0.003785
## Factor4
                          -2.428778
                                      5.095632 -0.477
                                                          0.634
## wind_45_135TRUE
                          -0.171010
                                      0.284161
                                                -0.602
                                                          0.548
## Factor4:wind_45_135TRUE 3.879541 13.376874
                                                0.290
                                                          0.772
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8562 on 274 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.002386,
                                   Adjusted R-squared: -0.01218
```

```
## F-statistic: 0.1638 on 4 and 274 DF, p-value: 0.9565
# Wind speed + factor 4 and interaction with SE wind
flare_factor_weighted_4b <- lm(weighted.count ~ wsp_ms + Factor4*wind_135_180,
                             data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_4b)
##
## Call:
## lm(formula = weighted.count ~ wsp_ms + Factor4 * wind_135_180,
##
      data = normalized_daily_data_5c_less_o3)
##
## Residuals:
      Min
               1Q Median
                              3Q
                                     Max
## -2.2269 -0.2186  0.0794  0.3693  3.8404
##
## Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                           ## wsp_ms
                           0.001297
                                     0.039954
                                               0.032
                                                       0.9741
## Factor4
                          -5.716640 5.512131 -1.037
                                                        0.3006
## wind_135_180TRUE
                          -0.440258
                                      0.229503 -1.918
                                                        0.0561 .
## Factor4:wind 135 180TRUE 18.354002 9.757795
                                               1.881
                                                        0.0610 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.851 on 274 degrees of freedom
    (1 observation deleted due to missingness)
## Multiple R-squared: 0.01456,
                                 Adjusted R-squared: 0.0001782
## F-statistic: 1.012 on 4 and 274 DF, p-value: 0.4014
# Wind speed + factor 4 and interaction with SW wind
flare_factor_weighted_4c <- lm(weighted.count ~ wsp_ms + Factor4*wind_180_270,
                             data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_4c)
##
## Call:
## lm(formula = weighted.count ~ wsp ms + Factor4 * wind 180 270,
      data = normalized_daily_data_5c_less_o3)
##
## Residuals:
##
      Min
               1Q Median
                              3Q
                                     Max
## -2.1911 -0.1952 0.0539 0.4087 3.8937
##
## Coefficients:
                            Estimate Std. Error t value Pr(>|t|)
                                     0.201270 10.540 <2e-16 ***
## (Intercept)
                             2.121372
                            -0.001567
                                       0.040444 -0.039
                                                          0.969
## wsp_ms
## Factor4
                            1.058349
                                      5.364665
                                                 0.197
                                                          0.844
## wind 180 270TRUE
                                      0.224576
                                                          0.524
                             0.143445
                                                 0.639
## Factor4:wind_180_270TRUE -10.634150
                                      9.623656 -1.105
                                                          0.270
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8547 on 274 degrees of freedom
```

```
(1 observation deleted due to missingness)
## Multiple R-squared: 0.005983, Adjusted R-squared: -0.008528
## F-statistic: 0.4123 on 4 and 274 DF, p-value: 0.7997
# Wind speed + factor 5 and interaction with East wind
flare_factor_weighted_5a <- lm(weighted.count ~ wsp_ms + Factor5*wind_45_135,
                              data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_5a)
##
## Call:
## lm(formula = weighted.count ~ wsp_ms + Factor5 * wind_45_135,
##
      data = normalized_daily_data_5c_less_o3)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -2.2299 -0.1901 0.0789 0.3725 3.9421
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                           2.01637
                                     0.18083 11.151 <2e-16 ***
                                              0.418
## wsp_ms
                           0.01530
                                      0.03658
                                                         0.676
## Factor5
                           4.62551
                                      6.25483
                                               0.740
                                                         0.460
## wind_45_135TRUE
                          -0.40644
                                     0.37405 -1.087
                                                         0 278
## Factor5:wind_45_135TRUE 21.30900 23.30214 0.914
                                                         0.361
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8537 on 274 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.008204,
                                   Adjusted R-squared: -0.006275
## F-statistic: 0.5666 on 4 and 274 DF, p-value: 0.6871
# Wind speed + factor 5 and interaction with SE wind
flare_factor_weighted_5b <- lm(weighted.count ~ wsp_ms + Factor5*wind_135_180,
                              data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_5b)
##
## Call:
## lm(formula = weighted.count ~ wsp_ms + Factor5 * wind_135_180,
##
      data = normalized_daily_data_5c_less_o3)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -2.2259 -0.1876 0.0693 0.3775 3.9290
##
## Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
                                                        <2e-16 ***
                                       0.18889 10.710
## (Intercept)
                            2.02295
                                       0.03643
                                                0.500
                                                          0.618
## wsp_ms
                            0.01822
## Factor5
                            4.19811
                                       7.25463
                                                0.579
                                                          0.563
## wind 135 180TRUE
                           -0.15866
                                       0.20317 -0.781
                                                          0.436
## Factor5:wind_135_180TRUE 6.06208
                                      12.22399
                                               0.496
                                                          0.620
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.8545 on 274 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.006345,
                                   Adjusted R-squared: -0.008161
## F-statistic: 0.4374 on 4 and 274 DF, p-value: 0.7816
\# Wind speed + factor 5 and interaction with SW wind
flare_factor_weighted_5c <- lm(weighted.count ~ wsp_ms + Factor5*wind_180_270,
                              data = normalized_daily_data_5c_less_o3)
summary(flare_factor_weighted_5c)
##
## Call:
## lm(formula = weighted.count ~ wsp_ms + Factor5 * wind_180_270,
##
       data = normalized_daily_data_5c_less_o3)
##
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -2.2696 -0.2009 0.0671 0.3748 3.9556
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
                                       0.18525 10.689
## (Intercept)
                            1.98021
                                                         <2e-16 ***
## wsp_ms
                            0.02098
                                       0.03655
                                               0.574
                                                          0.566
## Factor5
                            6.25646
                                       7.02199
                                                 0.891
                                                          0.374
## wind_180_270TRUE
                           -0.06960
                                       0.21480 -0.324
                                                          0.746
## Factor5:wind_180_270TRUE -0.16687
                                      12.88229 -0.013
                                                          0.990
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8551 on 274 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.005087,
                                   Adjusted R-squared: -0.009438
## F-statistic: 0.3502 on 4 and 274 DF, p-value: 0.8438
# Check relationship between avg flare distance and flare factor (4 & 5)
# Linear model
flare_factor_dist <- lm(distToLovi ~ Factor4 + Factor5, data = normalized_daily_data_5c_less_o3)
summary(flare_factor_dist)
##
## Call:
## lm(formula = distToLovi ~ Factor4 + Factor5, data = normalized_daily_data_5c_less_o3)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -34.449 -2.443 -0.139
                            2.266 31.399
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 54.7821
                           0.8756 62.564
                                            <2e-16 ***
## Factor4
                7.2656
                          39.7289
                                    0.183
                                             0.855
                                    1.236
## Factor5
               64.5797
                          52.2590
                                             0.218
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 6.883 on 252 degrees of freedom
## (25 observations deleted due to missingness)
## Multiple R-squared: 0.008425, Adjusted R-squared: 0.0005557
## F-statistic: 1.071 on 2 and 252 DF, p-value: 0.3444
```