

NMF

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```
# load the packages
library(NMF)
library(tidyverse)
library(gridExtra)
library(readxl)
```

Procedure

1. Remove hourly observation with missing observation for any chemical
2. Remove background noise level using min values (except for chemicals with minimum value $< 2 \times \text{LOD}$ and maximum value $> 100 \times \text{LOD}$)
3. Zero values are converted to a random value between 0 and $0.5 \times \text{LOD}$
4. Normalize using 0th & 99th quantile
5. Compute weight matrix according to Guha's paper, without LOQ

Reading the data

```
# read the radon data
# Old:
# hourly_radon <- readRDS("hourly_radon.rds")
# New:
hourly_data <- readRDS("../DataProcessing/Trailer_hourly_merge_20240905.rds")

# remove NAs
hourly_nona <- hourly_data %>% select(-c(temp_bb,rhi, esf_bb, distToLovi,inv_dist,
                                         distToLovi_wells, monthly_oil, monthly_gas)) %>% na.omit()

vocs <- c("ethane", "ethene", "propane", "propene",
          "1_3-butadiene", "i-butane", "n-butane",
          "acetylene", "cyclopentane", "i-pentane",
          "n-pentane", "n-hexane", "isoprene", "n-heptane",
          "benzene", "n-octane", "toluene", "ethyl-benzene",
          "m&p-xylene", "o-xylene")

# retrieving the vocs, removing everything else except the vocs
hourly_vocs <- hourly_nona %>% select(any_of(vocs))

# retrieving the non-vocs: co2_ppm, nox, ch4, h2s, so2, o3
# double check this
non_vocs <- c('ch4', 'co2_ppm', 'co', 'h2s', 'so2', 'nox', 'o3')
hourly_non_vocs <- hourly_nona %>% select(all_of(non_vocs)) %>% rename('co2' = 'co2_ppm')

hourly_full_nona <- cbind(hourly_non_vocs, hourly_vocs)
```

```

# retrieve a vector of yearmonth
hourly_dates <- hourly_nona %>%
  mutate(yearmonth = substring(day, 0, 7)) %>%
  pull(yearmonth)

```

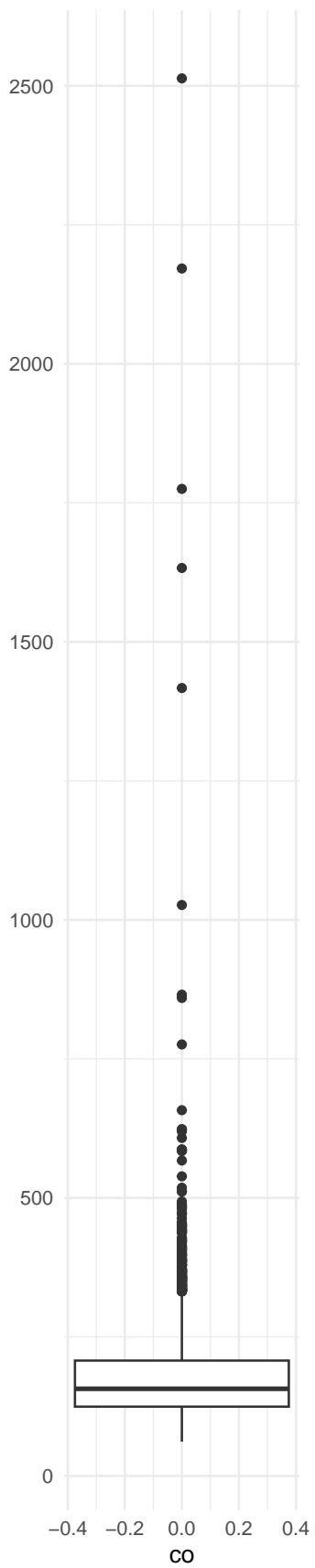
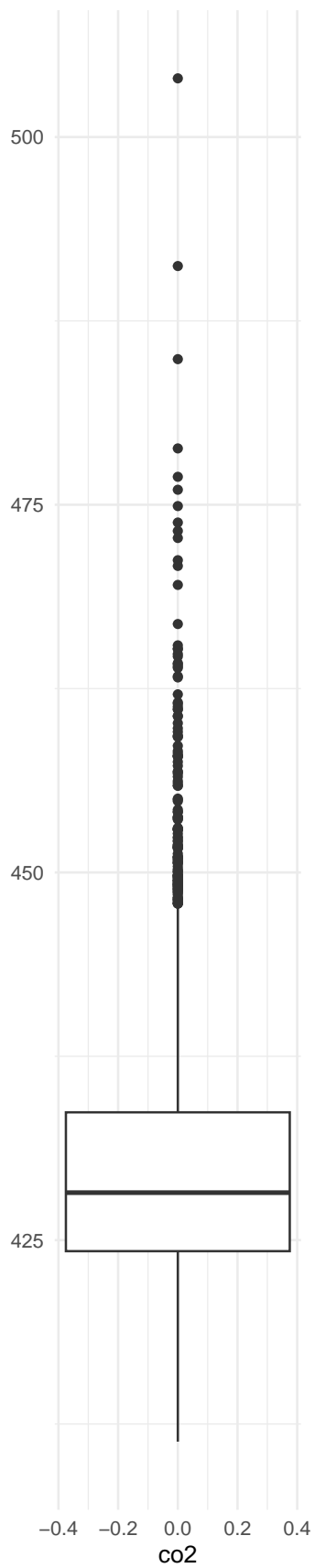
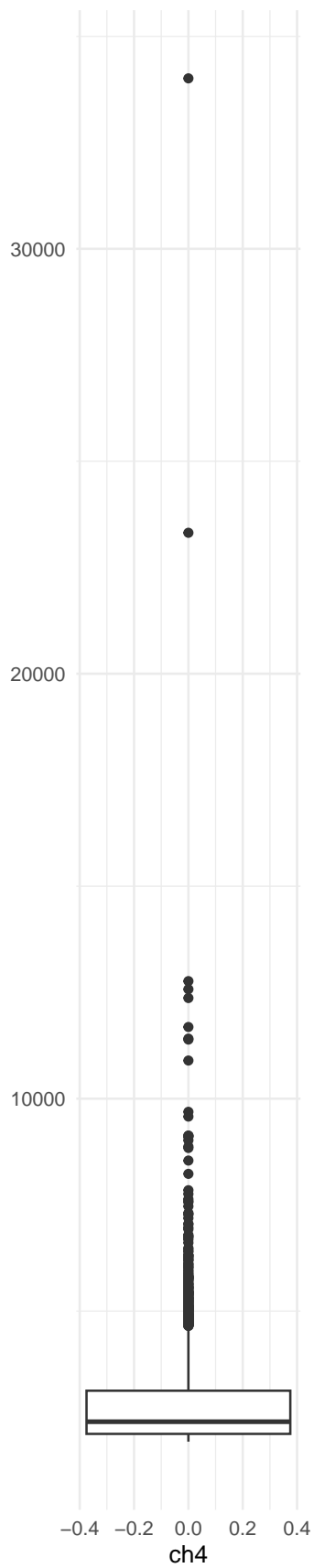
Data visualisation

```

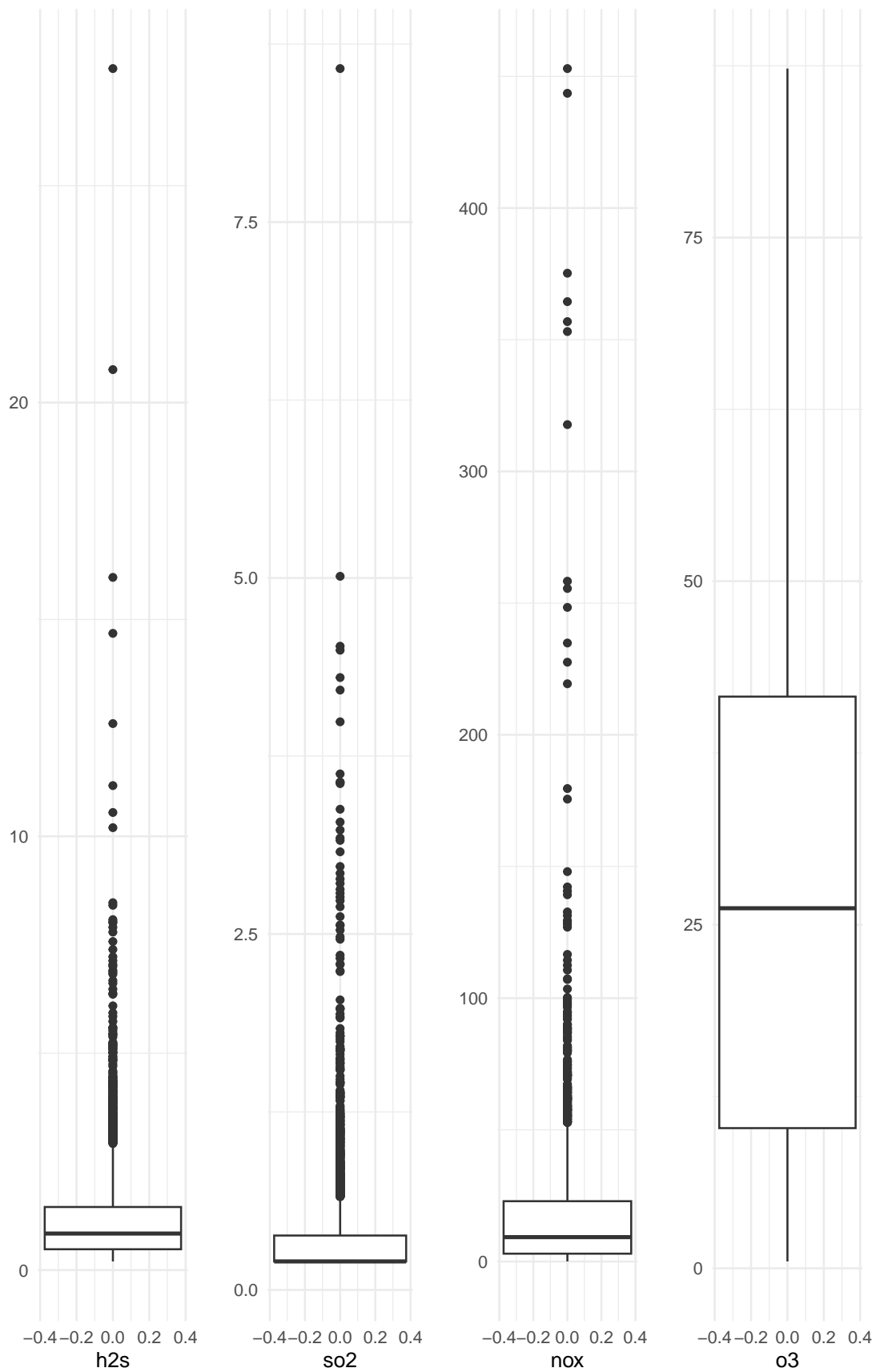
non_vocs <- c('ch4', 'co2', 'co', 'h2s', 'so2', 'nox', 'o3')
for (compound in non_vocs) {
  assign(paste0(compound, '_boxplot'),
    ggplot(hourly_non_vocs) +
      geom_boxplot(aes(y = .data[[compound]])) +
      labs(x = compound, y = '') +
      theme_minimal()
}

grid.arrange(ch4_boxplot, co2_boxplot, co_boxplot, nrow = 1)

```



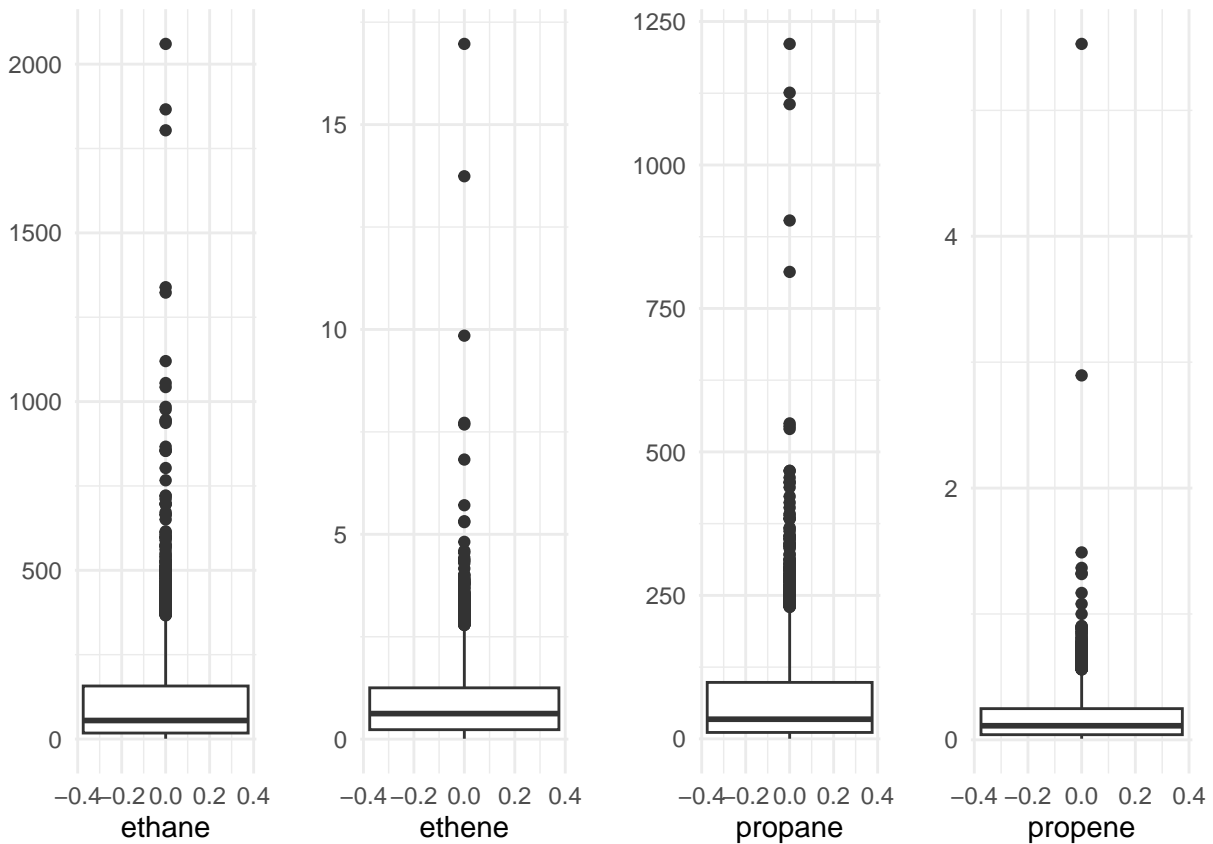
```
grid.arrange(h2s_boxplot, so2_boxplot, nox_boxplot, o3_boxplot, nrow = 1)
```



```

for (compound in vocs) {
  assign(paste0(compound, '_boxplot'),
    ggplot(hourly_vocs) +
      geom_boxplot(aes(y = .data[[compound]])) +
      labs(x = compound, y = '') +
      theme_minimal()
}
grid.arrange(get(paste0(vocs[1], '_boxplot')), get(paste0(vocs[2], '_boxplot')),
  get(paste0(vocs[3], '_boxplot')), get(paste0(vocs[4], '_boxplot')), nrow = 1)

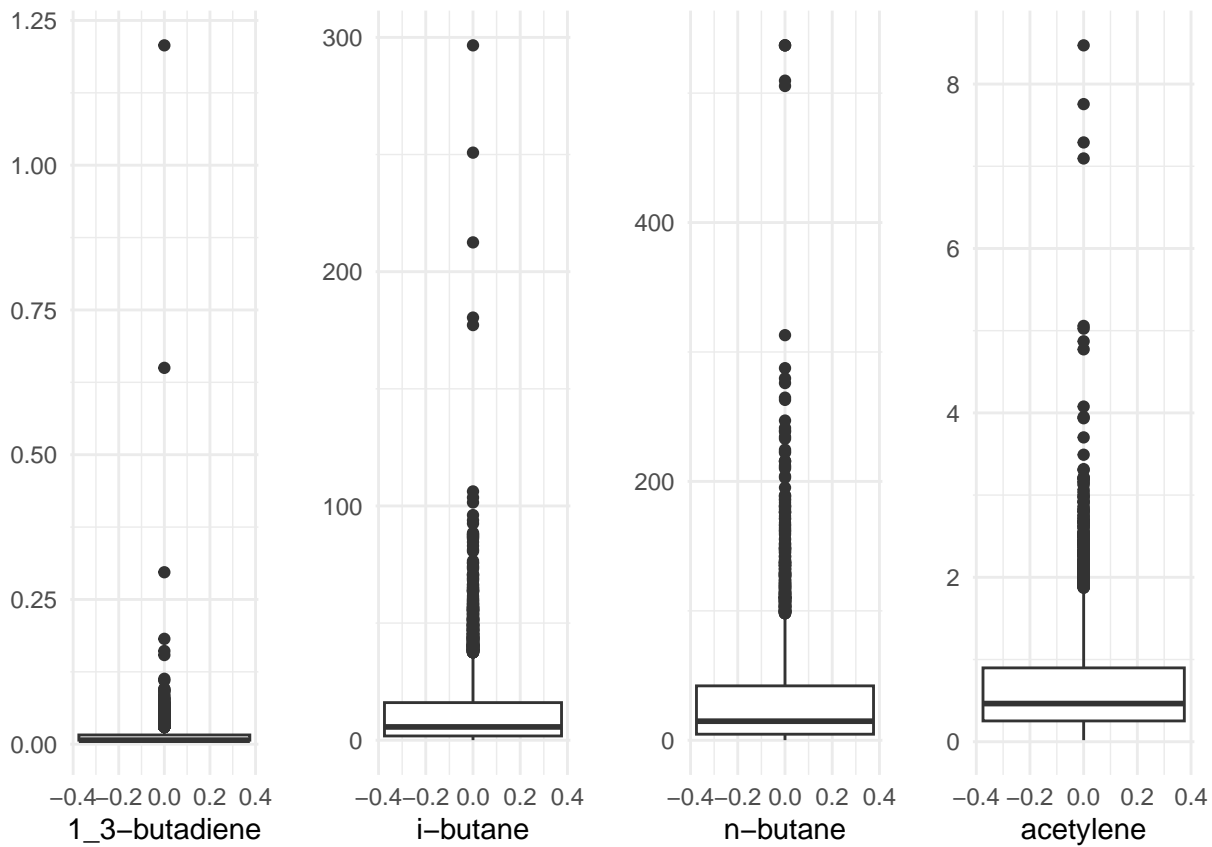
```



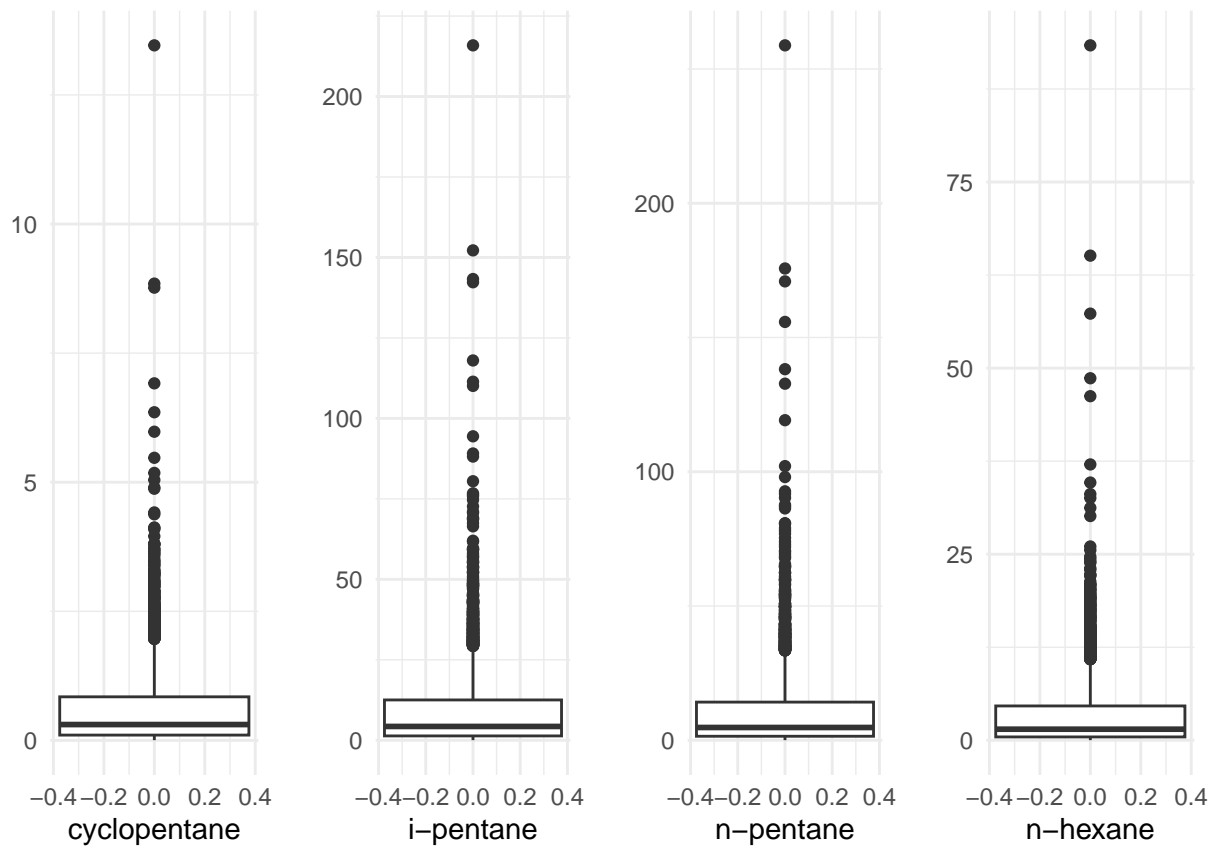
```

grid.arrange(get(paste0(vocs[5], '_boxplot')), get(paste0(vocs[6], '_boxplot')),
  get(paste0(vocs[7], '_boxplot')), get(paste0(vocs[8], '_boxplot')), nrow = 1)

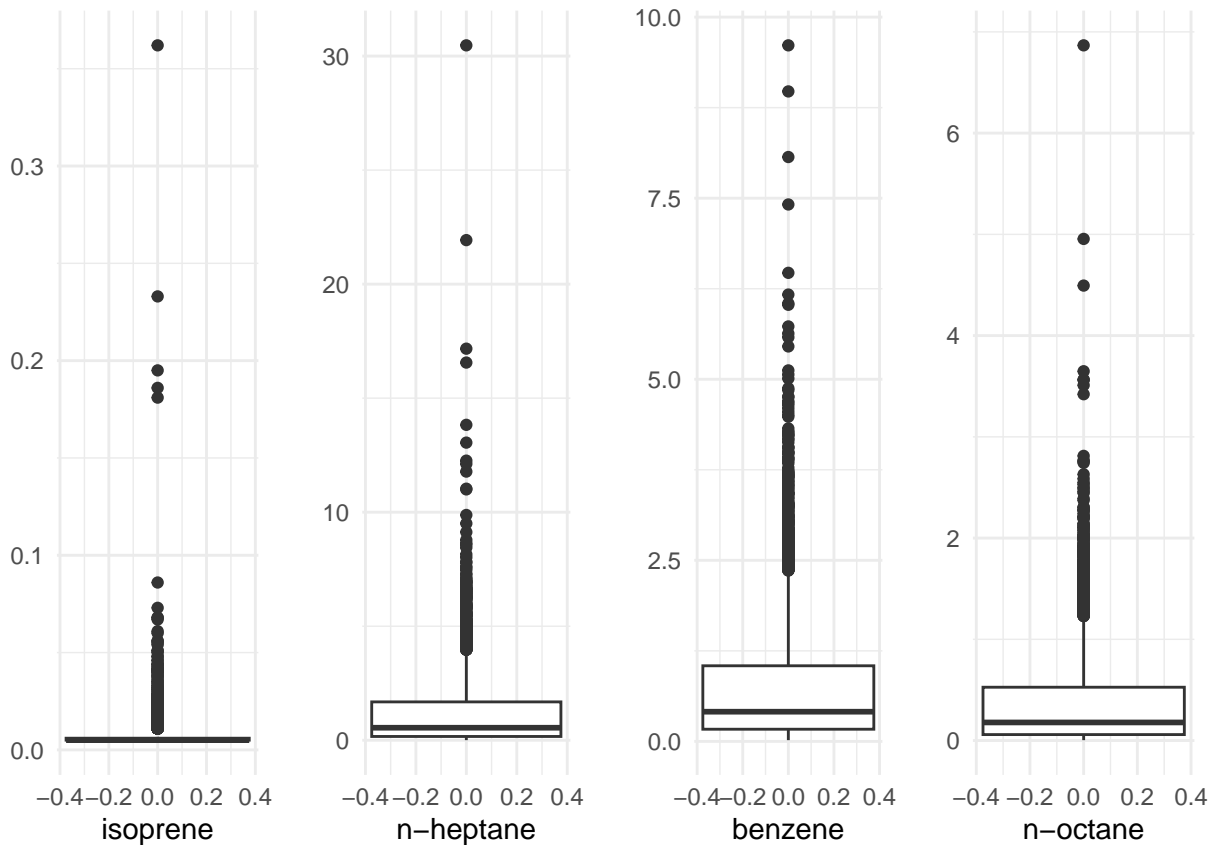
```



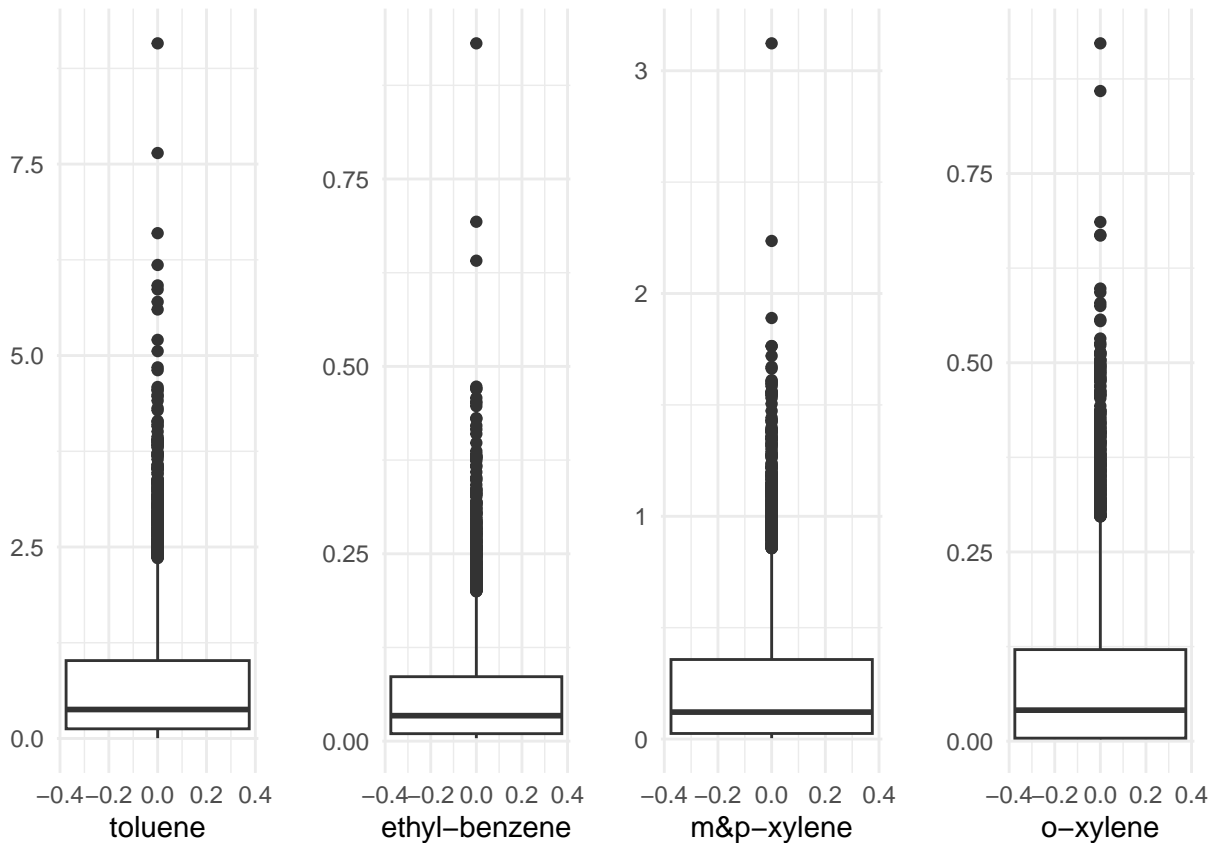
```
grid.arrange(get(paste0(vocs[9], '_boxplot')), get(paste0(vocs[10], '_boxplot')),
              get(paste0(vocs[11], '_boxplot')), get(paste0(vocs[12], '_boxplot')), nrow = 1)
```



```
grid.arrange(get(paste0(vocs[13], '_boxplot')), get(paste0(vocs[14], '_boxplot')),
              get(paste0(vocs[15], '_boxplot')), get(paste0(vocs[16], '_boxplot')), nrow = 1)
```

```
grid.arrange(get(paste0(vocs[17], '_boxplot')), get(paste0(vocs[18], '_boxplot')),
              get(paste0(vocs[19], '_boxplot')), get(paste0(vocs[20], '_boxplot')), nrow = 1)
```



Data preprocessing

```
# Define LOD for each chemical
LOD_non_voc <- c('ch4' = 0.9,
                 'co2' = 0.0433,
                 'co' = 40,
                 'h2s' = 0.4,
                 'so2' = 0.4,
                 'nox' = 0.05,
                 'o3' = 1)

LOD_voc_monthly <- read_csv('../data/LNM_VOC_LOD_Rounded.csv') %>% select(-1)
# extract the yearmonth from date variables
LOD_voc_monthly <- LOD_voc_monthly %>%
  mutate(yearmonth = strptime(as.POSIXct(start_date, format = '%Y-%m-%d %H:%M:%S', tz = 'UTC'), '%Y-%m-%d %H:%M:%S'))

LOD_voc_monthly <- LOD_voc_monthly %>%
  select(-c(start_date, end_date)) %>%
  select(!any_of(ends_with('half_ldl')))

colnames(LOD_voc_monthly) <- str_replace_all(names(LOD_voc_monthly), '_ldl', '')

LOD_voc_avg <- read_xlsx('../data/LNM_VOC_Uncertainties.xlsx', skip = 1)
LOD_voc_avg <- LOD_voc_avg %>%
  select(1, 4) %>%
```

```

rename('LOD' = 2, 'chemical' = 1) %>%
head(20)

# find the min for background-levels
background_levels <- sapply(hourly_full_nona, min)
background_levels

##          ch4          co2          co          h2s          so2
##    1928.000    411.300    61.630    0.200    0.200
##          nox          o3          ethane          ethene          propane
##      0.025      0.500      0.916      0.011      0.224
##    propene 1_3-butadiene    i-butane    n-butane    acetylene
##      0.009      0.007      0.035      0.090      0.019
## cyclopentane    i-pentane    n-pentane    n-hexane    isoprene
##      0.005      0.038      0.042      0.021      0.005
##    n-heptane    benzene    n-octane    toluene ethyl-benzene
##      0.004      0.017      0.004      0.004      0.004
##    m&p-xylene    o-xylene
##      0.004      0.004

get_info <- function(column) {
  N <- length(column)
  background <- quantile(column, 0)
  quantile1 <- quantile(column, 0.01)
  quantile99 <- quantile(column, 0.99)
  n_background <- sum(column == background)
  max <- max(column)
  return(c(N, quantile1, quantile99, max, background, n_background))
}

info_table <- hourly_full_nona %>%
  reframe(across(everything(), ~ get_info(.x)))

info_table <- info_table %>%
  mutate(rownames = c('N', '1st percentile', '99th percentile', 'Max', 'Background', '# Background')) %>%
  pivot_longer(-rownames) %>%
  pivot_wider(names_from = rownames, values_from = value)

knitr::kable(info_table)

```

name	N	1st percentile	99th percentile	Max	Background	# Background
ch4	4497	1963.40000	6318.81200	34010.900	1928.000	1
co2	4497	417.09000	457.87120	503.990	411.300	1
co	4497	84.90720	444.04320	2513.440	61.630	1
h2s	4497	0.20000	5.18084	27.700	0.200	777
so2	4497	0.20000	1.83896	8.578	0.200	3065
nox	4497	0.22700	92.01080	452.959	0.025	2
o3	4497	0.50000	72.11200	87.300	0.500	255
ethane	4497	1.80852	536.67200	2060.000	0.916	1
ethene	4497	0.01100	3.52212	16.970	0.011	163
propane	4497	0.81700	305.54000	1211.000	0.224	1
propene	4497	0.00900	0.70228	5.528	0.009	401
1_3-butadiene	4497	0.00700	0.05904	1.207	0.007	3126

name	N	1st percentile	99th percentile	Max	Background	Background	#
i-butane	4497	0.14496	63.53760	296.600	0.035		1
n-butane	4497	0.34792	171.37600	536.900	0.090		1
acetylene	4497	0.04900	2.66204	8.471	0.019		1
cyclopentane	4497	0.00500	3.12356	13.460	0.005		96
i-pentane	4497	0.10396	51.02080	215.900	0.038		1
n-pentane	4497	0.10300	58.10280	258.800	0.042		1
n-hexane	4497	0.04196	18.32640	93.360	0.021		2
isoprene	4497	0.00500	0.03204	0.362	0.005		2815
n-heptane	4497	0.01500	6.58924	30.470	0.004		5
benzene	4497	0.02700	3.87512	9.610	0.017		3
n-octane	4497	0.00400	2.01452	6.867	0.004		100
toluene	4497	0.01296	3.53640	9.077	0.004		11
ethyl-benzene	4497	0.00400	0.31604	0.931	0.004		898
m&p-xylene	4497	0.00400	1.31824	3.123	0.004		814
o-xylene	4497	0.00400	0.45912	0.922	0.004		1266

```

#adjustments that were made according to paper
#William: I'm guessing this refers to Gunnar's paper section 2.2 and Guha 3.3
adjusting_neg_bg_from_lod <- function(chemical, LOD, background, hourly_data){
  # get min and max
  min_value <- min(hourly_data[chemical], na.rm = TRUE)
  max_value <- max(hourly_data[chemical], na.rm = TRUE)
  # if min less than double LOD or max > 100 times LOD
  # adjust to -100 (for entire column???)
  if (min_value < 2 * LOD & max_value > 100 * LOD ){
    return (0)
  }
  return (background)
}

# Check if background is negligible for non voc
# merge background and LOD
background_lod_non_voc <- tibble(chemical = non_vocs,
                                LOD = LOD_non_voc,
                                background = unname(background_levels[non_vocs]))
adjusted_background_non_voc <- background_lod_non_voc %>%
  rowwise() %>%
  mutate(min = min(hourly_full_nona[chemical], na.rm = TRUE),
         LODx2 = 2 * LOD,
         criterion1 = min(hourly_full_nona[chemical], na.rm = TRUE) < 2 * LOD,
         max = max(hourly_full_nona[chemical], na.rm = TRUE),
         LODx100 = 100 * LOD,
         criterion2 = max(hourly_full_nona[chemical], na.rm = TRUE) > 100 * LOD,
         adjusted_background = adjusting_neg_bg_from_lod(chemical, LOD, background, hourly_full_nona))

# Check if background is negligible for voc
# merge background and LOD
background_lod_voc <- LOD_voc_avg %>%
  left_join(tibble(chemical = setdiff(names(background_levels), non_vocs),
                  background = background_levels[setdiff(names(background_levels), non_vocs)]))

## Joining with `by = join_by(chemical)`

```

```

adjusted_background_voc <- background_lod_voc %>%
  rowwise() %>%
  mutate(min = min(hourly_full_nona[chemical], na.rm = TRUE),
         LODx2 = 2 * LOD,
         criterion1 = min(hourly_full_nona[chemical], na.rm = TRUE) < 2 * LOD,
         max = max(hourly_full_nona[chemical], na.rm = TRUE),
         LODx100 = 100 * LOD,
         criterion2 = max(hourly_full_nona[chemical], na.rm = TRUE) > 100 * LOD,
         adjusted_background = adjusting_neg_bg_from_lod(chemical, LOD, background, hourly_full_nona))

# So now we have the adjusted background concentrations
subtract_adj_bg <- function(column, chemical) {
  print(chemical)
  result <-
  return (result)
}
hourly_nona_bgrm <- hourly_full_nona %>%
  mutate(across(adjusted_background_non_voc$chemical, ~ .x - adjusted_background_non_voc$adjusted_backg
hourly_nona_bgrm <- hourly_nona_bgrm %>%
  mutate(across(adjusted_background_voc$chemical, ~ .x - adjusted_background_voc$adjusted_background[a

# look at zero values
colSums(hourly_nona_bgrm == 0)

##          ch4          co2          co          h2s          so2
##          1           1           1          777         3065
##         nox          o3         ethane         ethene         propane
##          0          255           1           0           1
##        propene 1_3-butadiene        i-butane        n-butane        acetylene
##          0          3126           1           1           0
##   cyclopentane        i-pentane        n-pentane        n-hexane        isoprene
##          0           1           1           2         2815
##        n-heptane        benzene        n-octane        toluene ethyl-benzene
##          0           0           0           0           0
##        m&p-xylene        o-xylene
##          0           0

# replace negative values with random values between 0 and 0.5*LOD
set.seed(123)
replace_zero_with_random <- function(column, name, LOD_df){
  LOD <- LOD_df$LOD[LOD_df$chemical == name]
  column <- if_else(column == 0, round(runif(length(column), 0, 0.5 * LOD), 3), column)
  return (column)
}

hourly_nona_bgrm_zerorepl <- hourly_nona_bgrm %>%
  mutate(across(adjusted_background_non_voc$chemical, ~ replace_zero_with_random(.x, cur_column(), adju

hourly_nona_bgrm_zerorepl <- hourly_nona_bgrm_zerorepl %>%
  mutate(across(adjusted_background_voc$chemical, ~ replace_zero_with_random(.x, cur_column(), adjusted.

```

Normalize the non-vocs

```

#normalizing function
normalize_column <- function(column){
  background <- quantile(column, 0)
  max <- quantile(column, 1) # this could be adjusted
  return ((column - background)/(max - background))
}

# normalize all
hourly_nona_bgrm_zerorepl_norm <- as_tibble(sapply(as.list(hourly_nona_bgrm_zerorepl), normalize_column))
summary(hourly_nona_bgrm_zerorepl_norm)

```

```

##          ch4              co2              co              h2s
## Min.      :0.000000    Min.      :0.0000    Min.      :0.00000    Min.      :0.00000
## 1st Qu.:0.005697    1st Qu.:0.1397    1st Qu.:0.02347    1st Qu.:0.01022
## Median :0.014615    Median :0.1826    Median :0.03663    Median :0.02338
## Mean     :0.027164    Mean     :0.1998    Mean     :0.04550    Mean     :0.03517
## 3rd Qu.:0.037362    3rd Qu.:0.2415    3rd Qu.:0.05734    3rd Qu.:0.04564
## Max.      :1.000000    Max.      :1.0000    Max.      :1.00000    Max.      :1.00000
##          so2              nox              o3              ethane
## Min.      :0.000000    Min.      :0.000000    Min.      :0.0000    Min.      :0.000000
## 1st Qu.:0.007997    1st Qu.:0.006515    1st Qu.:0.1117    1st Qu.:0.008171
## Median :0.015756    Median :0.020376    Median :0.2960    Median :0.026203
## Mean     :0.026295    Mean     :0.036923    Mean     :0.3080    Mean     :0.051422
## 3rd Qu.:0.023633    3rd Qu.:0.050500    3rd Qu.:0.4735    3rd Qu.:0.075895
## Max.      :1.000000    Max.      :1.000000    Max.      :1.0000    Max.      :1.000000
##          ethene          propane          propene          1_3-butadiene
## Min.      :0.00000    Min.      :0.000000    Min.      :0.000000    Min.      :0.000000
## 1st Qu.:0.01303    1st Qu.:0.009005    1st Qu.:0.005798    1st Qu.:0.001667
## Median :0.03615    Median :0.028067    Median :0.018663    Median :0.004167
## Mean     :0.05116    Mean     :0.054283    Mean     :0.028932    Mean     :0.007500
## 3rd Qu.:0.07324    3rd Qu.:0.081075    3rd Qu.:0.043305    3rd Qu.:0.007500
## Max.      :1.00000    Max.      :1.000000    Max.      :1.000000    Max.      :1.000000
##          i-butane          n-butane          acetylene          cyclopentane
## Min.      :0.000000    Min.      :0.000000    Min.      :0.00000    Min.      :0.000000
## 1st Qu.:0.005999    1st Qu.:0.008556    1st Qu.:0.02769    1st Qu.:0.007284
## Median :0.019042    Median :0.027302    Median :0.05265    Median :0.022445
## Mean     :0.038815    Mean     :0.055538    Mean     :0.07600    Mean     :0.043917
## 3rd Qu.:0.054019    3rd Qu.:0.078140    3rd Qu.:0.10400    3rd Qu.:0.062356
## Max.      :1.000000    Max.      :1.000000    Max.      :1.00000    Max.      :1.000000
##          i-pentane          n-pentane          n-hexane          isoprene
## Min.      :0.000000    Min.      :0.000000    Min.      :0.00000    Min.      :0.000000
## 1st Qu.:0.006092    1st Qu.:0.005596    1st Qu.:0.00465    1st Qu.:0.002801
## Median :0.019717    Median :0.018229    Median :0.01578    Median :0.005602
## Mean     :0.041448    Mean     :0.039184    Mean     :0.03511    Mean     :0.010377
## 3rd Qu.:0.057853    3rd Qu.:0.054789    3rd Qu.:0.04925    3rd Qu.:0.011204
## Max.      :1.000000    Max.      :1.000000    Max.      :1.00000    Max.      :1.000000
##          n-heptane          benzene          n-octane          toluene
## Min.      :0.000000    Min.      :0.00000    Min.      :0.000000    Min.      :0.00000
## 1st Qu.:0.005317    1st Qu.:0.01574    1st Qu.:0.008014    1st Qu.:0.01345
## Median :0.017889    Median :0.04097    Median :0.025499    Median :0.04122
## Mean     :0.039271    Mean     :0.07624    Mean     :0.054094    Mean     :0.07760
## 3rd Qu.:0.055078    3rd Qu.:0.10706    3rd Qu.:0.076206    3rd Qu.:0.11165
## Max.      :1.000000    Max.      :1.00000    Max.      :1.000000    Max.      :1.00000
##          ethyl-benzene          m&p-xylene          o-xylene

```

```
## Min.      :0.000000   Min.      :0.000000   Min.      :0.000000
## 1st Qu.:0.006472   1st Qu.:0.006733   1st Qu.:0.000000
## Median :0.032363   Median :0.037512   Median :0.04031
## Mean    :0.061284   Mean    :0.076834   Mean    :0.08577
## 3rd Qu.:0.088457   3rd Qu.:0.113177   3rd Qu.:0.12745
## Max.    :1.000000   Max.    :1.000000   Max.    :1.00000
```

Combine and Transpose

```
normalized_matrix <- as.matrix(hourly_nona_bgrm_zerorepl_norm) #important: using the normalized VOCs for

# Transpose <- cbind(Normalized_Data, Merged_VOCs)
# rownames(Transpose) <- as.character(Transpose[,1]) # I'm not able to run this line, but it shouldn't
# transpose_normalized_matrix <- t(as.matrix(normalized_matrix))

number_row<- dim(normalized_matrix)[1] #store number of rows (used for checking)
number_column<- dim(normalized_matrix)[2] #store number of columns
```

NMF section

```
# compute weight matrix (uncertainties)
# Based on the Guha paper
# next comment is from the other nmf R file
weight_matrix <- matrix(0, nrow = nrow(normalized_matrix), ncol = ncol(normalized_matrix))
LOD_merged <- tibble(chemical = c(adjusted_background_non_voc$chemical, adjusted_background_voc$chemical),
                        LOD = c(adjusted_background_non_voc$LOD, adjusted_background_voc$LOD))

LOD_merged <- tibble(chemical = names(hourly_nona_bgrm_zerorepl_norm)) %>%
  left_join(LOD_merged)

## Joining with `by = join_by(chemical)`

# creating uncertainty Matrix
for (i in 1:number_row) {
  for (j in 1:number_column) {
    xij <- normalized_matrix[i, j]
    LOD <- LOD_merged$LOD[[j]]
    # Get LOD value for this row
    if (j == 1) {
      # based on equation 6, we sqrt ch4 (at column = 1) and times by 1
      weight_matrix[i, j] <- sqrt(xij)
    } else if (j == 2) {
      # 0.25 for co2
      weight_matrix[i, j] <- 0.25 * sqrt(xij)
    } else if (j == 3) {
      # 0.5 for CO
      weight_matrix[i, j] <- 0.5 * sqrt(xij)
    } else if (xij <= LOD) {
      weight_matrix[i, j] <- 2 * LOD # equation 5a) in reference paper
    } else {
      weight_matrix[i, j] <- sqrt(((0.1 * xij)**2 + LOD**2)) #equation 5c) in reference paper
    }
  }
}
```

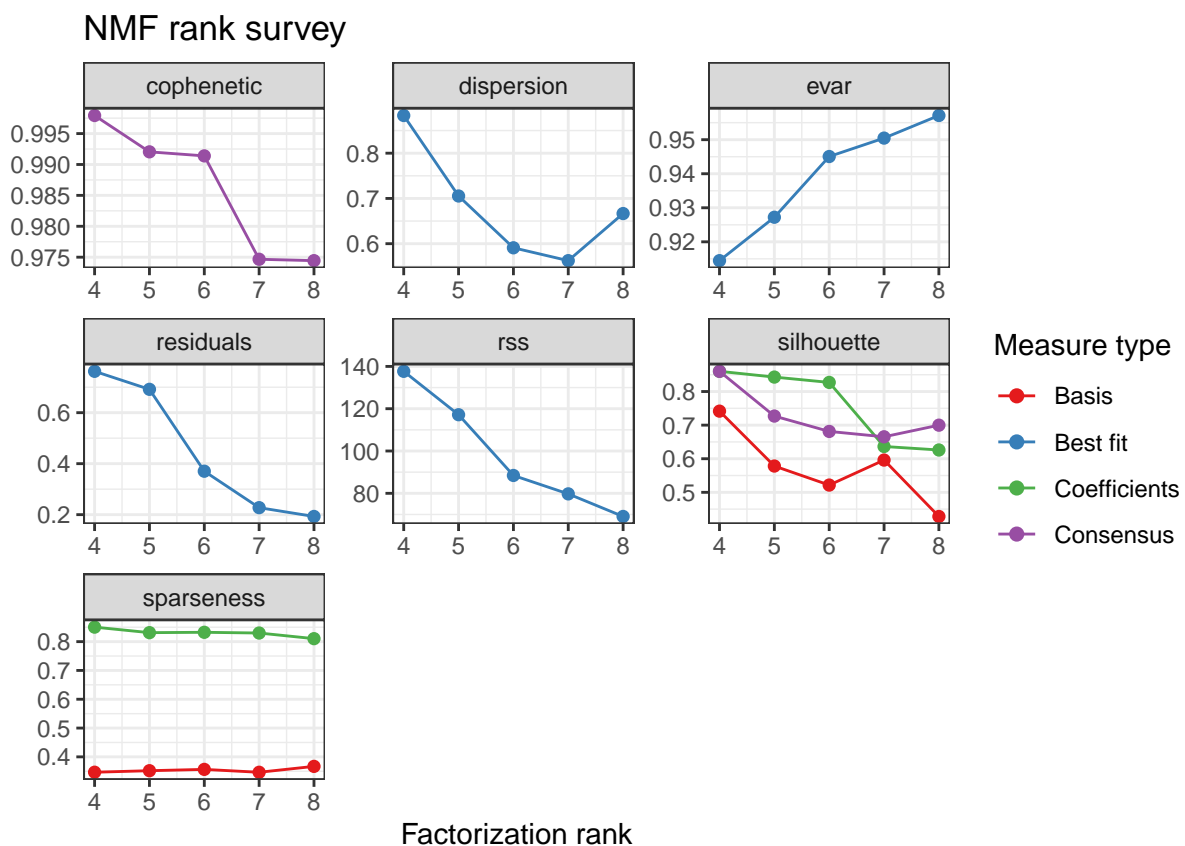
```

# set a seed for nmf
# set.seed(123)
# #function below used to estimate the optimal rank and will be used in the nmf() function.
# # takes around 20-30 mins to run
# estimate_rank <- nmfEstimateRank(normalized_matrix, 4:8, method = "ls-nmf", weight = weight_matrix, 3)
# # # changing the range of rank to 2:20 from 4:20
# saveRDS(estimate_rank, 'estimate_rank.rds')

estimate_rank <- readRDS('estimate_rank.rds')
measures <- estimate_rank$measures
fit <- estimate_rank$fit
consensus <- estimate_rank$consensus

# plots the NMF rank survey
plot(estimate_rank)

```



```

# fitting the optimal rank based on the above plots
# the choice of the optimal rank needs to be discussed
output <- nmf(normalized_matrix, rank = 4, weight = weight_matrix, method = "ls-nmf")
W <- basis(output)
H <- coef(output)

```

Source contributions

```

# Convert H to a data frame for ggplot
H_df <- as.data.frame(H)

```



```

# Add a column for component
H_df$Component <- names(as.data.frame(W))

# Reshape data to long format
H_long <- pivot_longer(H_df, cols = -Component, names_to = "Chemical", values_to = "Contribution")

# Define the desired order of chemicals
desired_order <- c(
  # NMHCs - Alkanes
  "ethane", "propane", "i-butane", "n-butane", "i-pentane", "n-pentane",
  "n-hexane", "cyclopentane", "n-heptane", "n-octane",

  # NMHCs - Alkenes
  "ethene", "propene", "1_3-butadiene", 'isoprene',

  # NMHCs - Alkynes
  "acetylene",

  # NMHCs - Aromatics
  "benzene", "toluene", "ethyl-benzene", "o-xylene", "m&p-xylene",

  # Inorganic Gases - CO and CO2
  "co", "co2",

  # Nitrogen Oxides (NOx)
  "nox",

  # Sulfur Compounds
  "h2s", "so2",

  # Ozone (if included)
  "o3",

  # Methane
  "ch4"
)

get_component_plot <- function(data, component, title) {
  component_data <- subset(data, Component == component)
  component_data <- component_data %>%
    mutate(Chemical = factor(Chemical, levels = desired_order))

  plot <- ggplot(component_data, aes(x = Chemical, y = Contribution)) +
    geom_bar(stat = "identity", position = "dodge", fill = "orange") +
    theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
    geom_text(aes(label = sprintf("%.2f", round(Contribution, 2))), color = "blue", size = 3, n
    labs(x = "Chemical", y = "Contribution", title = title)+
    theme(
      text = element_text(size = 14), # Base text size for all text elements
      axis.title = element_text(size = 16), # Size of axis titles
      axis.text = element_text(size = 12), # Size of axis text (tick labels)
      plot.title = element_text(size = 18) # Size of the plot title
    )
}

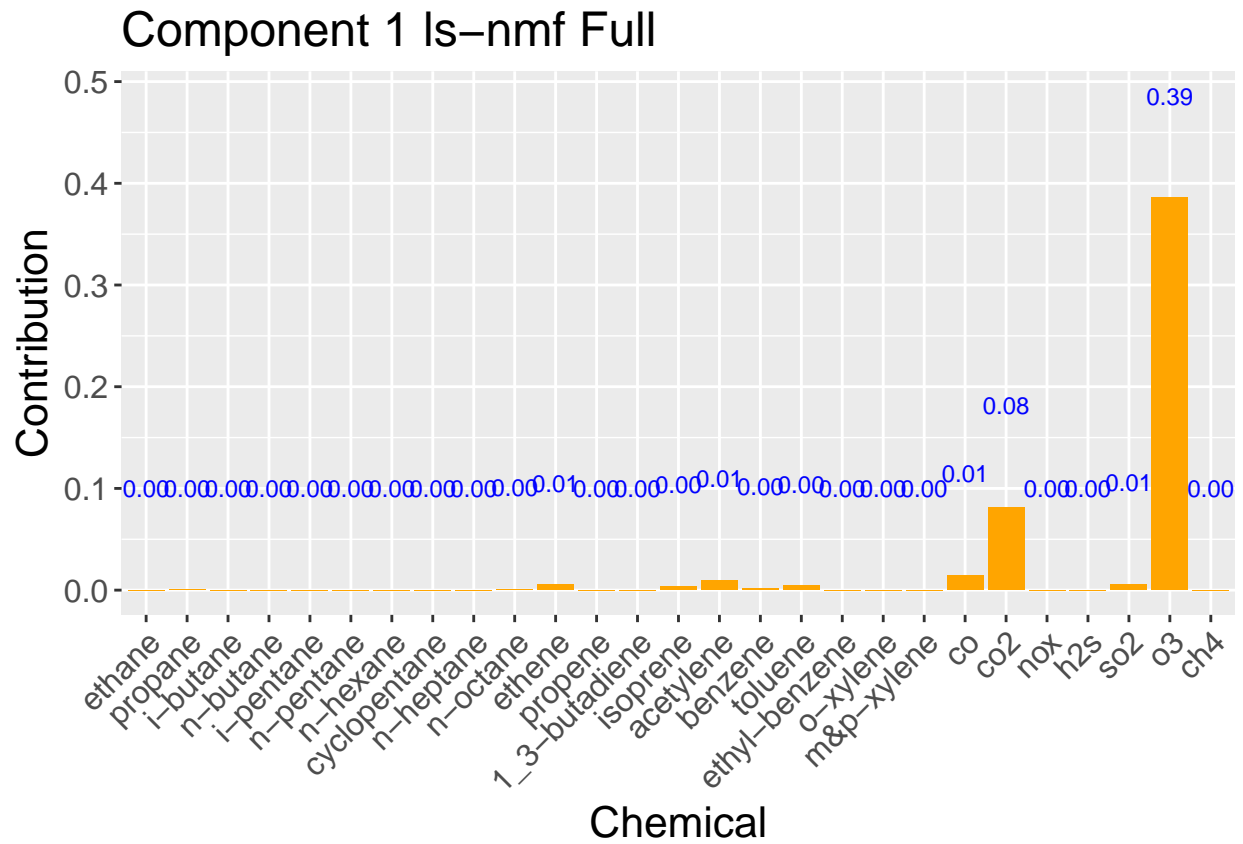
```

```

    return(plot)
  }

nmfplt_1_ls <- get_component_plot(H_long, 'V1', 'Component 1 ls-nmf Full')
nmfplt_1_ls

```

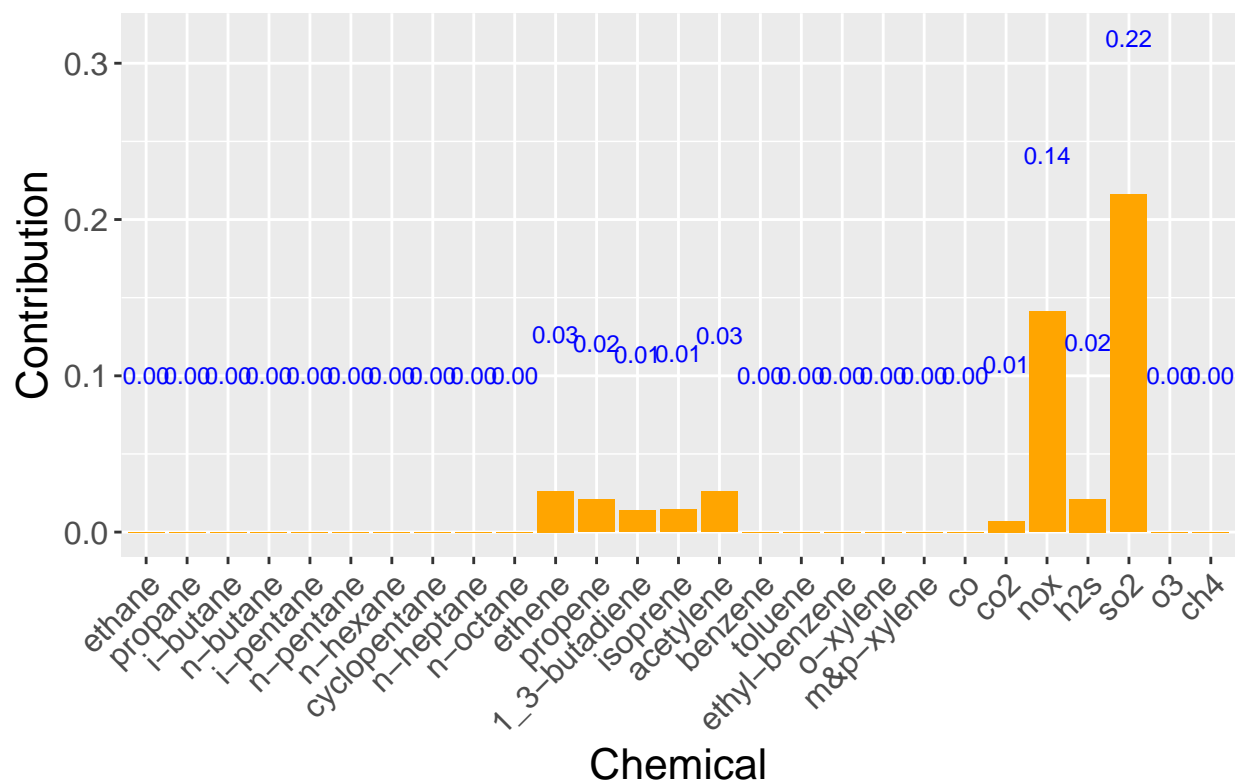


```

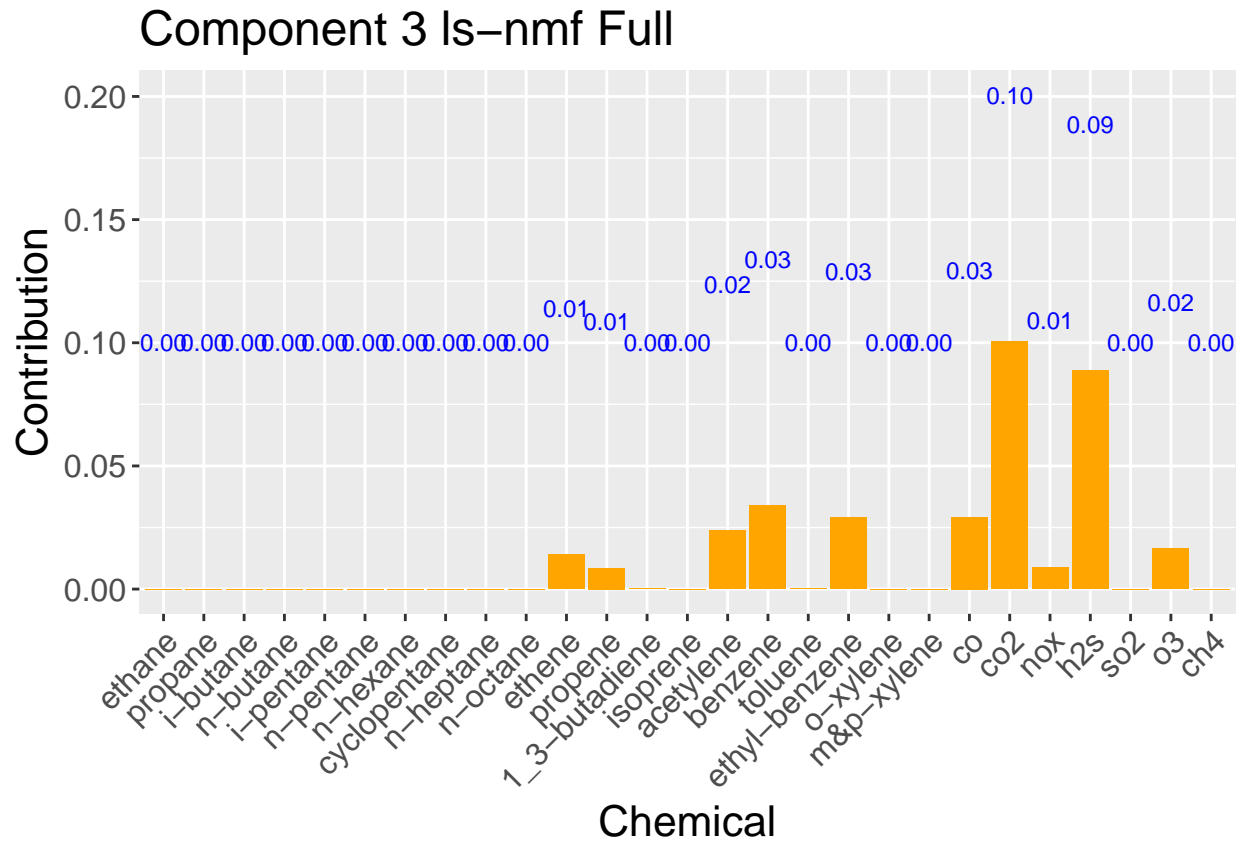
nmfplt_2_ls <- get_component_plot(H_long, 'V2', 'Component 2 ls-nmf Full')
nmfplt_2_ls

```

Component 2 ls-nmf Full

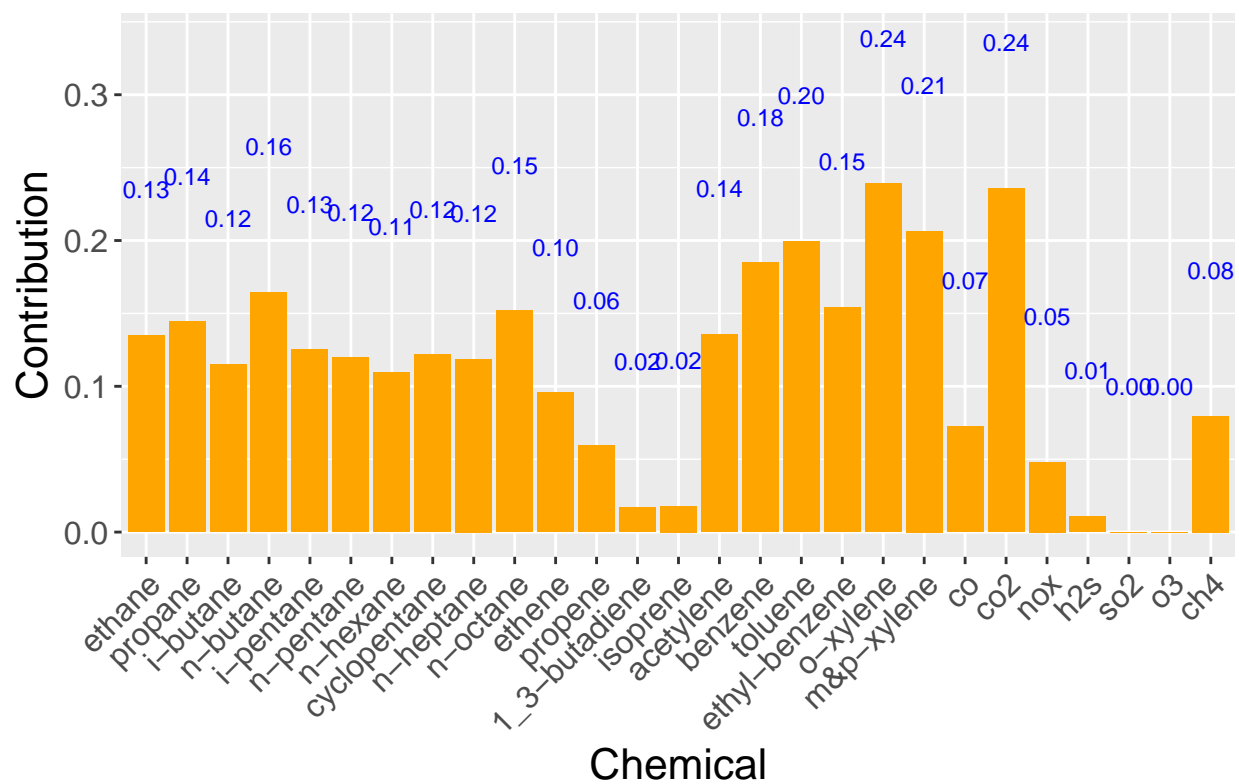


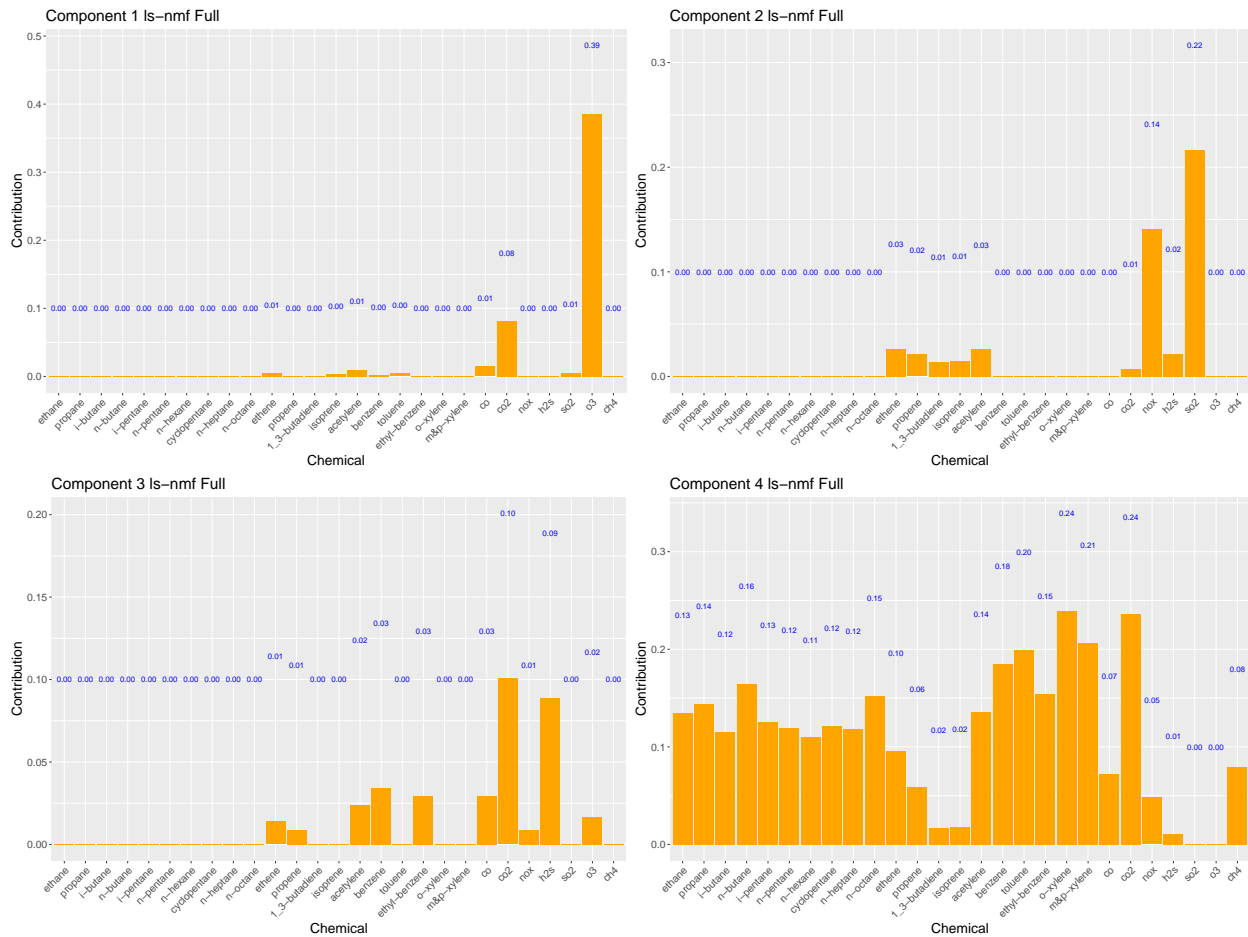
```
nmfplt_3_ls <- get_component_plot(H_long, 'V3', 'Component 3 ls-nmf Full')
nmfplt_3_ls
```



```
nmfplt_4_ls <- get_component_plot(H_long, 'V4', 'Component 4 ls-nmf Full')
nmfplt_4_ls
```

Component 4 ls-nmf Full





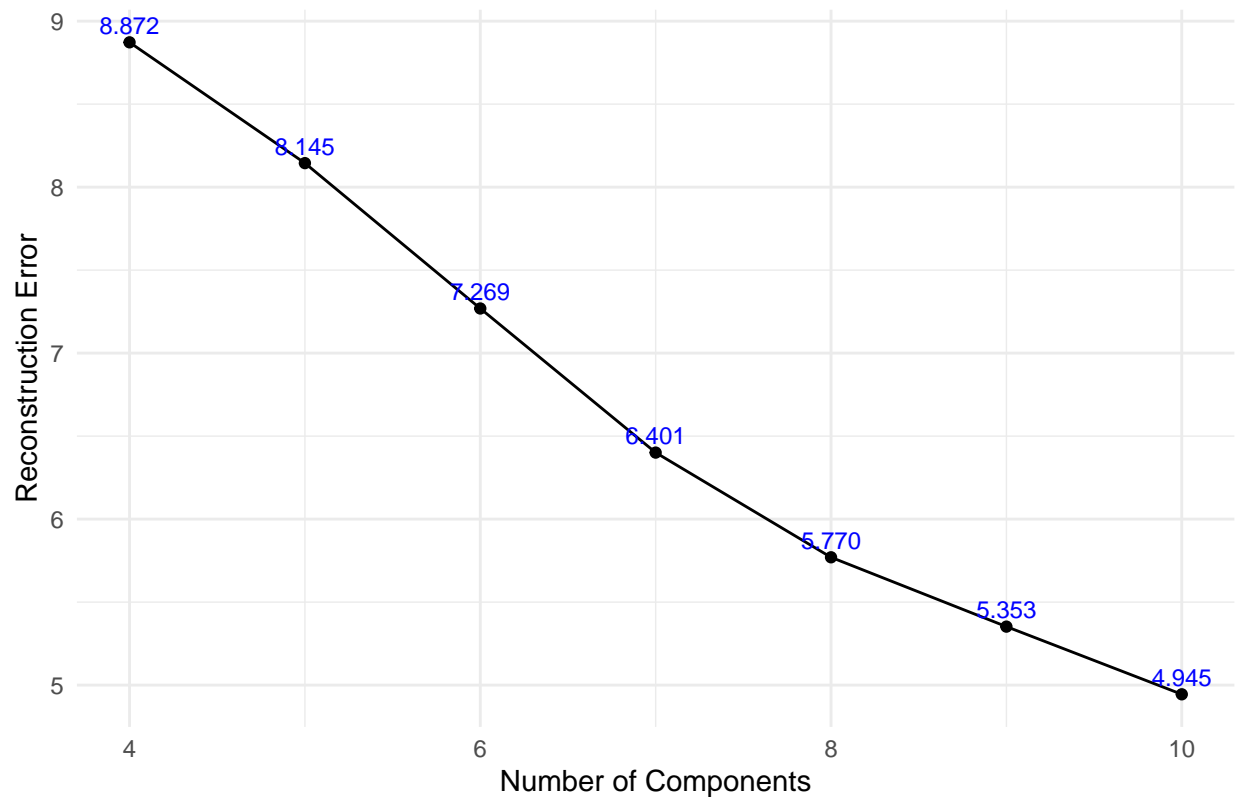
NMF - Eva

```
# Try Eva's approach
components <- 4:10
errors <- numeric(length(components) - 4)

# Loop over the number of components
# for (n in components) {
#   nmf_result <- nmf(normalized_matrix, rank = n, method = "KL", seed='nndsud')
#   reconstruction <- basis(nmf_result) %*% coef(nmf_result)
#   error <- norm(normalized_matrix - reconstruction, type = "F")
#   errors[n-3] <- error
#   print(paste0('Completed ', n - 3, ' out of 7'))
# }
#
# saveRDS(errors, 'errors_norm.rds')

errors <- readRDS('errors_norm.rds')
```

NMF Reconstruction Error vs. Number of Components



```
## [1] 8.872266
```

```
## Warning in sqrt(S[i] * termp) * uup: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termp) * vvp: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

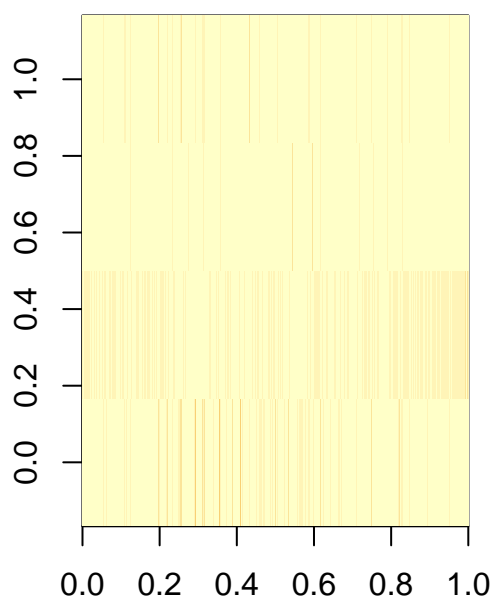
```
## Warning in sqrt(S[i] * termp) * uup: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termp) * vvp: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

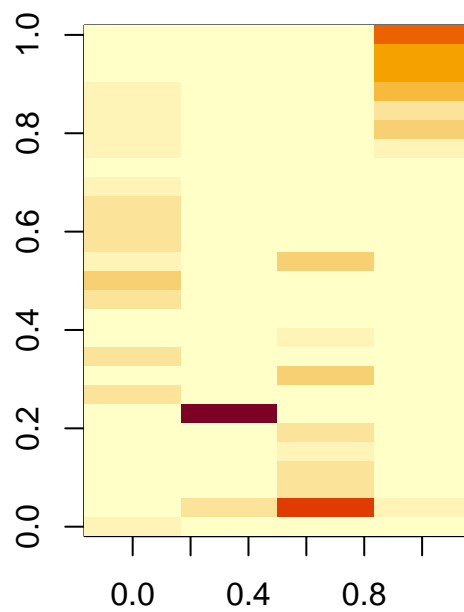
```
## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

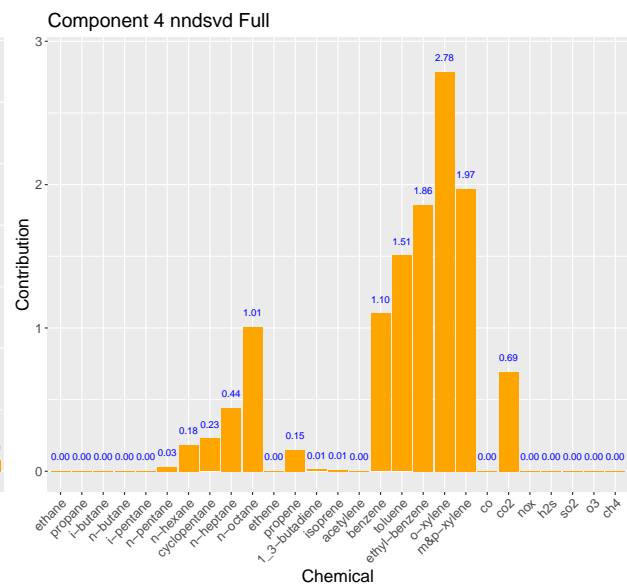
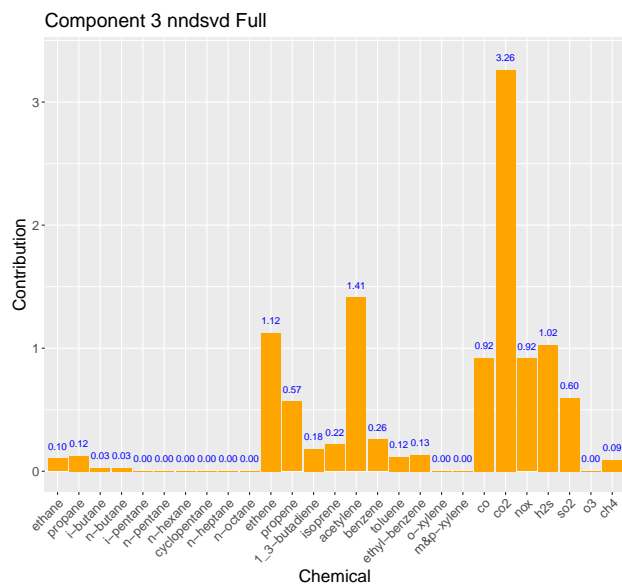
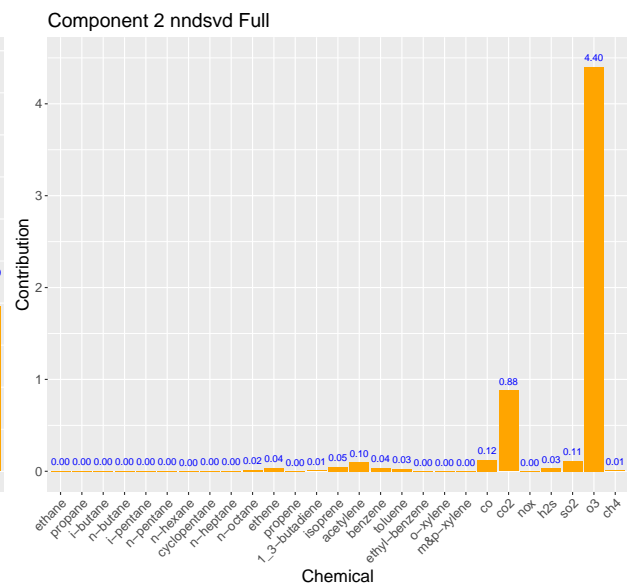
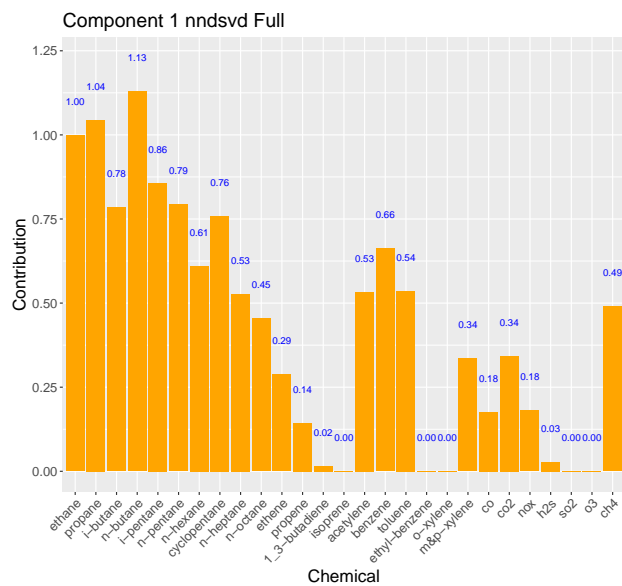
```
## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

Basis Matrix (W)



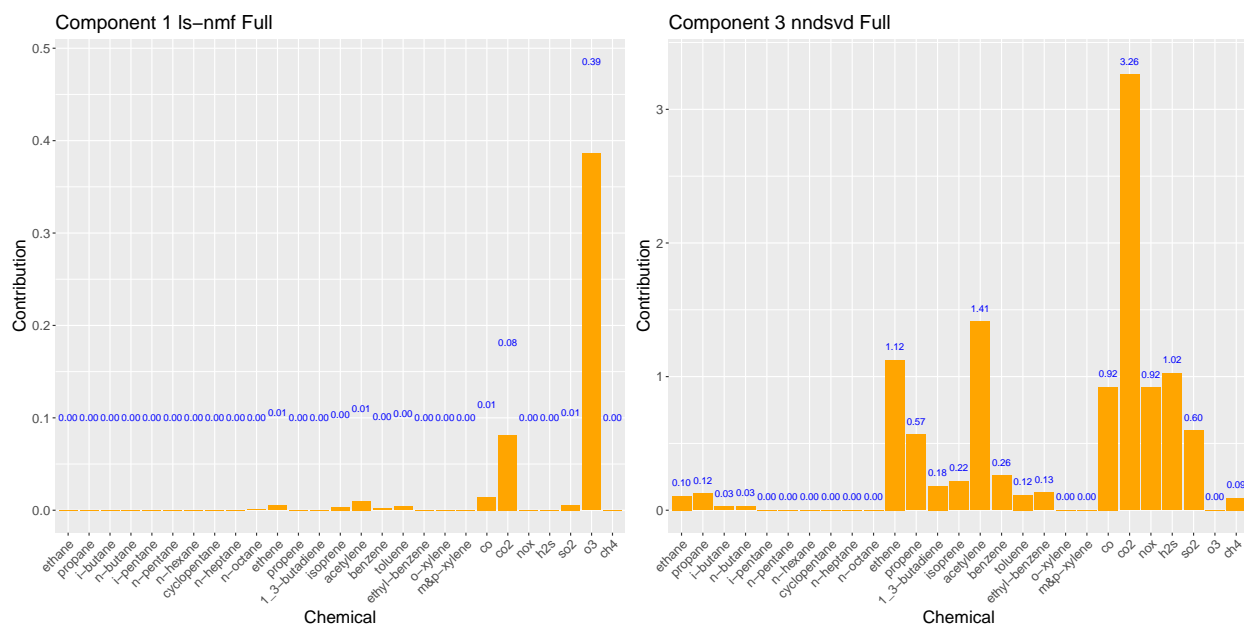
Coefficient Matrix (H)



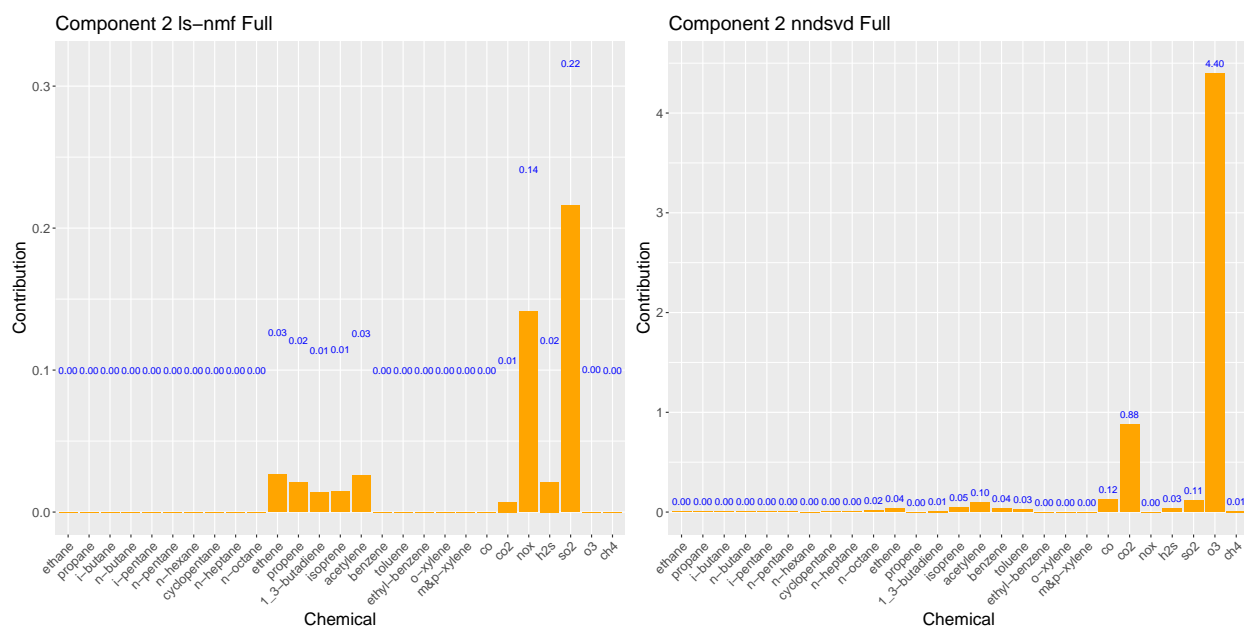


Method comparisons

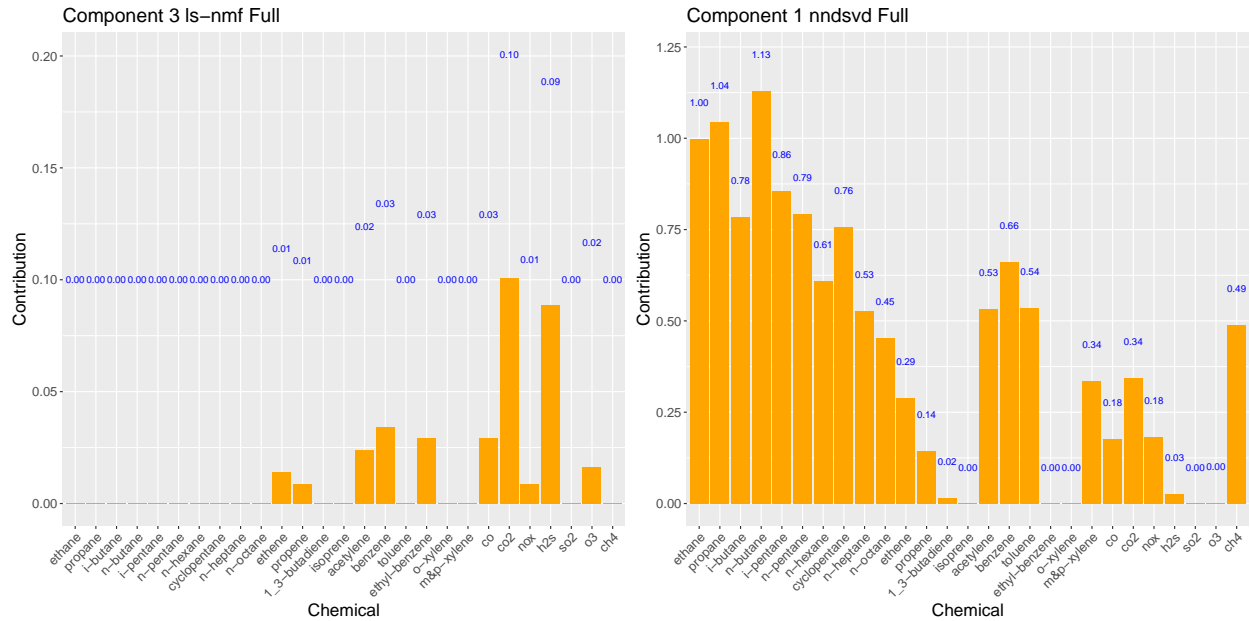
```
grid.arrange(nmfplt_1_ls, nmfplt_3_svd, ncol = 2)
```



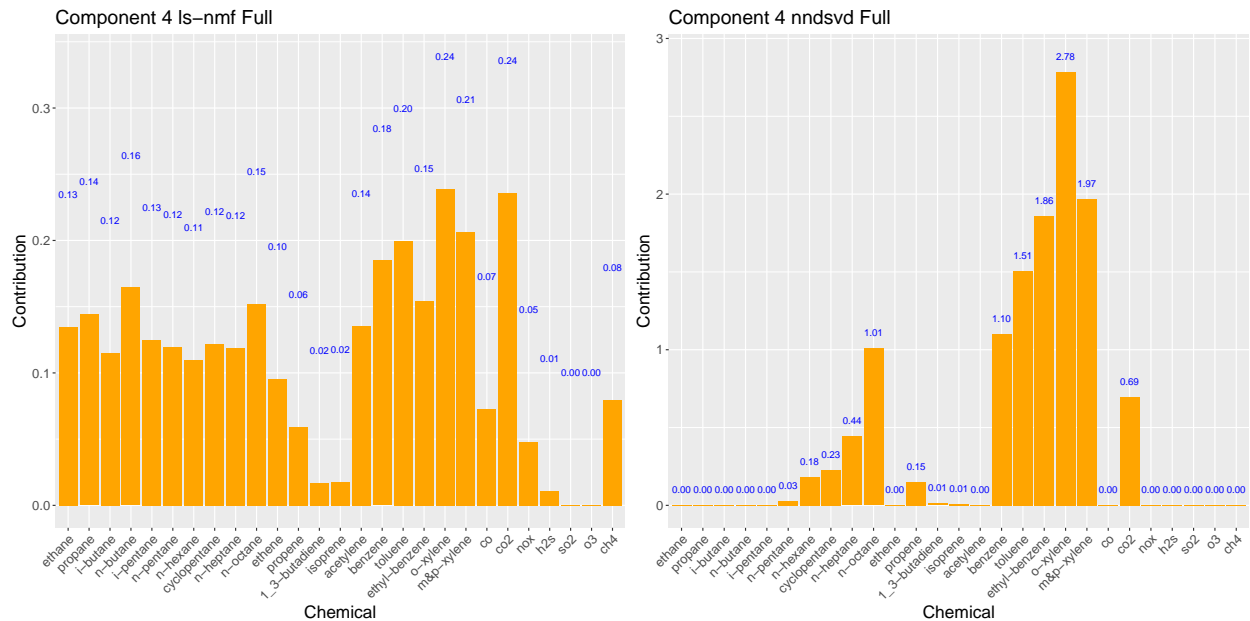
```
grid.arrange(nmfplt_2_ls, nmfplt_2_svd, ncol = 2)
```



```
grid.arrange(nmfplt_3_ls, nmfplt_1_svd, ncol = 2)
```



```
grid.arrange(nmfplt_4_ls, nmfplt_4_svd, ncol = 2)
```



Remove Ozone

4 Components

```
normalized_matrix_less_o3 <- normalized_matrix[,setdiff(colnames(normalized_matrix), "o3")]
```

```
nmf_result_4c_less_o3 <- nmf(normalized_matrix_less_o3, rank = 4, method = "KL", seed='nndsvd')
```

```
## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

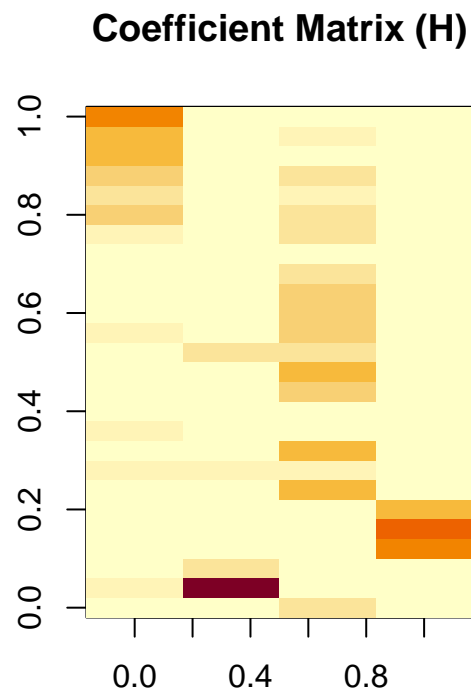
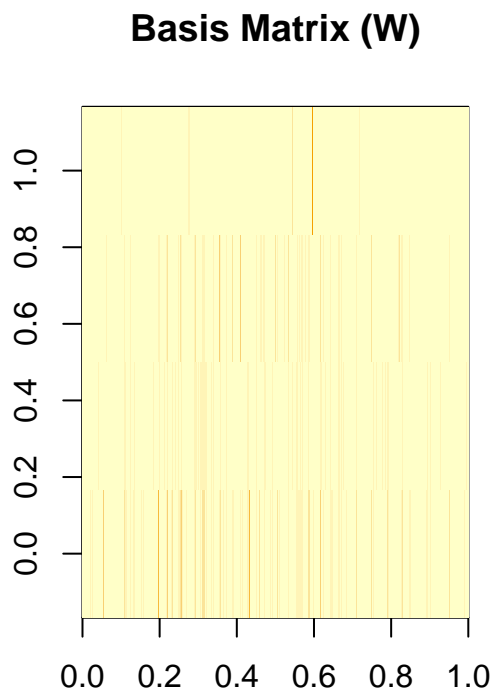
## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

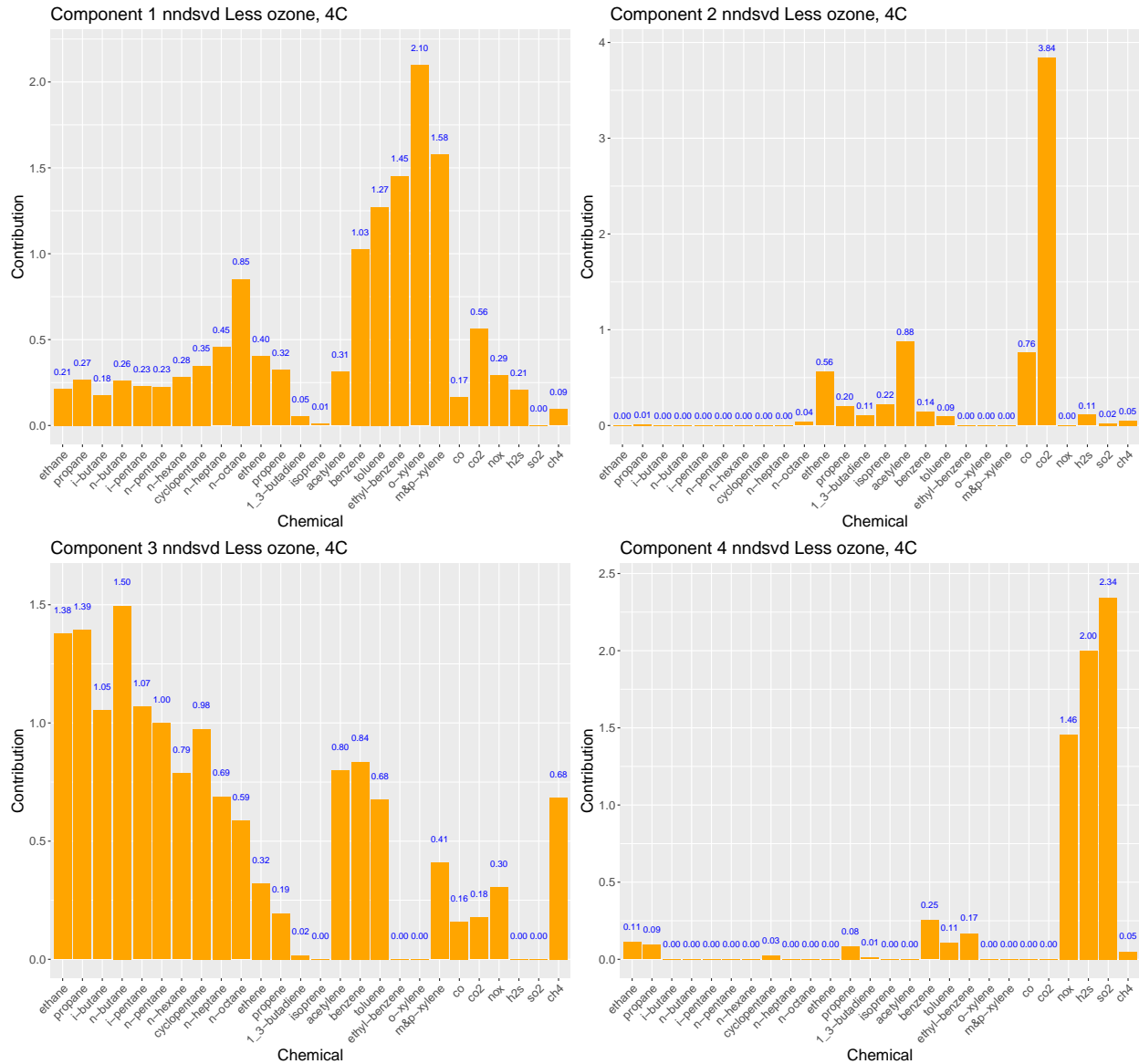
## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

basis_matrix_4c_less_o3 <- basis(nmf_result_4c_less_o3)
coef_matrix_4c_less_o3 <- coef(nmf_result_4c_less_o3)

par(mfrow = c(1, 2))
image(basis_matrix_4c_less_o3, main = "Basis Matrix (W)")
image(coef_matrix_4c_less_o3, main = "Coefficient Matrix (H)")
```





5 Components

```
nmf_result_5c_less_o3 <- nmf(normalized_matrix_less_o3, rank = 5, method = "KL", seed='nndsvd')
```

```
## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
```

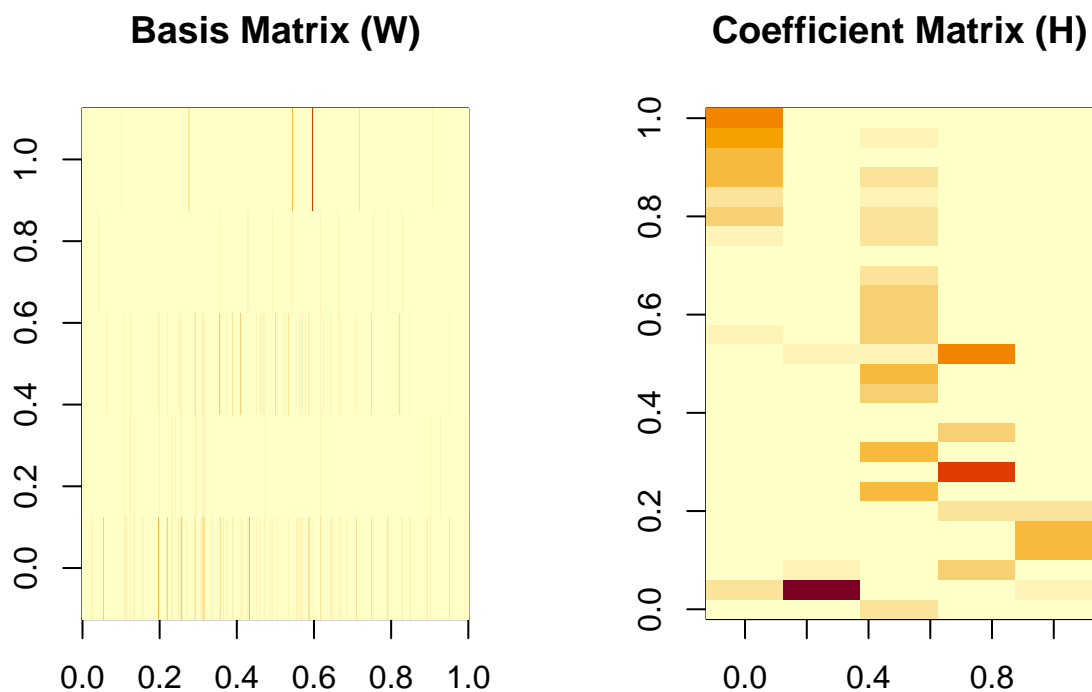
```
## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

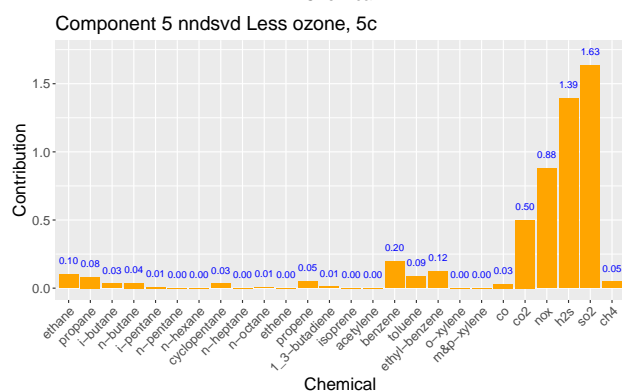
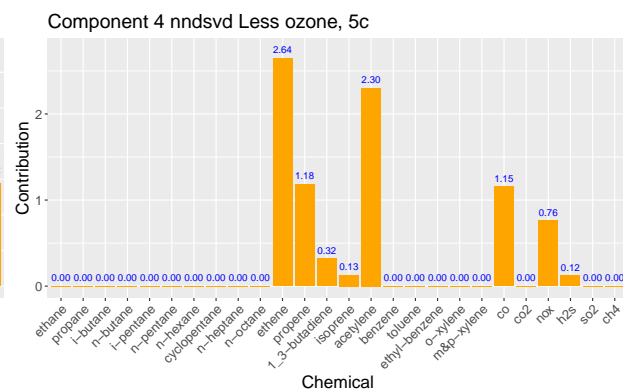
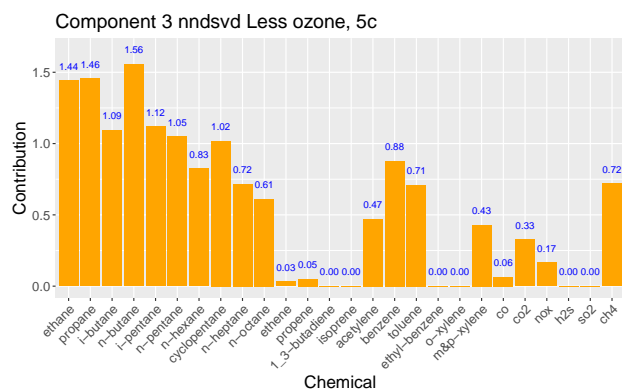
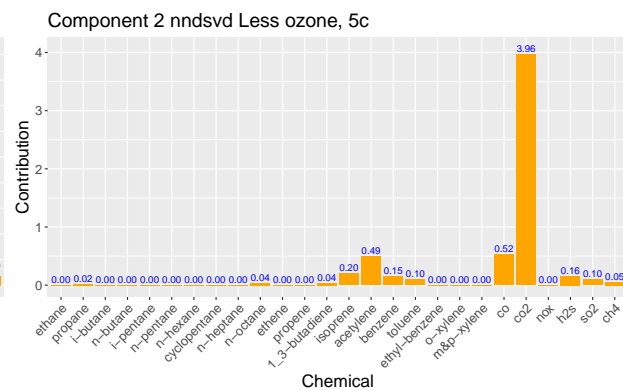
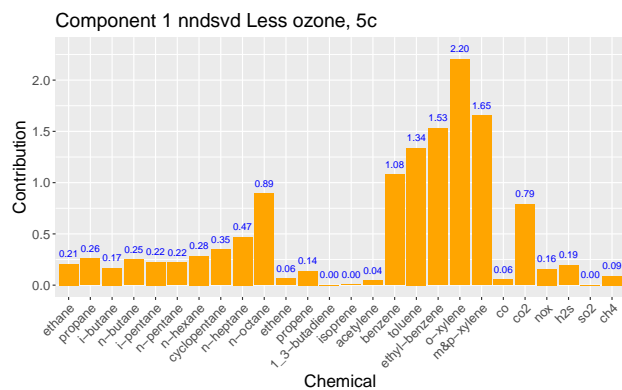
## Warning in sqrt(S[i] * termp) * uup: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

## Warning in sqrt(S[i] * termp) * vvp: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

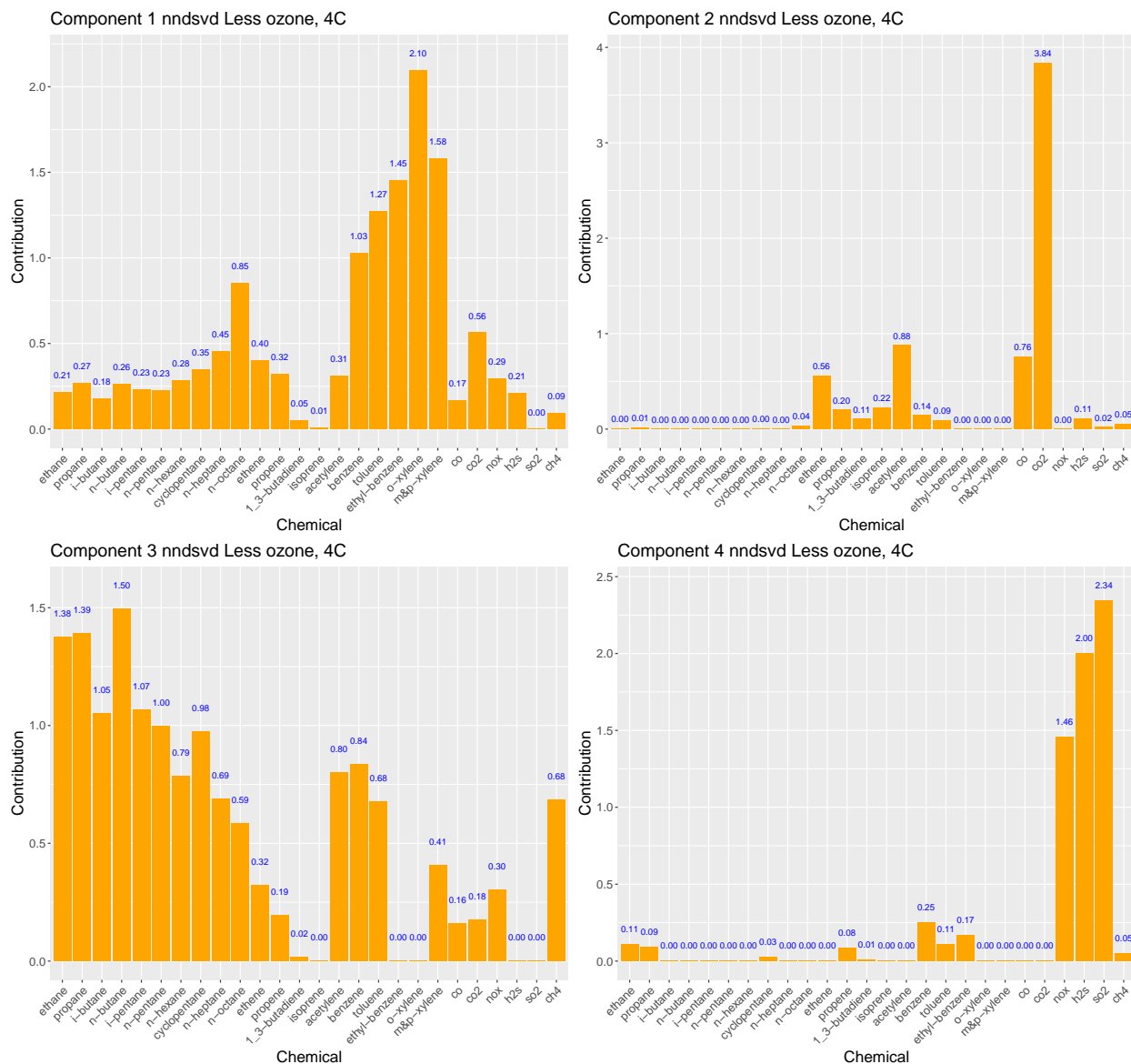
basis_matrix_5c_less_o3 <- basis(nmf_result_5c_less_o3)
coef_matrix_5c_less_o3 <- coef(nmf_result_5c_less_o3)

par(mfrow = c(1, 2))
image(basis_matrix_5c_less_o3, main = "Basis Matrix (W)")
image(coef_matrix_5c_less_o3, main = "Coefficient Matrix (H)")
```





Compare to 4 components



Remove Ozone + chemicals with more than 500+ background values

4 Components

```
normalized_matrix_less_o3_lotbg <- normalized_matrix[,setdiff(colnames(normalized_matrix), c('o3', 'h2o'))]
nmf_result_4c_less_o3_lotbg <- nmf(normalized_matrix_less_o3_lotbg, rank = 4, method = "KL", seed='nnds')

## Warning in sqrt(S[i] * term_p) * uup: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

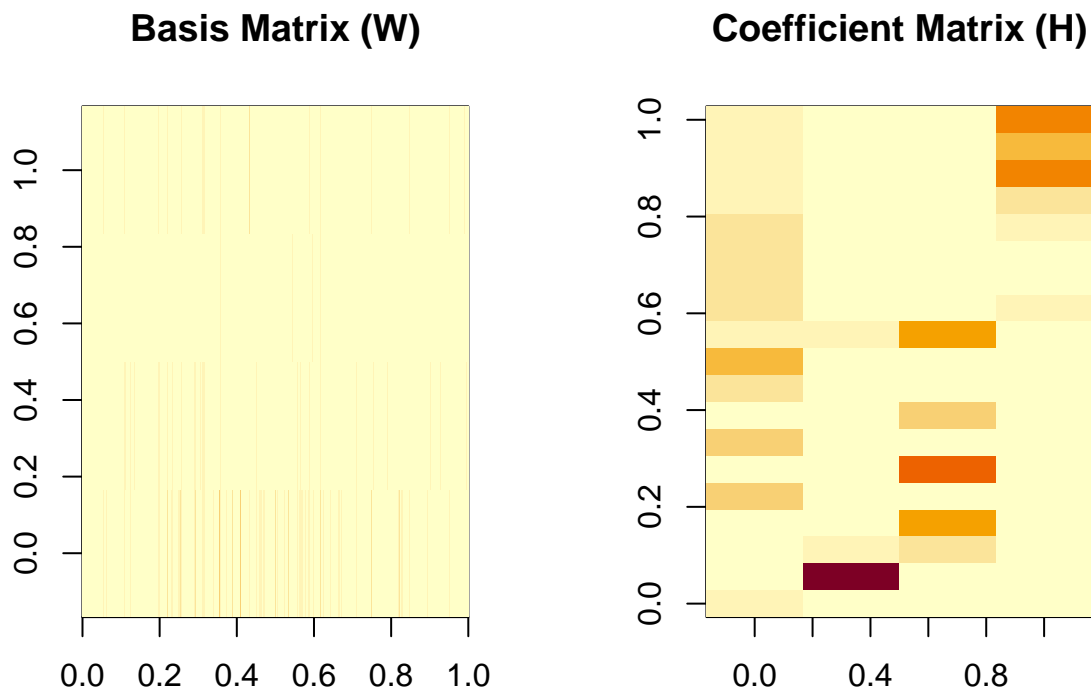
## Warning in sqrt(S[i] * term_p) * vvp: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

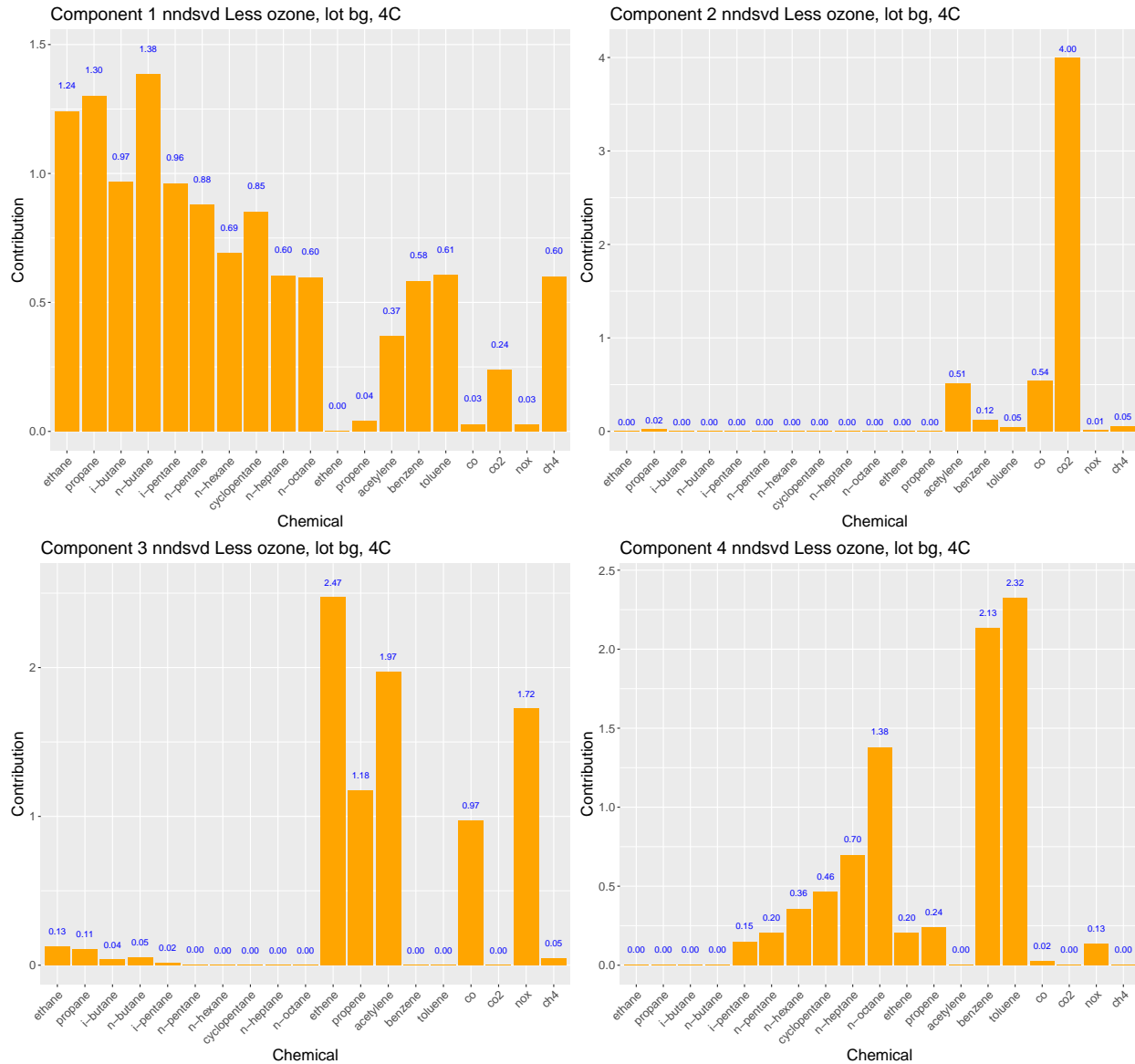
## Warning in sqrt(S[i] * term_p) * uup: Recycling array of length 1 in array-vector arithmetic is deprecated
```



```
## Use c() or as.vector() instead.
## Warning in sqrt(S[i] * termp) * vvp: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.
basis_matrix_4c_less_o3_lotbg <- basis(nmf_result_4c_less_o3_lotbg)
coef_matrix_4c_less_o3_lotbg <- coef(nmf_result_4c_less_o3_lotbg)

par(mfrow = c(1, 2))
image(basis_matrix_4c_less_o3_lotbg, main = "Basis Matrix (W)")
image(coef_matrix_4c_less_o3_lotbg, main = "Coefficient Matrix (H)")
```





5 Components

```
nmf_result_5c_less_o3_lotbg <- nmf(normalized_matrix_less_o3_lotbg, rank = 5, method = "KL", seed='nndsvd')
```

```
## Warning in sqrt(S[i] * termp) * uup: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termp) * vvp: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termp) * uup: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termp) * vvp: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

```
## Warning in sqrt(S[i] * termn) * uun: Recycling array of length 1 in array-vector arithmetic is deprecated.
## Use c() or as.vector() instead.
```

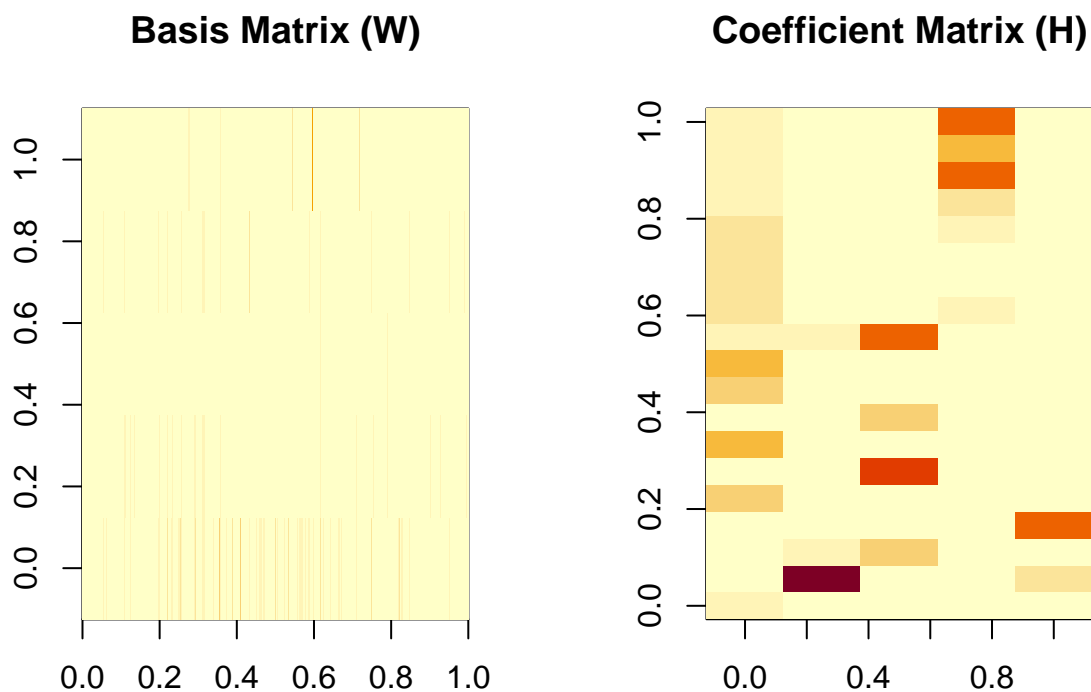
```
## Warning in sqrt(S[i] * termn) * vvn: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

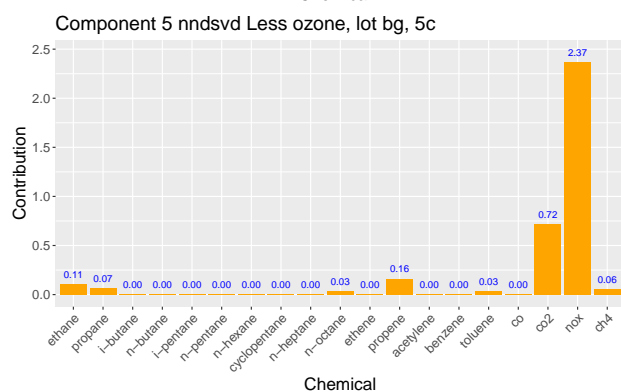
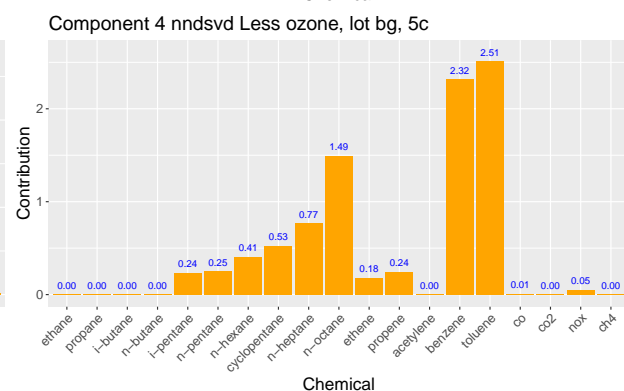
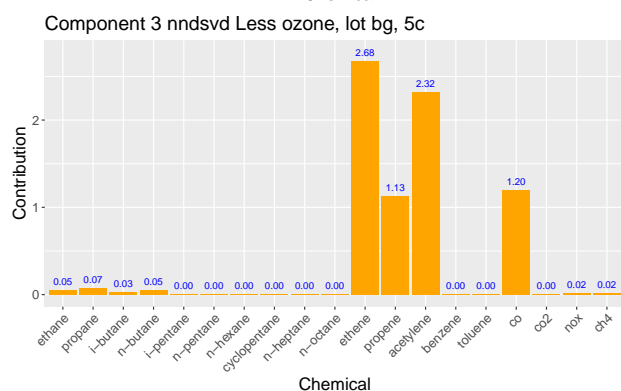
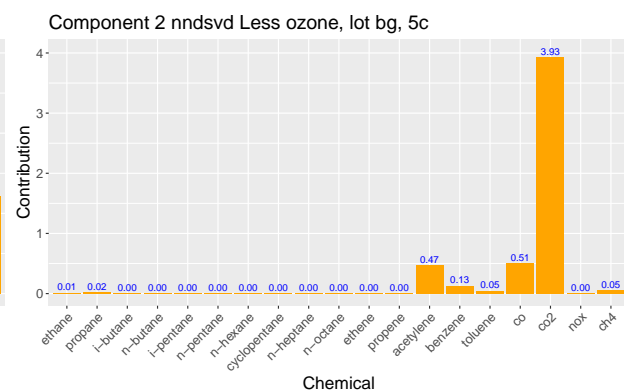
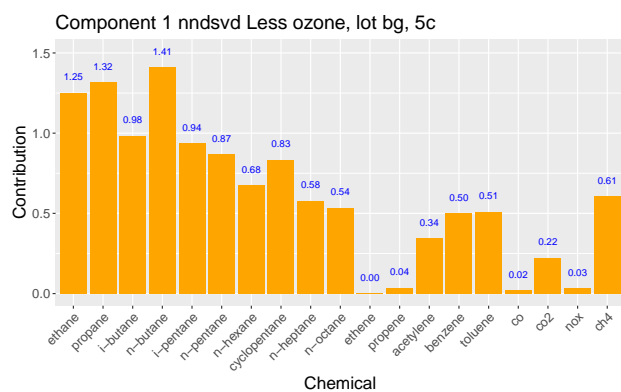
## Warning in sqrt(S[i] * termp) * uup: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

## Warning in sqrt(S[i] * termp) * vvp: Recycling array of length 1 in array-vector arithmetic is deprecated
## Use c() or as.vector() instead.

basis_matrix_5c_less_o3_lotbg <- basis(nmf_result_5c_less_o3_lotbg)
coef_matrix_5c_less_o3_lotbg <- coef(nmf_result_5c_less_o3_lotbg)

par(mfrow = c(1, 2))
image(basis_matrix_5c_less_o3_lotbg, main = "Basis Matrix (W)")
image(coef_matrix_5c_less_o3_lotbg, main = "Coefficient Matrix (H)")
```





Compare to 4 components

