

Genetic Algorithm for solving Sudokus

Here is a quick overview how we tried to solve this problem.

- **Representation:**

Our Sudokus are represented by 2-dimensional arrays with the size 9 x 9.

- **Initialization:**

After the already known fixed numbers are added to the initial Sudoku, we calculate additional fixed numbers. In order to do so, we check for every cell if there exists a number which can only be placed in this particular cell based on the already known numbers in its row, column and 3x3 subgrid. If so, we add that number to the initial Sudoku.

When this process finds no more additional initial values, all the 3x3 subgrids are filled with values, such that every subgrid is feasible (Contains every value from 1 to 9 once). This process is repeated x times, in order to get an initial population of size x.

- **Evaluation:**

In order to evaluate the fitness, we count the existing contradictions of a Sudoku (Multiple occurrences of numbers in rows or columns are considered a contradiction). Then we also calculate the standard deviation value, by adding each number of a row or column and checking the deviation to the value of 45 (which is the sum of the numbers from 1 to 9).

Finally the fitness value is calculated by considering both the number of contradictions and the standard deviation value.

- **Recombination:**

The recombination in our solution is done by slices between the 3x3 subgrids. In a k-Tournament the 2 fittest out of k possible parents are selected, which are then recombined randomly via either a single slice (only one slice after a random number of 3x3 subgrids) or multiple slices (50% chance of a slice between every 3x3 subgrid). With this kind of recombination we guarantee that our 3x3 subgrids stay feasible.

- **Mutation:**

Our mutation is basically performed via a permutation inside of a 3x3 subgrid. We randomly select between three approaches: Either two random cells are switched, or all the values between two cells are reversed, or we do both. This process is performed on one random 3x3 subgrid of a Sudoku. Because we only use permutations we guarantee that our 3x3 subgrids stay feasible.

- **Selection:**

In our selection process we consider all parents and newly added children of our population. We sort them based on their fitness and then select x out of them, with x being our population size. The fitter a Sudoku is, the more likely it is to get selected by the algorithm (Although no Sudoku, except the fittest one, can be sure to get selected). The formula used for this calculation is: $(\text{size} - \text{ranking}) / \text{size}$. With size being the number of parents and children combined, and ranking being the position of the Sudoku in the list, sorted by fitness.

Additional Info:

- We have implemented two strategies in our algorithm, the so called solveSingle and the solveMultiple. In the solveSingle mode we run the algorithm normally after generating our initial population. But in the solveMultiple mode we generate a few initial populations in order to run the algorithm on all of them and get the fittest solutions of all of them. These fittest solutions are then combined to form a new initial population and the algorithm is performed one more time with this population.
- The algorithm stops when either a correct solution for a Sudoku is found or after a certain number of iterations (in case no correct solution could be found). If the latter is the case the best Sudoku calculated so far is returned.
- To run the project please import it into Eclipse (Import existing project into workspace) and run the SolverExec.java file.