

# Appendix D

## List of Algorithms

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**Algorithm 1** Blockbuster Algorithm ([Brownlees et al. \(2018\)](#))

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**Require:** The return matrix  $Y \in \mathbb{R}^{N \times T}$  and the number of groups  $K \in \mathbb{R}^+$ .

- 1: Compute the sample covariance matrix  $S$ .
  - 2: Compute the eigenvectors corresponding to the  $K$  largest eigenvalues of  $S$  and construct the matrix  $\tilde{U} \in \mathbb{R}^{N \times K}$ .
  - 3: Standardize each row of  $\tilde{U}$  by its Euclidean norm to obtain the row-normalized sample eigenvector matrix  $X$ , where each element is computed as  $x_{nk} = \frac{\tilde{u}_{nk}}{\|\tilde{u}_n\|_2}$ .
  - 4: Apply the  $K$ -means algorithm to the rows of  $X$ .
- return** K-means partition  $\hat{\Pi}_K = \{\hat{\Pi}_1, \dots, \hat{\Pi}_K\}$  as the estimate of the asset groups.
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**Algorithm 2** Adaptive Blockbuster Algorithm ([De Nard \(2022\)](#))

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**Require:** The return matrix  $Y \in \mathbb{R}^{N \times T}$ .

- 1: Compute the sample covariance matrix  $S = \frac{1}{T-1}YY'$ , and its spectral decomposition  $S = UVU'$ .
  - 2: Standardize the sorted eigenvalue vector  $\tilde{V} = \text{sort}(\text{diag}(V))$  by the Euclidean norm and denote it by  $Y$ , where each element is computed as  $y_n = \frac{\tilde{v}}{\|\tilde{V}\|_2}$ .
  - 3: Apply a Kernel Density Estimate to  $Y$  and compute the number of resulting local minimas  $M$ .
  - 4: Use  $Y$  and  $K = M + 1$  as inputs for the Blockbuster Algorithm (Algorithm 1).
- return** K-means partition  $\hat{\Pi}_K = \{\hat{\Pi}_1, \dots, \hat{\Pi}_K\}$  as the estimate of the asset groups.
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