

The Pantograph Mk-II: A Haptic Instrument*

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Abstract—We describe the redesign and the performance evaluation of a high-performance haptic device system called the Pantograph. The device is based on a two degree-of-freedom parallel mechanism which was designed for optimized dynamic performance, but which also is well kinematically conditioned. The results show that the system is capable of producing accurate tactile signals in the DC–400 Hz range and can resolve displacements of the order of 10 μm . Future improvements are discussed.

Index Terms—Haptic Devices. Parallel Mechanisms. Mechanism Conditioning. Performance Measures.

I. INTRODUCTION

The scientific study of touch, the design of computational methods to synthesize tactile signals, studies in the control of haptic interfaces, the development of force reflecting virtual environments, and other activities, all require the availability of devices that can produce reliable haptic interaction signals. In some cases, it is needed to produce well controlled stimuli. In other cases, it is important to have the knowledge of the structural dynamics of a device, but in all cases, these activities entail having devices which are well characterized.

Following SensAble's Phantom® and Immersion's Impulse Engine®, several new commercially-available general-purpose haptic devices have been recently introduced: MPB's Freedom-6S®, Force Dimension's Omega®, Haption's Virtuoso®, Immersion Canada's PenCat/Pro®; plus other application-specific devices. In addition, interesting, low-complexity, high-performance devices have also become available, either from research institutions or from commercial sources [9], [10], [15], [21]. We felt, nonetheless, that a general-purpose laboratory system having high performance features, would be a valuable tool.

With this in mind, we set out to redesign the 'Pantograph' haptic device, first demonstrated at the 1994 ACM SIGCHI conference in Boston, MA [22]. Our first goal was the creation of an open architecture system which could be easily replicated from blueprints and from a list of off-the-shelf components. The second goal was to obtain a system which would have superior and known performance characteristics so that it

could be used as a scientific instrument. Our intention is to make the system available in open-source, hardware and software.

An important aspect of the Pantograph, a planar parallel mechanism (Fig. 1d), is the nature of its interface: a non-slip plate on which the fingerpad rests (Fig. 1e). Judiciously programmed tangential interaction forces f_T at the interface (Fig. 1e) have the effect of causing fingertip deformations and tactile sensations that resemble exploring real surfaces.

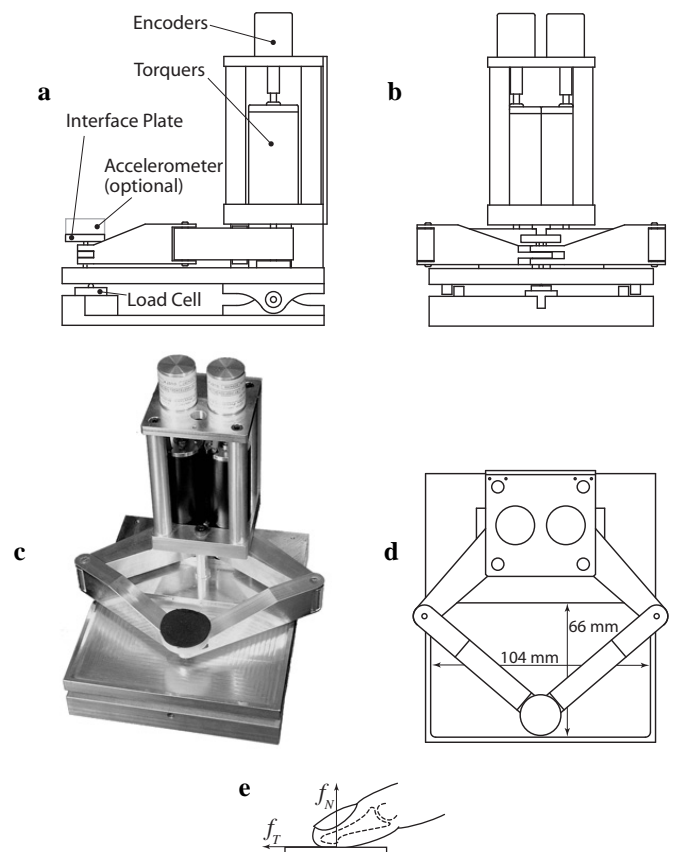


Fig. 1. Pantograph Mk II electromechanical hardware. **a)** Side view showing the main electromechanical components. **b)** Front view. **c)** Photograph. **d)** Top view of the five-bar mechanism and plate constrained to 2-DOF. **e)** The interaction force has two components: f_N is measured by the load cell and f_T results from coupling the finger tip to the actuators via linkages.

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II. COMPONENTS

a) *Mechanical Structure:* The mechanical design was not changed from the original device. The dimensions, as well as the shape of the links, were determined from dynamic performance considerations [13], rather than from kinetostatic considerations [24]. Statically, the structure must resist bending when loaded vertically. The proximal links (Fig. 2a) have a pocketed box design which gives them the structure of a wishbone horizontally where they are dynamically loaded and otherwise of a hollow beam for torsional static strength. The distal links (Fig. 2b) have an axial dynamic load and behave like cantilevers under the vertical static load, therefore they have a tapered shape to reduce weight.

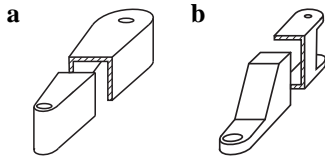


Fig. 2. Internal structure of the beams. a) Proximal link. b) Distal Link.

b) *Normal Force Sensing:* To render arbitrary virtual surface interaction forces, the normal component of the force must be known. A sensor could have been put in the plate, however, locating the sensor (loadcell Omega Engineering model LCKD-5; conditioner Newport Electronics model INFS-0010-DC-7) under the entire device is also possible, since the normal force is entirely due to the user and hence has low bandwidth. This way, the force sensor does not ‘see’ any inertial forces (a tip mounted force sensor could be sensitive to acceleration and give erroneous readings). The static load due to the weight of the device was eliminated by locating the hinge under the center of mass (Fig. 1a).

c) *Accelerometer:* To measure the device transfer function, to provide detailed information about the high-frequency movements of the plate for use in other experiments (for example involving acceleration feedback to render textures or shock sensations, or to investigate the coupled dynamics of the finger pad), a dual-axis MEMS accelerometer (Analog Device; model ADXL250) was embedded in an interchangeable plate (Fig. 1a).

d) *Motors:* Two conventional coreless DC motors (Maxon RE-25 graphite brushes) are used as torquers. Although this solution is clearly suboptimal, it was used for simplicity and will be further discussed in the Section V. We experimented with both graphite and metal brushes. The friction due to metal brushes is lower, but the electrical coupling they provide at low speeds with the windings is not as good as with graphite brushes. It was observed that the electrical resistance varied so greatly and so rapidly from one commutator blade to the next that current feedback was ineffective to compensate for this variation, resulting in noticeable transient drops in the torque.

e) *Position Sensors:* The servo quality potentiometers used in the original Pantograph could only provide 10 bits of

resolution over the workspace if their signal was unprocessed. These were replaced by optical rotary incremental encoders. Two models were evaluated that had the required resolution and form factor. Models from Gurley Precision Instruments Inc. (model R119S01024Q5L16B188P04MN; 65,536 CPR) and MicroE Systems Inc. (model M1520S-40-R1910-HA; 100,000 CPR) both gave good results. The Gurley sensors are less expensive and easier to commission while the MicroE sensors require alignment and protective custom housing.

f) *Electronics:* An integrated 4-channel “hardware-in-the-loop” PCI card from Quanser Inc. (model Q4) with 24-bit encoder counters, unbuffered, low delay analog-to-digital/digital-to-analog channels proved to be a convenient and cost effective solution (read encoders, read acceleration and force signal, write actuator currents) that could support two devices. The current amplifier design is crucial given the observed variation of the motor winding resistance due to commutation. Low gain current amplifiers built around the NS power chip LM12CL proved to be only partially effective. Better performance should be provided in the future by Quanser’s LCAM amplifiers.

III. KINEMATICS

The kinematic structure is a five-bar planar linkage represented in Fig 3. The end-plate is located at point P_3 and moves in a plane with two degree-of-freedom with respect to the ground link, where the actuators and sensors are located at P_1 and P_5 . The configuration of the device is determined by the position of the two angles θ_1 and θ_5 and the force at the tool tip P_3 is due to torques applied at joints 1 and 5.

The nominal values of the link lengths a_i are in mm:

$$a_{\text{nom}} = [63 \ 75 \ 75 \ 63 \ 25]^T.$$

A. Direct Kinematics

The direct kinematics problem consists of finding the position of point P_3 from the two sensed joint angles θ_1 and θ_5 . The base frame is set so that its z axis passes through P_1 . It was in the past solved using various approaches, the latest provided in [6]. These approaches all share the observation that P_3 is at the intersection of two circles, the centers and the radii of which are known. The circles of radii a_2 and a_3 are centered at:

$$P_2(x_2, y_2) = [a_1 \cos(\theta_1), a_1 \sin(\theta_1)]^T, \quad \text{and} \quad (1)$$

$$P_4(x_4, y_4) = [a_4 \cos(\theta_5) - a_5, a_4 \sin(\theta_5)]^T. \quad (2)$$

and intersect at two points corresponding to two configurations. The device, however, always operates in the configuration that has the largest y . We used a geometric approach to find them. Let $P_3 = (x_3, y_3)$ and $P_h = (x_h, y_h)$ be the intersection between the segment P_2P_4 and the height of triangle $P_2P_3P_4$.

Which motor we can use to avoid this problem?

We find

$$\|\mathbf{P}_2 - \mathbf{P}_h\| = \frac{(a_2^2 - a_3^2 + \|\mathbf{P}_4 - \mathbf{P}_2\|^2)}{(2\|\mathbf{P}_4 - \mathbf{P}_2\|)}, \quad (3)$$

$$\mathbf{P}_h = \mathbf{P}_2 + \frac{\|\mathbf{P}_2 - \mathbf{P}_h\|}{\|\mathbf{P}_2 - \mathbf{P}_4\|}(\mathbf{P}_4 - \mathbf{P}_2), \quad (4)$$

$$\|\mathbf{P}_3 - \mathbf{P}_h\| = \sqrt{a_2^2 - \|\mathbf{P}_2 - \mathbf{P}_h\|^2}. \quad (5)$$

The end effector position $\mathbf{P}_3(x_3, y_3)$ is then given by

$$? \quad x_3 = x_h \pm \frac{\|\mathbf{P}_3 - \mathbf{P}_h\|}{\|\mathbf{P}_2 - \mathbf{P}_4\|}(y_4 - y_2), \quad (6)$$

$$? \quad y_3 = y_h \mp \frac{\|\mathbf{P}_3 - \mathbf{P}_h\|}{\|\mathbf{P}_2 - \mathbf{P}_4\|}(x_4 - x_2). \quad (7)$$

The useful solution has a positive sign in Eq. (6) and negative sign in Eq. (7). Since in the workspace $x_4 < x_2$, the solution with a negative sign yields larger y .

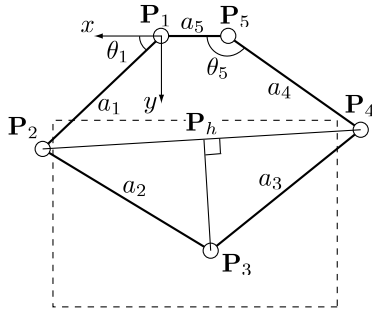


Fig. 3. Model of the kinematics used to compute the direct problem.

B. Inverse Kinematics

Parallel manipulators frequently have an inverse kinematics problem that is simpler than the direct kinematics problem. The Pantograph is no exception. The problem is to find the angles θ_1 and θ_5 given the position of point \mathbf{P}_3 . A pentagon can be divided into three triangles, see Fig. 4 which makes the solution straightforward:

$$\theta_1 = \pi - \alpha_1 - \beta_1, \quad \theta_5 = \alpha_5 + \beta_5, \quad (8)$$

where

$$\alpha_1 = \arccos\left(\frac{a_1^2 - a_2^2 + \|\mathbf{P}_1, \mathbf{P}_3\|}{2a_1\sqrt{\|\mathbf{P}_1, \mathbf{P}_3\|}}\right), \quad (9)$$

$$\beta_1 = \text{atan2}(y_3, -x_3), \quad (10)$$

$$\beta_5 = \arccos\left(\frac{a_4^2 - a_3^2 + \|\mathbf{P}_5, \mathbf{P}_3\|}{2a_4\sqrt{\|\mathbf{P}_5, \mathbf{P}_3\|}}\right), \quad (11)$$

$$\alpha_5 = \text{atan2}(y_3, x_3 + a_5). \quad (12)$$

This solves the inverse kinematics for a generic Pantograph with arm lengths a_i , as long as the device is in a configuration such that $\alpha_1 > 0$ and $\beta_5 > 0$, which puts it in the permitted workspace.

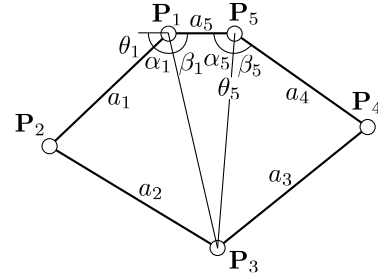


Fig. 4. Dividing the pentagon into three triangles.

C. Differential Kinematics

The Jacobian matrix can be found by direct differentiation of the direct kinematic map with respect to the actuated joints θ_1 and θ_5 :

$$\mathbf{J} = \begin{bmatrix} \partial x_3 / \partial \theta_1 & \partial x_3 / \partial \theta_5 \\ \partial y_3 / \partial \theta_1 & \partial y_3 / \partial \theta_5 \end{bmatrix} = \begin{bmatrix} \partial_1 x_3 & \partial_5 x_3 \\ \partial_1 y_3 & \partial_5 y_3 \end{bmatrix} \quad (13)$$

where $\partial_i \cdot$ denotes the partial derivative with respect to θ_i . Let $d = \|\mathbf{P}_2 - \mathbf{P}_4\|$, $b = \|\mathbf{P}_2 - \mathbf{P}_h\|$ and $h = \|\mathbf{P}_3 - \mathbf{P}_h\|$.

Applying the chain rule to Eqs. (6) and (7):

$$\partial_1 x_2 = a_1 \sin(\theta_1), \quad \partial_1 y_2 = a_1 \cos(\theta_1), \quad (14)$$

$$\partial_5 x_4 = a_4 \sin(\theta_5), \quad \partial_5 y_4 = a_4 \cos(\theta_5), \quad (15)$$

$$\partial_1 y_4 = \partial_1 x_4 = \partial_5 y_2 = \partial_5 x_2 = 0, \quad \partial_i h = -b \partial_i b / h \quad (16)$$

$$\partial_i d = \frac{(x_4 - x_2)(\partial_i x_4 - \partial_i x_2) + (y_4 - y_2)(\partial_i y_4 - \partial_i y_2)}{d} \quad (17)$$

$$\partial_i b = \partial_i d - \frac{\partial_i d(a_2^2 - a_3^2 + d^2)}{2d^2} \quad (18)$$

$$\begin{aligned} \partial_i y_h &= \partial_i y_2 \\ &+ \frac{\partial_i b d - \partial_i d b}{d^2}(y_4 - y_2) + \frac{b}{d}(\partial_i y_4 - \partial_i y_2) \end{aligned} \quad (19)$$

$$\begin{aligned} \partial_i x_h &= \partial_i x_2 \\ &+ \frac{\partial_i b d - \partial_i d b}{d^2}(x_4 - x_2) + \frac{b}{d}(\partial_i x_4 - \partial_i x_2) \end{aligned} \quad (20)$$

$$\begin{aligned} \partial_i y_3 &= \partial_i y_h \\ &- \frac{h}{d}(\partial_i x_4 - \partial_i x_2) - \frac{\partial_i h d - \partial_i d h}{d^2}(x_4 - x_2) \end{aligned} \quad (21)$$

$$\begin{aligned} \partial_i x_3 &= \partial_i x_h \\ &+ \frac{h}{d}(\partial_i y_4 - \partial_i y_2) + \frac{\partial_i h d - \partial_i d h}{d^2}(y_4 - y_2) \end{aligned} \quad (22)$$

D. Kinematic Conditioning

All entries of the Jacobian have the dimension of lengths mapping angular velocities $\omega = [\dot{\theta}_1 \ \dot{\theta}_5]^\top$ to linear velocities $v = [\dot{x}_3 \ \dot{y}_3]^\top$: $v = \mathbf{J} \omega$. Thus, the 2-norm of the Jacobian matrix (which also is a length) has the physical meaning of scaling the sensor nominal resolution to the nominal resolution of the device. The Jacobian matrix is well conditioned on all the workspace and the device becomes isotropic at (Fig. 5):

$$\theta_{1 \text{ iso}} = \arccos\left(-\frac{25}{126} + \frac{25\sqrt{2}}{42}\right), \quad \theta_{5 \text{ iso}} = \pi - \theta_{1 \text{ iso}} \quad (23)$$

corresponding to the point $\mathbf{P}_{\text{iso}} \simeq (-12.5, 101.2)$ in Fig. 5. At this point the two distal links intersect orthogonally at

$H_2 = ?$

the tip and the end effector is equidistant from the actuated joints. Here, the Jacobian matrix maps disks in the angular velocity joint space to disks in the tip velocity space. There are just two such points. The other point which has a negative y is not used. The isotropic region is near the edge of the workspace but this is an acceptable compromise given that the main objective is dynamic performance. The device, as dimensioned, has a large region of dynamic near-isotropy spreading over most of the workspace [13].

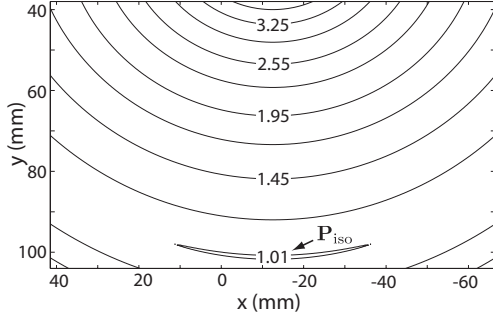


Fig. 5. Condition number of the Jacobian of the Pantograph over the workspace. The device is isotropic at the point P_{iso} .

If $\|\cdot\|_2$ denotes the largest singular value of a matrix, then expression:

$$\|\Delta \mathbf{X}\| \leq \|\mathbf{J}\|_2 \|\Delta \theta_1 \Delta \theta_5\|^T \quad (24)$$

where $\Delta \mathbf{X} = [\Delta x \Delta y]^T$ is the resolution of the device and $\Delta \theta_i$ the resolution of an encoder. This allows us to plot the ideal resolution of the device in Fig. 6 for the case where encoders with 65K CPR are used.

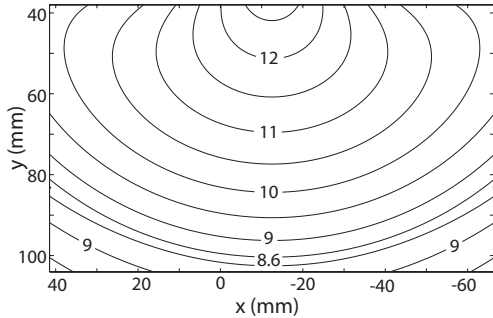


Fig. 6. Resolution of the Pantograph in the workspace, measurement unit is the μm . The device is equipped with two encoders with 2^{16} counts per revolution, the resolution is $\|\Delta \mathbf{X}\| = \|\mathbf{J}\|_2 \sqrt{2} \frac{2\pi}{2^{16}}$.

E. Calibration

Since the angles are measured by incremental encoders, the origin needs to be calibrated at system startup. The workspace of the device is mechanically limited to a rectangular area which can be used for this purpose. In a first maneuver, point P_3 is brought by the user to the bottom left corner of the workspace to roughly calibrate the encoders. The user then proceeds to acquire many calibration points by sliding the end effector along the four edges (bottom, right, top, left). Points

acquired on the bottom edge all have the same y coordinate, so on this edge, $P_3^i = (x_3^i, y^\downarrow)$ where y^\downarrow is the known common value of the coordinate, and similarly for the other edges: y^\uparrow for the top edge, x^\leftarrow for the left edge, and x^\rightarrow for the right.

Call the θ_1^i and θ_5^i , the measurements acquired. The components of the direct kinematic function are x_3 and y_3 : $\mathbf{P}_3 = [x_3(\theta_1, \theta_5) \ y_3(\theta_1, \theta_5)]^T$. The device can be calibrated by minimizing the error function

$$E = \sum_{i=1}^{N_\downarrow} [y^\downarrow - y_3(\theta_1^{\downarrow} + \theta_1^0, \theta_5^{\downarrow} + \theta_5^0)]^2 + \sum_{i=1}^{N_\rightarrow} [x^\rightarrow - x_3(\theta_1^{\rightarrow} + \theta_1^0, \theta_5^{\rightarrow} + \theta_5^0)]^2 + \sum_{i=1}^{N_\uparrow} [y^\uparrow - y_3(\theta_1^{\uparrow} + \theta_1^0, \theta_5^{\uparrow} + \theta_5^0)]^2 + \sum_{i=1}^{N_\leftarrow} [x^\leftarrow - x_3(\theta_1^{\leftarrow} + \theta_1^0, \theta_5^{\leftarrow} + \theta_5^0)]^2, \quad (25)$$

over the zero positions θ_1^0 and θ_5^0 : $\min_{\theta_1^0, \theta_5^0} E$. This is accomplished using the Levenberg-Marquardt algorithm [8]. The results are satisfying since the two offset angles are found with an uncertainty of 6-7 counts which can be attributed to backlash in the joints 2 and 4 as further discussed in Section IV-B.

IV. RESULTS

The importance of the static and dynamic behavior of haptic devices, accounting for the mechanical structure, transmission and drive electronics has been well recognized by device designers [1], [2], [7], [14], [20], [23].

Guidelines for measuring the performance characteristics of force feedback haptic devices were documented in [12]. Among these guidelines two are particularly important, in addition to the usual requirement of minimizing interference with the process being measured. The first specifies that the characteristics must be measured where the device is in contact with the skin. The second recognizes the fact that a haptic device has a response that depends on the load. Therefore, load reflecting the conditions of actual use must be applied during the measurements. From this view point, measurement of the system response from the actuator side and without a load, as it is sometimes done (e.g. [4]), fails to provide the sought information. A useful actuator-side technique that quantifies the structural properties of a device in terms of a “structural deformation ratio” (SRD) was nevertheless suggested [19]. It was not used here since the complete system response provides richer information.

A. Experimental System Response

The frequency response (from amplifier current command to acceleration at the tip) was measured with a system analyzer (DSP Technology Inc., SigLab model 20-22) using chirp excitation. This technique was used because it is more precise and more robust to nonlinearities (and more time consuming) than an ARMAX procedure.

Measurements were performed under three conditions. The first corresponded to the unloaded condition. In order to prevent the device from drifting away during identification, it was held in place by a loosely taught rubber band. The second

condition was created by lightly touching the interface plate while the response was measured. In the third condition, the device was loaded by pressing firmly on it.

An ideal device should have a uniform gain across all frequencies (and would have to a SDR index of 1.0 [19]). Fig. 7 shows all three responses on the same graph but offset by 10 dB for clarity. The response was indeed flat over a wide bandwidth (40 to 300 Hz). But irregularities occurred in the low and the high frequency regions.

In the low frequency region, the rise in gain for the “unloaded response” was most probably due to presence of the rubber band and can be ignored. However contact with a finger creates a low Q resonance (Q factor 2 to 3) which shifted up in frequency when the finger pressed harder. This could be explained by the nonlinear nature of tissues. These observations conspire to indicate that indeed, it would be difficult to reduce the finger to that of a linear time invariant system without risking to oversimplify the dynamics of the actual system [10], [18].

In the high frequency region, there were two notable events in the response. The “unloaded response” first shows what is the typical fingerprint of a sharp, low-loss structural resonance (pole-zero pair) in the 400-500 Hz band. This could be attributed to flexibility inside the motor as these often emit acoustic noise at this frequency upon torque transients (this is also the case of all haptic interfaces using the same “bell coreless” motors). As the finger presses harder on the interface, this resonance is progressively masked by the load but probably continues to occur, but is unseen at the tip. Now, what is more difficult to explain are the additional events in the 900 Hz region, which instead of being attenuated by a larger load as one would expect, are actually enhanced to reach up to 30 dB of gain, a rather large magnitude indeed. If these were due to structural resonance of the linkages, then one would observe a shift in frequency due to nonlinear buckling. But it is not the case. This problem will be further discussed in Section V. In the meantime we established that the device can reliably be used in the DC-400 Hz range provided that proper roll-off filters are used [3].

B. Resolution

We estimated the actual device resolution using the setup shown in Fig. 8a. A micropositioner was connected to joint 3 so it could back-drive the device along the y axis in the vicinity of point P_{iso} . Backlash and other joint imperfections were likely to deteriorate the resolution of the device but should not be considered first. To minimize their influence, a constant torque was applied by the motor to preload the joints. Fig 8b shows the encoders values when the tip is moved by 50 μm . This verifies the resolution determined from the analysis of the Jacobian matrix.

V. CONCLUSION AND DISCUSSION

This paper has described the redesign of the Pantograph haptic device with a view to increase its performance so it would be capable of providing high quality haptic rendering.

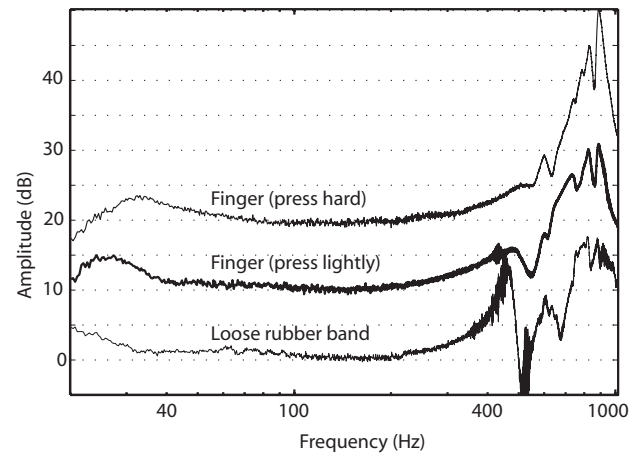


Fig. 7. Frequency Response of the device when an identical signal is sent to both the amplifiers to create an horizontal movement. The intensity of the movement is measured with an accelerometer approximately parallel to the movement. The response curves relative to the finger are shifted of +10 dB (light pressure) and +20 dB (hard pressure).

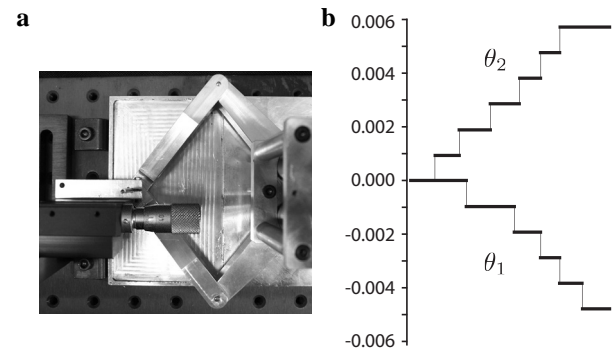


Fig. 8. a) Setup used to verify resolution. b) Encoder reading during a linear movement of 50 μm . The plot shows that there are 5 or 6 ticks, matching the analysis made with the Jacobian.

Its performance was evaluated and found to meet the initial expectations of uniform and wide bandwidth response. However, while the device operates very well, several points still need attention. The manner in which they can be addressed is now discussed by order of increasing implementation difficulty.

- 1) The backlash in the joints in certain conditions, particularly when the plate is not statically loaded, can reach several encoders ticks. The cause was simple to find and so will be the solution to eliminate it. The present bearings were specified of ordinary quality. In fact, their backlash specifications match the observations. They should be replaced by higher quality bearings since clearly this is a limiting factor.
- 2) The device is machined out of aluminum. It is possible that the metallic structure participates in the observed unwanted high frequency resonance. Composite materials could be used to manufacture haptic devices with structural properties designed to optimize their response (e.g. adjust for critical damping) [17].

- 3) The device should incorporate a source of calibrated viscous damping [5], something which is the subject of on-going work.
- 4) "Bell coreless" motors work well but are less than ideal for haptic device applications due to (1) their sharp internal resonance characterized in this paper, and (2) use of un-needed brushes in a limited angle application [24]. Motors having an absence of torque ripple, absence of cyclical reluctant torque (cogging), optimized structural properties, and absence of friction (in addition to high torque, of course) should be designed specifically for this application. Recent proposals for electronic compensation of the injurious properties of motors designed for other purposes fall short of our requirements in this respect [16].

Search for better motors for this application.

Finally, we hope to be able to release the system publicly in a near future, even if not all the points discussed above are fully addressed. At the present time however, the system is in use to carry out studied in high fidelity friction and texture synthesis techniques [3], [11].

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