

Journal of Statistical Software

MMMMMM YYYY, Volume VV, Issue II.

doi: 10.18637/jss.v000.i00

casebase: An Alternative Framework For Survival Analysis

Sahir Bhatnagar *
McGill University

Maxime Turgeon *
University of Manitoba

Jesse Islam McGill University James Hanley McGill University Olli Saarela University of Toronto

Abstract

The abstract of the article. * joint co-authors

Keywords: keywords, not capitalized, Java.

1. Introduction

The purpose of the **casebase** package is to provide practitioners with an easy-to-use software tool to predict the risk (or cumulative incidence (CI)) of an event, for a particular patient. The following points should be noted:

- 1. hazard ratios
- 2. If, however, the absolute risks are of interest, they have to be recovered using the semiparametric Breslow estimator
- 3. Alternative approaches for fitting flexible hazard models for estimating absolute risks, not requiring this two-step approach? Yes! (Hanley and Miettinen 2009)

(Hanley and Miettinen 2009) propose a fully parametric hazard model that can be fit via logistic regression. From the fitted hazard function, cumulative incidence and, thus, risk functions of time, treatment and profile can be easily derived.

2. Literature review

	Parameters	Density R function	dist	
	(location in red)			
Exponential	rate	dexp	"exp"	
Weibull (accelerated failure	shape, scale	dweibull	"weibull"	
time)				
Weibull (proportional haz-	shape, scale	dweibullPH	"weibullPH"	
ards)				
Gamma	shape, rate	dgamma	"gamma"	
Log-normal	meanlog, sdlog	dlnorm	"lnorm"	
Gompertz	shape, rate	dgompertz	"gompertz"	
Log-logistic	shape, scale	dllogis	"llogis"	
Generalized gamma (Pren-	<mark>mu</mark> , sigma, Q	dgengamma	"gengamma"	
tice 1975)				
Generalized gamma (Stacy	shape, <mark>scale</mark> , k	dgengamma.orig	"gengamma.orig"	
1962)				
Generalized F (stable)	<mark>mu</mark> , sigma, Q, P	dgenf	"genf"	
Generalized F (original)	mu, sigma, s1, s2	dgenf.orig	"genf.orig"	

Table 1: Built-in parametric survival distributions in **flexsurv**.

To conduct our review on current methods available in survival analysis, a scraper was coded to examine all packages in the survival task view on CRAN (2019). There was a total of 259 packages, many of which are not relevant to the problems casebase addresses. To filter these packages, a scraper was used to search for competing risks, cumulative incidence functions, non-proportional hazards and penalization. This reduced our set of 259 packages down to 60. From here, we manually examined each package to determine which ones are comparable to casebase, with either a different approach to the same problems or future features we would like to add to casebase.

These packages can belong to three main categories: non-proportional hazards, regularization and competing risks. Besides these three main categories, there are extra features of interest as well. Table 2 summarizes the findings.

Many packages exist that implement semi-parametric Cox models. Of those, **glmnet** (2011)???, **glmpath** (2018), **penalized** (2010), **RiskRegression** (2019) introduce penalization in their model fitting. **CoxRidge** (2015), **rstpm2** (2019) and **survival** (2015) include penalization, but they implement the extended cox model permitting intuitive non proportional hazard modeling while the previous four do not. In terms of penalization, the benefits of **casebase** comes from its flexibility. Linear models have a wide tool set, considerably larger than those made for Cox regression. **casebase** permits many regularization tools developed for linear regression to be repurposed within a survival context.

Parametric models permit non-proportional hazards and are implemented in a handful of packages. Of interest are **CFC** (2019), **flexsurv** (2016), **SmoothHazard** (2017), **rsptm2** (2019) and **survival** (2015). **SmoothHazard** is limited to Weibull distributions (2017), whereas **flexsurv** and **survival** contain implementations for users to supply any distribution they would like (2015), (2016). **flexsurv**, **smoothhazard**, **mets** and **rstpm2** can use splines, permitting a flexible fit over time (2016), (2017), (2014), (2019). Though **casebase** is limited to three distributions at the moment, it also uses splines allowing for distributions that may not be

consistent over survival time.

Of the methods mentioned so far, only **CFC**, **flexsurv**, **mets** and **survival** contain implementations for competing risks (2019), (2016), (2014), (2015). The differentiating factor between these packages and **casebase** is that **casebase** handles competing risks through multiple logistic regression. **SmoothHazard**, **survival** and **Rstpm2** can handle interval censoring, whereas **casebase** currently cannot. Interval censoring is a simple feature to implement and is a potential improvement to add to **casebase**.

Of all the packages listed in Table 2, **CFC**, **Flexsurv**, **mets**, **RiskRegression**, **rstpm2** and **survival** have implementations for cumulative incidence (2019), (2016), (2014), (2019), (2015). Since **casebase** is parametric, the baseline hazard is known and requires integration to retrieve the cumulative incidence. This is similar to the approaches of **CFC** and **flexsurv** (2019), (2016), while the other packages use semi-parametric approaches to retrieve the baseline after fitting (2014), (2019). **rstpm2** and **survival** use both for their respective parametric and semi-parametric model implementations (2019), (2015).

Package	Competing Risks	Non-proportional	Penalization	Splines	Parametric	Semi-parametric	Interval/left Censoring	Absolute Risk
casebase Hanley and Miettinen (2009)	x	x	x	X	x			x
CFC Sharabiani and Mahani (2019)	x	x			x			x
coxRidge Perperoglou (2015)		x	x			x		
crrp Fu	x		x					
fastcox Yi and Zou			x			x		
Flexrsurv Clerc-Urmā's, Grzebyk, Hā@delin, and CENSUR working survival group (2017)		x		x	x			Cumulative hazard?
Flexsurv Jackson (2016)	x	x		x	x			Cumulative hazard?
glmnet Simon et al. (2011)			x			x		
glmpath Park and Hastie (2018)			x			x		
mets Scheike et al. (2014)	x			x		x		x
penalized Goeman, Meijer, Chaturvedi, and Lueder (2019)			x			x		
RiskRegression Gerds et al. (2019)			x			x		x
Rstpm2 Clements et al. (2019)		x	x	x	x	x	x	Cumm haz
SmoothHazard Touraine et al. (2017)		x		x	x		x	
Survival Therneau (2015)	x	x			x	x	x	x

Table 2: Different features of interest in various survival packages.

3. Theoretical details

As discussed in Hanley & Miettinen (2009), the key idea behind case-base sampling is to discretize the study base into an infinite amount of *person moments*. These person moments are indexed by both an individual in the study and a time point, and therefore each person moment has a covariate profile, an exposure status and an outcome status attached to it. We note that there is only a finite number of person moments associated with the event of interest (what Hanley & Miettinen call the *case series*). The case-base sampling refers to the sampling from the base of a representative finite sample called the *base series*.

As shown by Saarela & Arjas (2015) (and further expanded in Saarela (2016)), writing the likelihood arising from this data-generating mechanism using the framework of non-homogeneous Poisson processes, we eventually reach an expression where each person-moment's contribution is of the form

$$\frac{h(t)^{dN(t)}}{\rho(t)+h(t)},$$

where N(t) is the counting process associated with the event of interest, h(t) is the corresponding hazard function, and $\rho(t)$ is the hazard function for the Poisson process associated with case-base sampling. This parametric form suggests that we can readily estimate log-hazards of the form $\log(h(t)) = g(t;X)$ using logistic regression, where each observation corresponds to a person moment, the function g(t;X) is linear in a finite number of parameters, and where we treat $-\log(\rho(t))$ as an offset.

In Hanley & Miettinen (2009), the authors suggest performing case-base sampling uniformly, i.e. to sample the base series uniformly from the study base. In terms of Poisson processes, this sampling strategy corresponds essentially to a time-homogeneous Poisson process with intensity equal to b/B, where b is the number of sampled observations in the base series, and B is the total population-time for the study base. More complex examples are also available; see for example Saarela & Arjas (2015), where the probabilities of the sampling mechanism are proportional to the cardiovascular disease event rate given by the Framingham score.

The casebase package fits the family of hazard functions of the form

$$h(t; X) = \exp[g(t; X)]$$

where t denotes time and X, the individual's covariate profile. Different functions of t lead to different parametric hazard models. The simplest of these models is the one-parameter exponential distribution which is obtained by taking the hazard function to be constant over the range of t.

$$h(t;X) = \exp(\beta_0 + \beta_1 X)$$

The instantaneous failure rate is independent of t, so that the conditional chance of failure in a time interval of specified length is the same regardless of how long the individual has been in the study. This is also known as the *memoryless property* (Kalbfleisch and Prentice, 2002). The Gompertz hazard model is given by including a linear term for time:

$$h(t;X) = \exp(\beta_0 + \beta_1 t + \beta_2 X)$$

Use of log(t) yields the Weibull hazard which allows for a power dependence of the hazard on time (Kalbfleisch and Prentice, 2002):

$$h(t; X) = \exp(\beta_0 + \beta_1 \log(t) + \beta_2 X)$$

For competing-risk analyses with J possible events, we can show that each person-moment's contribution of the likelihood is of the form

$$\frac{h_j(t)^{dN_j(t)}}{\rho(t) + \sum_{i=1}^J h_j(t)},$$

where $N_j(t)$ is the counting process associated with the event of type j and $h_j(t)$ is the corresponding hazard function. As may be expected, this functional form is similar to the terms appearing in the likelihood function for multinomial regression.¹

4. Implementation details

$$\log\left(\frac{P(Y=j\mid X)}{P(Y=J\mid X)}\right) = X^T \beta_j, \qquad j = 1, \dots, J-1$$

¹Specifically, it corresponds to the following parametrization:

The functions in the casebase package can be divided into two categories: 1) data visualization, in the form of population-time plots; and 2) parametric modeling. We explicitly aimed at being compatible with both data.frames and data.tables. This is evident in some of the coding choices we made, and it is also reflected in our unit tests.

4.1. Population-time plots

4.2. Parametric modeling

The parametric modeling step was separated into three parts:

- 1. case-base sampling;
- 2. estimation of the smooth hazard function;
- 3. calculation of the risk function.

By separating the sampling and estimation functions, we allowed the possibility of users implementing more complex sampling scheme, as described in Saarela (2016).

The sampling scheme selected for sampleCaseBase was described in Hanley and Miettinen (2009): we first sample along the "person" axis, proportional to each individual's total follow-up time, and then we sample a moment uniformly over their follow-up time. This sampling scheme is equivalent to the following picture: imagine representing the total follow-up time of all individuals in the study along a single dimension, where the follow-up time of the next individual would start exactly when the follow-up time of the previous individual ends. Then the base series could be sampled uniformly from this one-dimensional representation of the overall follow-up time. In any case, the output is a dataset of the same class as the input, where each row corresponds to a person-moment. The covariate profile for each such person-moment is retained, and an offset term is added to the dataset. This output could then be used to fit a smooth hazard function, or for visualization of the base series.

The fitting function fitSmoothHazard starts by looking at the class of the dataset: if it was generated from sampleCaseBase, it automatically inherited the class cbData. If the dataset supplied to fitSmoothHazard does not inherit from cbData, then the fitting function starts by calling sampleCaseBase to generate the base series. In other words, the occasional user can bypass sampleCaseBase altogether and only worry about the fitting function fitSmoothHazard.

The fitting function retains the familiar formula interface of glm. The left-hand side of the formula should be the name of the column corresponding to the event type. The right-hand side can be any combination of the covariates, along with an explicit functional form for the time variable. Note that non-proportional hazard models can be achieved at this stage by adding an interaction term involving time. The offset term does not need to be specified by the user, as it is automatically added to the formula.

To fit the hazard function, we provide several approaches that are available via the family parameter. These approaches are:

- glm: This is the familiar logistic regression.
- glmnet: This option allows for variable selection using Lasso or elastic-net. This functionality is provided through the glmnet package (Friedman, Hastie, and Tibshirani 2010).

- gam: This option provides support for *Generalized Additive Models* via the gam package (Hastie and Tibshirani 1987).
- gbm: This option provides support for *Gradient Boosted Trees* via the gbm package. This feature is still experimental.

In the case of multiple events, the hazard is fitted via multinomial regression as performed by the **VGAM** package. This package was selected for its ability to fit multinomial regression models with an offset.

Once a model-fit object has been returned by fitSmoothHazard, all the familiar summary and diagnostic functions are available: print, summary, predict, plot, etc. Our package provides one more functionality: it computes risk functions from the model fit. For the case of a single event, it uses the familiar identity

$$S(t) = \exp\left(-\int_0^t h(u; X) du\right).$$

The integral is computed using either the stats::integrate function or Monte-Carlo integration. The risk function (or cumulative incidence function) is then defined as

$$CI(t) = 1 - S(t).$$

For the case of a competing-event analysis, the event-specific risk is computed using the following procedure: first, we compute the overall survival function (i.e. for all event types):

$$S(t) = \exp\left(-\int_0^t H(u;X)du\right), \qquad H(t;X) = \sum_{i=1}^J h_j(t;X).$$

From this, we can derive the event-specific subdensities:

$$f_i(t) = h_i(t)S(t).$$

Finally, by integrating these subdensities, we obtain the event-specific cumulative incidence functions:

$$CI_j(t) = \int_0^t f_j(u) du.$$

We created absoluteRisk as an S3 generic, with methods for the different types of outputs of fitSmoothHazard. The method dispatch system of R then takes care of matching the correct output to the correct methodology for calculating the cumulative incidence function, without the user's intervention.

In the following sections, we illustrate these functionalities in the context of three case studies.

5. Case study 1-European Randomized Study of Prostate Cancer Screening

To introduce the different features available, we make use of the European Randomized Study of Prostate Cancer Screening data; this dataset is available through the **casebase** package:

The results of this study were published by [schroder2009screening]. This data was obtained using the approach described in [liu2014recovering].

Population time plots can be extremely informative graphical displays of survival data. They should be the first step in an exploratory data analysis. We facilitate this task in the **casebase** package using the **popTime** function. We first create the necessary dataset for producing the population time plots, and we can produce the plot by using the corresponding **plot** method:

```
R> pt_object <- casebase::popTime(ERSPC, event = "DeadOfPrCa")
R> plot(pt_object)
```

We can also create exposure stratified plots by specifying the exposure argument in the popTime function:

We can also plot them side-by-side using the ncol argument:

```
R> plot(pt_object_strat, ncol = 2)
```

First, we fit a Cox model to the data, examine the hazard ratio for the screening group (relative to the control group), and plot the cumulative incidence function (CIF).

We can plot the CIF for each group:

```
R> new_data <- data.frame(ScrArm = c("Control group", "Screening group"),</pre>
R>
                           ignore = 99)
R>
R> plot(survfit(cox_model, newdata = new_data),
        xlab = "Years since Randomization",
R>
R.>
        ylab = "Cumulative Incidence",
        fun = "event",
R>
        xlim = c(0,15), conf.int = FALSE, col = c("red", "blue"),
R>
        main = sprintf("Estimated Cumulative Incidence (risk) of Death from Prostate
R.>
                        Cancer Screening group Hazard Ratio: %.2g (%.2g, %.2g)",
R.>
```

```
R>
                        exp(coef(cox_model)),
R.>
                        exp(confint(cox_model))[1],
                        exp(confint(cox_model))[2]))
R>
R>
  legend("topleft",
          legend = c("Control group", "Screening group"),
R>
          col = c("red", "blue"),
R>
R>
          1ty = c(1, 1),
          bg = "gray90")
R>
```

Next we fit several models using case-base sampling. The models we fit differ in how we choose to model time.

The fitSmoothHazard function provides an estimate of the hazard function h(x,t) is the hazard function, where t denotes the numerical value of a point in prognostic/prospective time and x is the realization of the vector X of variates based on the patient's profile and intervention (if any).

The absoluteRisk function provides an estimate of the cumulative incidence curves for a specific risk profile using the following equation:

$$CI(x,t) = 1 - \exp\left(-\int_0^t h(x,u)du\right)$$

In the plot below, we overlay the estimated CIF from the casebase exponential model on the Cox model CIF:

```
R> smooth_risk_exp <- casebase::absoluteRisk(object = casebase_exponential,
R>
                                               time = seq(0, 15, 0.1),
                                               newdata = new_data)
R>
R.>
R> plot(survfit(cox_model, newdata = new_data),
R>
        xlab = "Years since Randomization",
        ylab = "Cumulative Incidence",
R>
        fun = "event",
R.>
        xlim = c(0,15), conf.int = FALSE, col = c("red","blue"),
R.>
R.>
        main = sprintf("Estimated Cumulative Incidence (risk) of Death from Prostate
                        Cancer Screening group Hazard Ratio: %.2g (%.2g, %.2g)",
R>
R>
                        exp(coef(cox_model)),
                        exp(confint(cox_model))[1],
R.>
                        exp(confint(cox_model))[2]))
R.>
```

As we can see, the exponential model is not a good fit. Based on what we observed in the population time plot, where more events are observed later on in time, this poor fit is expected. A constant hazard model would overestimate the cumulative incidence earlier on in time, and underestimate it later on; this is what we see on the cumulative incidence plot. This example demonstrates the benefits of population time plots as an exploratory analysis tool.

Next we enter time linearly into the model:

```
R> casebase_time <- fitSmoothHazard(DeadOfPrCa ~ Follow.Up.Time + ScrArm,
R>
                                     data = ERSPC,
R>
                                     ratio = 100)
R.>
R> summary(casebase_time)
R> exp(coef(casebase_time))
R> exp(confint(casebase_time))
R> smooth_risk_time <- casebase::absoluteRisk(object = casebase_time,
R>
                                              time = seq(0,15,0.1),
R.>
                                              newdata = new_data)
R>
R> plot(survfit(cox_model, newdata = new_data),
        xlab = "Years since Randomization",
R>
        ylab = "Cumulative Incidence",
R>
        fun = "event",
R>
        xlim = c(0,15), conf.int = FALSE, col = c("red","blue"),
R.>
R>
        main = sprintf("Estimated Cumulative Incidence (risk) of Death from Prostate
R>
                        Cancer Screening group Hazard Ratio: %.2g (%.2g, %.2g)",
R>
                        exp(coef(cox_model)),
R.>
                        exp(confint(cox_model))[1],
                        exp(confint(cox_model))[2]))
R>
R> lines(smooth_risk_time[,1], smooth_risk_time[,2], col = "red", lty = 2)
R> lines(smooth_risk_time[,1], smooth_risk_time[,3], col = "blue", lty = 2)
R>
R> legend("topleft",
          legend = c("Control group (Cox)", "Control group (Casebase)",
R>
```

We see that the Weibull model leads to a better fit.

Next we try to enter a smooth function of time into the model using the splines package:

```
R> casebase_splines <- fitSmoothHazard(DeadOfPrCa ~ bs(Follow.Up.Time) + ScrArm,</pre>
R>
                                        data = ERSPC,
                                         ratio = 100)
R>
R>
R> summary(casebase_splines)
R> exp(coef(casebase_splines))
R> exp(confint(casebase_splines))
R> smooth_risk_splines <- absoluteRisk(object = casebase_splines,</pre>
R>
                                         time = seq(0,15,0.1),
R>
                                         newdata = new_data)
R>
R> plot(survfit(cox_model, newdata = new_data),
R>
        xlab = "Years since Randomization",
        ylab = "Cumulative Incidence",
R>
R>
        fun = "event",
R>
        xlim = c(0,15), conf.int = FALSE, col = c("red","blue"),
R>
        main = sprintf("Estimated Cumulative Incidence (risk) of Death from Prostate
R>
                        Cancer Screening group Hazard Ratio: %.2g (%.2g, %.2g)",
                        exp(coef(cox_model)),
R>
R.>
                        exp(confint(cox_model))[1],
R>
                        exp(confint(cox_model))[2]))
R> lines(smooth_risk_splines[,1], smooth_risk_splines[,2], col = "red", lty = 2)
R> lines(smooth_risk_splines[,1], smooth_risk_splines[,3], col = "blue", lty = 2)
R.>
R> legend("topleft",
R>
          legend = c("Control group (Cox)", "Control group (Casebase)",
                      "Screening group (Cox)", "Screening group (Casebase)"),
R>
          col = c("red", "red", "blue", "blue"),
R.>
R>
          1ty = c(1, 2, 1, 2),
          bg = "gray90")
R>
```

It looks like the best fit.

Since we are within the GLM framework, we can easily test for which model better fits the data using a Likelihood Ratio Test (LRT). The null hypothesis here is that the linear model is just as good as the larger (in terms of number of parameters) splines model.

```
R> anova(casebase_time, casebase_splines, test = "LRT")
```

As expected, we see that splines model provides a better fit.

6. Case study 2-Bone-marrow transplant

The next example shows how case-base sampling can also be used in the context of a competing risk analysis. For illustrative purposes, we will use the same data that was used in Scrucca et al (2010). The data was downloaded from the main author's website, and it is also available as part of the **casebase** package.

R> data(bmtcrr)

The data contains information on 177 patients who received a stem-cell transplant for acute leukemia. The event of interest is relapse, but other competing causes (e.g. transplant-related death) were also recorded Several covariates were also captured at baseline: sex, disease type (acute lymphoblastic or myeloblastic leukemia, abbreviated as ALL and AML, respectively), disease phase at transplant (Relapse, CR1, CR2, CR3), source of stem cells (bone marrow and peripheral blood, coded as BM+PB, or only peripheral blood, coded as PB), and age. A summary of these baseline characteristics appear in Table 3. We note that the statistical summaries were generated differently for different variable types: for continuous variables, we gave the range, followed by the mean and standard deviation; for categorical variables, we gave the counts for each category.

Variable	Description	Statistical summary
Sex	Sex	M=Male (100)
		F=Female (77)
D	Disease	ALL (73)
		AML (104)
Phase	Phase	CR1 (47)
		CR2 (45)
		CR3 (12)
		Relapse (73)
Source	Type of transplant	BM+PB (21)
		PB (156)
Age	Age of patient (years)	4 – 62
		30.47 (13.04)
Ftime	Failure time (months)	0.13 – 131.77
		20.28 (30.78)
Status	Status indicator	0=censored (46)
		1 = relapse (56)
		2=competing event (75)

Table 3: Baseline characteristics of patients in the stem-cell transplant study.

In order to try and visualize the incidence density of relapse, we can look at the corresponding population-time plot. In Figure ??, failure times associated with relapse are highlighted on the plot using red points, while Figure ?? provides a similar population-time plot for competing events.

Our main objective is to compute the absolute risk of relapse for a given set of covariates. First, we fit a smooth hazard to the data; for the sake of this example, we opted for a linear term for time:

```
R> model_cb <- fitSmoothHazard(
R>         Status ~ ftime + Sex + D + Phase + Source + Age,
R>         data = bmtcrr,
R>         ratio = 100,
R>         time = "ftime")
```

From the fit object, we can extract both the hazard ratios and their corresponding confidence intervals:

As we can see, the only significant hazard ratio is the one associated with the phase of the disease at transplant. More precisely, being in relapse at transplant is associated with a hazard ratio of 3.92 when compared to CR1.

Given our estimate of the hazard function, we can compute the absolute risk curve for a fixed covariate profile. We performed this computation for a 35 year old woman who received a stem-cell transplant from peripheral blood at relapse. We compared the absolute risk curve for such a woman with acute lymphoblastic leukemia with that for a similar woman with acute myeloblastic leukemia. Figure ?? shows these two curves as a function of time. This figure also shows the Kaplan-Meier estimate fitted to the two disease groups (ignoring the other covariates).

```
R> # Pick 100 equidistant points between 0 and 60 months
R> time_points <- seq(0, 60, length.out = 50)
R>
R> # Data.frame containing risk profile
R> newdata <- data.frame("Sex" = factor(c("F", "F"),</pre>
                                          levels = levels(bmtcrr[, "Sex"])),
R>
                          "D" = c("ALL", "AML"),
R>
                          "Phase" = factor(c("Relapse", "Relapse"),
R>
                                            levels = levels(bmtcrr[,"Phase"])),
R>
                          "Age" = c(35, 35),
R>
R.>
                          "Source" = factor(c("PB", "PB"),
                                             levels = levels(bmtcrr[, "Source"])))
R>
R>
R> # Estimate absolute risk curve
R> risk_cb <- absoluteRisk(object = model_cb, time = time_points,</pre>
R>
                            method = "numerical", newdata = newdata)
```

se study 3-Study to Understand Prognoses Preferences Outcomes and Risks of Trea

We examined the Study to Understand Prognoses Preferences Outcomes and Risks of Treatment (SUPPORT) dataset (REF from main site). the SUPPORT dataset tracks death for individuals who are considered seriously ill within a hospital. Imputation was conducted using

the default methods in the mice package in R, available on CRAN. Before imputation, there was a total of 1000 individuals and 35 variables. After imputation, we have 474 observations where 67.5% of individuals in the study experience the event of interest. The SUPPORT dataset will be used to demonstrate regularization within casebase (REF), while comparing their absolute risk preditions for a new individual. A description of each variable can be found in Table 4 and a breakdown of each categorical variable in Table 5. The data was downloaded from the main author's website, and it is also available as part of the casebase package.

Hospital death as a covariate was removed, as this is directly informative of death. The glmnet package(REF) on CRAN was used to introduce elastic net, lasso and ridge regressions to casebase. To visualize the effect of imputation on incidence density, we can refer to the pre-imputation population-time plot in Figure ?? and post-imputation population time plot in Figure ??. The incidence density is consistent between imputed and complete datasets.

```
R> #demonstrating incidence density before imputation
R> plot(casebase::popTime(as.data.frame(support), time = "d.time", event = "death"))
R> #demonstrating incidence density after imputation
```

R> plot(casebase::popTime(as.data.frame(workingCompleteData),time = "d.time",event = "deat

Our main objective is to compute the absolute risk of death for a given set of covariates, using regularization when fitting our model. First, we fit a smooth hazard to the data; for the sake of this example, we opted for a linear term for time. As casebase makes use of the glmnet package, we interact with the fitsmoothhazard.fit function using a matrix interface, where y contains the time and event variables and x contains all other variables we would like to include in the model. For the SUPPORT dataset, all factor variables were converted into

dummy variables. Here, we used lasso penalization by setting alpha to 1.

```
R> #Using casebase's glmnet implementation, using splines and a case to base ratio of 100,
R> #to determine the hazard function
R> cb.Model=casebase::fitSmoothHazard.fit(x,y,family="glmnet",time="d.time",event="death",
R> formula_time = ~d.time,alpha=1,ratio=100)
```

Then, we take our model and use the absoluteRisk function to integrate and retrieve our absolute risk function.

We will compare this curve to a regularized version of cox regression, and a kaplan-meier survival curve. The regularized cox regression absolute risk curve required two extra steps to retrive. Coxnet from the glmnet package has tools to fit a regularized cox model, but requires that a survival object skeleton of the selected variables, so that the survival package tools can be used to retrive the absolute risk. We handle this by fitting a regularized cox model with the glmnet package, and a cox model from the survival package with the selected variables from

the regularized fit. This second model serves as a skeleton that permits the use of survival package functions. The coefficients from the regularized model will replace the coefficients in our skeleton, the resulting model will have the correct coefficients when integrating, but will have an incorrect standard error. For the purposes of this case study, we are only interested in the absolute risk curve itself and not the standard error.

```
R> #Create u and xCox, which will be used when fitting Cox with glmnet.
R> u=survival::Surv(time = as.numeric(y[,2]), event = as.factor(y[,1]))
R> xCox=as.matrix(sparse.model.matrix(death~.-d.time,data=completeData))[-c(sam),]
R> #hazard for cox using glmnet
R> coxglmFit=glmnet::cv.glmnet(x=xCox,y=u, family="cox",alpha=1)
R> #convergence demonstrated in plot
R> plot(coxglmFit)
R> #taking the coefficient estimates for later use
R> nonzero_covariate_cox <- predict(coxglmFit, type = "nonzero", s = "lambda.1se")</pre>
R> nonzero_coef_cox <- coef(coxglmFit, s = "lambda.1se")</pre>
R> #creating a new dataset that only contains the covariates chosen through glmnet.
R> #cleanCoxData<- as.data.frame(cbind(as.numeric(workingData$d.time),as.factor(workingData
R> cleanCoxData<-as.data.frame(cbind(as.numeric(y[,2]),as.numeric(y[,1]),xCox[,nonzero_cov
R> #newDataCox<-xCox[sam,nonzero_covariate_cox$X1]</pre>
R> #fitting a cox model using regular estimation, however we will not keep it.
R> #this is used more as an object place holder.
R> coxFit <- survival::coxph(Surv(time=V1,event=V2) ~ ., data = cleanCoxData)</pre>
R> #The coefficients of this object will be replaced with the estimates from coxglmFit.
R> #Doing so makes it so that everything is invalid aside from the coefficients.
R> #In this case, all we need to estimate the absolute risk is the coefficients.
R> #Std. error would be incorrect here, if we were to draw error bars.
R> coxFit$coefficients<-nonzero_coef_cox@x</pre>
R> #Fitting absolute risk curve for cox+glmnet
R> newDataCox=newData[nonzero_covariate_cox$X1-1]
R>
R> abCoxFit<-survival::survfit(coxFit,newdata=as.data.frame(t(newDataCox)),time = seq(0,ma</pre>
We used the survival package to calculate the kaplan-meier absolute risk function.
R> #creating a surv object to be used to fit an unadjusted absolute risk curve.
```

Now that our three absolute risk functions have been calculated, we compare them all in Figure ??. Both coxnet and casebase decrease the absolute risk by the end of the study, in comparison to kaplan-meier.

R> km <- survival::Surv(time = completeData\$d.time, event = completeData\$death)

R> abKm<-survival::survfit(km~1,type='kaplan-meier',conf.type='log')</pre>

R> # (Kaplan-Meier risk curve)

```
R> # A plot to compare all three Absolute risk (Commulative Incidence)
R> plot(casebaseAbsolute,type='l',col="black",lwd=2,main="Support- CaseBase vs. Cox+glmnet
```

```
R> lines(abCoxFit ,col="red",fun="event",lwd=3,conf.int = FALSE)
R> lines(abKm ,col="Blue",fun="event",lwd=3,conf.int = FALSE)
R> legend("bottom",
R> legend = c( "Casebase (Lasso+linear)", "semi-parametric (Cox)+glmnet", "KM curve")
R> col = c("black", "red", "Blue"),
R> lty = c(1, 1, 1),
By = "gray90")
```

8. Case study 4–Stanford Heart Transplant Data

Although the previous case studies provide a broad overview of the capabilities of **casebase**, they all have two properties in common:

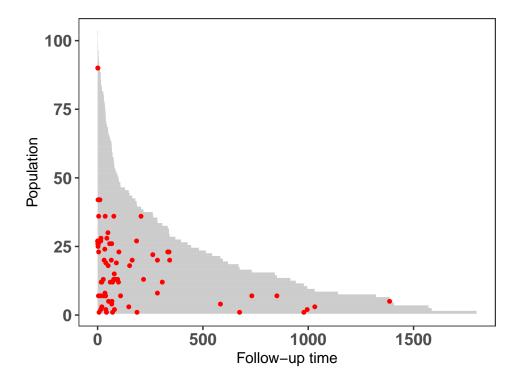
- All covariates are fixed, i.e. they do not change over time;
- The estimated hazard functions satisfy the "proportional hazard" assumption.

Case-base sampling has been used in the literature to study vaccination safety, where the exposure period was defined as the week following vaccination (Saarela and Hanley 2015). Hence, the main covariate of interest, i.e. exposure to the vaccine, was changing over time. In this context, case-base sampling offers an efficient alternative to nested case-control designs or self-matching.

The purpose of the next case study is to show how **casebase** can also be used for survival analysis problems that do not share the properties above. To this end, we will use the Stanford Heart Transplant Data (Clark, Stinson, Griepp, Schroeder, Shumway, and Harrison 1971, Crowley and Hu (1977)); we will use the version available in the **survival** package.

Recall the setting of this study: patients were admitted to the Stanford program after meeting with their physician and determining that they were unlikely to respond to other forms of treatment. After enrollment, the program searches for a suitable donor for the patient, which can take anywhere between a few days to almost a year. We are interested in the effect of a heart transplant on survival; therefore, the patient is considered exposed only after the transplant has occurred.

As before, we can look at the population-time plot for a graphical summary of the event incidence. As we can see, most events occur early during the follow-up period, and therefore we do not expect the hazard to be constant.



Since the exposure is time-dependent, we need to manually define the exposure variable *after* case-base sampling and *before* fitting the hazard function. For this reason, we will use the sampleCaseBase function directly.

Next, we will compute the number of days from acceptance into the program to transplant, and we use this variable to determine whether each population-moment is exposed or not.

```
R> # Define exposure variable
R> cb_data <- mutate(cb_data,
                      txtime = time_length(accept.dt %--% tx.date,
R+
                                            unit = "days"),
R+
R+
                      exposure = case_when(
R+
                        is.na(txtime) ~ OL,
R+
                        txtime > futime ~ OL,
                        txtime \le futime ~1L
R+
                      ))
R+
```

Finally, we can fit the hazard using various linear predictors.

```
R> library(splines)
R> # Fit several models
```

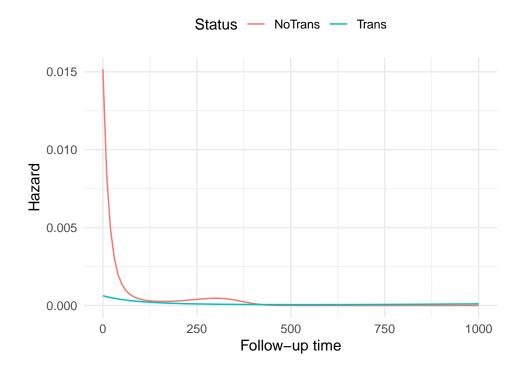
Note that the fourth model (i.e. fit4) includes an interaction term between exposure and follow-up time. In other words, this model no longer exhibit proportional hazards. The evidence of non-proportionality of hazards in the Stanford Heart Transplant data has been widely discussed (Arjas 1988).

We can then compare the goodness of fit of these four models using the Akaike Information Criterion (AIC).

As we can, the best fit is the fourth model. By visualizing the hazard functions for both exposed and unexposed individuals, we can more clearly see how the hazards are no longer proportional.

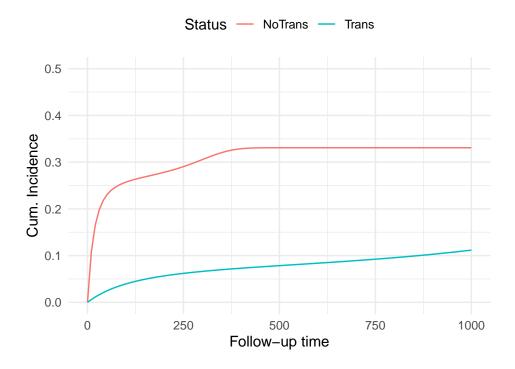
```
R> # Compute hazards---
R> # First, create a list of time points for both exposure status
R > hazard_data <- expand.grid(exposure = c(0, 1),
                              futime = seq(0, 1000,
R+
R+
                                            length.out = 100))
R> # Set the offset to zero
R> hazard_data$offset <- 0
R> # Use predict to get the fitted values, and exponentiate to
R> # transform to the right scale
R> hazard_data$hazard = exp(predict(fit4, newdata = hazard_data,
R+
                                     type = "link"))
R> # Add labels for plots
R> hazard_data$Status = factor(hazard_data$exposure,
R+
                               labels = c("NoTrans", "Trans"))
R>
R> ggplot(hazard_data, aes(futime, hazard, colour = Status)) +
R+
       geom_line() +
```

```
R+ theme_minimal() +
R+ theme(legend.position = 'top') +
R+ ylab('Hazard') + xlab('Follow-up time')
```



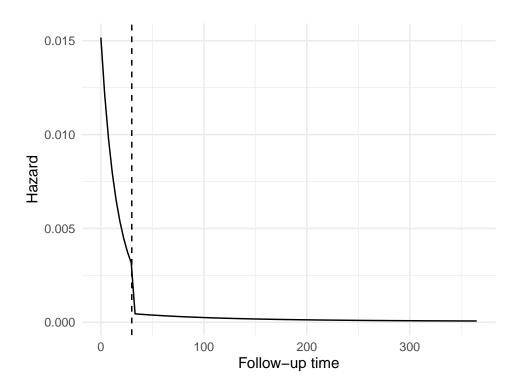
The non-proportionality seems to be more pronounced at the beginning of follow-up than the end. Finally, we can turn these estimate of the hazard function into estimates of the cumulative incidence functions.

```
R> # Compute absolute risk curves
R> newdata <- data.frame(exposure = c(0, 1))
R> absrisk <- absoluteRisk(fit4, newdata = newdata,
                            time = seq(0, 1000, length.out = 100))
R+
R>
R> colnames(absrisk) <- c("Time", "NoTrans", "Trans")</pre>
R>
R> # Rearrange the data
R> absrisk <- gather(as.data.frame(absrisk),</pre>
                      "Status", "Risk", -Time)
R+
R>
R> ggplot(absrisk, aes(Time, Risk, colour = Status)) +
R.+
     geom_line() +
     theme_minimal() +
R+
     theme(legend.position = 'top') +
R+
     expand_limits(y = 0.5) +
R+
     xlab('Follow-up time') + ylab('Cum. Incidence')
R+
```



Note that we can easily adapt the code above to the situation where a patient receives a heart transplant at a point in time of interest, for example after 30 days.

```
R> # Compute hazards---
R> # First, create a list of time points for both exposure status
R> one_yr_haz <- data.frame(futime = seq(0, 365,</pre>
R+
                                           length.out = 100))
R> one_yr_haz <- mutate(one_yr_haz,</pre>
R+
                         offset = 0,
                         exposure = if_else(futime < 30, 0, 1))</pre>
R+
R> one_yr_haz$hazard = exp(predict(fit4, newdata = one_yr_haz,
                                     type = "link"))
R+
R> ggplot(one_yr_haz, aes(futime, hazard)) +
     geom_line() +
R+
R+
     theme_minimal() +
     theme(legend.position = 'top') +
R+
     ylab('Hazard') + xlab('Follow-up time') +
R+
     geom_vline(xintercept = 30, linetype = 'dashed')
R+
```



We can then compare the 1-year mortality risk without transplant and with transplant at 30 days.

As we can see, the risk estimate at 1-year is about 30% lower if the patient receives a heart transplant at 30 days.

9. Discussion

In this article, we presented the R package casebase that provides functions to fit smooth parametric hazards and estimate cumulative incidence functions using case-base sampling.

We outlined the theoretical underpinnings of the approach, we provided details about our implementation, and we illustrated the merits of the approach and the package through three case studies.

In the following table we provide a comparison between the Cox model and case-base sampling:

10. Environment Details

This report was generated on 2019-12-08 12:31:41 using the following computational environment and dependencies:

```
R> # which R packages and versions?
R> devtools::session_info()
#> - Session info -----
#>
   setting value
#>
   version R version 3.6.1 (2019-07-05)
            Ubuntu 18.04.3 LTS
#>
            x86_64, linux-gnu
#>
   system
#>
   ui
            X11
   language (EN)
#>
#>
   collate en_CA.UTF-8
            en_CA.UTF-8
#>
   ctype
#>
            America/Winnipeg
   tz
#>
   date
            2019-12-08
#>
#>
   package
               * version
                           date
                                      lib source
   assertthat
#>
                 0.2.1
                           2019-03-21 [1] CRAN (R 3.6.1)
#>
   backports
                 1.1.5
                           2019-10-02 [1] CRAN (R 3.6.1)
#>
   broom
                 0.5.2
                           2019-04-07 [1] CRAN (R 3.6.1)
                           2019-07-18 [1] CRAN (R 3.6.1)
#>
   callr
                 3.3.1
#>
   casebase
               * 0.2.1.9001 2019-07-29 [1] local
                           2016-07-27 [1] CRAN (R 3.5.0)
#>
   cellranger
                 1.1.0
#>
   cli
                 1.1.0
                           2019-03-19 [1] CRAN (R 3.6.1)
                           2018-12-24 [4] CRAN (R 3.5.2)
#>
   codetools
                 0.2-16
#>
   colorspace
                 1.4-1
                           2019-03-18 [1] CRAN (R 3.6.1)
                           2017-09-16 [1] CRAN (R 3.5.0)
#>
   crayon
                 1.3.4
#>
   data.table
                 1.12.2
                           2019-04-07 [1] CRAN (R 3.6.1)
#>
   desc
                 1.2.0
                           2018-05-01 [1] CRAN (R 3.5.0)
                           2019-07-06 [1] CRAN (R 3.6.1)
#>
   devtools
                 2.1.0
                 0.6.22
                           2019-10-21 [1] CRAN (R 3.6.1)
#>
   digest
   dplyr
#>
               * 0.8.3
                           2019-07-04 [1] CRAN (R 3.6.1)
                 0.3.0
                           2019-09-20 [1] CRAN (R 3.6.1)
#>
   ellipsis
#>
   evaluate
                 0.14
                           2019-05-28 [1] CRAN (R 3.6.1)
#> forcats
               * 0.4.0
                           2019-02-17 [1] CRAN (R 3.6.1)
                           2017-12-12 [1] CRAN (R 3.5.0)
#> foreach
               * 1.4.4
```

```
#>
                  1.3.1
                              2019-05-06 [1] CRAN (R 3.6.1)
   fs
#>
                  0.0.2
                              2018-11-29 [1] CRAN (R 3.6.1)
   generics
                * 3.2.1
                              2019-08-10 [1] CRAN (R 3.6.1)
#>
   ggplot2
#>
   glmnet
                * 2.0-18
                              2019-05-20 [1] CRAN (R 3.6.1)
#>
                              2019-03-12 [1] CRAN (R 3.6.1)
   glue
                  1.3.1
#>
                  0.3.0
                              2019-03-25 [1] CRAN (R 3.6.1)
   gtable
#>
   haven
                  2.1.1
                              2019-07-04 [1] CRAN (R 3.6.1)
#>
                  0.5.2
                              2019-10-30 [1] CRAN (R 3.6.1)
   hms
#>
   htmltools
                  0.3.6
                              2017-04-28 [1] CRAN (R 3.5.0)
#>
   httr
                  1.4.1
                              2019-08-05 [1] CRAN (R 3.6.1)
                              2017-12-12 [1] CRAN (R 3.5.0)
#>
   iterators
                  1.0.9
#>
                  1.6
                              2018-12-07 [1] CRAN (R 3.6.1)
   jsonlite
                              2019-05-18 [1] CRAN (R 3.6.1)
#>
   knitr
                  1.23
#>
                  0.3
                              2014-08-23 [1] CRAN (R 3.5.0)
   labeling
                              2018-11-04 [4] CRAN (R 3.5.1)
#>
   lattice
                  0.20 - 38
#>
   lazyeval
                  0.2.2
                              2019-03-15 [1] CRAN (R 3.6.1)
#>
   lifecycle
                  0.1.0
                              2019-08-01 [1] CRAN (R 3.6.1)
#>
   lubridate
                * 1.7.4
                              2018-04-11 [1] CRAN (R 3.5.0)
#>
                              2014-11-22 [1] CRAN (R 3.5.0)
   magrittr
                * 1.5
                              2019-11-27 [4] CRAN (R 3.6.1)
#>
   Matrix
                * 1.2-18
#>
                  1.1.0
                              2017-04-21 [1] CRAN (R 3.5.0)
   memoise
#>
   mgcv
                  1.8-24
                              2018-06-18 [1] CRAN (R 3.5.1)
   modelr
                  0.1.5
                              2019-08-08 [1] CRAN (R 3.6.1)
#>
#>
                  0.5.0
                              2018-06-12 [1] CRAN (R 3.6.1)
   munsell
#>
   nlme
                  3.1-142
                              2019-11-07 [4] CRAN (R 3.6.1)
                              2019-06-29 [1] CRAN (R 3.6.1)
#>
   pillar
                  1.4.2
#>
                  1.0.3
                              2019-03-20 [1] CRAN (R 3.6.1)
   pkgbuild
#>
   pkgconfig
                  2.0.3
                              2019-09-22 [1] CRAN (R 3.6.1)
#>
   pkgload
                  1.0.2
                              2018-10-29 [1] CRAN (R 3.6.1)
                              2015-07-13 [1] CRAN (R 3.5.2)
#>
   prettyunits
                  1.0.2
#>
                  3.4.1
                              2019-07-18 [1] CRAN (R 3.6.1)
   processx
                              2018-12-21 [1] CRAN (R 3.6.1)
#>
                  1.3.0
   ps
#>
   purrr
                * 0.3.3
                              2019-10-18 [1] CRAN (R 3.6.1)
                              2019-11-12 [1] CRAN (R 3.6.1)
#>
   R6
                  2.4.1
#>
                  1.0.3
                              2019-11-08 [1] CRAN (R 3.6.1)
   Rcpp
#>
   readr
                * 1.3.1
                              2018-12-21 [1] CRAN (R 3.6.1)
#>
                  1.3.1
                              2019-03-13 [1] CRAN (R 3.6.1)
   readxl
                              2019-06-24 [1] CRAN (R 3.6.1)
#>
   remotes
                  2.1.0
#>
                  0.4.1
                              2019-10-24 [1] CRAN (R 3.6.1)
   rlang
                  1.16
                              2019-10-01 [1] CRAN (R 3.6.1)
#>
   rmarkdown
#>
   rprojroot
                  1.3 - 2
                              2018-01-03 [1] CRAN (R 3.5.0)
                              2019-03-19 [1] CRAN (R 3.6.1)
#> rstudioapi
                  0.10
#> rticles
                  0.9.1
                              2019-07-22 [1] Github (rstudio/rticles@8d56fc6)
#> rvest
                              2019-11-08 [1] CRAN (R 3.6.1)
                  0.3.5
#>
   scales
                  1.0.0
                              2018-08-09 [1] CRAN (R 3.6.1)
                             2018-11-05 [1] CRAN (R 3.6.1)
#>
   sessioninfo
                  1.1.1
                              2019-03-12 [1] CRAN (R 3.6.1)
#>
   stringi
                  1.4.3
```

```
* 1.4.0
                             2019-02-10 [1] CRAN (R 3.6.1)
#>
   stringr
#>
                * 2.44-1.1
                             2019-04-01 [4] CRAN (R 3.6.1)
   survival
                             2019-07-22 [1] CRAN (R 3.6.1)
#>
   testthat
                  2.2.0
#>
   tibble
                * 2.1.3
                             2019-06-06 [1] CRAN (R 3.6.1)
   tidyr
                * 1.0.0
                             2019-09-11 [1] CRAN (R 3.6.1)
#>
                  0.2.5
                             2018-10-11 [1] CRAN (R 3.5.2)
#>
   tidyselect
                * 1.2.1
#>
   tidyverse
                             2017-11-14 [1] CRAN (R 3.5.0)
#>
                  1.5.1
                             2019-07-04 [1] CRAN (R 3.6.1)
   usethis
#>
   vctrs
                  0.2.0
                             2019-07-05 [1] CRAN (R 3.6.1)
#>
   VGAM
                  1.1-1
                             2019-02-18 [1] CRAN (R 3.6.1)
                  2.1.2
                             2018-03-15 [1] CRAN (R 3.5.0)
#>
   withr
#>
   xfun
                  0.8
                             2019-06-25 [1] CRAN (R 3.6.1)
                  1.2.2
                             2019-08-09 [1] CRAN (R 3.6.1)
#>
   xm12
#>
                  2.2.0
                             2018-07-25 [1] CRAN (R 3.6.1)
   yaml
   zeallot
                  0.1.0
                             2018-01-28 [1] CRAN (R 3.5.1)
#>
#>
#> [1] /home/mturgeon/Rlibs
```

- #> [2] /usr/local/lib/R/site-library
- #> [3] /usr/lib/R/site-library
- #> [4] /usr/lib/R/library

The current Git commit details are:

```
R> # what commit is this file at?
R> git2r::repository(here::here())
```

#> Local: review-max /home/mturgeon/Documents/git_repositories/cbpaper

#> Head: [69663bb] 2019-12-08: Merge branch 'review-max' of https://github.com/sahirbh

References

Allignol A, Latouche A (2019). "CRAN Task View: Survival Analysis." URL https://cran.r-project.org/web/views/Survival.html.

Arjas E (1988). "A graphical method for assessing goodness of fit in Cox's proportional hazards model." *Journal of the American Statistical Association*, **83**(401), 204–212.

Clark DA, Stinson EB, Griepp RB, Schroeder JS, Shumway NE, Harrison D (1971). "Cardiac transplantation in man." Annals of Internal Medicine, **75**(1), 15–21.

Clements M, Liu XR, Lambert P, Jakobsen LH, Gasparini A, Smyth G, Alken P, Wood S, Ulerich R (2019). "Smooth Survival Models, Including Generalized Survival Models [R package rstpm2 version 1.5.1]." URL https://cran.r-project.org/web/packages/rstpm2/index.html.

- Clerc-Urmà s I, Grzebyk M, HÃ ©delin G, CENSUR working survival group (2017). flexr-surv: An R package for relative survival analysis. R package version 1.4.1, URL https://CRAN.R-project.org/package=flexrsurv.
- Crowley J, Hu M (1977). "Covariance analysis of heart transplant survival data." *Journal of the American Statistical Association*, **72**(357), 27–36.
- Friedman J, Hastie T, Tibshirani R (2010). "Regularization Paths for Generalized Linear Models via Coordinate Descent." *Journal of Statistical Software*, **33**(1). ISSN 1548-7660. doi:10.18637/jss.v033.i01.
- Fu Z (????). "Package crrp." URL https://cran.r-project.org/web/packages/crrp/index.html.
- Gerds TA, Blanche P, Mortersen R, Tollenaar N, Mogensen UB, Ozenne B (2019). "Risk Regression Models and Prediction Scores for Survival Analysis with Competing Risks [R package riskRegression version 2019.11.03]." URL https://CRAN.R-project.org/package=riskRegression.
- Goeman J, Meijer R, Chaturvedi N, Lueder M (2019). "Package penalized." URL https://cran.r-project.org/web/packages/penalized/index.html.
- Goeman JJ (2010). "L1 penalized estimation in the Cox proportional hazards model." Biometrical Journal, (52), -14.
- Hanley JA, Miettinen OS (2009). "Fitting smooth-in-time prognostic risk functions via logistic regression." The International Journal of Biostatistics, 5(1).
- Hastie T, Tibshirani R (1987). "Generalized additive models: some applications." *Journal of the American Statistical Association*, **82**(398), 371–386.
- Jackson C (2016). "flexsurv: A Platform for Parametric Survival Modeling in R." *Journal of Statistical Software*, **70**(8), 1–33. doi:10.18637/jss.v070.i08.
- Park MY, Hastie T (2018). "Package glmpath." URL https://CRAN.R-project.org/package=glmpath.
- Perperoglou A (2015). "Package CoxRidge." URL https://CRAN.R-project.org/package=CoxRidge.
- Saarela O (2016). "A case-base sampling method for estimating recurrent event intensities." *Lifetime data analysis*, **22**(4), 589–605.
- Saarela O, Arjas E (2015). "Non-parametric Bayesian Hazard Regression for Chronic Disease Risk Assessment." Scandinavian Journal of Statistics, 42(2), 609–626.
- Saarela O, Hanley JA (2015). "Case-base methods for studying vaccination safety." *Biometrics*, **71**(1), 42–52.
- Scheike TH, Holst KK, Hjelmborg JB (2014). "Estimating twin concordance for bivariate competing risks twin data." *Statistics in medicine*, **33**(7), 1193–1204.

Scrucca L, Santucci A, Aversa F (2010). "Regression modeling of competing risk using R: an in depth guide for clinicians." *Bone marrow transplantation*, **45**(9), 1388.

Sharabiani MT, Mahani AS (2019). "Package CFC." URL https://cran.r-project.org/web/packages/CFC/index.html.

Simon N, Friedman J, Hastie T, Tibshirani R (2011). "Regularization Paths for Cox's Proportional Hazards Model via Coordinate Descent." *Journal of Statistical Software*, **39**(5), 1–13. URL http://www.jstatsoft.org/v39/i05/.

Therneau TM (2015). A Package for Survival Analysis in S. Version 2.38, URL https://CRAN.R-project.org/package=survival.

Touraine C, Gerds TA, Joly P (2017). "SmoothHazard: An R Package for Fitting Regression Models to Interval-Censored Observations of Illness-Death Models." *Journal of Statistical Software*, **79**(7), 1–22. doi:10.18637/jss.v079.i07.

Yi Y, Zou H (????). "Package fastcox." URL https://cran.r-project.org/web/packages/fastcox/index.html.

Affiliation:

Sahir Bhatnagar * McGill University

1020 Pine Avenue West Montreal, QC, Canada H3A 1A2

E-mail: sahir.bhatnagar@mail.mcgill.ca

URL: http://sahirbhatnagar.com/

Maxime Turgeon * University of Manitoba

186 Dysart Road Winnipeg, MB, Canada R3T 2N2

E-mail: max.turgeon@umanitoba.ca URL: https://maxturgeon.ca/

Jesse Islam

McGill University

1020 Pine Avenue West Montreal, QC, Canada H3A 1A2

E-mail: jesse.islam@mail.mcgill.ca

James Hanley McGill University

1020 Pine Avenue West Montreal, QC, Canada H3A 1A2

E-mail: james.hanley@mcgill.ca

 $\label{eq:url:http://www.medicine.mcgill.ca/epidemiology/hanley/} URL: \verb|http://www.medicine.mcgill.ca/epidemiology/hanley/|$

Olli Saarela

University of Toronto

Dalla Lana School of Public Health, 155 College Street, 6th floor, Toronto, Ontario M5T

3M7, Canada

E-mail: olli.saarela@utoronto.ca

URL: http://individual.utoronto.ca/osaarela/

doi:10.18637/jss.v000.i00

http://www.jstatsoft.org/ http://www.foastat.org/

> Submitted: yyyy-mm-dd Accepted: yyyy-mm-dd

Name	Labels	Levels	Storage	NAs
age	Age		double	0
death	Death at any time up to NDI date:31DEC94		double	0
sex		2	integer	0
hospdead	Death in Hospital		double	0
slos	Days from Study Entry to Discharge		double	0
d.time	Days of Follow-Up		double	0
dzgroup		8	integer	0
dzclass		4	integer	0
num.co	number of comorbidities		double	0
edu	Years of Education		double	202
income		4	integer	349
scoma	SUPPORT Coma Score based on Glasgow D3		double	0
charges	Hospital Charges		double	25
totcst	Total RCC cost		double	105
totmcst	Total micro-cost		double	372
avtisst	Average TISS, Days 3-25		double	6
race		5	integer	5
$_{ m meanbp}$	Mean Arterial Blood Pressure Day 3		double	0
wblc	White Blood Cell Count Day 3		double	24
hrt	Heart Rate Day 3		double	0
resp	Respiration Rate Day 3		double	0
$_{ m temp}$	Temperature (celcius) Day 3		double	0
pafi	PaO2/(.01*FiO2) Day 3		double	253
alb	Serum Albumin Day 3		double	378
bili	Bilirubin Day 3		double	297
crea	Serum creatinine Day 3		double	3
sod	Serum sodium Day 3		double	0
ph	Serum pH (arterial) Day 3		double	250
glucose	Glucose Day 3		double	470
bun	BUN Day 3		double	455
urine	Urine Output Day 3		double	517
adlp	ADL Patient Day 3		double	634
adls	ADL Surrogate Day 3		double	310
sfdm2		5	integer	159
adlsc	Imputed ADL Calibrated to Surrogate		double	0

Table 4: A description of each variable in the SUPPORT dataset, taken from (REF).

Variable	Levels	
sex	female	
	$_{\mathrm{male}}$	
dzgroup	ARF/MOSF w/Sepsis	
	COPD	
	CHF	
	Cirrhosis	
	Coma	
	Colon Cancer	
	Lung Cancer	
	MOSF w/Malig	
dzclass	ARF/MOSF	
	COPD/CHF/Cirrhosis	
	Coma	
	Cancer	
income	under \$11k	
	11 - 25 k	
	25 - 50 k	
	>\$50k	
race	white	
	black	
	asian	
	other	
	hispanic	
sfdm2	no(M2 and SIP pres)	
	adl>=4 (>=5 if sur)	
	SIP > = 30	
	Coma or Intub	
	<2 mo. follow-up	

Table 5: A description of each level within each categorical variable in the dataset, taken from REF.