```
Name: Chan Kai Yin
SID: 1155124983
```

Q1

a.)

```
V^T = [[-2.72892220e-01 -5.11655370e-01 -3.65997772e-01 -2.18288336e-01
 -4.34381463e-01 -3.54970449e-01 -4.09198211e-01]
-3.30113929e-02 -6.71226587e-02 1.00164115e-02]
[-4.71915547e-01 7.92010632e-02 7.22885353e-01 -1.76991435e-01
 -3.69690775e-01 2.39586242e-01 -1.51858060e-01]
[-7.26004179e-02 1.71285014e-01 1.72998791e-01 -1.68478339e-01
  6.31512574e-01 -2.85638770e-01 -6.53207053e-01
[-3.76000996e-01 -2.79589227e-01 -1.45935518e-01 -6.05475565e-01
  4.24833065e-01 2.46807177e-01 3.88790900e-01]
-3.07018643e-01 -2.47808353e-02 -4.50503897e-02
[-1.71289418e-01 1.18188612e-01 2.39139495e-01 -3.16831951e-02
 -1.08660778e-04 -8.17906830e-01 4.79091087e-01]]
U = [[-0.30575453 - 0.28084225 - 0.17900878 - 0.57665451 - 0.64311746 - 0.22241214]
0.27898591
          [-0.2314542
Sigma = [[24.61024449 0.
                       0.
                               0.
                                        0.
                                                0.
  0.
[ 0.
         11.44513576 0.
                          0.
                                   0.
                                           0.
  0.
         1
[ 0.
         0.
                  9.21913422 0.
                                   0.
                                           0.
  0.
         1
[ 0.
         0.
                  0.
                          7.66940571 0.
                                           0.
  0.
         1
[ 0.
         0.
                  0.
                          0.
                                  4.81782202 0.
```

```
0. ]
[0. 0. 0. 0. 0. 0.

1.82238996
0. ]]
```

And the = U*Sigma*V^T

```
[[ 2.00000000e+00 5.0000000e+00 2.24820162e-15 6.00000000e+00 3.53883589e-15 3.00000000e+00 5.00000000e+00] [ 1.00000000e+00 4.00000000e+00 9.00000000e+00 4.05231404e-15 7.21644966e-16 3.00000000e+00 4.74967288e-15] [ 5.00000000e+00 5.55111512e-16 5.00000000e+00 9.99200722e-16 4.00000000e+00 1.0000000e+00 1.0000000e+00] [ -7.84095011e-16 8.00000000e+00 -3.54577478e-15 4.00000000e+00 8.0000000e+00 1.0000000e+00 -4.55364912e-16] [ 1.00000000e+00 9.0000000e+00 6.00000000e+00 3.00000000e+00 7.00000000e+00 8.00000000e+00 9.00000000e+00 ] [ 1.00000000e+01 2.00000000e+00 3.00000000e+00 -1.22124533e-15 5.00000000e+00 2.00000000e+00 5.000000000e+00] [
```

Which identical to A. Transform it to a 2-D space.

The Whole Doc:

```
[[-7.52469371 -3.2142777]

[-6.678405 2.48274797]

[-5.69614447 5.37994158]

[-8.79641846 -5.37869202]

[-17.29185993 -2.59103105]

[-9.77806553 7.0645575]]
```

Program:

b.)1

Doc7:

[[-6.85374965 -0.76467929]]

2.

Word space: 0.8633266263033915 Concept space: 0.9914060814075807

Program:

```
print(VT)

doc3 = A[2]
dco6 = A[5]
doc3_2d = doc3.dot(VT.T)
doc6_2d = dco6.dot(VT.T)
result = 1 - spatial.distance.cosine(doc3, dco6)
print(result)

result = 1 - spatial.distance.cosine(doc3_2d, doc6_2d)
print(result)
```

It extends from the above program.

2.)

```
import numpy import array
import numpy as np
from numpy import diag
from numpy import zeros
from scipy.linalg import svd
from scipy import spatial

from sklearn.decomposition import PCA

pca = PCA(25)

file = "bin_t_2.txt"

line_ls = []

with open(file, 'r') as f:
    for line in f.readlines():
        line_ls.append(line.strip().split())

A = np.array(line_ls)
line_ls = []

A = pca.fit_transform(A)

with open("test_bin_2d.txt", 'w') as f:
    for line in A:
        mat_str = " ".join(map(str_line))
        f.write(mat_str))

A = A - A.mean(axis=0)

# print(A)
```

I use this one to do the dimension reduction of the original training data set. So as the label file and testing files.

a.)

it should be 37. Cause in my view, give a same letter, there are quit a lot of differences between the uppercase and lowercase in shape, like Q and q, B and b. but there is 15 lowercase letters is similar to its uppercase which is C, I, J, K, L, M, O, P, S, U, V, W, X, Y and Z.

so we need to distinguish 52 case and set K = 37.

b.)
I use this program to transform those data set file.

```
import numpy import array
import numpy import diag
from numpy import zeros
from scipy.linalg import svd
from scipy import spatial

from sklearn.decomposition import PCA

pca = PCA(25)

file = "bin_t_2.txt"

line_ls = []
with open(file, 'r') as f:
    for line in f.readlines():
        line_ls.append(line.strip().split())
A = np.array(line_ls)
line_ls = []
A = pca.fit_transform(A)

with open("test_bin_2d.txt", 'w') as f:
    for line in A:
        mat_str = " ".join(map(str_line))
    f.write(mat_str)

A = A - A.mean(axis=0)

# print(A)
```

I use the previous k-mean MapReduce program (attached below), with some fine tune, including change all 784 to 25.

The k-means mapper:

```
#!/usr/bin/env python
import sys
import math
import numpy as np
cen = np.zeros((k, 784))
up_cen = np.zeros((k, 784))
arr_cen = np.zeros(k)
arr count cen v = np.ones(k)
arr_count_cen = np.ones(k)
def p_c_distance(pt, index_cen):
    dist =
    result = pt - cen[index_cen]
dist += np.sum((result*result))
     return dist
def read_to_cen():
    with open("cen_1.txt", "r") as f_c:
         for i in f_c.readlines():
              x = []
j = i.strip().split('\t')[0]
k = i.strip().split('\t')[1]
              for item in k.strip().split():
                 x.append(float(item))
              x = np.array(x)
def tran a(pt):
    x = []
     for i in pt.strip().split():
      x.append(float(i))
    x = np.asarray(x)
def cal new cen(pt, pos):
    new v = pt
    new v = np.array(new v)
    up_cen[pos] = up_cen[pos] + new_v
    arr_count_cen[pos] += 1
read_to_cen()
up cen = cen.copy()
```

```
dic14.ie.cuhk.edu.hk - PuTTY
```

The k-means reducer:

```
dictieculikedunk-Putty
import sys
import numpy as np
k = 37
wh_y = np.zeros((k, 788), dtype='float')
wh_sum = np.zeros(k)
arr_count_cen_y = np.zeros(k)
arr_count_cen_y = np.zeros(k)
arr_count_cen_y = np.zeros(k)
for line in sys.stdin:
    num_clu = int(line.strip().split('\t')[0])
    part_sum = float(line.strip().split('\t')[1])
    part_y = line.strip().split('\t')[2]

arr_part_y = line.strip().split(\t')[2]

arr_part_y = np.zeros(k)
for i in part_y.aspend(float(i))
arr_part_y = np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zeros(np.zero
```

I use this .sh file to run the k-means. For each caculation, I run 10 times to converage the k-means.

And then I calculate the accuracy with this program, same as the previous homework. Again with some fine tune, including change all 784 to 25.

The Accuracy of Clustering Performance with Random Seed 1:

Cluster	# train	Label	#	Classification
Number	images	of the	correctly	Accuracy (%)
	belongs	cluster	clustered	
	to the		images	
	cluster			
0	3723	1	821	0.220521
1	2774	26	2214	0.798125
2	3104	3	753	0.24259
3	3556	8	994	0.279528
4	3116	7	711	0.228177
5	2643	6	1023	0.38706
6	2294	17	1123	0.489538
7	3634	8	1442	0.396808
8	5171	9	1753	0.339006
9	3863	6	1581	0.409267
10	4002	14	1094	0.273363
11	2653	15	724	0.272899
12	3694	13	3312	0.896589
13	2503	1	898	0.358769
14	2836	3	1296	0.456982
15	2663	5	1833	0.688321
16	2345	18	916	0.390618
17	3821	17	1089	0.285004
18	3433	19	2547	0.741917
19	3752	20	561	0.14952
20	4307	10	1945	0.45159
21	3027	11	2046	0.675917
22	5485	9	1667	0.30392
23	4433	23	965	0.217686
24	2499	14	1596	0.638655
25	3136	15	2214	0.705995
26	3576	16	1815	0.50755
27	3781	4	2018	0.533721
28	2981	18	1730	0.580342
29	3350	2	1036	0.309254

30	4708	25	1372	0.291419
31	2819	21	1873	0.66442
32	2548	22	1721	0.675432
33	3671	23	2946	0.802506
34	3073	24	2296	0.747153
35	2515	22	1544	0.613917
36	3311	26	997	0.301117
Total	124800	N/A	56466	0.452452
Set				

The Accuracy of Clustering Performance with Random Seed 2:

Cluster	# train	Label	#	Classification
Number	images	of the	correctly	Accuracy (%)
	belongs	cluster	clustered	
	to the		images	
	cluster			
0	3725	1	817	0.219329
1	2835	26	2273	0.801764
2	3133	3	829	0.264603
3	3816	8	1134	0.29717
4	3181	7	731	0.229802
5	2614	6	1009	0.385998
6	2299	17	1066	0.46368
7	3751	8	1443	0.384697
8	5059	9	1738	0.343546
9	4056	6	1563	0.385355
10	4126	14	1154	0.27969
11	3380	15	1912	0.56568
12	3714	13	3313	0.89203
13	2418	1	881	0.364351
14	2638	3	1480	0.561031
15	2800	5	1933	0.690357
16	2380	18	1015	0.426471
17	3441	17	1024	0.297588
18	3069	19	2404	0.783317

19	4009	25	787	0.196308
20	4260	10	2049	0.480986
21	2948	11	1990	0.675034
22	5334	9	1661	0.311399
23	4419	23	959	0.217017
24	2640	14	1575	0.596591
25	2630	15	1733	0.658935
26	3564	16	1787	0.501403
27	3987	4	1855	0.465262
28	3066	18	1632	0.53229
29	3209	19	951	0.296354
30	4407	25	1267	0.287497
31	2717	21	1859	0.684211
32	2620	22	1685	0.64313
33	3665	23	2917	0.795907
34	3070	24	2259	0.735831
35	2479	22	1517	0.61194
36	3341	26	1048	0.313679
Total	124800	N/A	57250	0.458734
Set				

The Accuracy of Clustering Performance with Random Seed 3:

Cluster	# train	Label	#	Classification
Number	images	of the	correctly	Accuracy (%)
	belongs	cluster	clustered	
	to the		images	
	cluster			
0	3876	1	767	0.197884
1	2847	26	2281	0.801194
2	3126	3	822	0.262956
3	3816	8	1115	0.292191
4	3160	7	730	0.231013
5	2652	6	1025	0.386501
6	2172	17	1031	0.474678
7	3747	8	1430	0.381639
8	5385	9	1883	0.349675

				1
9	4324	6	1630	0.376966
10	4192	14	1178	0.281011
11	3441	15	1915	0.556524
12	3734	13	3319	0.888859
13	2413	1	880	0.364691
14	2644	3	1487	0.562405
15	2832	5	1944	0.686441
16	2683	18	979	0.36489
17	2958	17	894	0.302231
18	3038	19	2412	0.793943
19	4648	25	1171	0.251936
20	4269	10	2072	0.48536
21	2973	11	1995	0.671039
22	5340	9	1666	0.311985
23	4539	23	937	0.206433
24	2717	14	1641	0.603975
25	2605	15	1730	0.664107
26	3576	16	1831	0.512025
27	3970	4	1867	0.470277
28	3002	18	1658	0.552298
29	3152	19	916	0.290609
30	3229	25	1183	0.366367
31	2641	21	1851	0.700871
32	2734	22	1762	0.644477
33	3707	23	2940	0.793094
34	3077	24	2267	0.736757
35	2213	22	1412	0.638048
36	3368	26	1040	0.308789
Total	124800	N/A	57661	0.462027
Set				
•			_	

So, the seed 3 have the best performance, I use the seed 3 in part ${\rm d}.$

d.) For the test files:

Cluster	# train	Label	#	Classification	
Number	images	of the	correctly	Accuracy (%)	
	belongs	cluster	clustered		

	to the		images	
	cluster			
0	653	1	135	0.206738
1	446	26	357	0.800448
2	478	3	136	0.284519
3	632	8	200	0.316456
4	505	7	129	0.255446
5	453	6	161	0.355408
6	362	17	178	0.491713
7	598	8	232	0.38796
8	922	9	303	0.328633
9	716	6	258	0.360335
10	736	14	209	0.283967
11	556	15	314	0.564748
12	595	13	538	0.904202
13	420	1	156	0.371429
14	459	3	249	0.542484
15	448	5	304	0.678571
16	477	18	169	0.354298
17	490	17	143	0.291837
18	506	19	403	0.796443
19	788	25	197	0.25
20	724	10	337	0.46547
21	494	11	314	0.635628
22	871	9	292	0.335247
23	751	23	139	0.185087
24	446	14	277	0.621076
25	441	15	299	0.678005
26	601	16	311	0.517471
27	659	4	322	0.488619
28	471	18	265	0.562633
29	572	2	180	0.314685
30	537	25	197	0.366853
31	474	21	341	0.719409
32	487	22	307	0.63039
33	627	23	515	0.821372
34	511	24	365	0.714286

35	344	22	221	0.642442
36	550	26	165	0.3
Total	20800	N/A	9618	0.462403
Set				

Compare to the HW3 result, using this method have higher accuracy. More than that, I realize that the memory consumption of the program is much lesser because of each data's dimesion has been dectucted to 25 from 784. And the speed of map reduce and checking program is faster too.

Q3.)

- a.)
- i.) Item-item CF:
 - (2, 5) 0.2721655269759087
 - (2, 4) 0.17588161767036214
 - (2, 3) 0.09860132971832693
 - (2, 2) 1.0
 - (2, 1) -0.8571593913749194
 - (2,0) -0.13608276348795437

So, set the k = 2. And the most similar users for item C (2) is 5 and 4. So the answer is 4.39.

ii)

User-User CF:

- (1, 2) 0.23134069792952236
- (1, 4) -0.35000000000000003
- (1, 1) 1.0
- (1, 0) 0.35355339059327373

So, set the k = 2. And the most similar users for user II (1) is 0 and 2. So the answer is 4.60.

b.)

[[1.60181186 1.10155771 4.70852404 4.02325968 3.46382091 3.24415151]
[2.99738067 2.54936675 4.95571807 3.78009147 4.36990693 3.60615196]
[4.60012762 4.47794519 3.13993082 1.45924377 4.26033711 2.67962585]
[2.69458465 2.24724505 4.80723373 3.74062535 4.12135617 3.46697337]
[3.9587518 4.01563034 1.42240116 0.01145553 2.96531543 1.48791261]]
The predict rate is 4.95571807, far from both result from part a.

c.)

The update rule is incorrect:

```
P[i][k] = P[i][k] + alpha * (2 * eij * Q[k][j] - beta * P[i][k])
Q[k][j] = Q[k][j] + alpha * (2 * eij * P[i][k] - beta * Q[k][j])
This will not give the fastest descent direction.
```

The correct version:

```
p_tmp = P[i][k] + alpha * (2 * eij * Q[k][j] - beta * P[i][k])

q_tmp = Q[k][j] + alpha * (2 * eij * P[i][k] - beta * Q[k][j])

P[i][k] = p_tmp

Q[k][j] = q_tmp
```

Predict:

a.)

```
pg 18
works 27
but 32
donations 32
for 44
any 84
work 102
tm 116
this 132
project 243
her 252
or 263
gutenberg 316
said 2048
you 2528
with 2955
as 4516
his 11767
by 11876
is 23153
it 26331
he 31653
that 35513
i 59556
was 59656
in 223821
a 261914
to 339629
and 439567
of 5756275
the 1007946

DOD ▶ 4:Run ★ 5: Debug ♣ Python Console   Terminal
m 2020.1.5 available: // Update... (today 18:57)
```

b.)

If all distant items' frequency are blow n/k which in here refer the 1 % of total number of words, then the 1-pass algorithm will produce the wrong answer.



Or like the example in lecture slide p36, in this scenario the last one is in-correct classify as heavy hitter.

c.)

```
eyes 5
crab 1
that 35498
with 2941
sister 5
sourestnatured 1
lives 2
herself 1
he 31638
look 4
hour 21
this 117
work 87
cat 6
project 228
lucetta 235
and 439553
is 23138
in 223806
it 26317
states 1
howling 6
as 4502
troilus 590
seen 12
any 70
sir 372
write 37
you 2514
nay 31
mother 3
grandam 7
gutenberg 301
but 17
letter 1
parting 17
a 261900
thy 23
i 59541
dog 78
think 1
writ 129
enter 22
he 1007932
```

Mapper:

```
dictAiecuhkeduhk-PuTTY

If varr/bin/env python
import sys

k = 100

store = dict()

for line in sys.stdin:
    words = line.strip().split()
    for word in words:
        if (not store.get(str(word))) and len(store) < k-1:
            store(str(word)) = 1
        elif store.get(str(word)):
            store(str(word)) += 1
        elif not store.get(str(word)):
            for ele in list(store.keys()):
            store(ele) = -1
            if store(ele) <= 0:
                del store[ele]

$ store = dict(sorted(store.items(), key-lambda item: item[1]))

for ele, count in store.items():
            print('%s\t%' & (ele, count))</pre>
```

Result:

```
windsor 31
how
        24
sins
which
       51
you
       29037
woodman 18
shall 147
why
enter 67
beast 16
falstaff
               1192
gutenberg
               308
sir 3321
thunder 1
sides 14
       263028
off
       6
for
       8469
       74062
jove
       53
doe
       14
green
bribe 9
<mark>s</mark>leeves 3
the
      1009060
```