

# DATA CONVERTERS

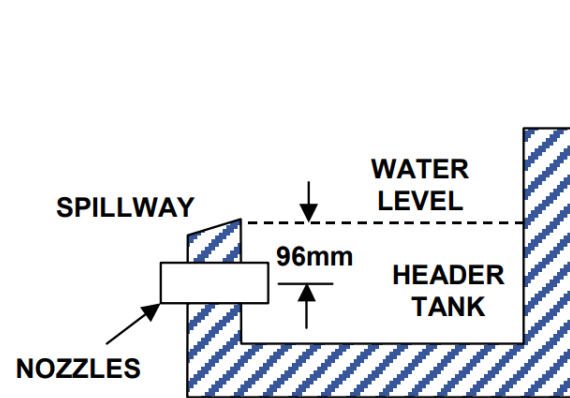
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Masum Hossain

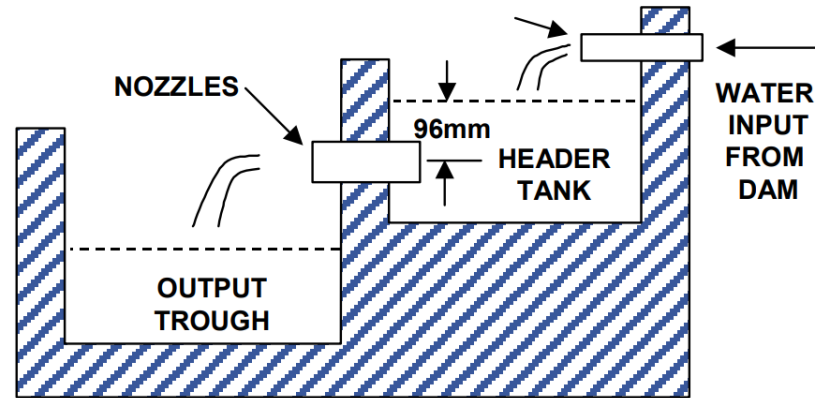
# Today's topic

- **Historical background on ADC**
- **Analog to Digital Conversion Process**
- **Quantization noise & SQNR**
- **SNDR, SFDR & ENOB**

# History of Data Converter: 18<sup>th</sup> Century

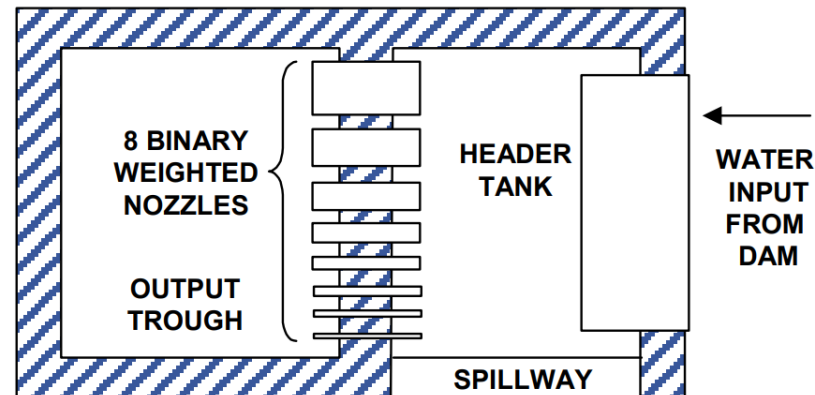


(A) HEADER SYSTEM: Note-The spillway and the nozzles need different outlets



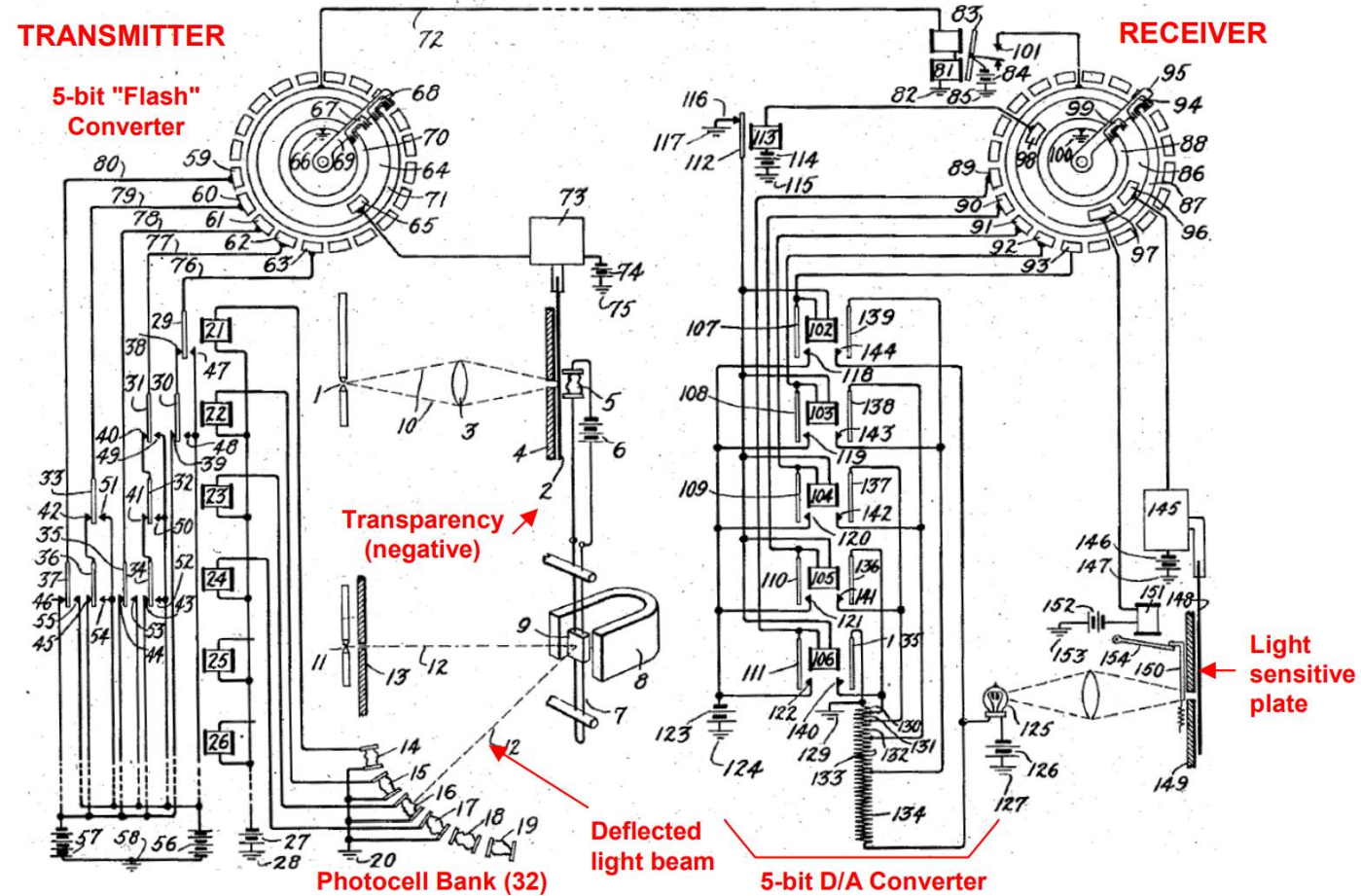
(B) SECTIONAL VIEW OF METERING SYSTEM

(C) TOP VIEW OF METERING SYSTEM DETAILS SHOWING BINARY WEIGHTED NOZZLES



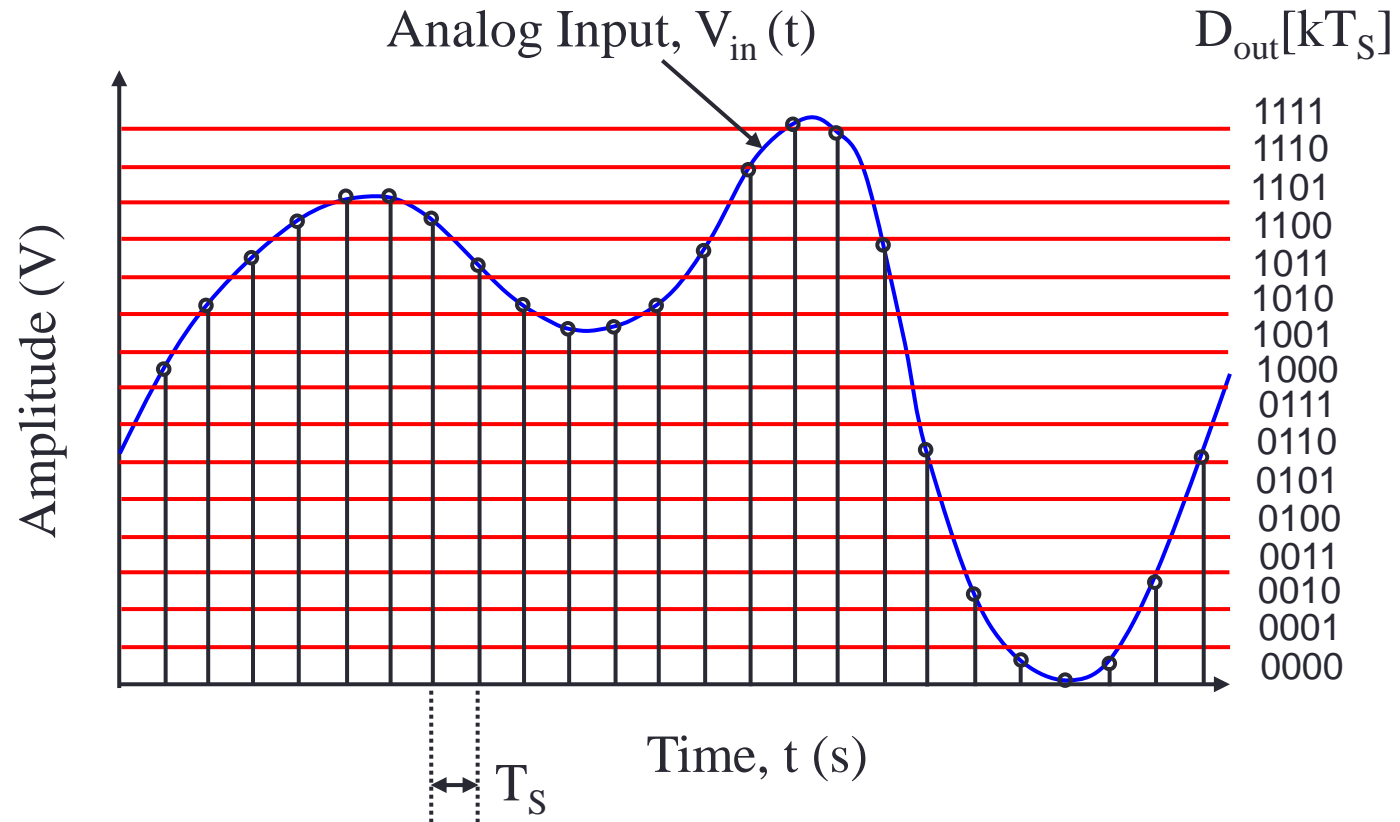
Adapted from:  
Kâzım Çeçen, "Sinan's Water Supply System in İstanbul," İstanbul Technical University / İstanbul Water and Sewage Administration, İstanbul Turkey, 1992-1993, pp. 165-167.

# History of Data Converter: 19<sup>th</sup> Century

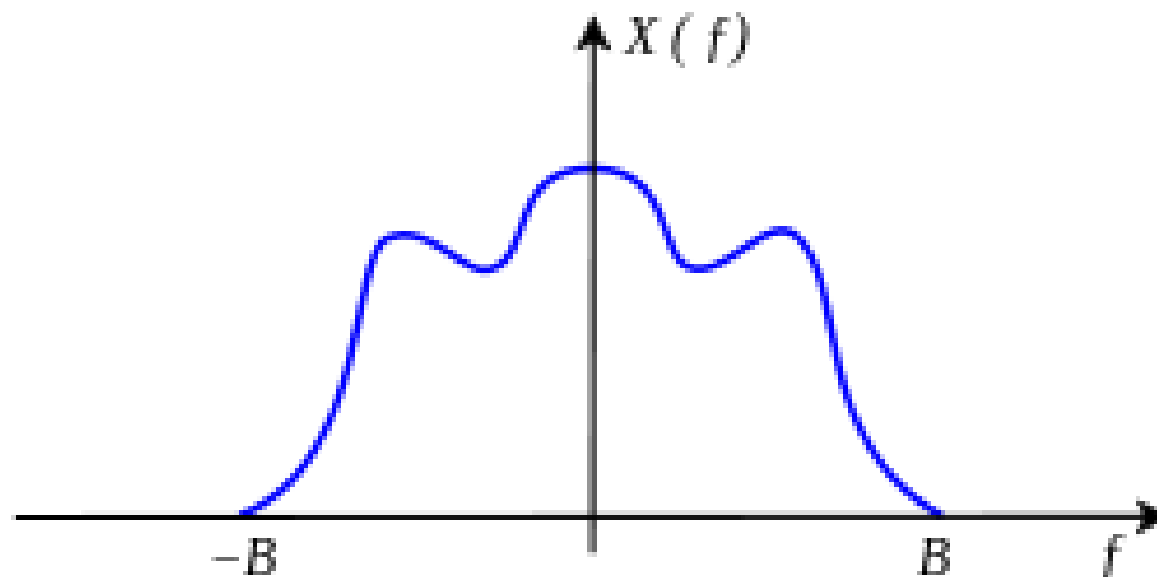


**Figure 1.5:** The First Disclosure of PCM: Paul M. Rainey, "Facimile Telegraph System," U.S. Patent 1,608,527, Filed July 20, 1921, Issued November 30, 1926

# Flash Data Converter

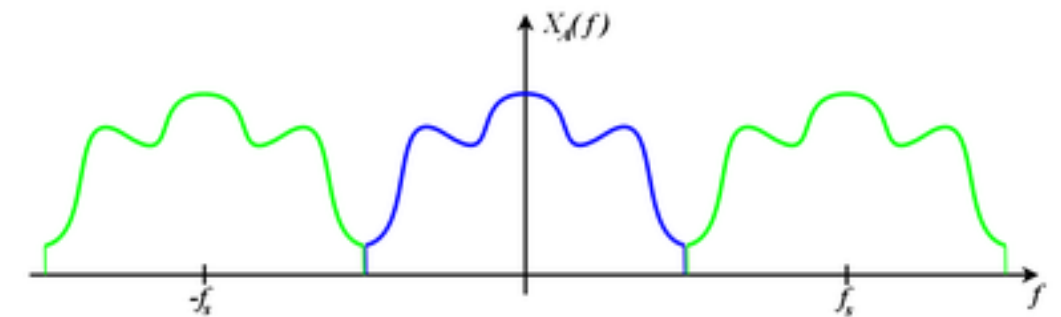
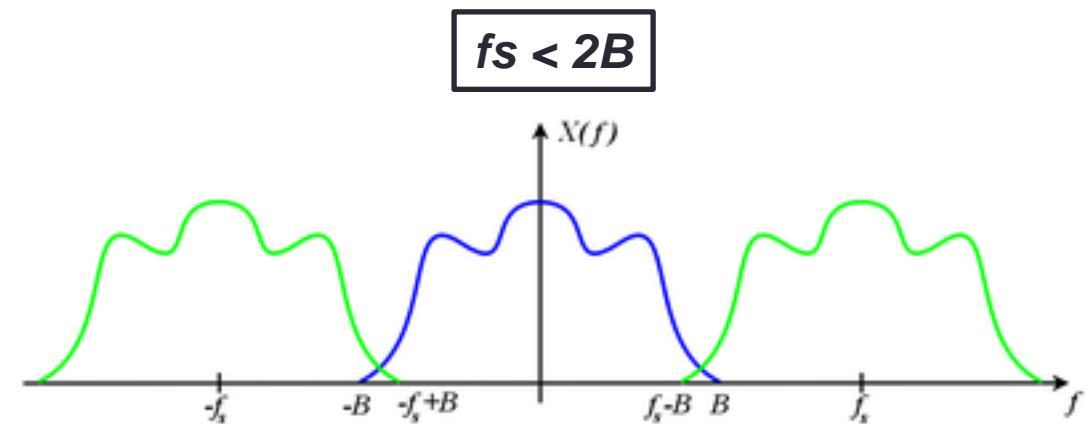
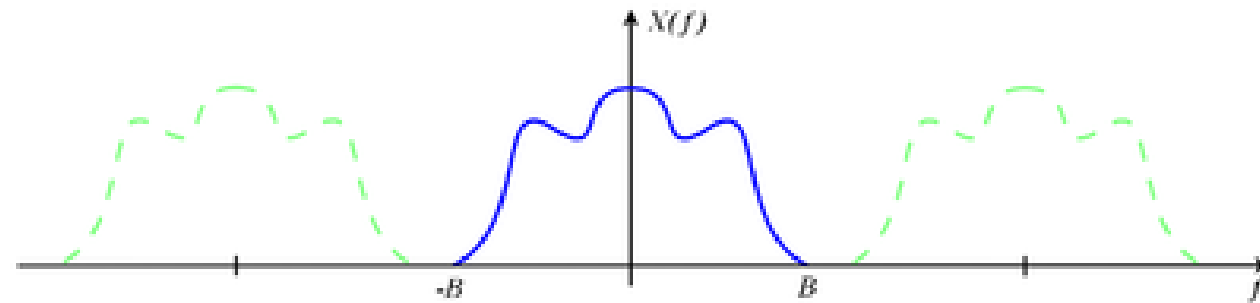
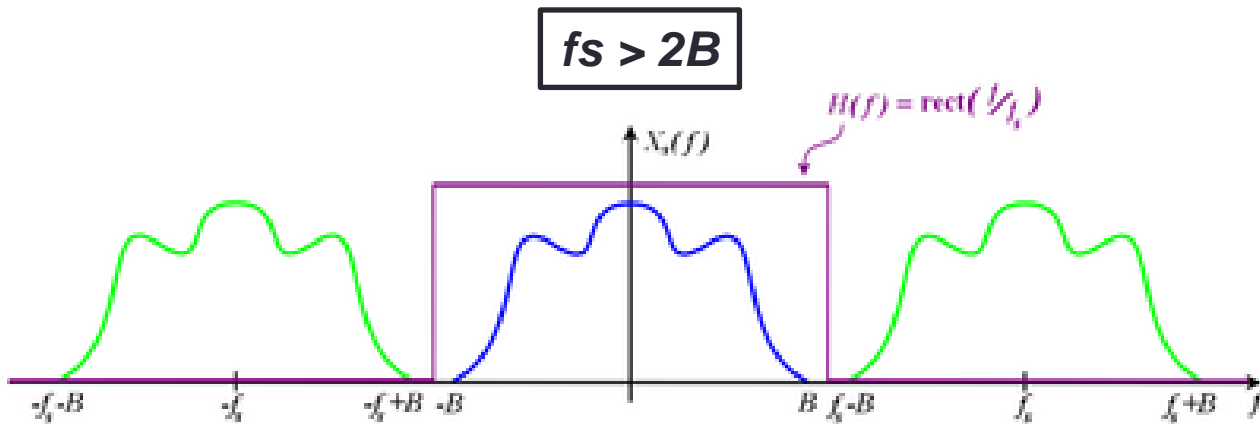


# What should be the sampling Rate?



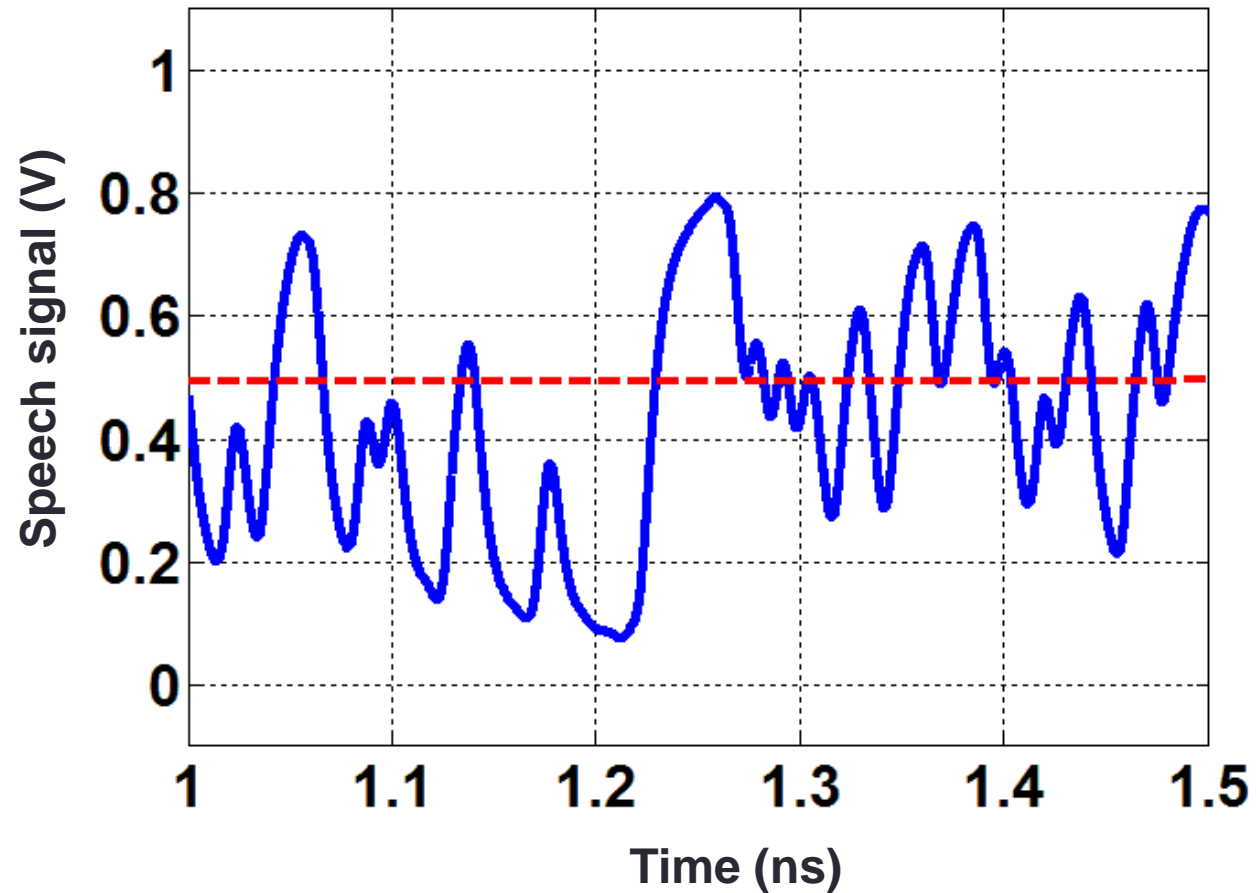
If a Signal has a Bandwidth of  $B$ , a sufficient sample-rate is  $2B$  samples/second, or anything larger. Equivalently, for a given sample rate  $f_s$ , perfect reconstruction is guaranteed possible for a bandlimit  $B < f_s/2$

# Nyquist Sampling Theorem



# Analog to Digital

To digitize an analog signal we need to set a 'threshold'  $\rightarrow 0.5$  in this case

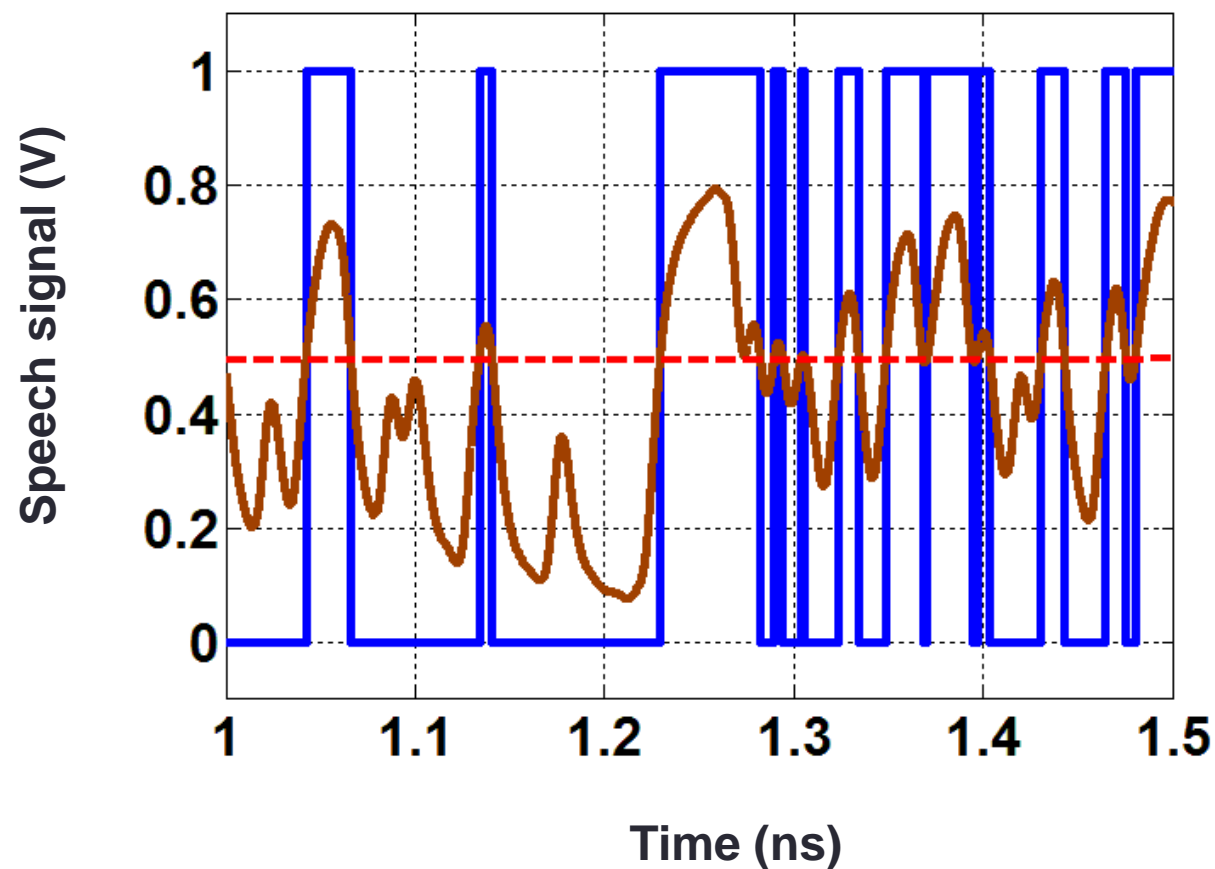




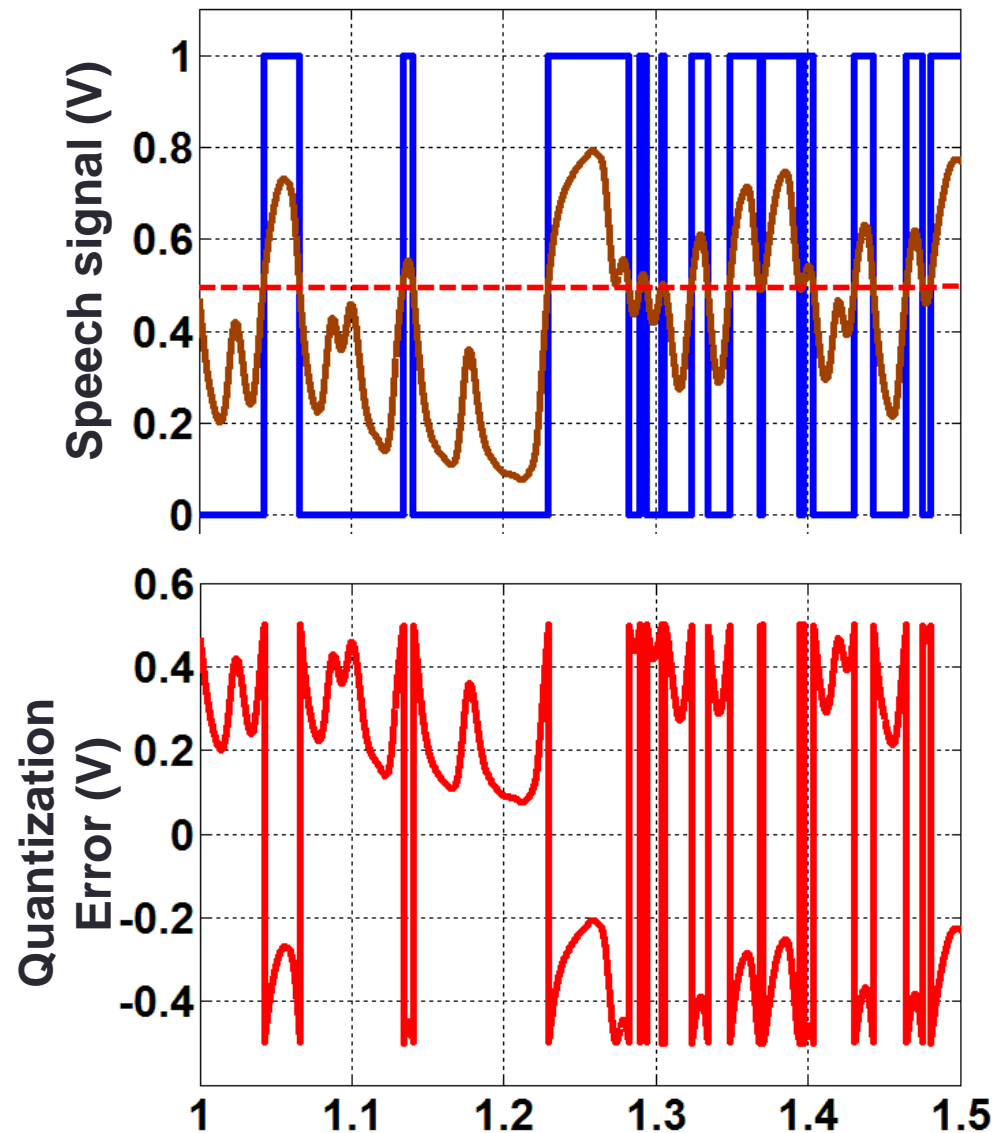
# Analog to Digital with 1 bit Quantizer

If signal is above 0.5  $\rightarrow$  digital output '1'

If signal is below 0.5  $\rightarrow$  digital output '0'

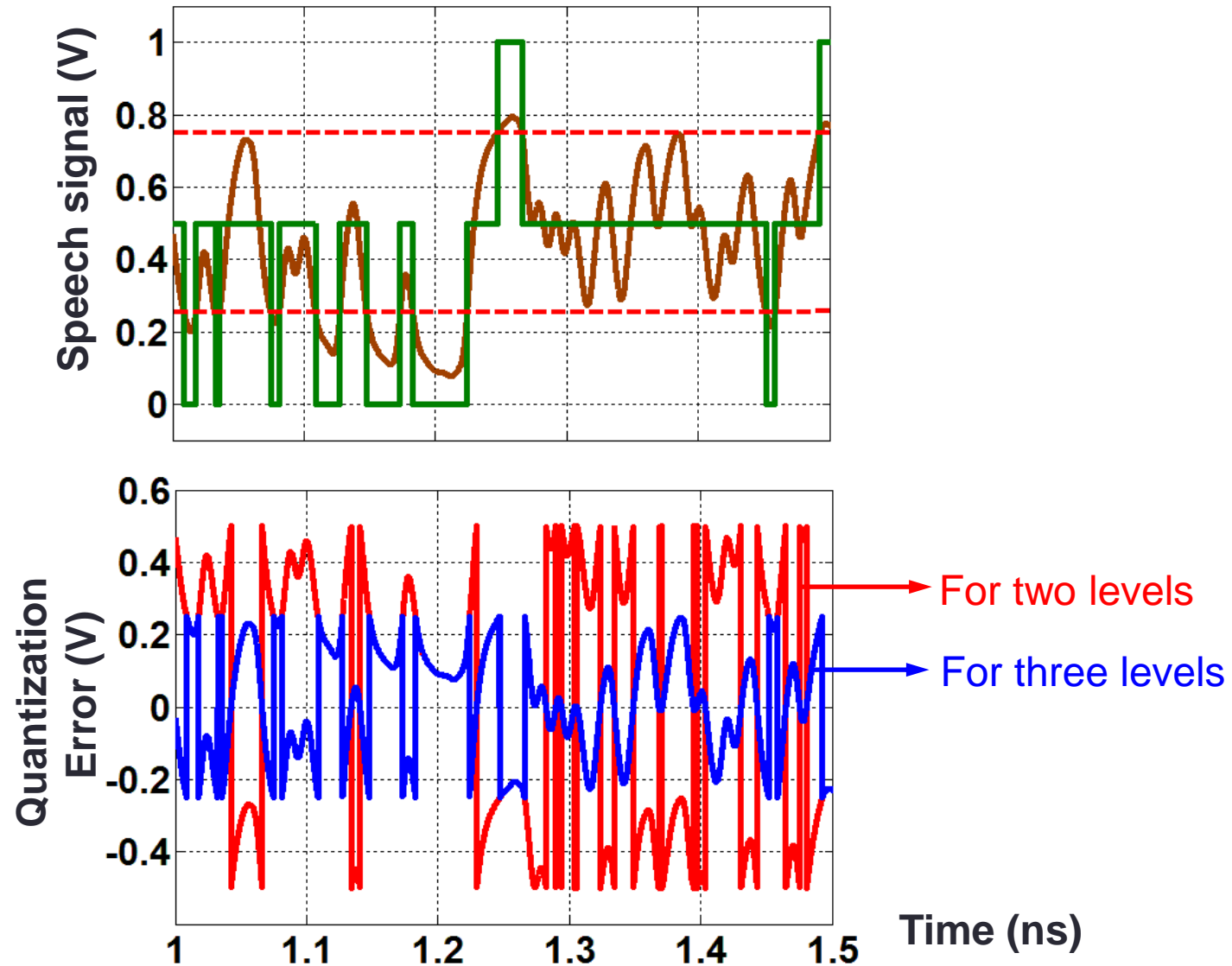


# Quantization Noise is Digital system

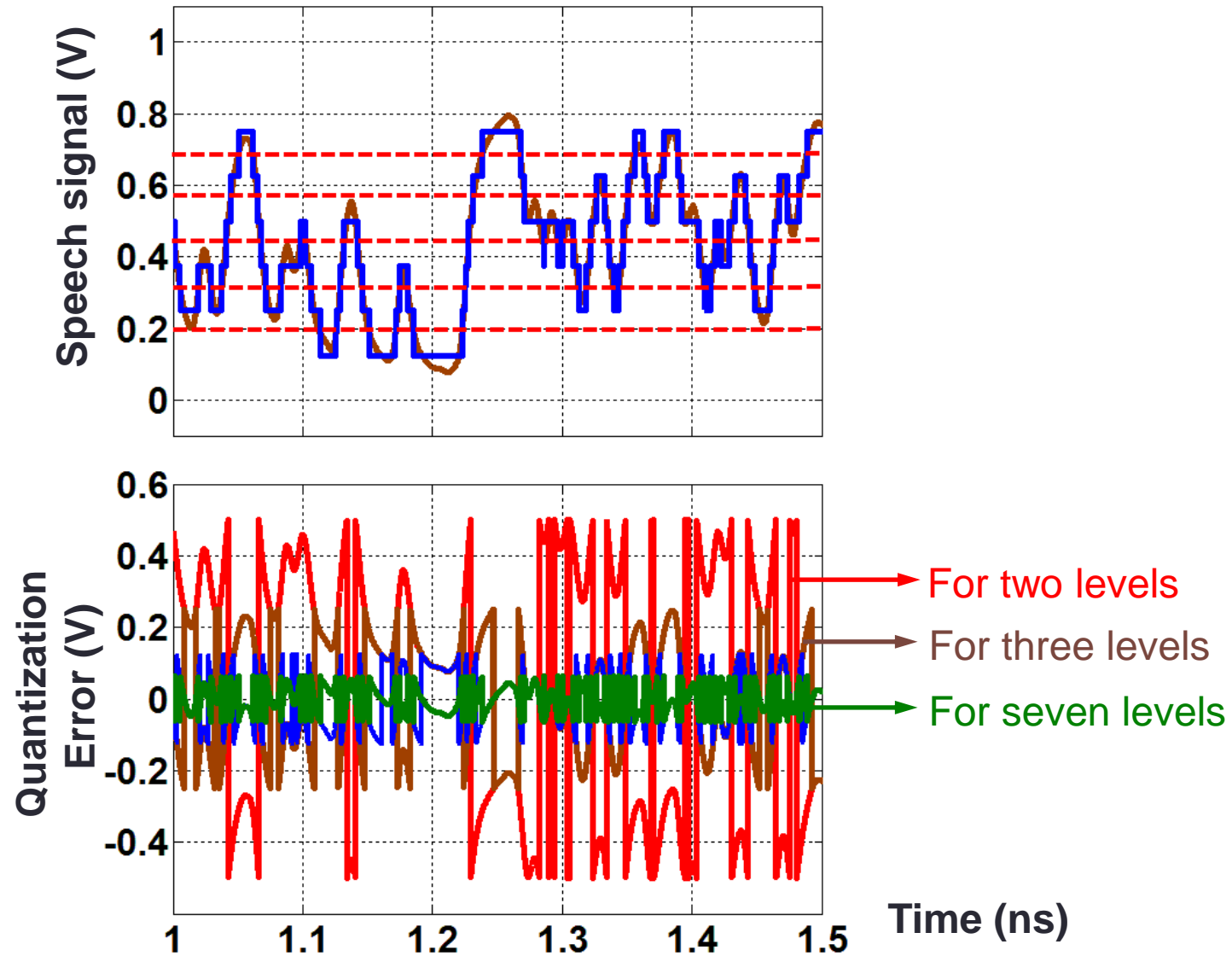


Quantization Error:  
The error that happens  
due to finite number  
of levels available  
in digital signal

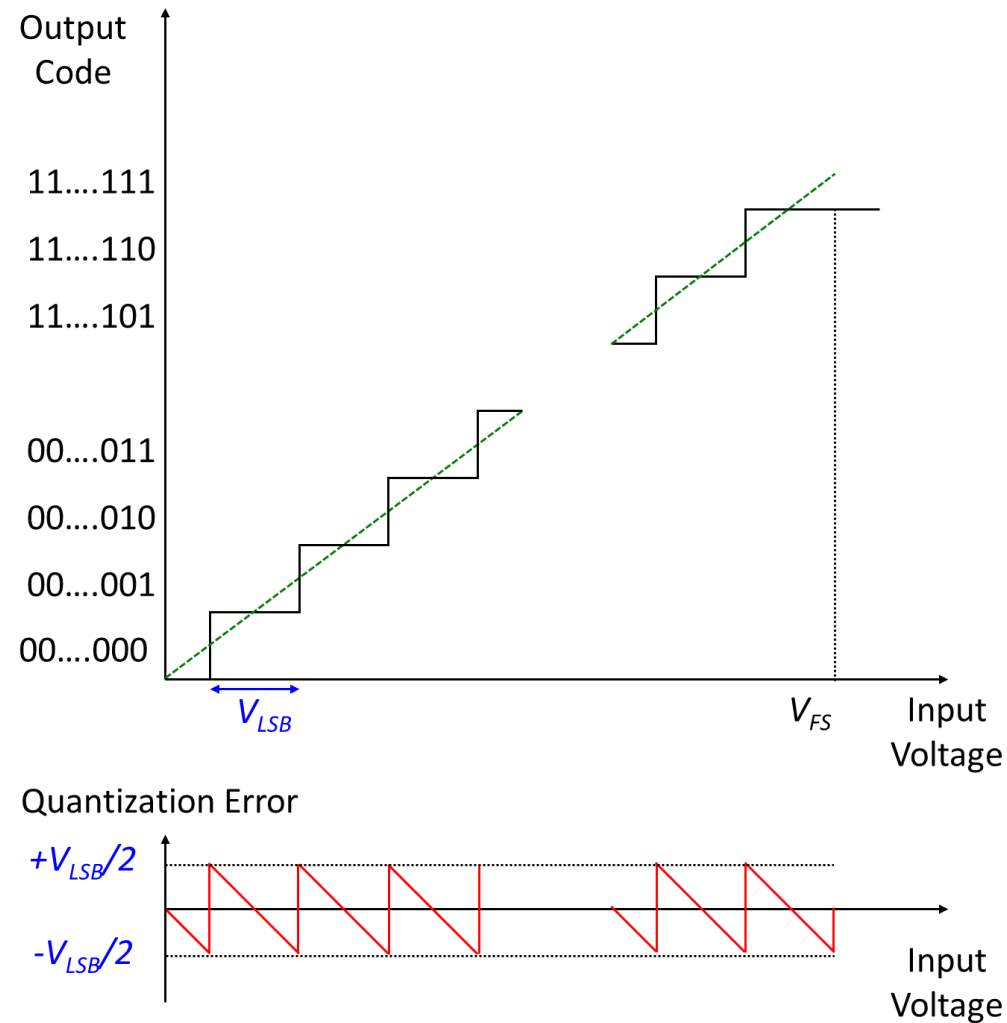
# Noise in Digital system



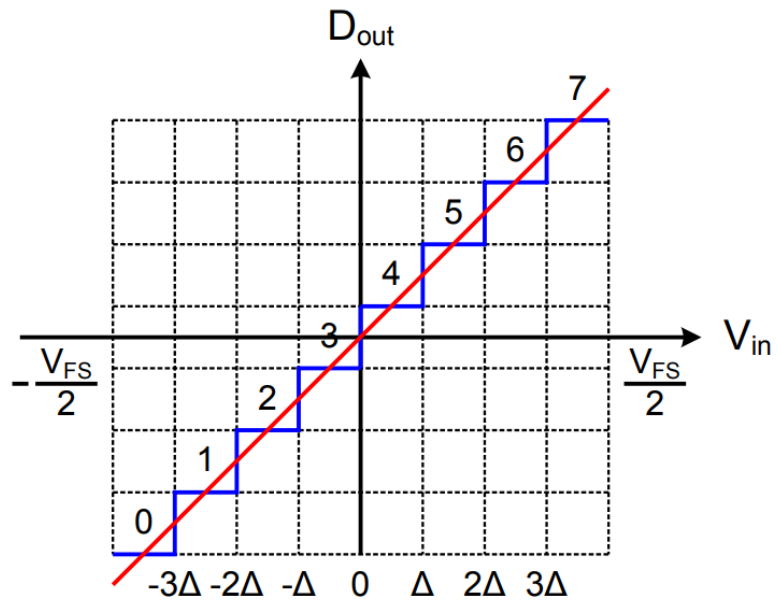
# Noise in Digital system



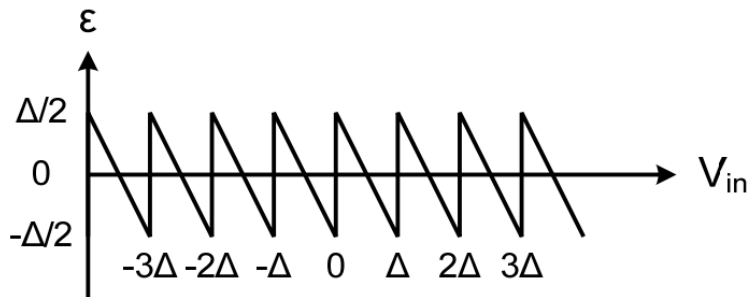
# Quantization Noise



**$2^N$  numbers of Comparisons  
For N bit resolution**



$N = 3$



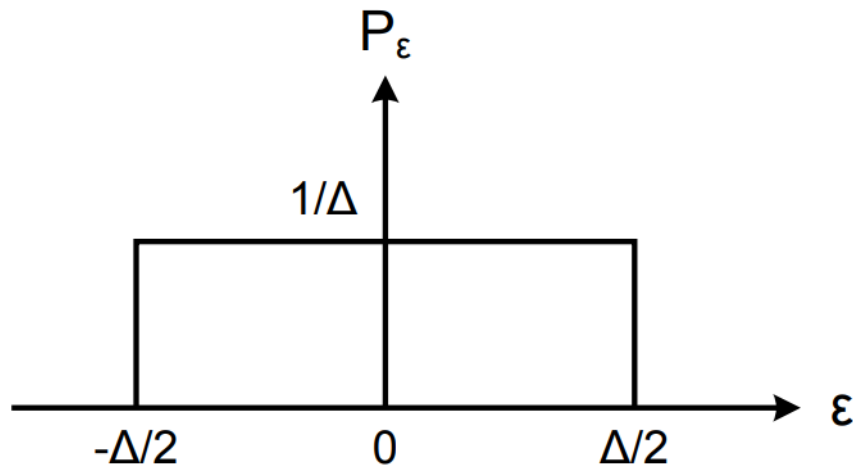
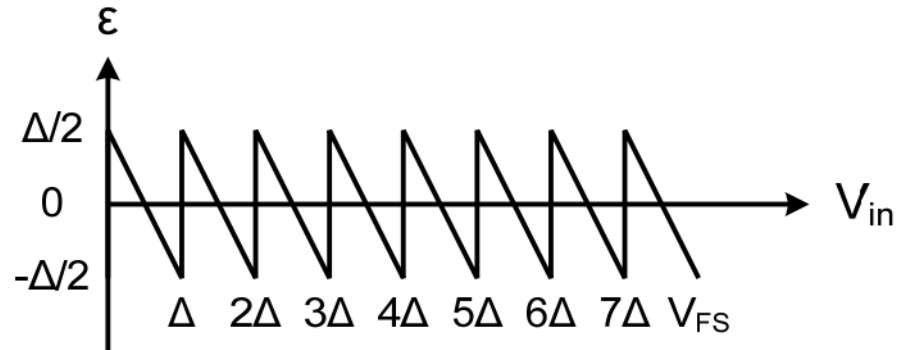
$$\Delta = \frac{V_{FS}}{2^N} = \text{LSB}$$

$$V_{in} \in [0, V_{FS}]$$

$$\epsilon = D_{out} \Delta - V_{in} = D_{out} \left( \frac{V_{FS}}{2^N} \right) - V_{in}$$

$$-\frac{\Delta}{2} \leq \epsilon \leq \frac{\Delta}{2}$$

“Random” quantization error is usually regarded as noise



### Assumptions:

- $N$  is large
- $0 \leq V_{in} \leq V_{FS}$  and  $V_{in} \gg \Delta$
- $V_{in}$  is active
- $\varepsilon$  is Uniformly distributed
- Spectrum of  $\varepsilon$  is white

$$\sigma_\varepsilon^2 = \int_{-\Delta/2}^{\Delta/2} \varepsilon^2 \cdot \frac{1}{\Delta} \cdot d\varepsilon = \frac{\Delta^2}{12}$$

# SQNR and ENOB

Assume  $V_{in}$  is sinusoidal with  $V_{p-p} = V_{FS}$ ,

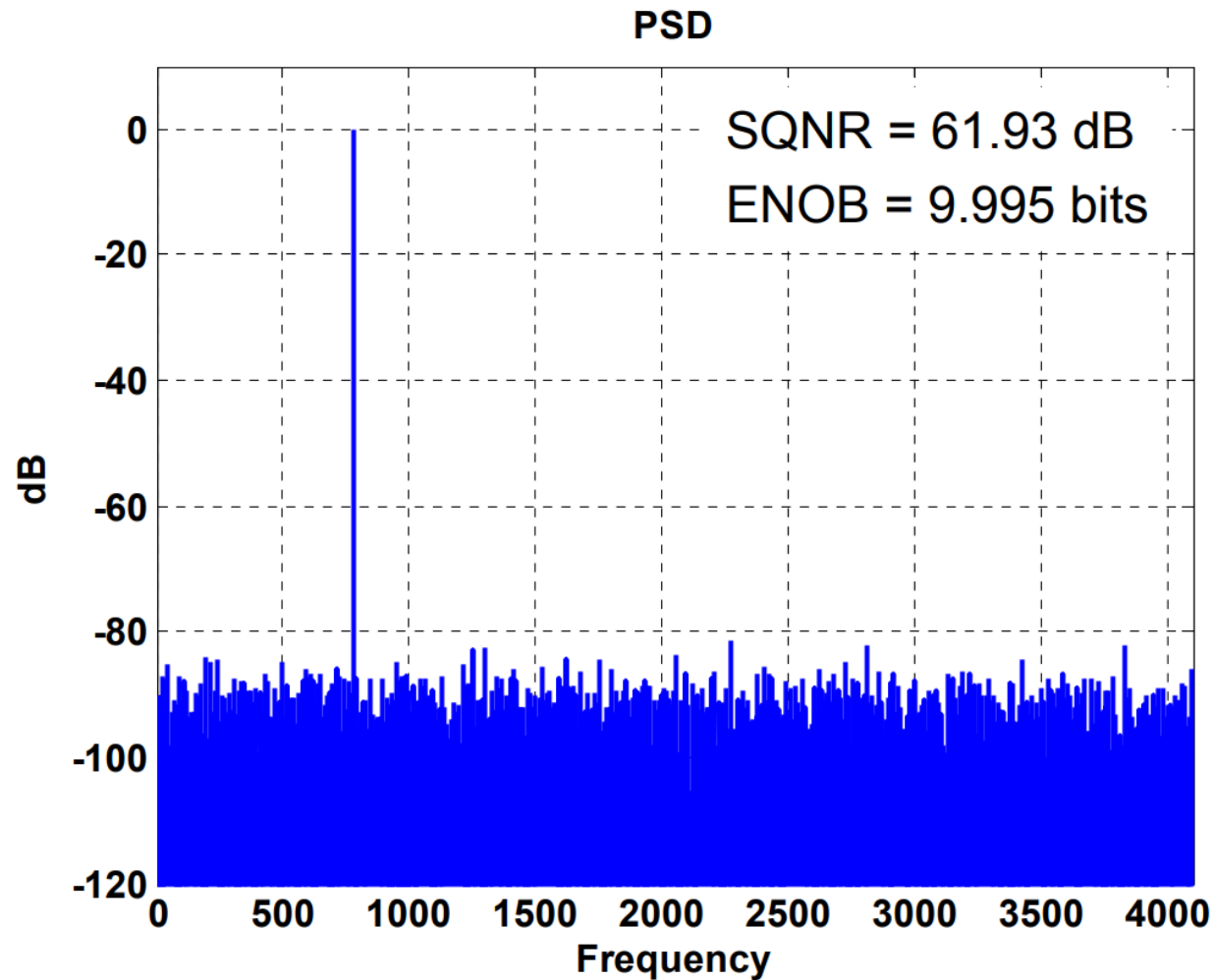
$$SQNR = \frac{V_{FS}^2 / 8}{\sigma_{\epsilon}^2} = \frac{(2^N \Delta)^2 / 8}{\frac{\Delta^2}{12}} = 1.5 \times 2^{2N},$$

$$SQNR = 6.02 \times N + 1.76 \text{ dB}$$

N (bits)	SQNR (dB)
8	49.9
10	62.0
12	74.0
14	86.0

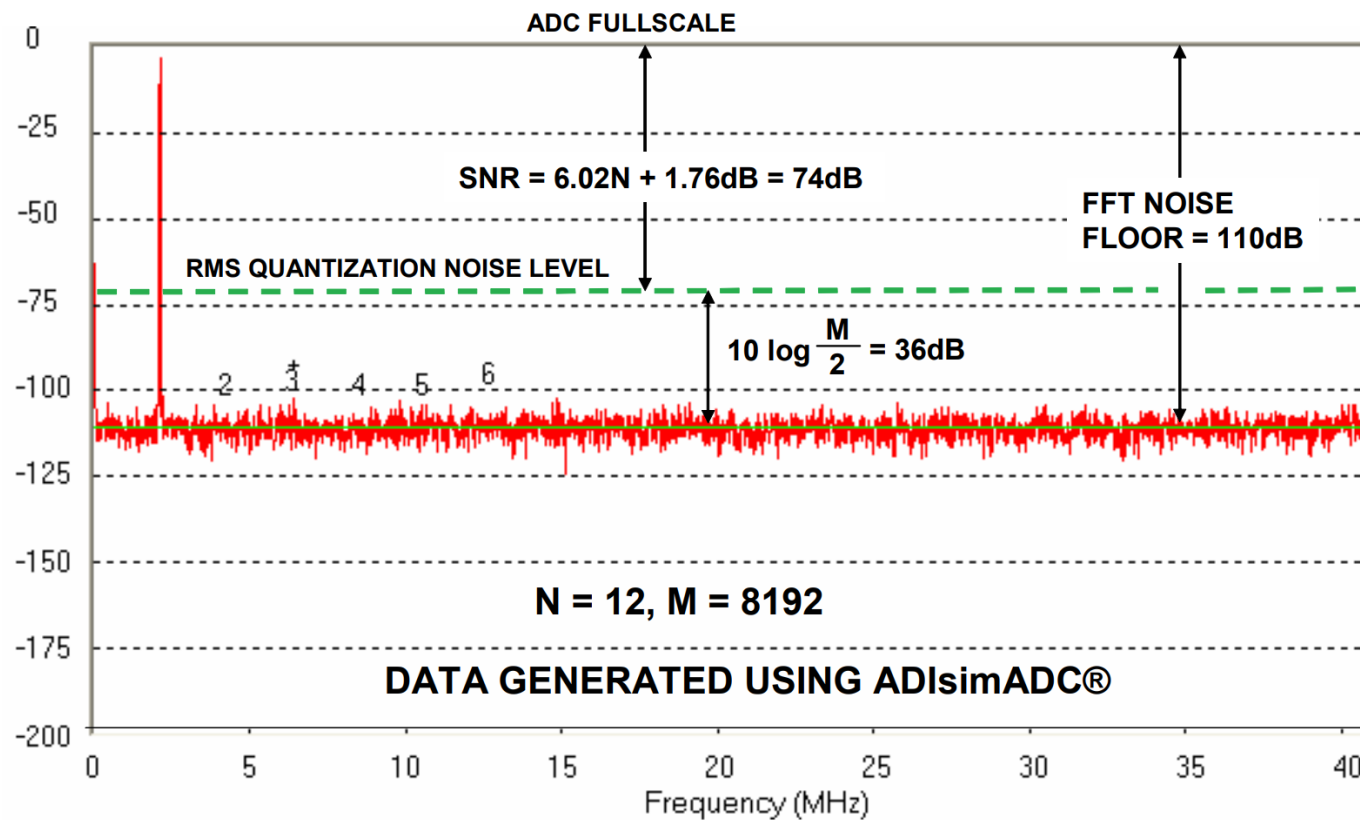
- SQNR depicts the theoretical performance of an ideal ADC
- In reality, ADC performance is limited by many other factors:
  - Electronic noise (thermal, 1/f, coupling/substrate, etc.)
  - Distortion (measured by THD, SFDR, IM3, etc.)





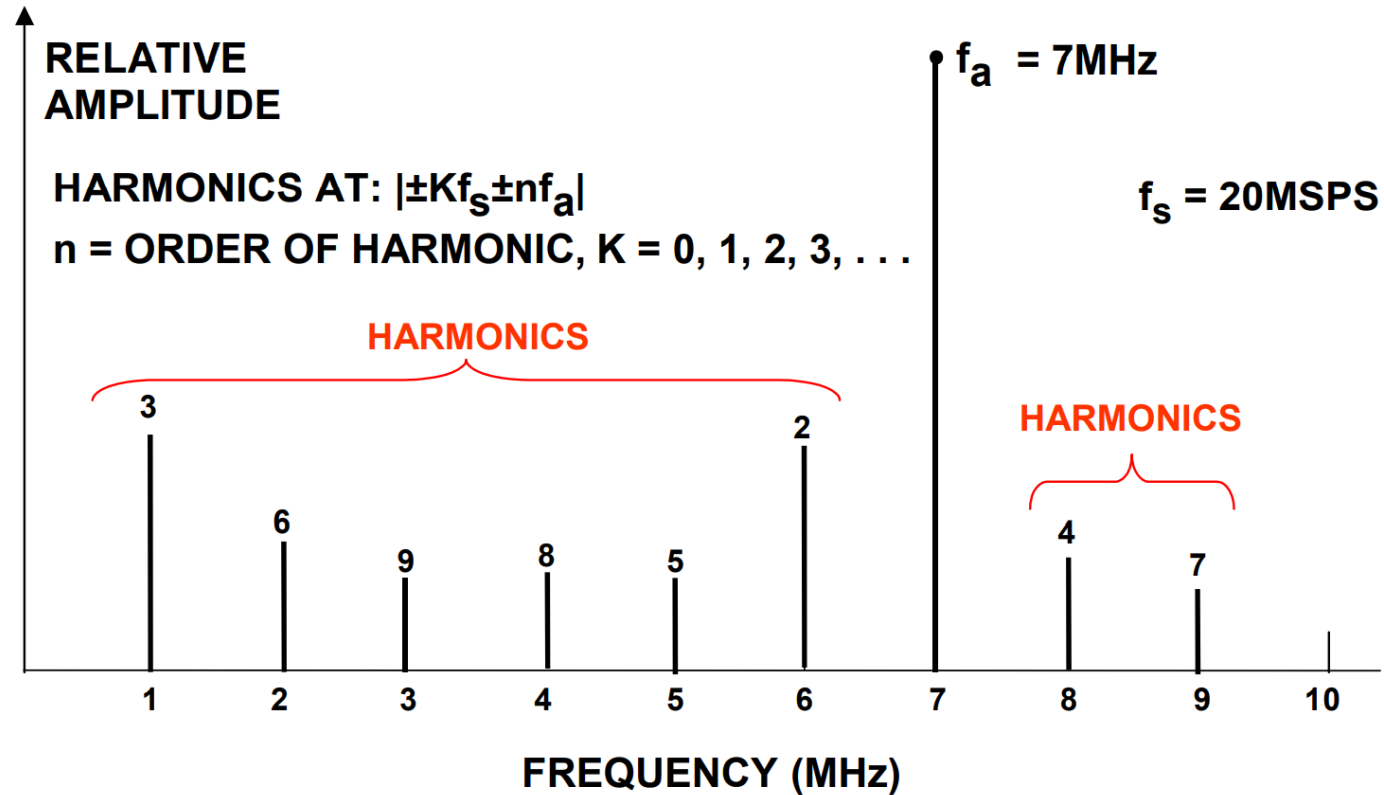
- $N = 10$  bits
- 8192 samples, only  $f = [0, f_s/2]$  shown
- Normalized to  $V_{in}$
- $f_s = 8192$ ,  $f_{in} = 779$
- $f_{in}$  and  $f_s$  must be incommensurate

$$ENOB = \frac{SQNR - 1.76 \text{ dB}}{6.02 \text{ dB}}$$



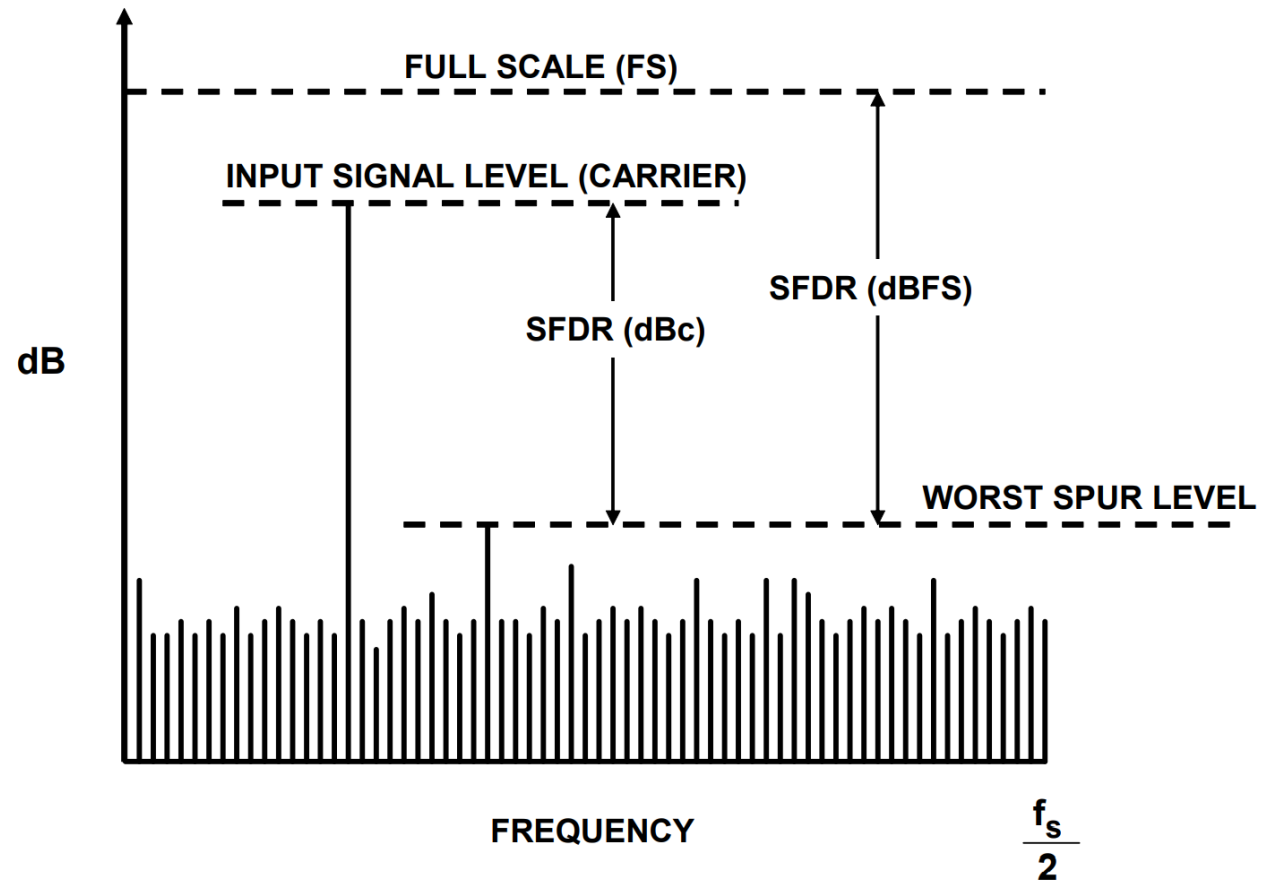
**Figure 2: FFT Output for an Ideal 12-Bit ADC, Input = 2.111MHz,  
 $f_s = 82\text{MSPS}$ , Average of 5 FFTs,  $M = 8192$ ,  
 Data Generated from [ADIsimADC®](#)**

# Nonlinear Distortion



**Figure 3: Location of Distortion Products: Input Signal = 7 MHz, Sampling Rate = 20 MSPS**

# SFDR



**Figure 4: Spurious Free Dynamic Range (SFDR)**

# Useful expressions

$$\text{ENOB} = \frac{\text{SINAD} - 1.76 \text{ dB}}{6.02}$$

$$\text{ENOB} = \frac{\text{SINAD}_{\text{MEASURED}} - 1.76 \text{ dB} + 20 \log \left( \frac{\text{Fullscale Amplitude}}{\text{Input Amplitude}} \right)}{6.02}.$$

$$\text{SNR} = 20 \log \left( \frac{S}{N} \right),$$

$$\text{THD} = 20 \log \left( \frac{S}{D} \right),$$

$$\text{SINAD} = 20 \log \left( \frac{S}{N + D} \right).$$

# Useful expressions

$$\frac{N + D}{S} = 10^{-\text{SINAD}/20}$$

Because the denominators of Eq. 6, Eq. 7, and Eq. 8 are all equal to S, the root sum N/S and D/S is equal to (N+D)/S as follows:

$$\frac{N + D}{S} = \left[ \left( \frac{N}{S} \right)^2 + \left( \frac{D}{S} \right)^2 \right]^{\frac{1}{2}} = \left[ \left( 10^{-\text{SNR}/20} \right)^2 + \left( 10^{-\text{THD}/20} \right)^2 \right]^{\frac{1}{2}}$$

$$\frac{N + D}{S} = \left[ 10^{-\text{SNR}/10} + 10^{-\text{THD}/10} \right]^{\frac{1}{2}}$$

Therefore, S/(N+D) must equal:

$$\frac{S}{N + D} = \left[ 10^{-\text{SNR}/10} + 10^{-\text{THD}/10} \right]^{-\frac{1}{2}},$$

and hence,

$$\text{SINAD} = 20 \log \left( \frac{S}{N + D} \right) = -10 \log \left[ 10^{-\text{SNR}/10} + 10^{-\text{THD}/10} \right]$$

Eq. 12 gives us SINAD as a function of SNR and THD.

Similarly, if we know SINAD and THD, we can solve for SNR as follows:

$$\text{SNR} = 20 \log \left( \frac{S}{N} \right) = -10 \log \left[ 10^{-\text{SINAD}/10} - 10^{-\text{THD}/10} \right]$$

Similarly, if we know SINAD and SNR, we can solve for THD as follows:

$$\text{THD} = 20 \log \left( \frac{S}{D} \right) = -10 \log \left[ 10^{-\text{SINAD}/10} - 10^{-\text{SNR}/10} \right]$$