

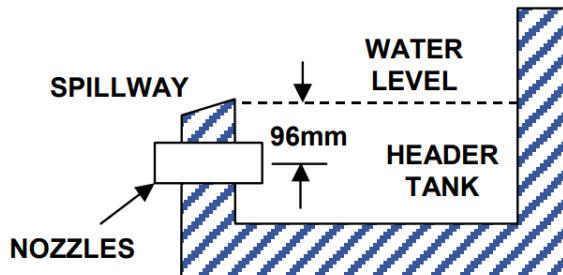
DATA CONVERTERS

Masum Hossain

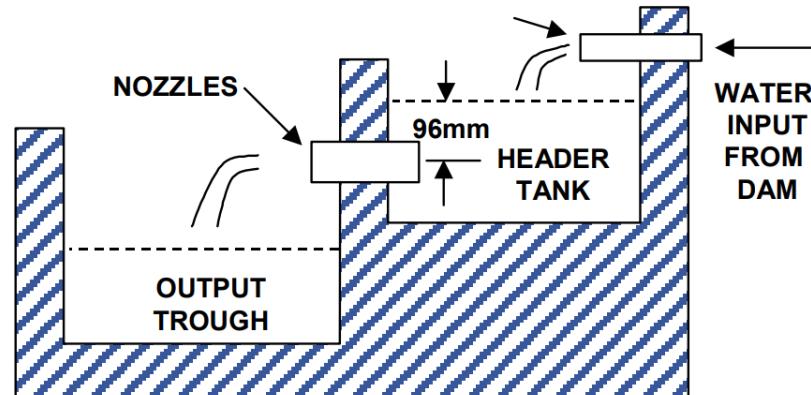
Today's topic

- Historical background on ADC
- Analog to Digital Conversion Process
- Quantization noise & SQNR
- SNDR, SFDR & ENOB

History of Data Converter: 18th Century



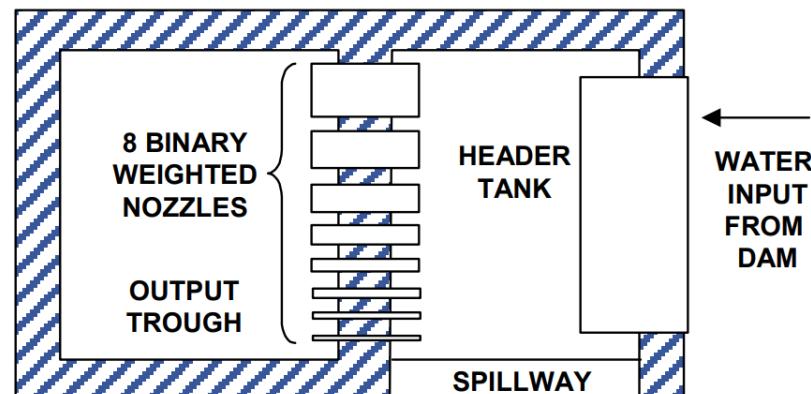
(A) HEADER SYSTEM: Note-The spillway and the nozzles need different outlets



(B) SECTIONAL VIEW OF METERING SYSTEM

(C) TOP VIEW OF
METERING SYSTEM
DETAILS SHOWING
BINARY WEIGHTED
NOZZLES

Adapted from:
Kâzım Çeçen, "Sinan's Water Supply
System in Istanbul," Istanbul Technical University /
Istanbul Water and Sewage Administration,
Istanbul Turkey, 1992-1993, pp. 165-167.



History of Data Converter: 19th Century

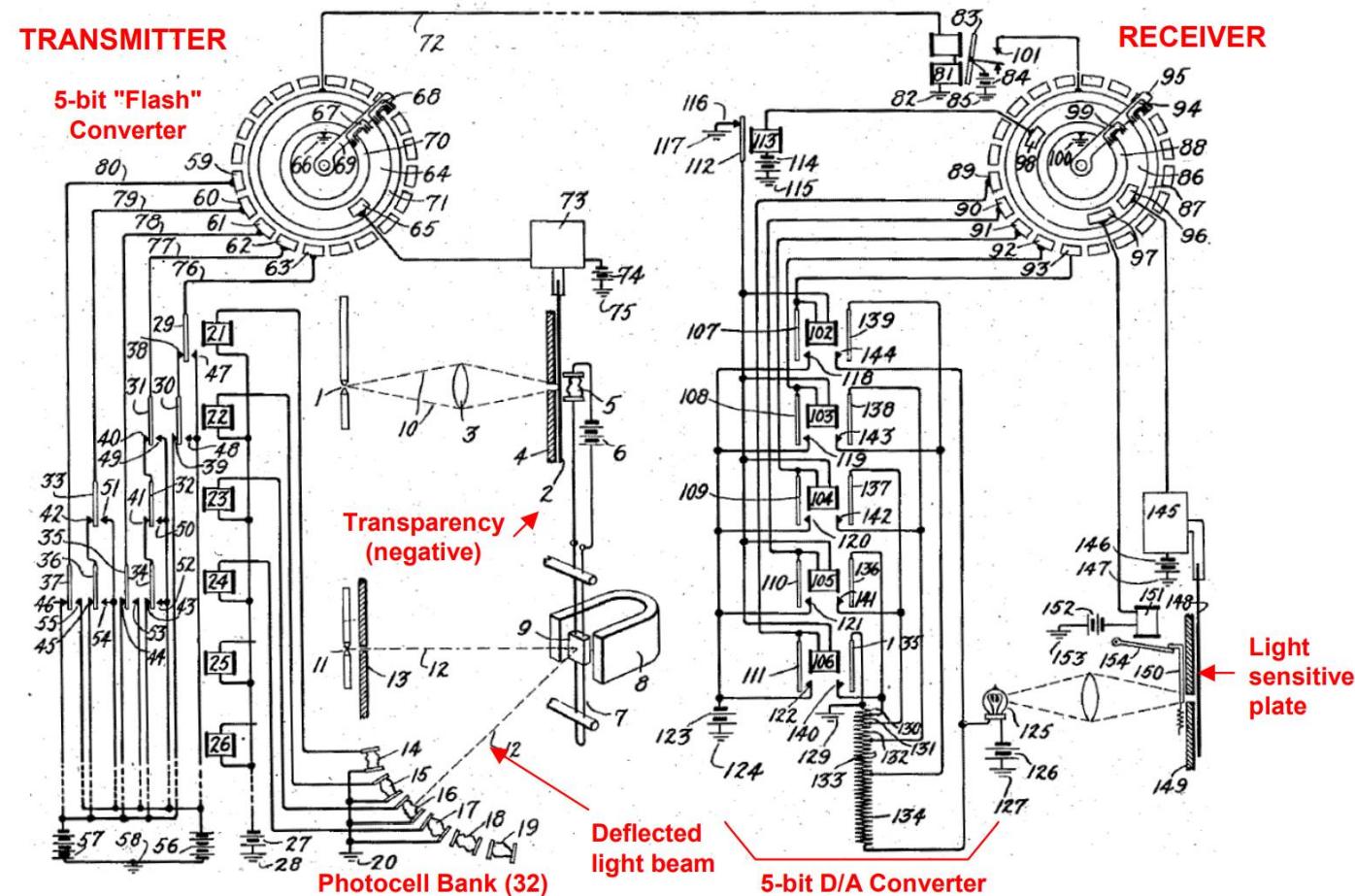
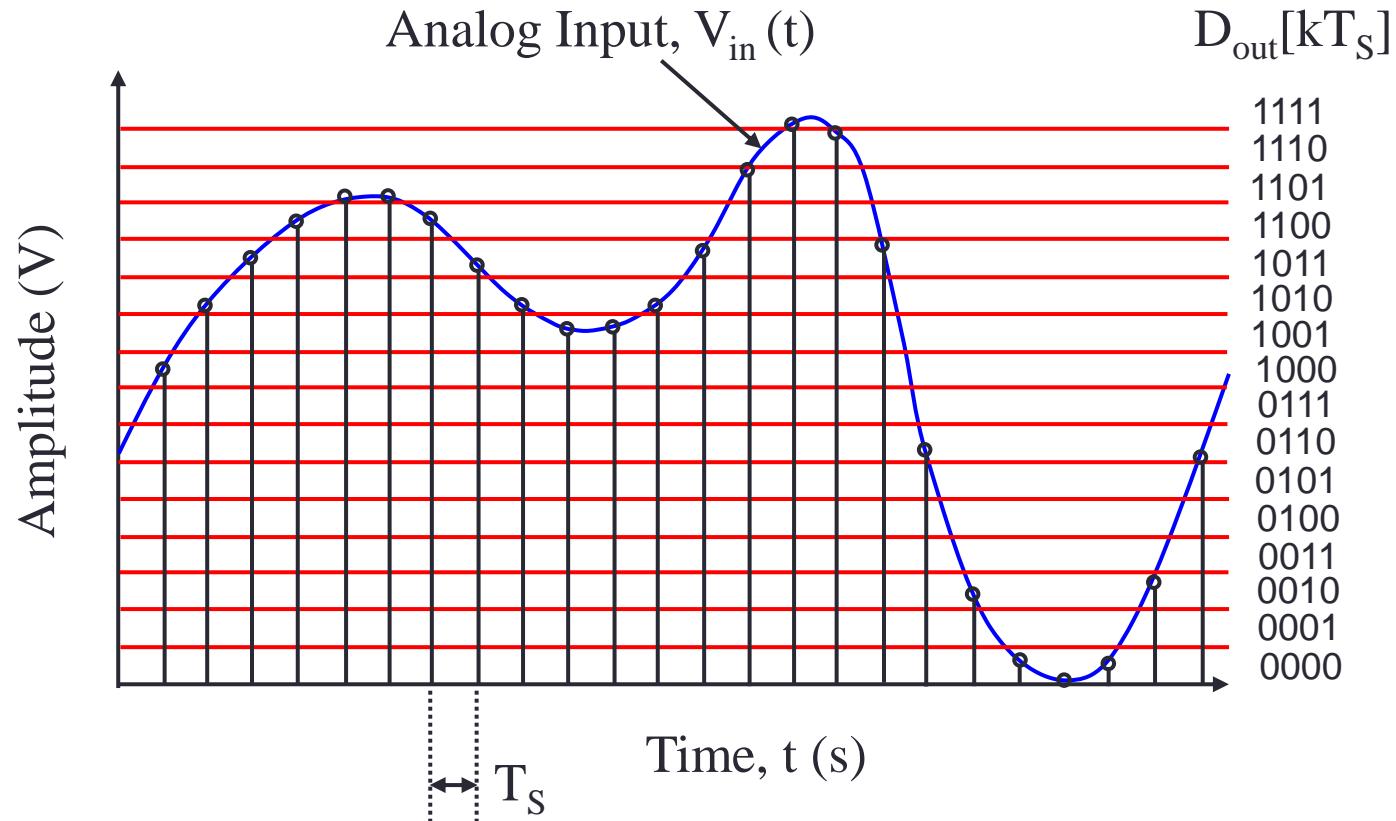
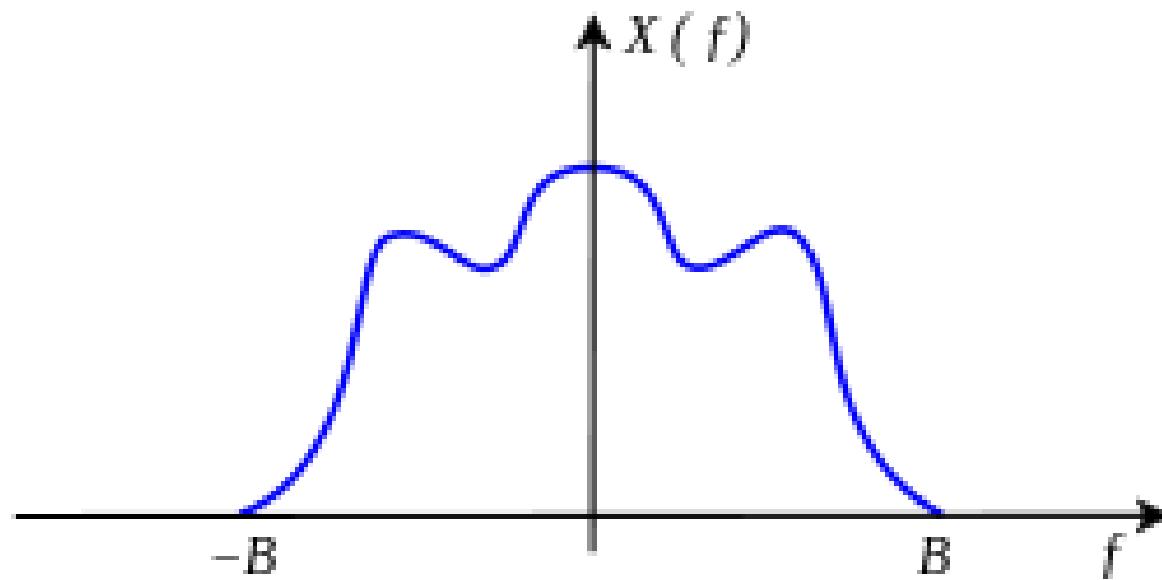


Figure 1.5: The First Disclosure of PCM: Paul M. Rainey, "Facimile Telegraph System," U.S. Patent 1,608,527, Filed July 20, 1921, Issued November 30, 1926

Flash Data Converter

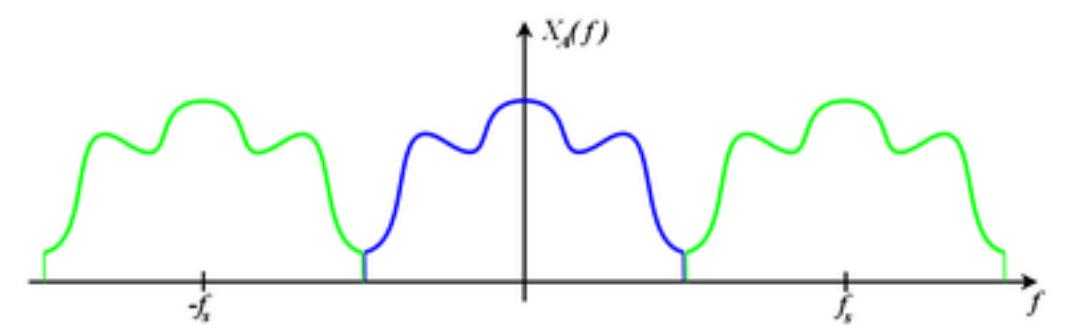
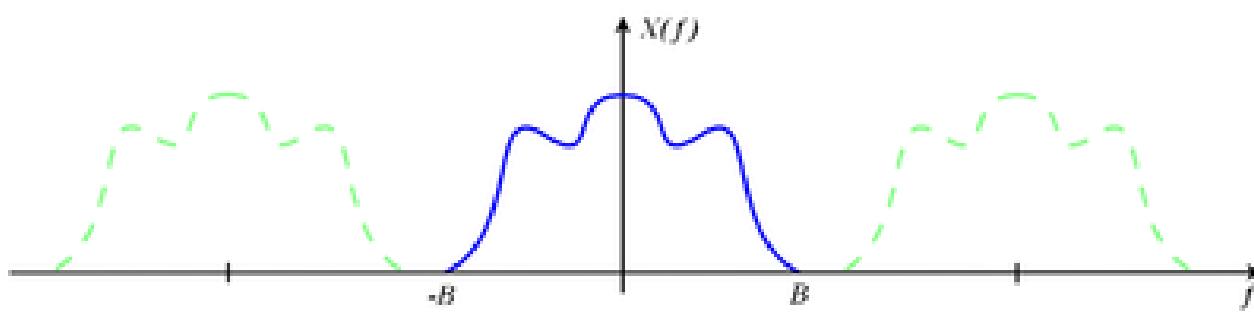
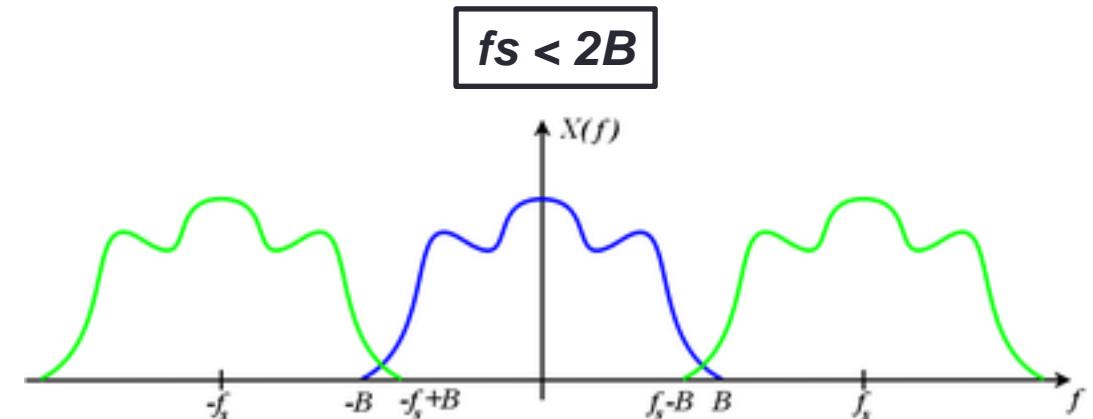
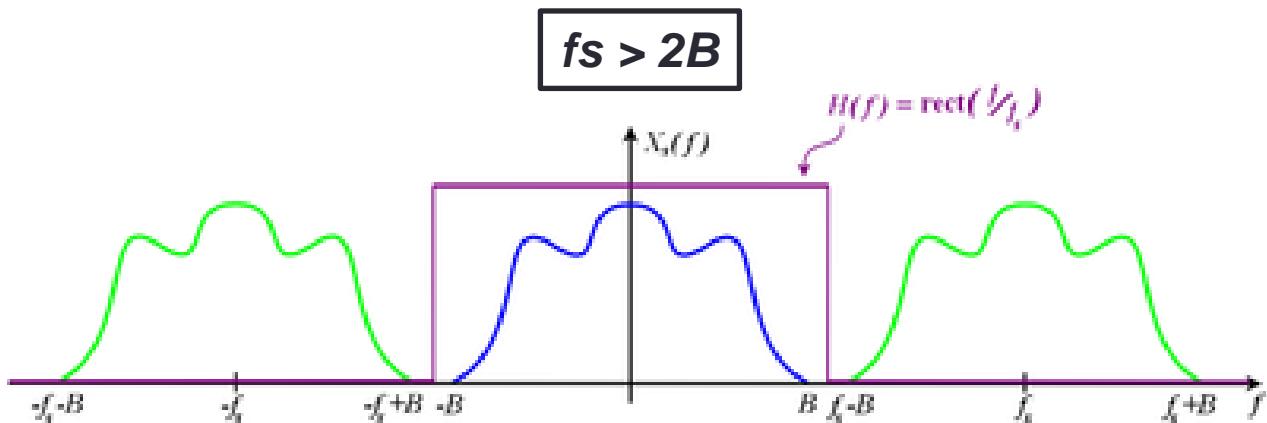


What should be the sampling Rate?



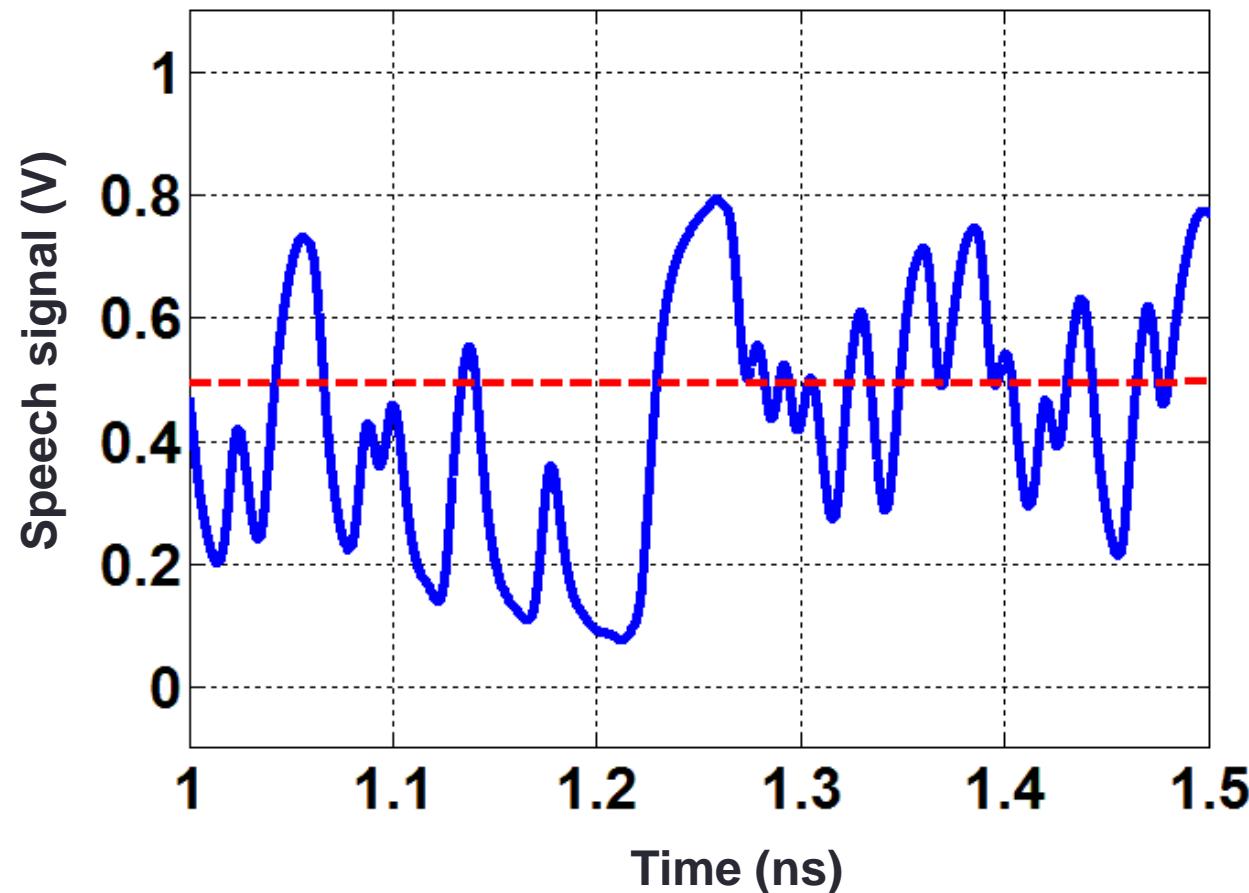
If a Signal has a Bandwidth of B , a sufficient sample-rate is $2B$ samples/second, or anything larger. Equivalently, for a given sample rate f_s , perfect reconstruction is guaranteed possible for a bandlimit $B < f_s/2$

Nyquist Sampling Theorem



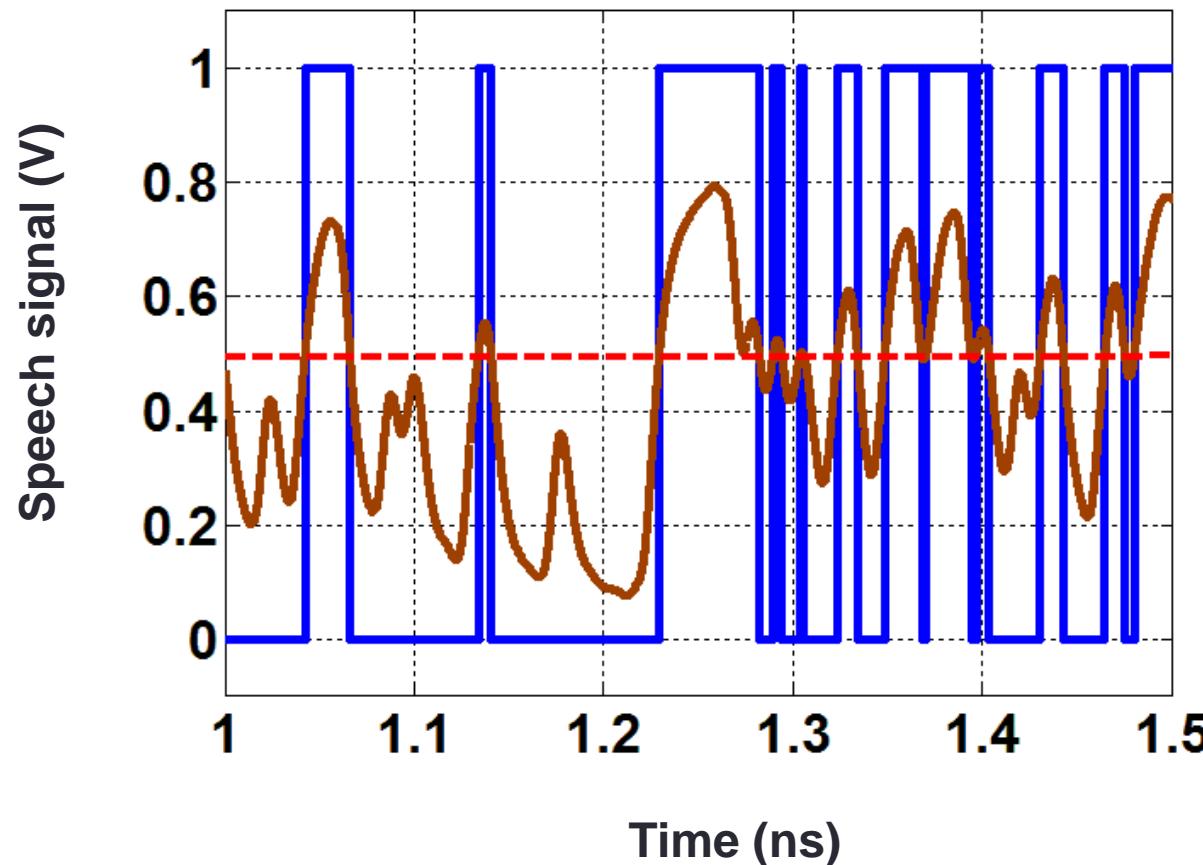
Analog to Digital

To digitize an analog signal we need to set a ‘threshold’ → 0.5 in this case

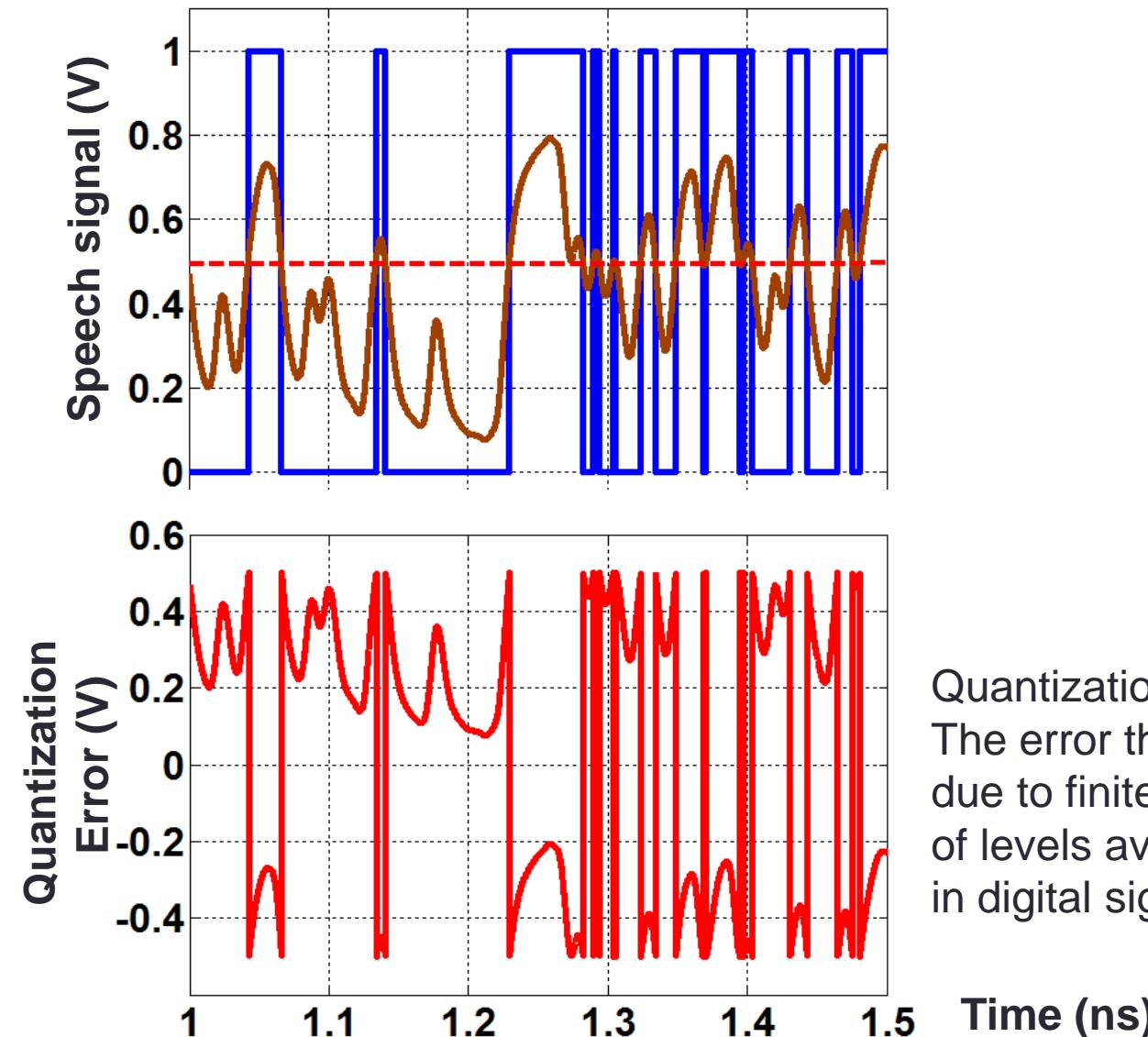


Analog to Digital with 1 bit Quantizer

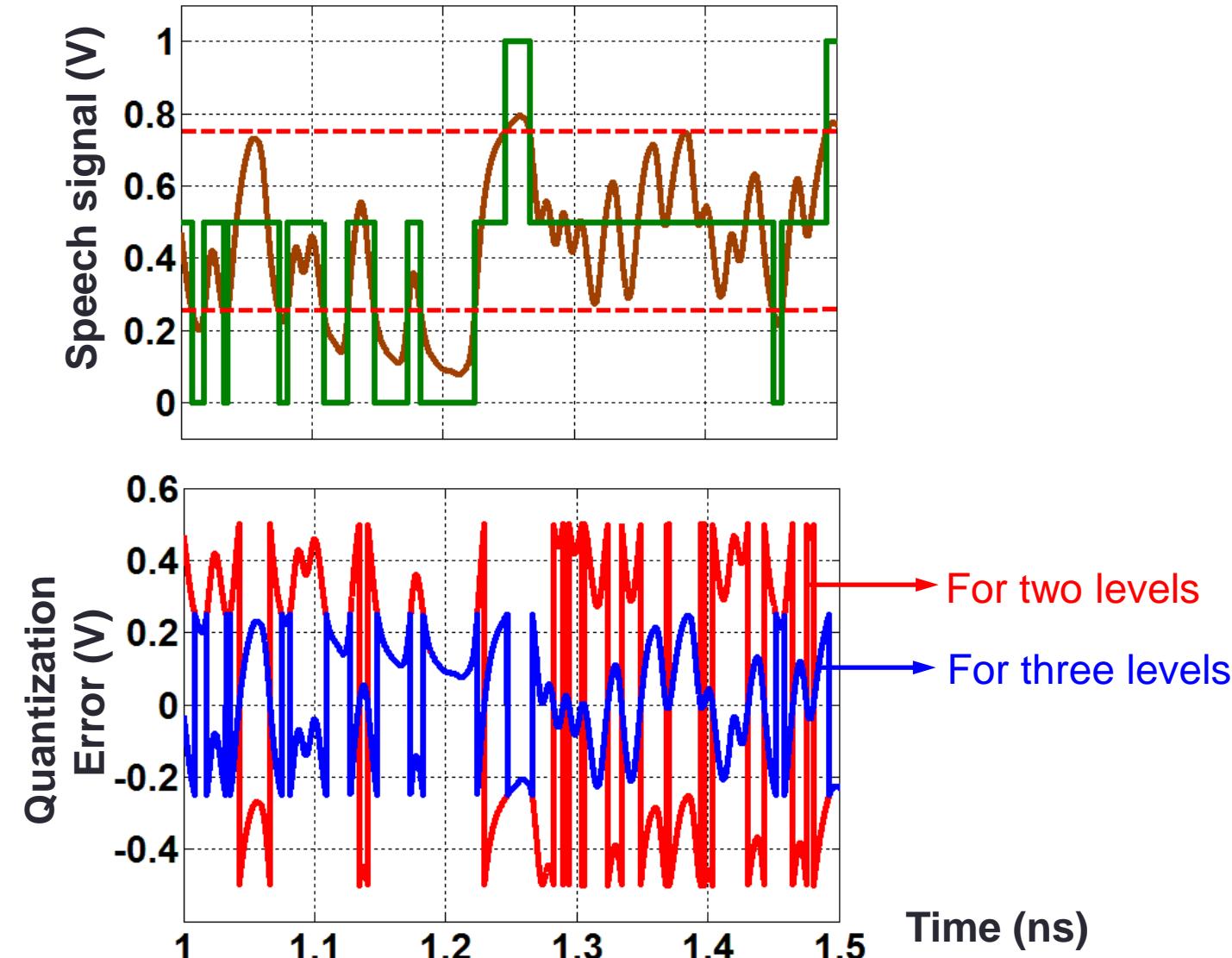
If signal is above 0.5 → digital output '1'
If signal is below 0.5 → digital output '0'



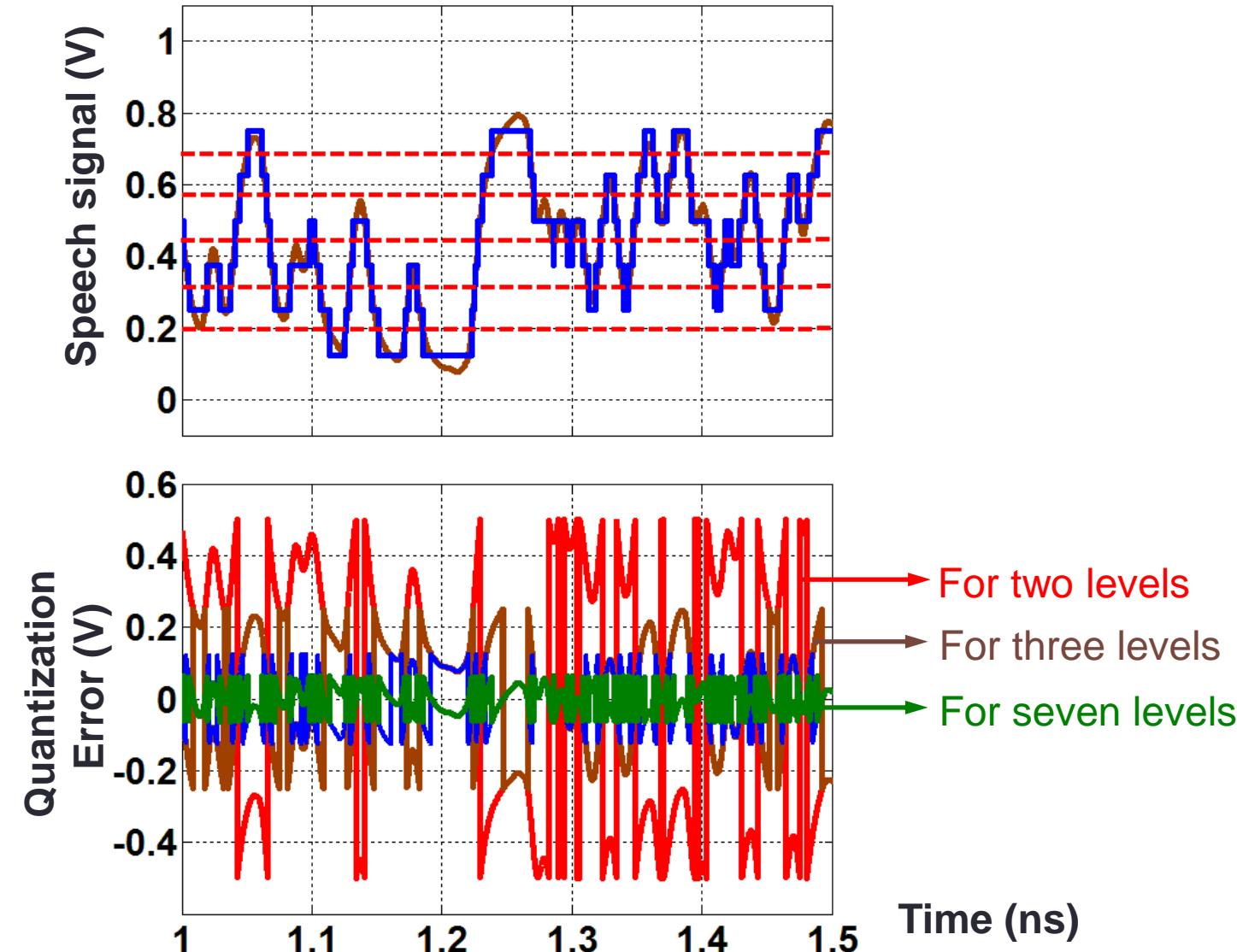
Quantization Noise is Digital system



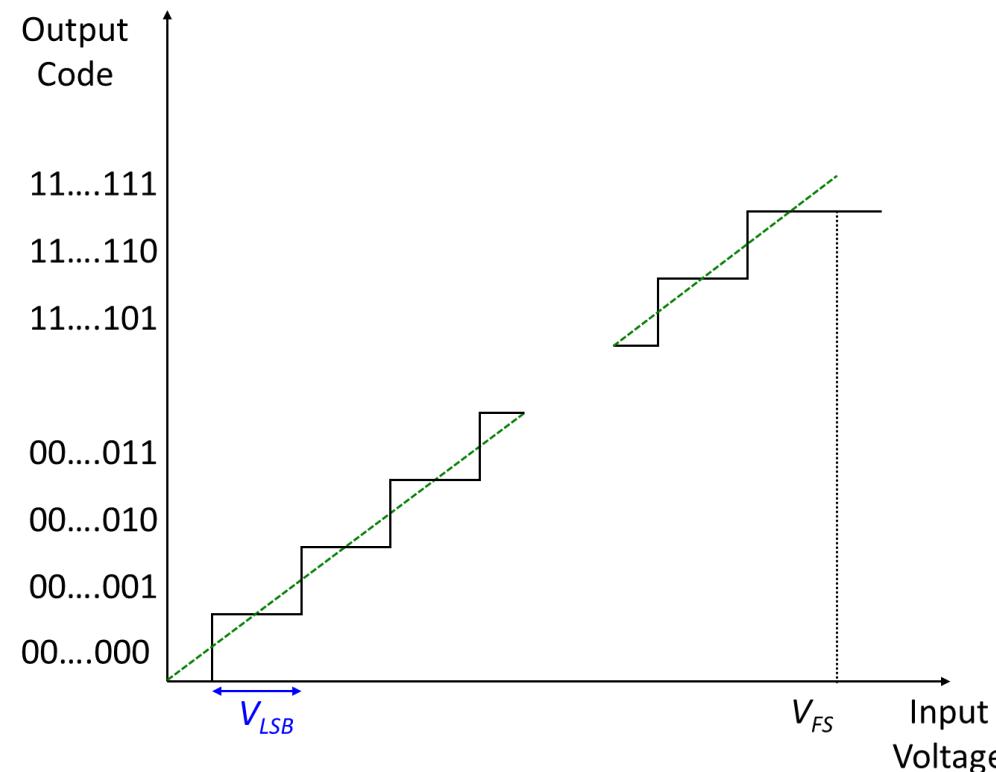
Noise is Digital system



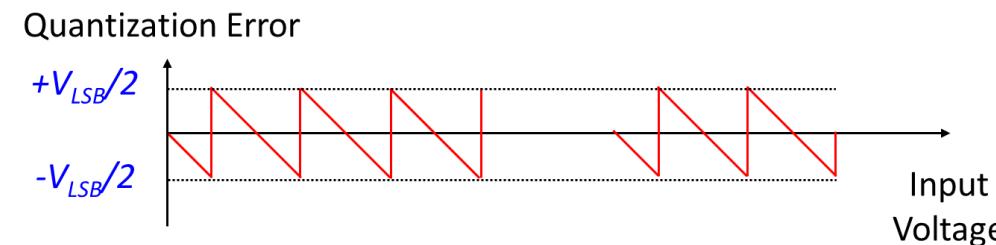
Noise is Digital system

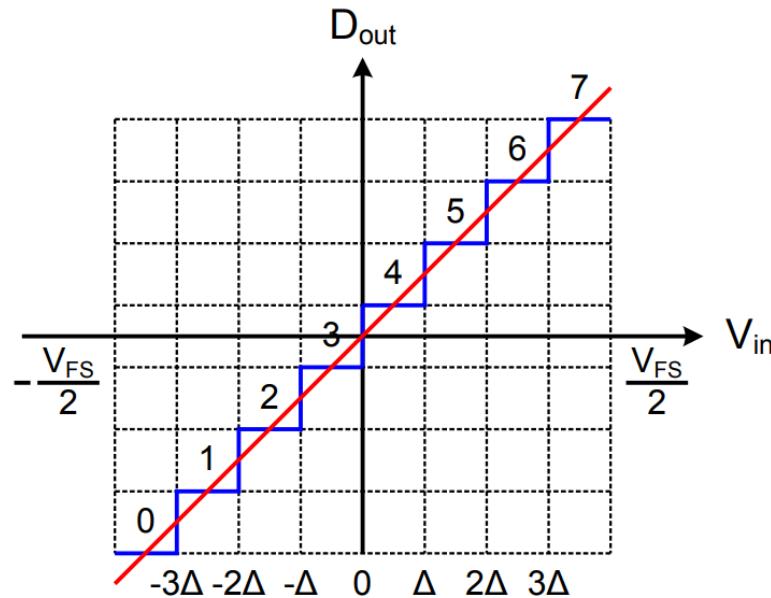


Quantization Noise

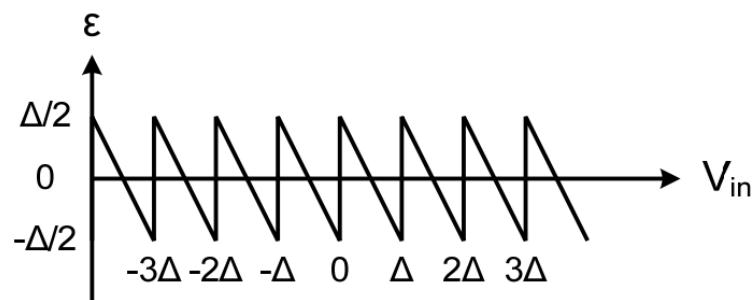


**2^N numbers of Comparisons
For N bit resolution**





$$N = 3$$



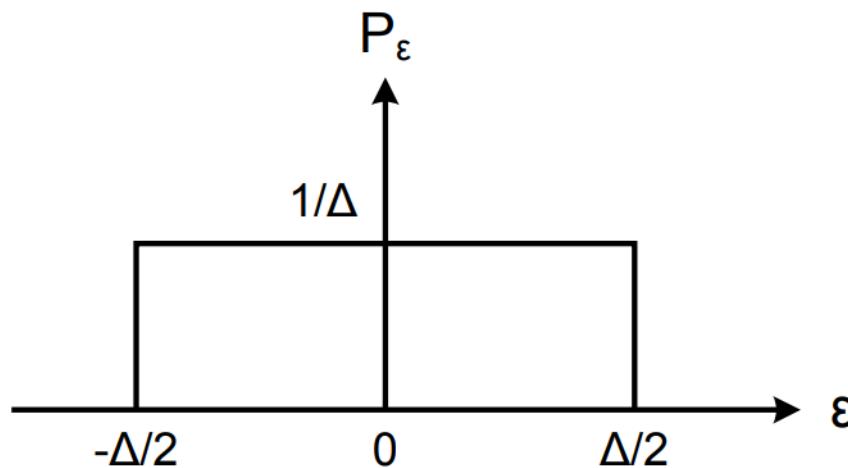
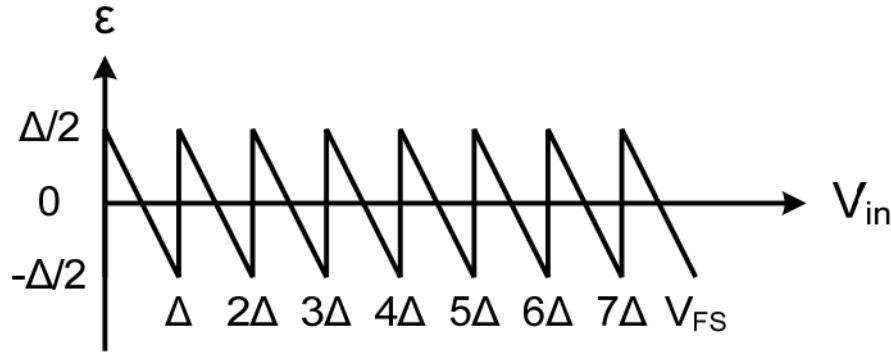
$$\Delta = \frac{V_{FS}}{2^N} = \text{LSB}$$

$$V_{in} \in [0, V_{FS}]$$

$$\epsilon = D_{out} \Delta - V_{in} = D_{out} \left(\frac{V_{FS}}{2^N} \right) - V_{in}$$

$$-\frac{\Delta}{2} \leq \epsilon \leq \frac{\Delta}{2}$$

“Random” quantization error
is usually regarded as noise



Assumptions:

- N is large
- $0 \leq V_{in} \leq V_{FS}$ and $V_{in} \gg \Delta$
- V_{in} is active
- ε is Uniformly distributed
- Spectrum of ε is white

$$\sigma_\varepsilon^2 = \int_{-\Delta/2}^{\Delta/2} \varepsilon^2 \cdot \frac{1}{\Delta} \cdot d\varepsilon = \frac{\Delta^2}{12}$$

SQNR and ENOB

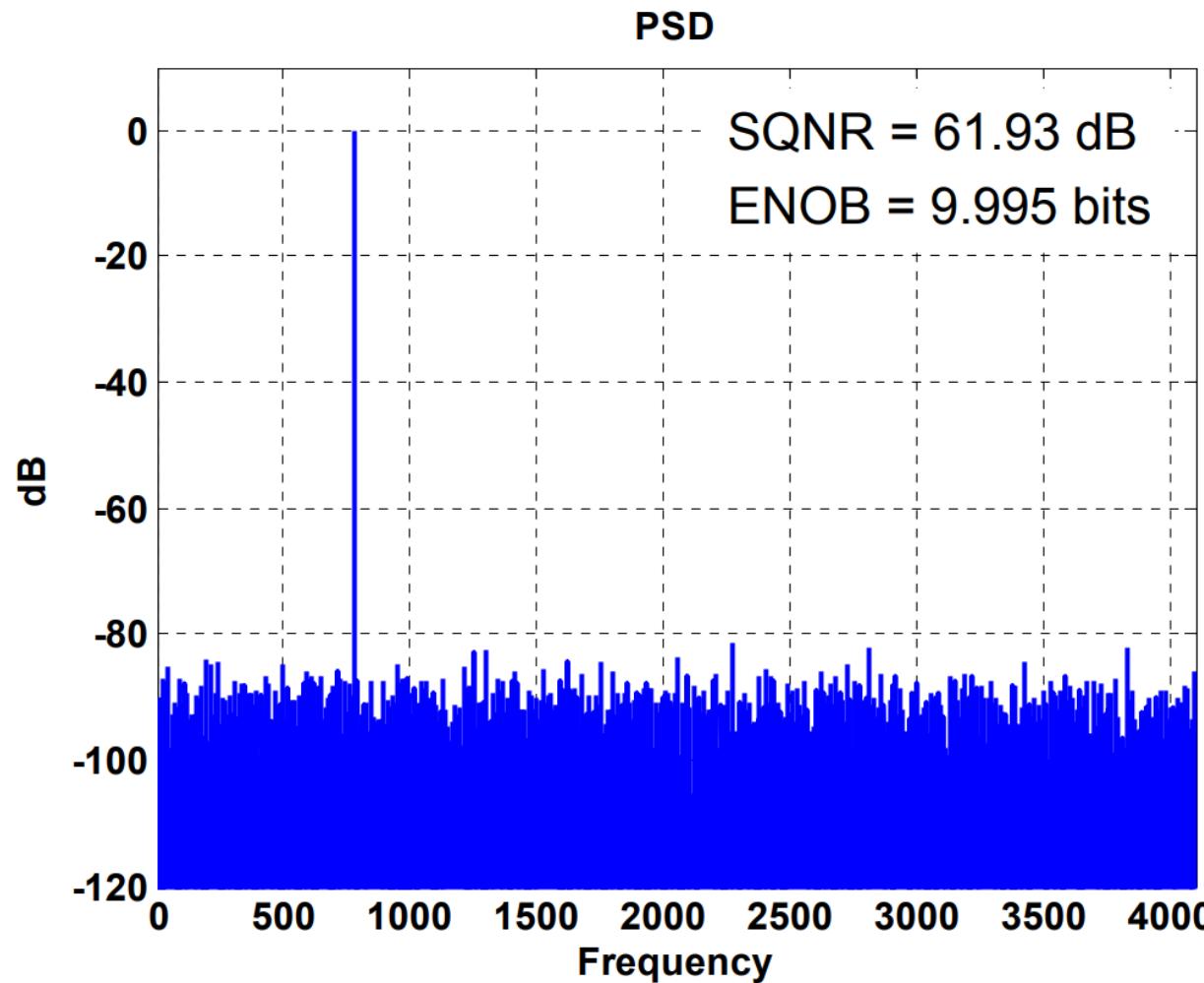
Assume V_{in} is sinusoidal with $V_{p-p} = V_{FS}$,

$$SQNR = \frac{V_{FS}^2 / 8}{\sigma_e^2} = \frac{(2^N \Delta)^2 / 8}{\Delta^2 / 12} = 1.5 \times 2^{2N},$$

SQNR = $6.02 \times N + 1.76$ dB

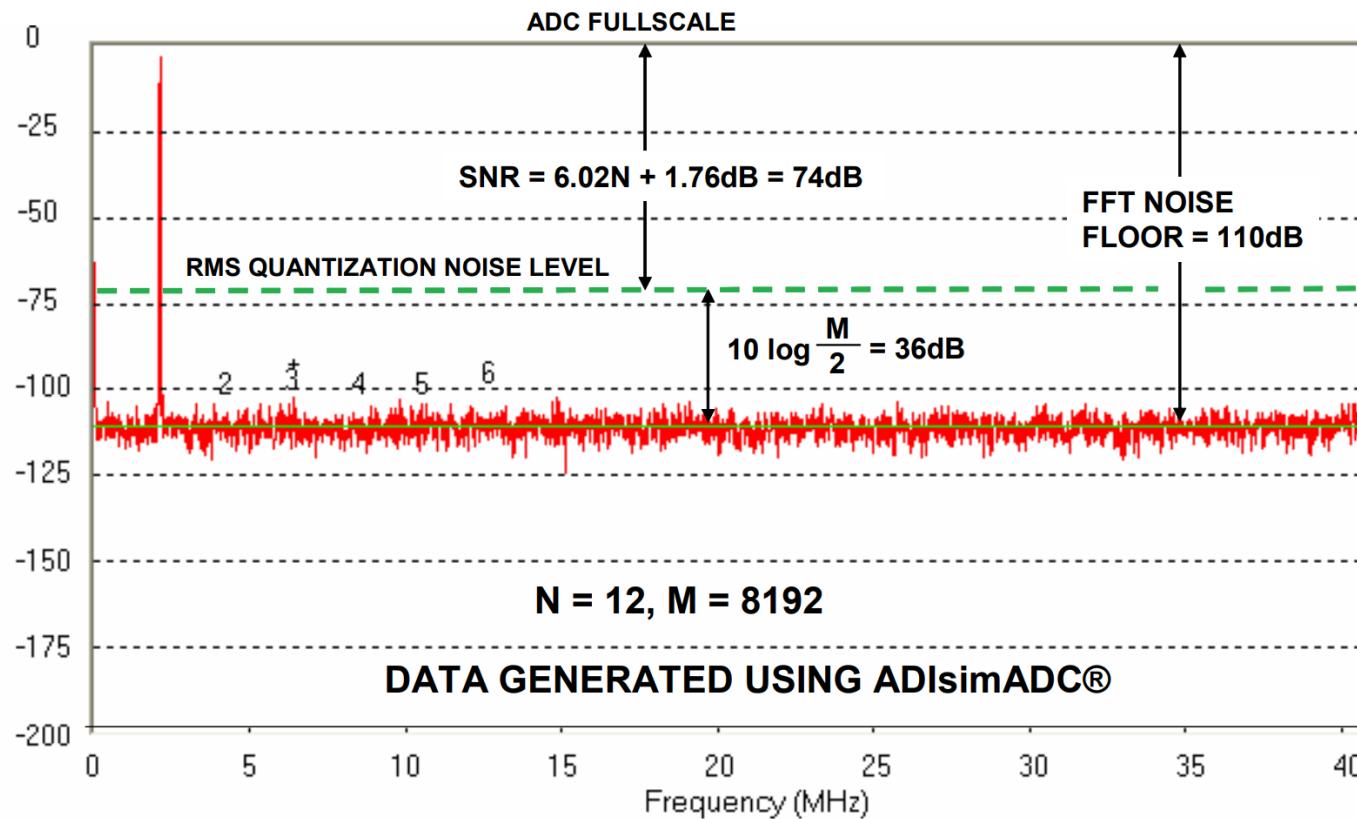
N (bits)	SQNR (dB)
8	49.9
10	62.0
12	74.0
14	86.0

- SQNR depicts the theoretical performance of an ideal ADC
- In reality, ADC performance is limited by many other factors:
 - Electronic noise (thermal, 1/f, coupling/substrate, etc.)
 - Distortion (measured by THD, SFDR, IM3, etc.)



- $N = 10$ bits
- 8192 samples, only $f = [0, f_s/2]$ shown
- Normalized to V_{in}
- $f_s = 8192, f_{in} = 779$
- f_{in} and f_s must be incommensurate

$$\text{ENOB} = \frac{\text{SQNR} - 1.76 \text{ dB}}{6.02 \text{ dB}}$$



**Figure 2: FFT Output for an Ideal 12-Bit ADC, Input = 2.111MHz,
 f_s = 82MSPS, Average of 5 FFTs, M = 8192,
Data Generated from [ADIsimADC®](#)**

Nonlinear Distortion

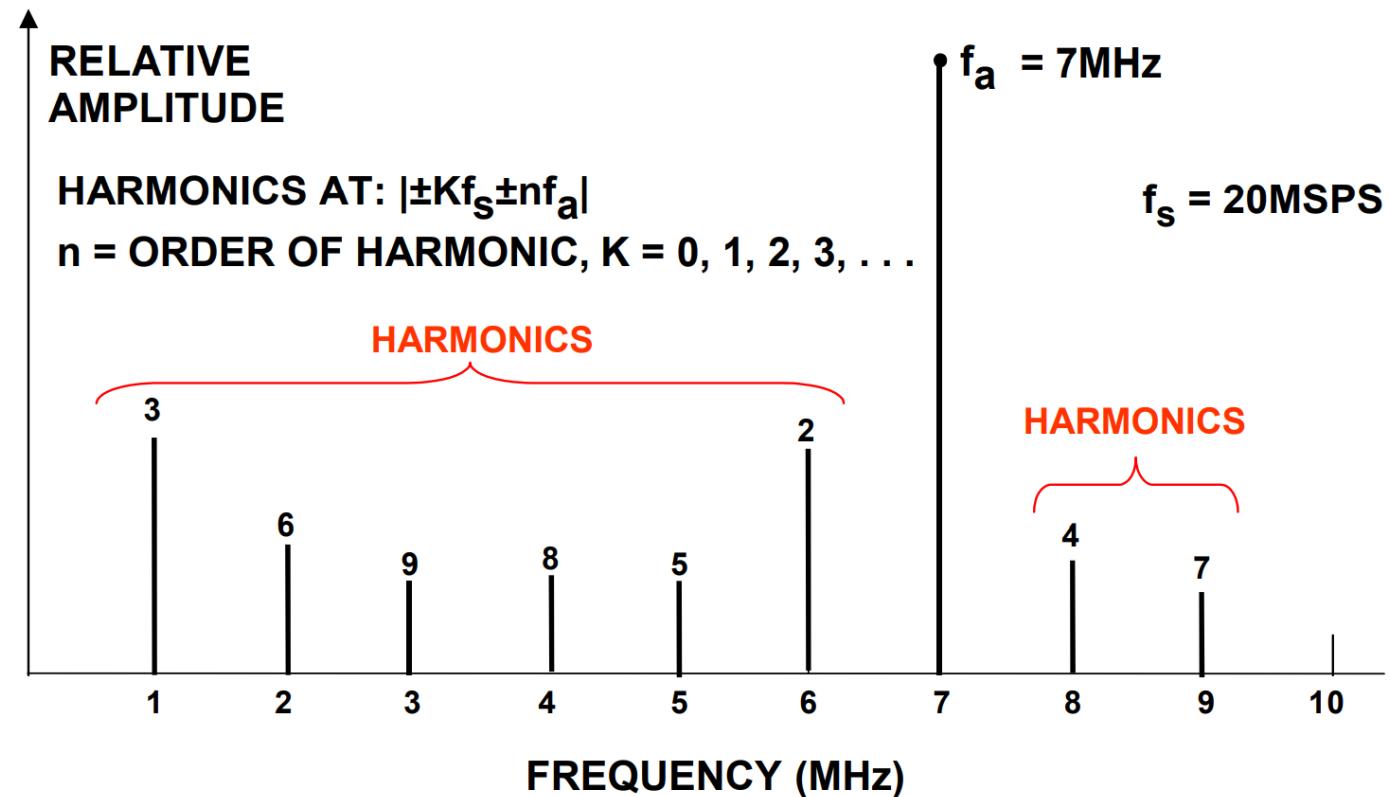


Figure 3: Location of Distortion Products: Input Signal = 7 MHz, Sampling Rate = 20 MSPS

SFDR

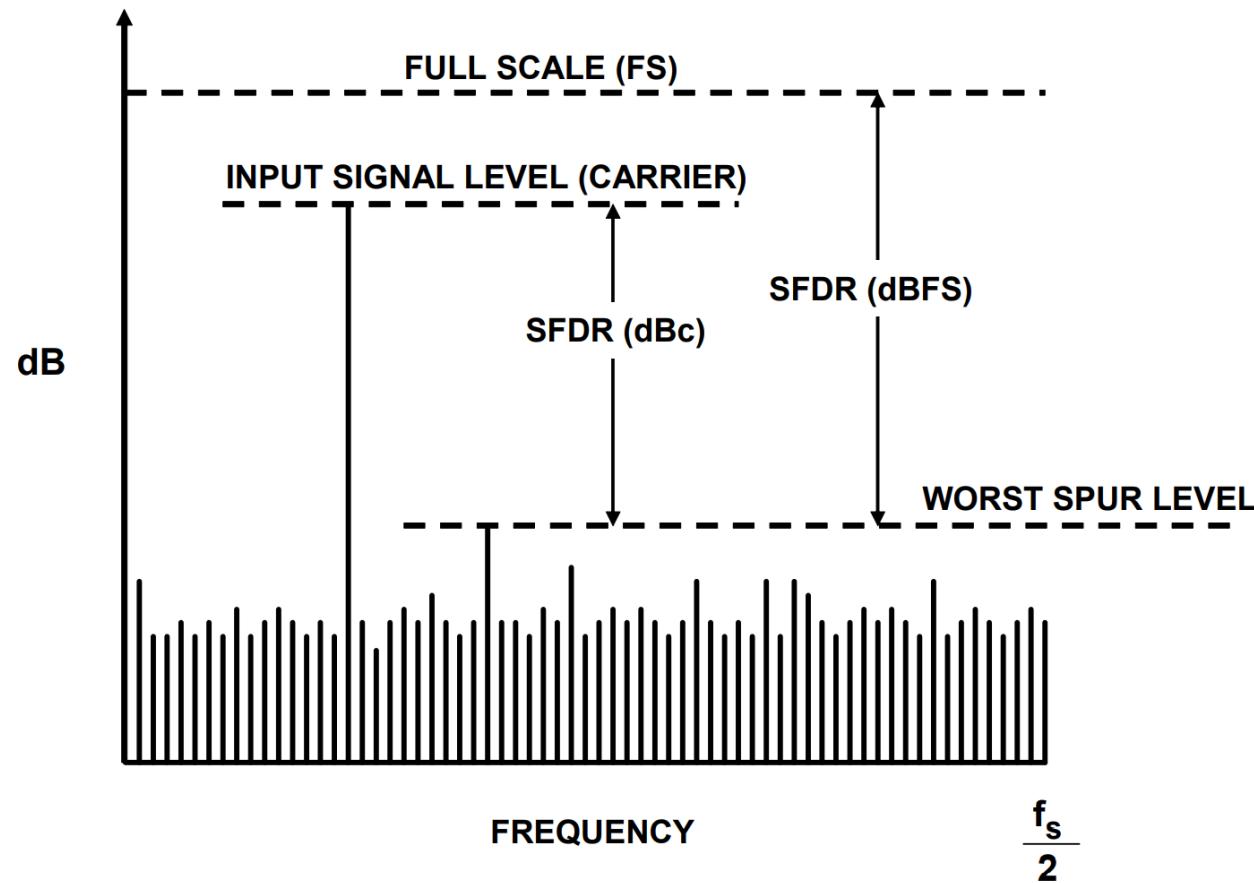


Figure 4: Spurious Free Dynamic Range (SFDR)

Useful expressions

$$\text{ENOB} = \frac{\text{SINAD} - 1.76 \text{ dB}}{6.02}$$

$$\text{ENOB} = \frac{\text{SINAD}_{\text{MEASURED}} - 1.76 \text{ db} + 20 \log \left(\frac{\text{Fullscale Amplitude}}{\text{Input Amplitude}} \right)}{6.02}.$$

$$\text{SNR} = 20 \log \left(\frac{S}{N} \right),$$

$$\text{THD} = 20 \log \left(\frac{S}{D} \right),$$

$$\text{SINAD} = 20 \log \left(\frac{S}{N + D} \right).$$

Useful expressions

$$\frac{N+D}{S} = 10^{-SINAD/20}$$

Because the denominators of Eq. 6, Eq. 7, and Eq. 8 are all equal to S, the root sum N/S and D/S is equal to (N+D)/S as follows:

$$\frac{N+D}{S} = \left[\left(\frac{N}{S} \right)^2 + \left(\frac{D}{S} \right)^2 \right]^{\frac{1}{2}} = \left[\left(10^{-SNR/20} \right)^2 + \left(10^{-THD/20} \right)^2 \right]^{\frac{1}{2}}$$

$$\frac{N+D}{S} = \left[10^{-SNR/10} + 10^{-THD/10} \right]^{\frac{1}{2}}.$$

Therefore, S/(N+D) must equal:

$$\frac{S}{N+D} = \left[10^{-SNR/10} + 10^{-THD/10} \right]^{-\frac{1}{2}},$$

and hence,

$$SINAD = 20 \log \left(\frac{S}{N+D} \right) = -10 \log \left[10^{-SNR/10} + 10^{-THD/10} \right]$$

Eq. 12 gives us SINAD as a function of SNR and THD.

Similarly, if we know SINAD and THD, we can solve for SNR as follows:

$$SNR = 20 \log \left(\frac{S}{N} \right) = -10 \log \left[10^{-SINAD/10} - 10^{-THD/10} \right].$$

Similarly, if we know SINAD and SNR, we can solve for THD as follows:

$$THD = 20 \log \left(\frac{S}{D} \right) = -10 \log \left[10^{-SINAD/10} - 10^{-SNR/10} \right].$$