

# Theory for `lset-opt` package

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## 1 Definitions

**grid** A two-dimensional regularly-spaced  $m \times n$  set of points.

$\phi$ ,  $\phi_i$ , **or**  $\phi(x, y)$  Level-set function defined on grid. The zero-crossing of  $\phi$  defines the contour of the shapes on the grid.

## 2 Initialization

Given a candidate level-set function,  $\hat{\phi}$ , a regularized  $\phi$  is computed in the following way:

1. If any element of  $\hat{\phi}$ ,  $\hat{\phi}_i$ , is exactly equal to 0, then let  $\hat{\phi}_i = \epsilon$  where  $\epsilon$  is the smallest positive number available.
2. For all  $\hat{\phi}_i$  not adjacent to a boundary point, fix the corresponding  $\phi_i$  as

$$\phi_i = \text{sign}(\hat{\phi}_i) = \begin{cases} -1 & \hat{\phi}_i < 0, \\ +1 & \hat{\phi}_i > 0. \end{cases} \quad (1)$$

3. To determine the remaining  $\phi_i$ , solve the following:

$$\text{minimize} \quad \|D\phi\|^2 \quad (2)$$

$$\text{subject to} \quad A\phi = 0, \quad (3)$$

where

**3 Conversion to fractional-filling**

**4 Topology update**