

Downloading Application

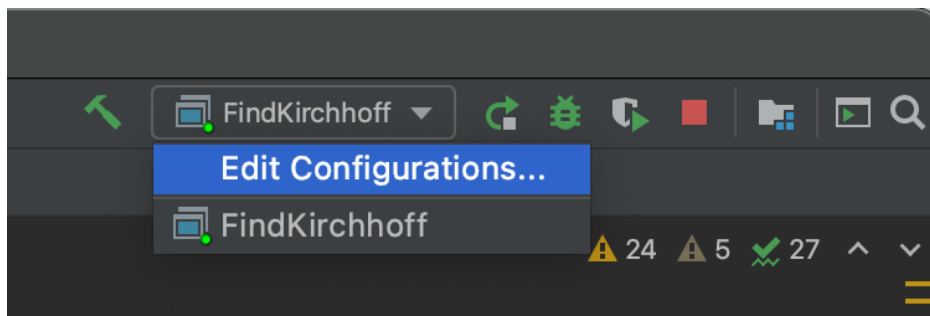
1. Download IntelliJ at <https://www.jetbrains.com/idea/download/#section=mac>, community version
2. Open the downloaded dmg, drag it into “Applications”
3. Open IntelliJ
4. From IntelliJ, open the entire “Kirchhoff Code” folder that I sent
5. Click “src”, go to “FindKirchhoff.java”

To use the code:

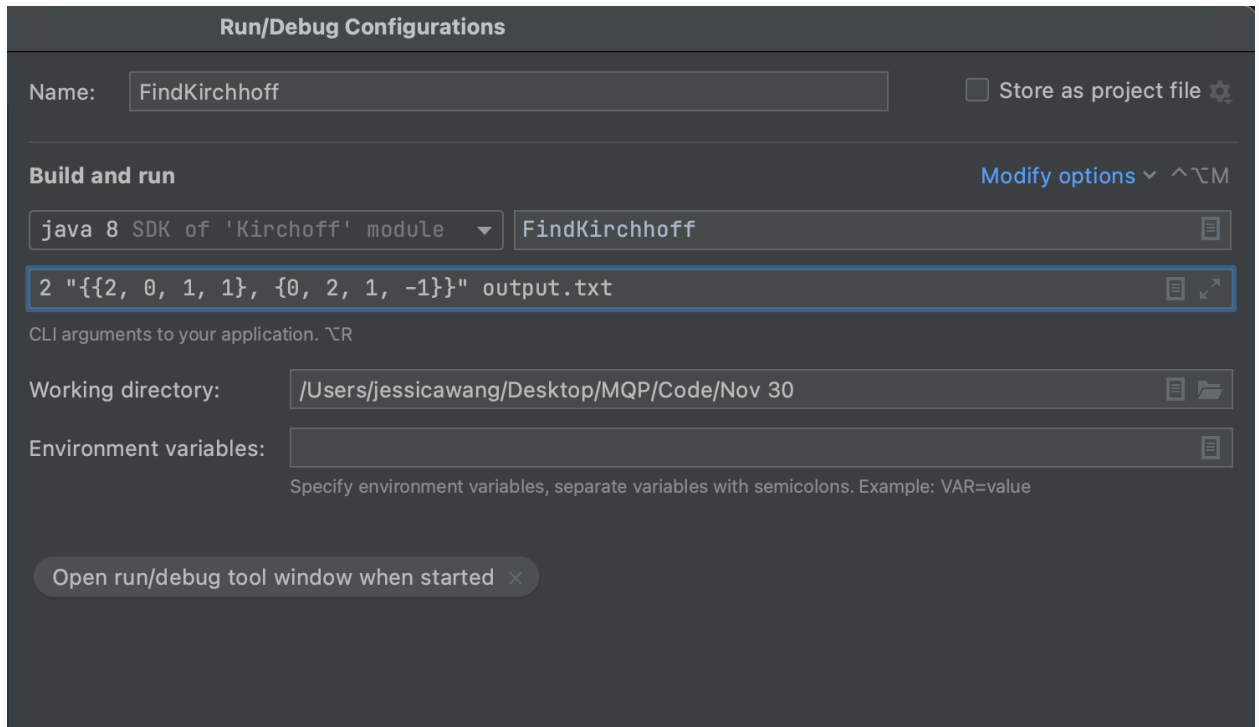
1. To find Kirchhoff graphs **with row matrix**, first make sure the appropriate line in the “main” function is not commented out. (Here at line 45 there is no “//” in front of the code, so it is functioning)

```
44     try(FileWriter writer = new FileWriter(outputFile, append: true)) {  
45         find_kirchhoff_with_matrix(r, multiplicity, wants_prime: true, writer, outputFile);  
46         //find_kirchhoff_with_cuts(r, store, multiplicity, true, writer, outputFile);  
47     }
```

Go to top right and click “Edit Configurations”



And type in to the box:



The format is:

`multiplicity "Row Matrix" output.txt`

So the line

`2 "{2, 0, 1, 1}, {0, 2, 1, -1}" output.txt`

means we want to find all Kirchhoff graphs of multiplicity 2 with matrix

$$R = \begin{bmatrix} 2 & 0 & 1 & 1 \\ 0 & 2 & 1 & -1 \end{bmatrix}$$

and we want to put all the information of the Kirchhoff graph into a text file called "output.txt", which can be found in the same folder of the code.

2. Another way to use the code is to give it a list of **vertex cuts** instead of the row matrix.

Again, make sure the appropriate line in "main" is lit up:

```

44     try(FileWriter writer = new FileWriter(outputFile, append: true)) {
45         //find_kirchhoff_with_matrix(r, multiplicity, true, writer, outputFile);
46         find_kirchhoff_with_cuts(r, store, multiplicity, wants_prime: true, writer, outputFile);
47     }

```

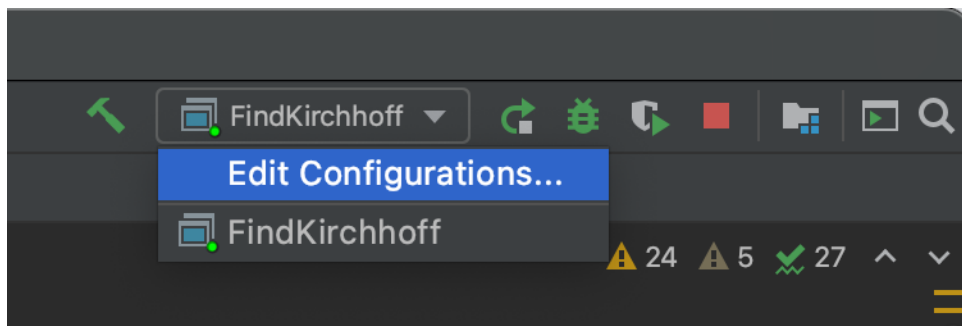
And change the first few lines like this:

```

31 ▶ @ public static void main(String[] args) throws IOException {
32
33
34     int multiplicity = Integer.parseInt(args[0]);
35     int[][] r = stringToArray(args[1]);
36     int[][] store = stringToArray(args[2]);
37     File outputFile = new File(args[3]);

```

Now we can once again go to “edit configurations”



In the box, the format is now:

```

multiplicity "Row Matrix" "Vertex Cuts" output.txt

```

So this block of code

```

6
"{{2, 0, 1, 1}, {0, 2, 1, -1}}"
"{{-6, -6, -6, 0}, {-6, -4, -5, -1}, {-6, -2, -4, -2}, {-6, 0, -3, -3},
{-6, 2, -2, -4}, {-6, 4, -1, -5}, {-6, 6, 0, -6}, {-4, -6, -5, 1}, {-4, -4, -4, 0},
{-4, -2, -3, -1}, {-4, 0, -2, -2}, {-4, 2, -1, -3}, {-4, 4, 0, -4}, {-4, 6, 1, -5},
{-2, -6, -4, 2}, {-2, -4, -3, 1}, {-2, -2, -2, 0}, {-2, 0, -1, -1}, {-2, 2, 0, -2},
{-2, 4, 1, -3}, {-2, 6, 2, -4}, {0, -6, -3, 3}, {0, -4, -2, 2}, {0, -2, -1, 1}, {0, 0, 0, 0},
{0, 2, 1, -1}, {0, 4, 2, -2}}"
output.txt

```

Means that we want to find all Kirchhoff graphs of multiplicity 6, associated with the row

matrix $R = \begin{bmatrix} 2 & 0 & 1 & 1 \\ 0 & 2 & 1 & -1 \end{bmatrix}$, using the list of vertex cuts that we have inputted, and save all the information into a file called “output.txt”.

Remark

“find_kirchhoff_with_matrix” will take longer to run than “find_kirchhoff_with_cuts”, because the matrix function must first find all the appropriate vertex cuts before trying to find any graph.

Structure of the code

Below is a short description of the backtracking exhaustive search algorithm for a given matrix R and multiplicity m_{\max} .

1. Find all possible vertex cuts with entries between $-m_{\max}$ and m_{\max} by finding all linear combinations of the row vectors of R . Let Λ be the set of all possible vertex cuts with an arbitrary order. Initialize \mathbb{T} to be an empty list which we will add vertices into. This will serve as our “to-do” list.
2. Construct an anchor vertex, assign the first vertex cut in Λ to the anchor vertex. Add the set of edges according to the vertex cut. If doing so results in vertices to have coordinates (x_1, x_2) where $x_1 < x_2$, then we abandon this vertex cut and remove all the vertices that were constructed. Add all vertices neighboring to the anchor vertex to \mathbb{T} .
3. Go to the next vertex in the graph (according to the order in \mathbb{T}), assign an appropriate vertex cut to it. Delete this vertex in \mathbb{T} and add its neighboring vertices to \mathbb{T} . If the current vertex cut is not in Λ or doing so results in having $m(\mathbf{G})$ greater than m_{\max} , then we abandon this vertex and goes back to the previous vertex, and assign the next vertex cut in Λ to it.
4. We repeat step 3 until either
 - we find a graph with all vertices assigned to a vertex cut in S , which means we have likely found a Kirchhoff graph, or
 - we have exhausted all cuts in S , which means there is no Kirchhoff graph with multiplicity n , $n < m_{\max}$ associated to R .
5. If a Kirchhoff graph is found, we add it to a list of graphs, and continue the process with step 2 to find the next possible graph until \mathbb{T} is empty.

Examples

Both examples from the section above mean we want to find all prime and composite graphs of multiplicity 4 with the given row matrix and list of cuts.

It produces the following 19 graphs:

