

California State Polytechnic University | Pomona  
Electrical and Computer Engineering Department  
Control System Laboratory  
ECE 3709L  
Fall 2018  
DC Motor Control | Final Report

From:  
Johnny Estrada  
Electrical and Computer Engineering Department

To:  
Professor Tarek Elsharhawy  
Electrical and Computer Engineering Department

Date:  
December 6, 2018

## **Table of Contents**

|            |  |           |
|------------|--|-----------|
| <b>1.0</b> | <b>OBJECTIVE .....</b>   | <b>3</b>  |
| <b>2.0</b> | <b>PROCEDURE .....</b>   | <b>3</b>  |
| <b>3.0</b> | <b>SUMMARY &amp; CONCLUSION .....</b>                          | <b>3</b>  |
|            | <b>APPENDIX A: BLOCK DIAGRAM .....</b>                         | <b>5</b>  |
|            | <b>APPENDIX B: WIRING SCHEMATIC AND CIRCUIT ASSEMBLY .....</b> | <b>6</b>  |
|            | <b>APPENDIX C: SOFTWARE SETUP .....</b>                        | <b>8</b>  |
|            | <b>APPENDIX C CONTINUED .....</b>                              | <b>9</b>  |
|            | <b>APPENDIX D: TE TUNING METHOD .....</b>                      | <b>10</b> |
|            | <b>APPENDIX E: THE MATHEMATICAL MODEL .....</b>                | <b>11</b> |
|            | <b>APPENDIX F: FREQUENCY RESPONSE ANALYSIS .....</b>           | <b>12</b> |
|            | <b>APPENDIX G: AUTOMATION OF MATLAB .....</b>                  | <b>14</b> |
|            | <b>APPENDIX H: MATLAB PID TUNER .....</b>                      | <b>16</b> |
|            | <b>APPENDIX I: LOAD SETUP .....</b>                            | <b>19</b> |
|            | <b>APPENDIX J: TE TUNING VS. PID TUNER MATLAB .....</b>        | <b>21</b> |
|            | <b>APPENDIX K: ACCUMULATED GRADES .....</b>                    | <b>29</b> |
|            | <b>REFERENCES .....</b>  | <b>39</b> |

## 1.0 Objective

The objective of this lab was to acquire an understanding of control systems engineering through experience with design, testing, and model implementation.

## 2.0 Procedure

1. Block Diagram highlighting key components & interactions. (Appendix A)
2. Wiring schematic and circuit assembly. (Appendix B)
3. Software Setup. (Appendix C)
4. Performance of TE Tuning Method. (Appendix D)
5. Development of a mathematical model of the system. (Appendix E)
6. Frequency Response Analysis (SISO). (Appendix F)
7. Automation of Matlab analysis (script). (Appendix G)
8. PID Tuner Design using Matlab. (Appendix H).
9. Load execution. (Appendix I)
10. Analysis performance with load with consideration and application of previous procedures. (Appendix J)

## 3.0 Summary & Conclusion

The controller performed adequately, sustaining most of the load in both direction with the original  $K_I$  and  $K_P$  parameters that were supplied to the LabView module. However, the response for the downward direction was inadvertently too fast given that gravity is a much bigger factor in this direction adding to the speed at which the elevator would travel. Therefore, to compensate we applied a higher integral gain allowing the aggressive nature of the response downward to formulate into a recognizable smooth curve

within the given timing constraints. This obstacle and the fact that weight of the quarters was not evenly distributed throughout the platform are both major factors affecting the ultimate result of the whole elevator. In this regard, the first tuning method proved to be the most practical as it allowed for a seamless transition into more suitable parameters for the load system. Some of the tools that we learned in the earlier weeks, specifically the application of Matlab in analysis of the final product, were applied seamlessly now that we had knowledge of what to search for as well as how to manipulate the built-in PID tuner.

## Appendix A: Block Diagram

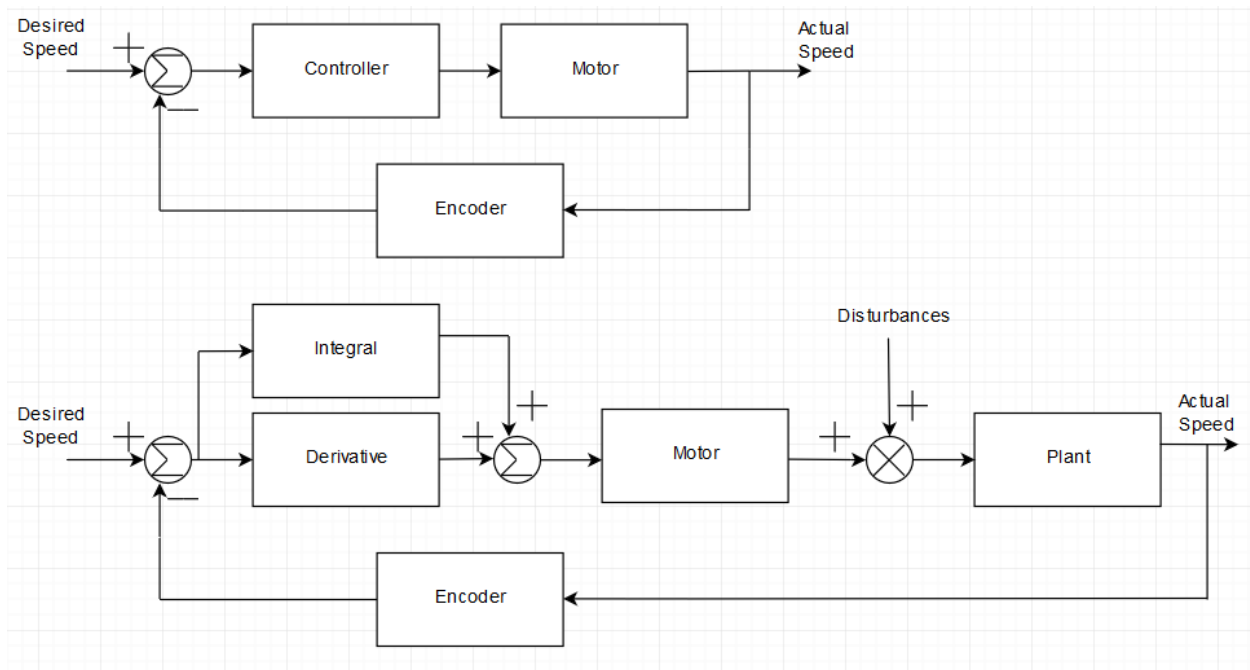


Figure A1

## Appendix B: Wiring Schematic and Circuit Assembly

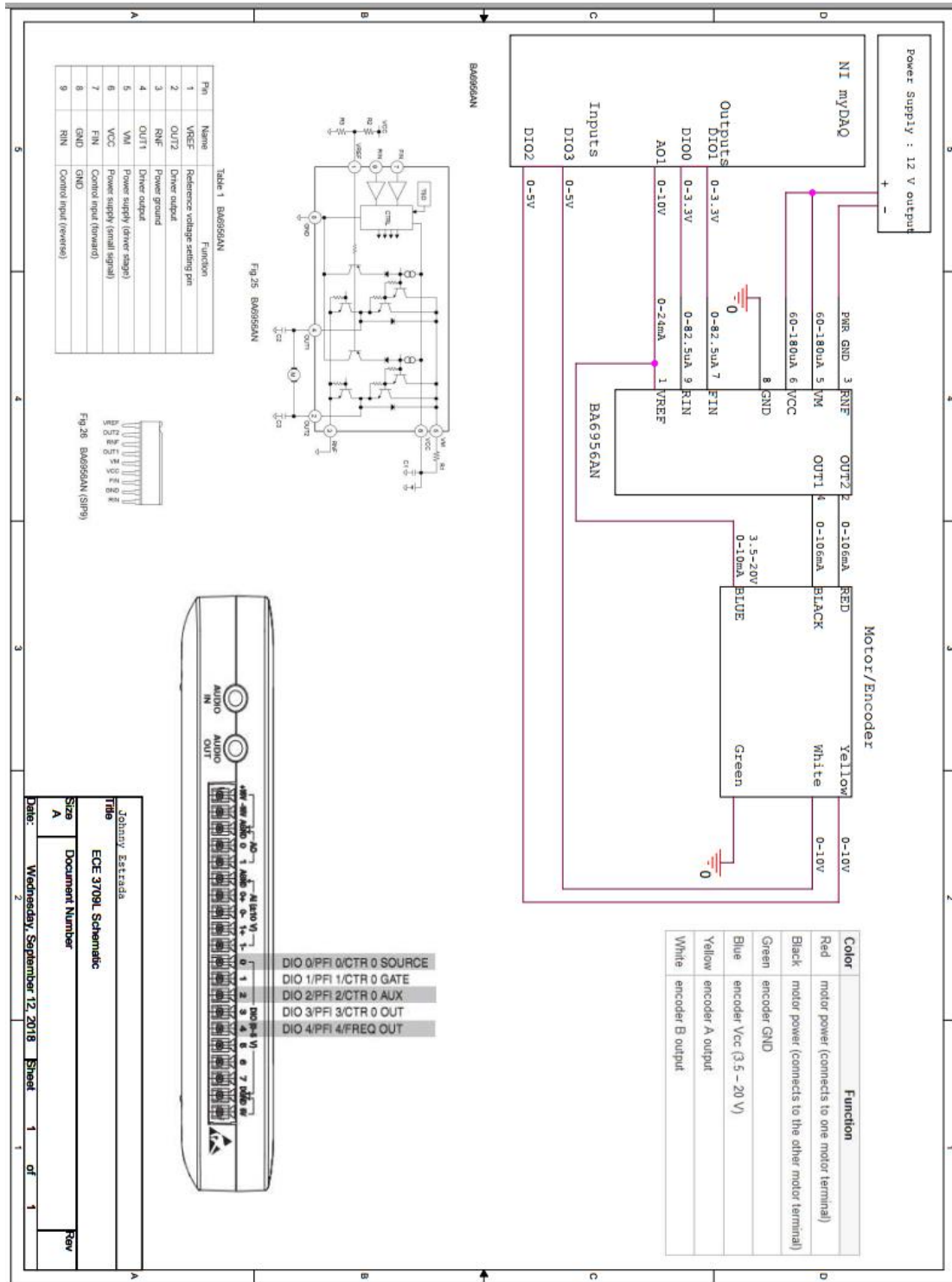


Figure B1

## Appendix B Continued

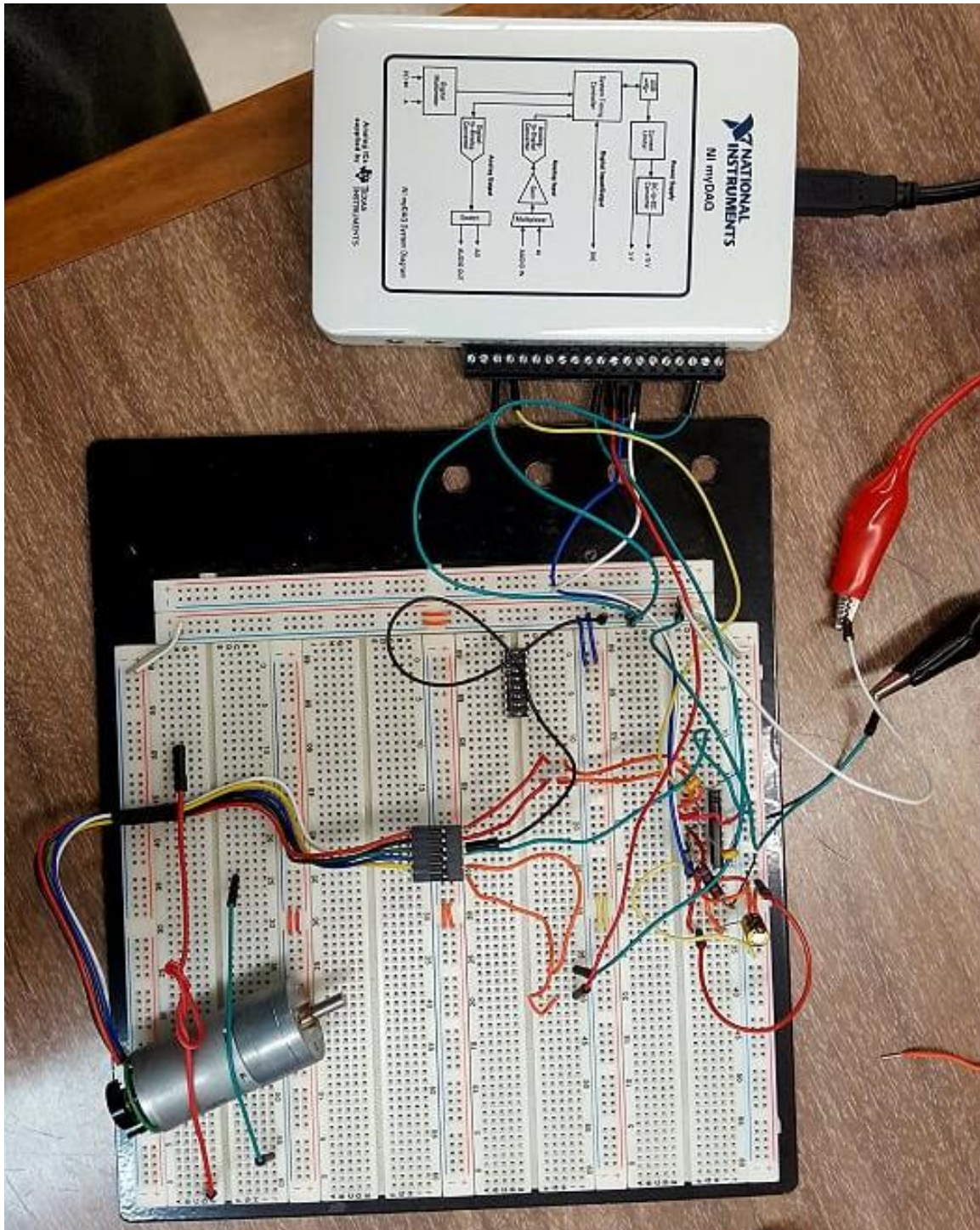


Figure B2

## Appendix C: Software Setup

### ECE 309L Software Files



#### PI Controller (SubVI).vi

Attached Files:  [PI Controller \(SubVI\).vi](#) (15.263 KB)



#### Signal Conditioning (SubVI).vi

Attached Files:  [Signal Conditioning \(SubVI\).vi](#) (8.104 KB)



#### Speed PI Control.vi


Attached Files:  [Speed PI Control.vi](#) (254.773 KB)

Figure C1

Files used for the initial setup of the LabView software that is used for the project: the first two files are supporting modules for the overall driving file Speed PI Control. Putting these files in the same directory so that the program knows where to the main and supporting files. The naming of said files also will cause issues. After this is done opening the files will open the following windows:

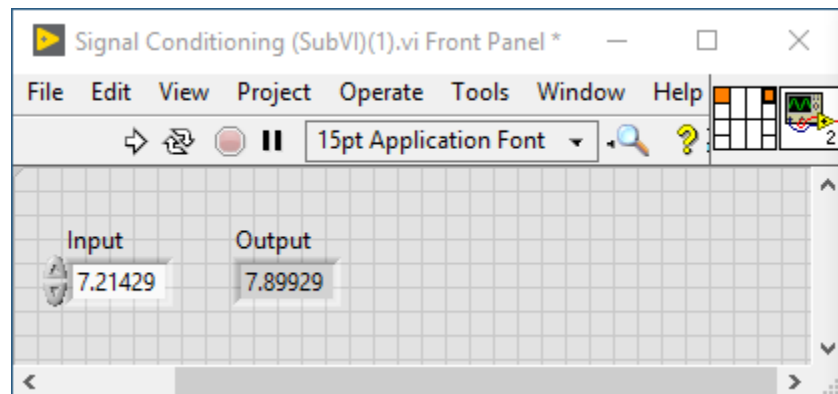


Figure C2



## Appendix C Continued

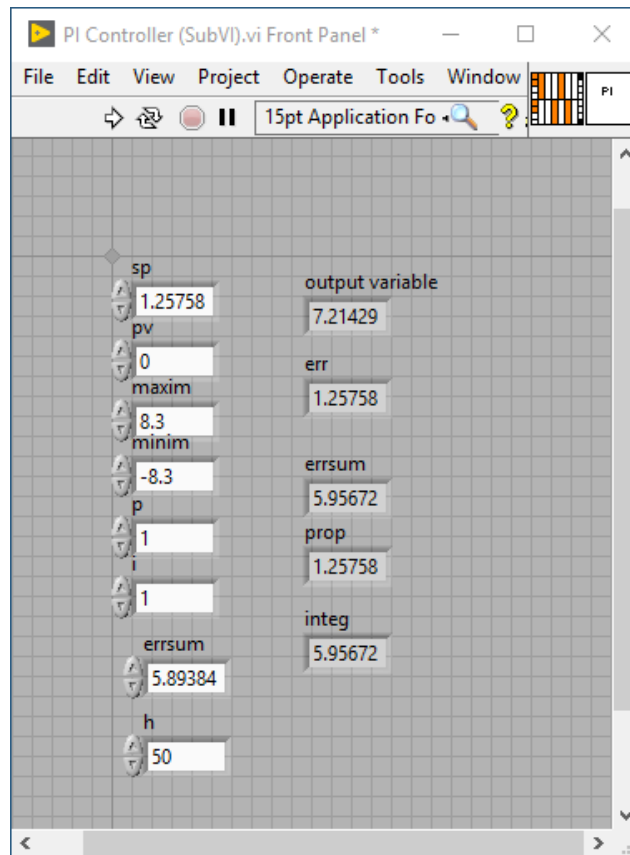


Figure C3

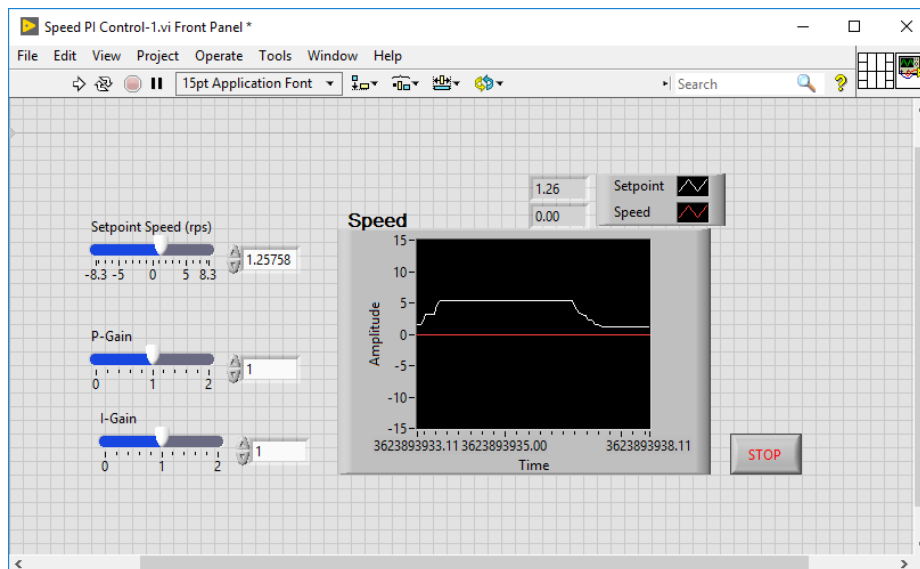


Figure C4

## Appendix D: TE Tuning Method

In this tuning method we are tracking the response of the motor in real time. This allows us to tune the motor in a manner that enables us to pinpoint an optimal response for a given set of PID parameters. In this case P-Gain and I-Gain are adjusted to get a response that suits the designer's constraints, in our case a decent rise time and settling time.

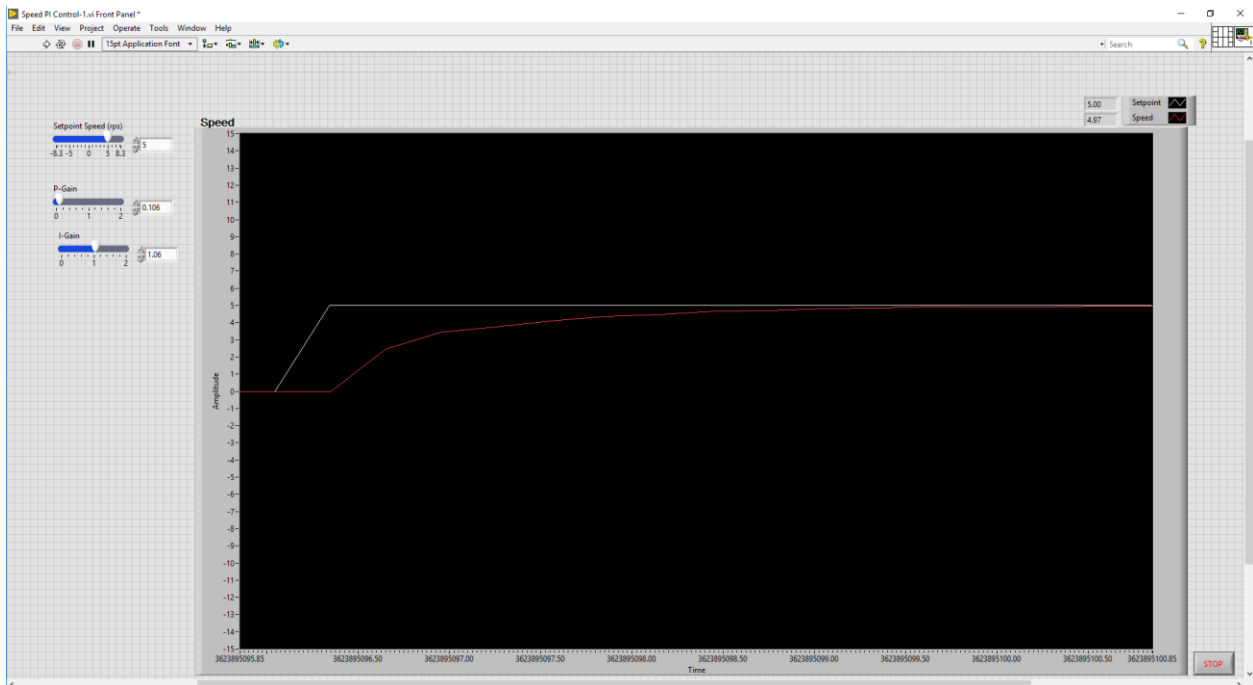


Figure D1

The sampling rate and the gear ratio are adjusted accordingly. A higher sampling rate will yield a smoother response as the system is able to take more data and therefore adjust in a more controlled manner. Increasing the P-Gain will yield a faster rise time. Increasing the I-Gain will adjust how fast this system approaches zero error, this effect therefore elongates the amount of time it takes to reach that set point. Once the motor is adjusting or responding in the preferred manner take down the parameters for the P and I gain.

## Appendix E: The Mathematical Model

The system model was derived from the mathematical equations describing the voltage  $V$  applied and the rotational speed of the shaft  $\theta$  (“DC Motor Speed: System Modeling”, 2018).

Using this knowledge, a transfer function was developed with the given variables in mind:

|                   |                                 |  |
|-------------------|---------------------------------|--|
| (J)               | moment of inertia of the rotor  | $0.01 \text{ kg} * \text{m}^2$             |
| (b)               | motor viscous friction constant | $0.1 \text{ N} * \text{m} * \text{s}$      |
| (K <sub>E</sub> ) | electromotive force constant    | $0.01 \text{ V} / \text{rad} / \text{sec}$ |
| (K <sub>T</sub> ) | motor torque constant           | $0.01 \text{ N} * \text{m} / \text{Amp}$   |
| (R)               | electric resistance             | $1 \text{ ohm}$                            |
| (L)               | electric inductance             | $0.5 \text{ H}$                            |

Table E1

### Transfer Function Model

$$P(s) = \frac{\dot{\theta}(s)}{V(s)} = \frac{K}{(Js + b)(Ls + R) + K^2} \quad \left[ \frac{\text{rad/sec}}{\text{V}} \right] \quad (1)$$

## Appendix F: Frequency Response Analysis

For the frequency response analysis, we perform the analysis on an open-loop system using equation (1). This in turn will allow us to see how the closed loop system will behave. Considering things like gain and phase margin will allow us to see the type of play we have for stability. The Open Loop frequency response also has a good indication of how the close loop transient response will behave with respect to the response speed and the percent overshoot.

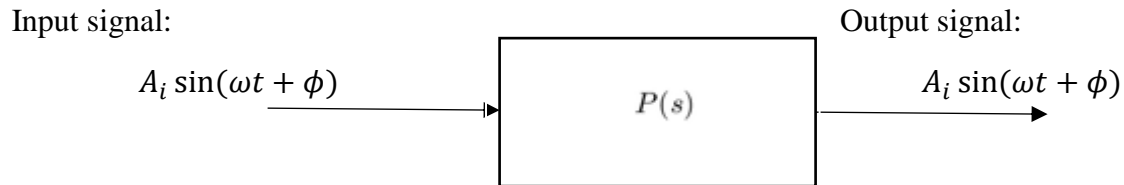


Figure F1

For the analysis MATLAB was used, the code has been omitted for now. Essentially it makes the transfer function and proportional gain was added to the system to bring it over the 0-dB line, this in turn would allow for a margin to be seen readily. The target phase margin was  $\sim 60$  degrees. With these two parameters and a whole arsenal of Bode Plots to analyze, close loop transient response can easily be made. In this case a phase margin of 59.2 deg and a gain margin of 70 dB . We can also gather the bandwidth from here as the conditions for this are satisfied as well. Data will have to be inspected.

## Appendix F Continued

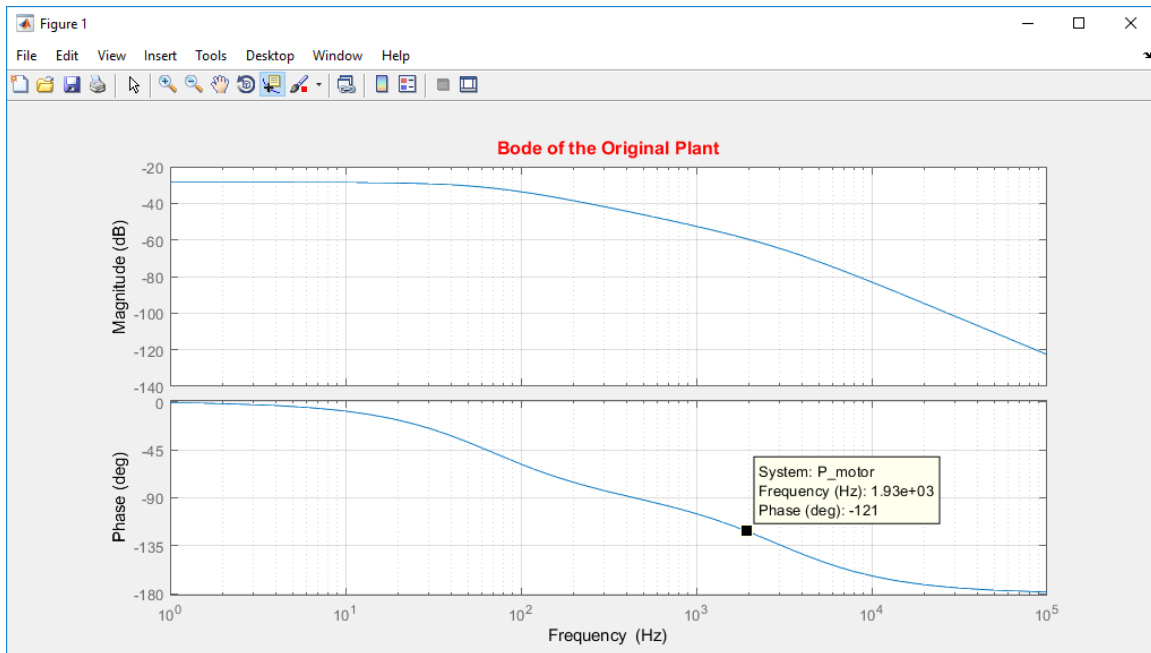


Figure F2

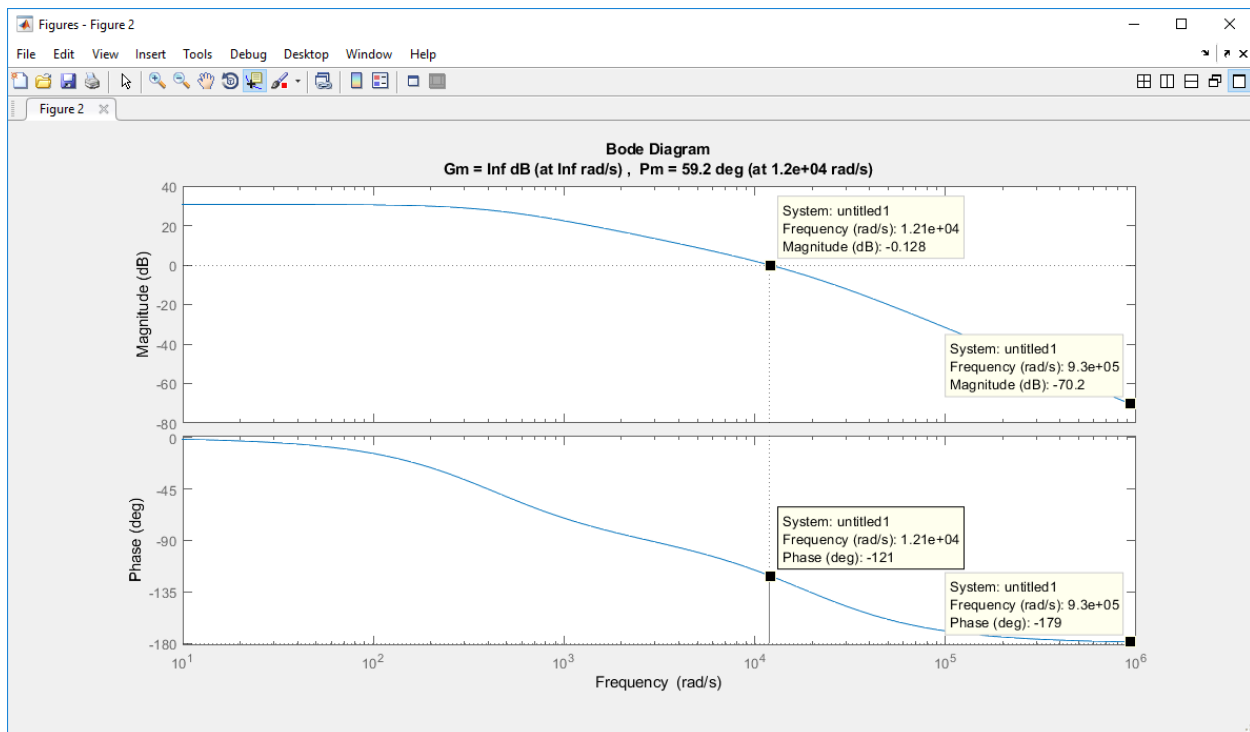


Figure F3

## Appendix G: Automation of Matlab

**%setup transfer function definition**

```
J = 2.5277e-6;  
b = .047;  
Kt = .015; %using the assumption that Kt = Ke  
Ke = .0214;  
R = 8.5;  
L =  
20.4e-3; s  
= tf('s');  
P_motor = Ke/((J*s+b)*(L*s+R)+Ke^2);
```

**%Setup options for bode plot**

```
opts = bodeoptions('cstprefs');  
opts.FreqUnits = 'Hz';  
opts.Grid = 'on';  
opts.Title.String = 'Bode of the Original Plant';  
opts.Title.Color = [1 0 0];  
opts.Title.FontSize = 12;
```

**%Open-Loop plant transfer function Bode Plot**

```
figure(1);  
bode(P_motor,opts);  
%Raising the system so that it can have a crossover frequency %chosen  
frequency % %was arbitrary as there was no target phase margin  
[mag, phase, w] = bode(P_motor, 100);
```

**%exact phase margin for gain crossover f of 100**

```
ph_marg = 180 + phase;  
%exact magnitude at crossover f  
exact_mag = 20*log10(mag);  
%exact magnitude is my P-Gain in dB or P-Gain of 1/.0079 = 126.58 will
```

**%yield an open-loop gain of 1 at f cross**

```
%proportional gain C is 1 divided the magnitude of processed magnitude  
C = 1/mag;  
figure(2);  
margin(C*P_motor);
```

**%saving the new system**

```
withG = (C*P_motor);
```

**%PID Tuner setup with a baseline reference of shifted system**

```
Tune = pidtune(C*P_motor,'PI'); pidTuner(C*P_motor, Tune);
```

## **Appendix G Continued**

The following Matlab script code was produced through the two different weeks we went over frequency response analysis, this made it possible to reproduce most of the work covered in those weeks and some in the previous weeks. This also enabled us to easily refer back to previous results and compare the new data with old, were we could gather some insight. We also noticed that our model would reach closer values when we performed the tuning in Matlab with consideration to a crossover frequency. Another great thing about this was the fact that we could now look at any other parameters for our transfer function and see the direct effect of that change. For example, when the magnitude of the dominant pole in the function was brought closer to the imaginary axis the phase change would increase to a range of 0 to 180 and would show the characteristics of a two-pole system, very different with the final function.

## Appendix H: Matlab PID Tuner

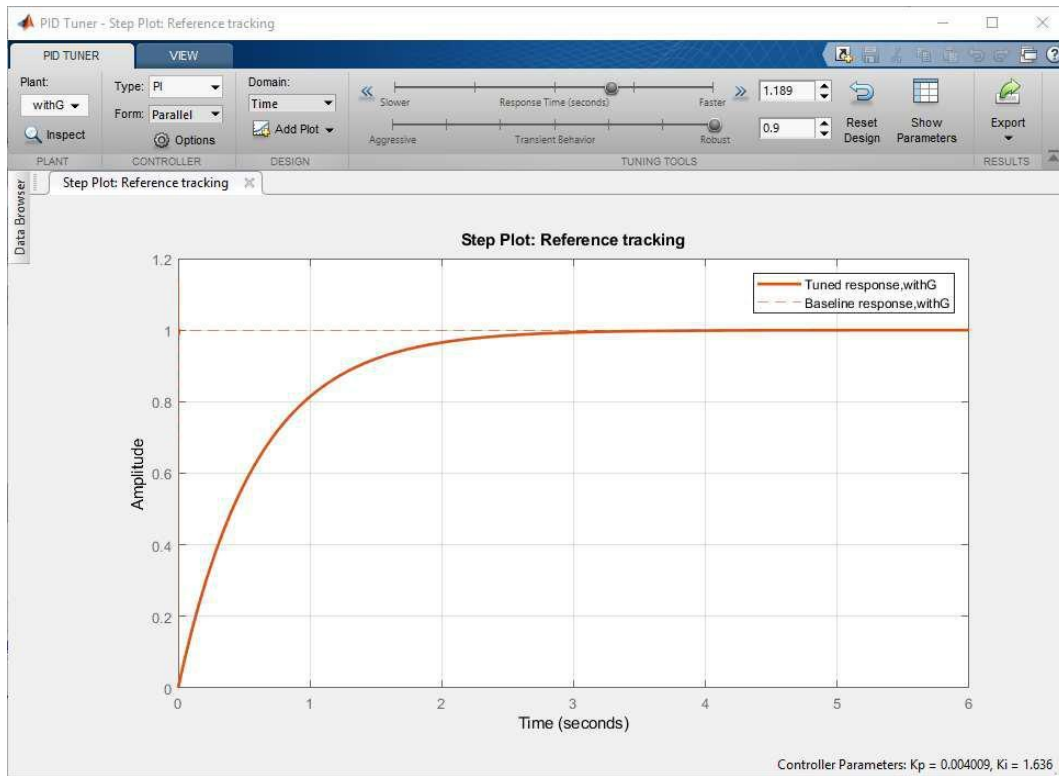


Figure H1

|       | Tuned     | Baseline  |
|-------|-----------|-----------|
| $K_p$ | 0.0040091 | 1.0888    |
| $K_i$ | 1.6357    | 1246.7789 |
| $K_d$ | n/a       | n/a       |
| $T_f$ | n/a       | n/a       |

|                       | Tuned               | Baseline           |
|-----------------------|---------------------|--------------------|
| Rise time             | 1.31 seconds        | 0.00189 seconds    |
| Settling time         | 2.33 seconds        | 0.00708 seconds    |
| Overshoot             | 0 %                 | 13.5 %             |
| Peak                  | 1                   | 1.13               |
| Gain margin           | Inf dB @ Inf rad/s  | Inf dB @ Inf rad/s |
| Phase margin          | 90 deg @ 1.68 rad/s | 60 deg @ 746 rad/s |
| Closed-loop stability | Stable              | Stable             |

Figure H2



## **Appendix H Continued**

When using the PID Tuner we found that there were two different implementations of the PID, parallel and standard form. These different implementations differ in how the variables are processed for the controller. However, in our case there was no real discrepancy in the different methods. What did affect the tuner was the plant that was being tuned, when we tuned the plant that had no crossover frequency, we got KI and KP that were simply too large, hence the importing and tuning of the model with crossover frequency. This was our solution to that hurdle, and it worked out well as the values extracted from Matlab were very close to the values in the TE Tuning method. The real time analysis is shown in Figure H3 and the corresponding data as well.

## Appendix H Continued

| Time (sec) | Time - Setpoint | Amplitude - Setpoint | Amplitude - Speed |
|------------|-----------------|----------------------|-------------------|
| 0.340      | 3625149972      | 2                    | 0.971             |
| 0.540      | 3625149973      | 2                    | 1.2623            |
| 0.740      | 3625149973      | 2                    | 1.4565            |
| 0.940      | 3625149973      | 2                    | 1.60215           |
| 1.140      | 3625149973      | 2                    | 1.7478            |
| 1.340      | 3625149973      | 2                    | 1.8449            |
| 1.540      | 3625149974      | 2                    | 1.89345           |
| 1.740      | 3625149974      | 2                    | 1.942             |
| 1.940      | 3625149974      | 2                    | 1.89345           |
| 2.140      | 3625149974      | 2                    | 1.99055           |
| 2.340      | 3625149974      | 2                    | 1.99055           |
| 2.540      | 3625149975      | 2                    | 1.99055           |
| 2.740      | 3625149975      | 2                    | 1.99055           |
| 2.940      | 3625149975      | 2                    | 1.99055           |
| 3.140      | 3625149975      | 2                    | 1.99055           |
| 3.340      | 3625149975      | 2                    | 1.99055           |
| 3.540      | 3625149976      | 2                    | 1.99055           |
| 3.740      | 3625149976      | 2                    | 1.99055           |
| 3.940      | 3625149976      | 2                    | 2.0391            |
| 4.140      | 3625149976      | 2                    | 1.99055           |
| 4.340      | 3625149976      | 2                    | 1.99055           |
| 4.540      | 3625149977      | 2                    | 1.99055           |
| 4.740      | 3625149977      | 2                    | 1.99055           |
| 4.940      | 3625149977      | 2                    | 2.0391            |

Table H1

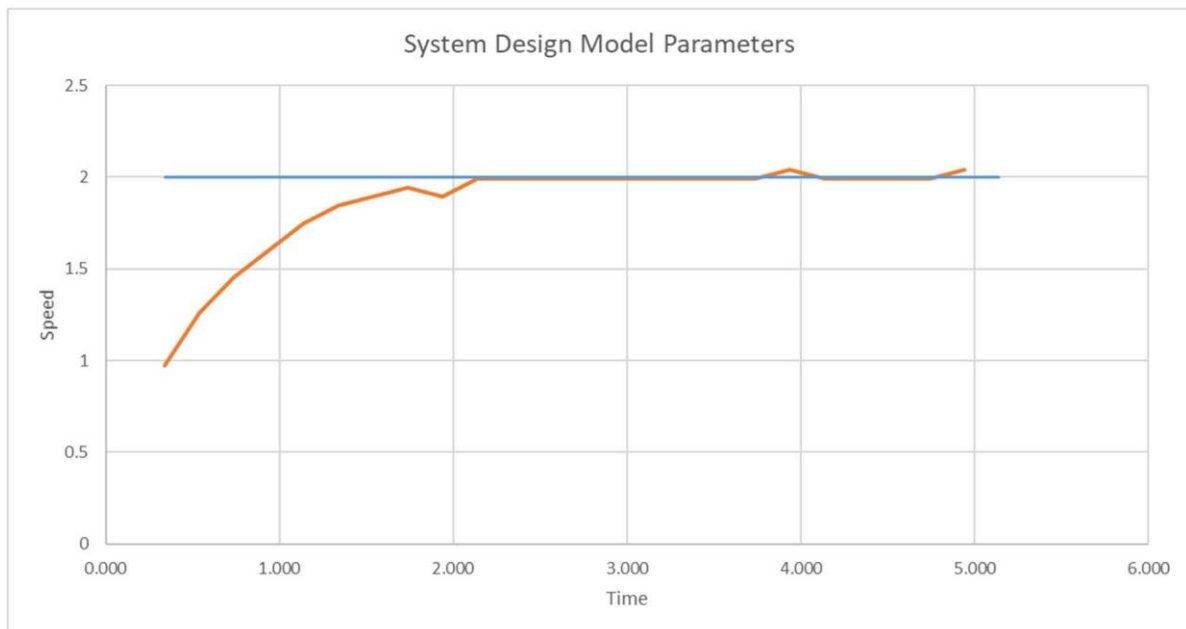


Figure H3

## Appendix I: Load Setup

The load was a simple elevator that would carry weight up and down. It consisted of a platform made of wood that had 3 holes on both sides placed in a triangle to evenly distribute the weight that the elevator would encounter later. Then yarn was applied to simulate a cable like structure, a knot was made and then a one piece of yarn would be winded and un-winded to bring the elevator up and down. A clamp was used as our foundational support to hold the motor in place. For the weight quarters were used, exactly 20 at maximum load and 10 for half the load. Weighing in at about 114 g plus the weight of the platform the elevator would stagnate a little at maximum load but overall it was able to perform adequately enough, with minor changes to the controller.



Figure I1

## Appendix I Continued



Figure I2

## Appendix J: TE Tuning Vs. PID Tuner Matlab

We found that the control parameters from the tuning we had done in previous weeks was working well but the motor needed a small amount of compensation for the fact that now it was not just spinning in the air. The friction of the yarn as it winded and gravity to work against we decided that the response needed a stronger integral value so that the motor would perform in the given time constraints that we had decided on. Our “rise time” was satisfied but a settling time was never really met. Hence the increase in integral control as to reduce the amount of time the motor kept underperforming. The data with just using the TE Tuning method is presented next.

| Time - Setpoint | Amplitude - Setpoint | Time - Speed | Amplitude - Speed | Time  |
|-----------------|----------------------|--------------|-------------------|-------|
| 3626304645      | 3                    | 3626304645   | 2.2333            | -0.19 |
| 3626304646      | 3                    | 3626304645   | 1.5536            | 0.01  |
| 3626304646      | 3                    | 3626304646   | 2.1362            | 0.21  |
| 3626304646      | 3                    | 3626304646   | 2.4275            | 0.41  |
| 3626304646      | 3                    | 3626304646   | 2.67025           | 0.61  |
| 3626304646      | 3                    | 3626304646   | 2.7188            | 0.81  |
| 3626304647      | 3                    | 3626304646   | 2.8159            | 1.01  |
| 3626304647      | 3                    | 3626304647   | 3.15575           | 1.21  |
| 3626304647      | 3                    | 3626304647   | 3.3985            | 1.41  |
| 3626304647      | 3                    | 3626304647   | 3.25285           | 1.61  |
| 3626304647      | 3                    | 3626304647   | 3.1072            | 1.81  |
| 3626304648      | 3                    | 3626304647   | 3.0101            | 2.01  |
| 3626304648      | 3                    | 3626304648   | 2.913             | 2.21  |
| 3626304648      | 3                    | 3626304648   | 2.86445           | 2.41  |
| 3626304648      | 3                    | 3626304648   | 2.913             | 2.61  |
| 3626304648      | 3                    | 3626304648   | 2.86445           | 2.81  |
| 3626304649      | 3                    | 3626304648   | 2.913             | 3.01  |
| 3626304649      | 3                    | 3626304649   | 2.913             | 3.21  |
| 3626304649      | 3                    | 3626304649   | 2.86445           | 3.41  |
| 3626304649      | 3                    | 3626304649   | 2.96155           | 3.61  |
| 3626304649      | 3                    | 3626304649   | 2.96155           | 3.81  |
| 3626304650      | 3                    | 3626304649   | 2.96155           | 4.01  |
| 3626304650      | 3                    | 3626304650   | 2.913             | 4.21  |
| 3626304650      | 3                    | 3626304650   | 2.913             | 4.41  |
| 3626304650      | 3                    | 3626304650   | 2.86445           | 4.61  |

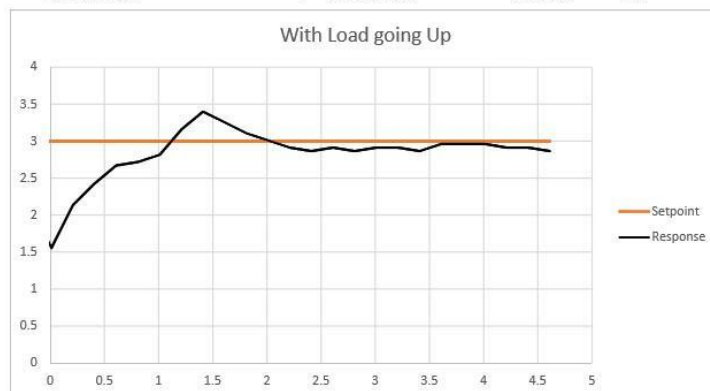


Figure J1

## Appendix J Continued

| Time - Setpoint | Amplitude - Setpoint | Time - Speed | Amplitude - Speed | Time |
|-----------------|----------------------|--------------|-------------------|------|
| 3626304763      | -3                   | 3626304763   | -1.89345          | 0    |
| 3626304764      | -3                   | 3626304764   | -2.913            | 0.21 |
| 3626304764      | -3                   | 3626304764   | -2.47605          | 0.4  |
| 3626304764      | -3                   | 3626304764   | -3.25285          | 0.61 |
| 3626304764      | -3                   | 3626304764   | -2.913            | 0.81 |
| 3626304764      | -3                   | 3626304764   | -3.44705          | 1.01 |
| 3626304765      | -3                   | 3626304765   | -3.54415          | 1.21 |
| 3626304765      | -3                   | 3626304765   | -3.54415          | 1.41 |
| 3626304765      | -3                   | 3626304765   | -3.44705          | 1.61 |
| 3626304765      | -3                   | 3626304765   | -3.44705          | 1.81 |
| 3626304765      | -3                   | 3626304765   | -3.2043           | 2.01 |
| 3626304766      | -3                   | 3626304766   | -3.1072           | 2.21 |
| 3626304766      | -3                   | 3626304766   | -3.1072           | 2.41 |
| 3626304766      | -3                   | 3626304766   | -3.2043           | 2.61 |
| 3626304766      | -3                   | 3626304766   | -3.1072           | 2.81 |
| 3626304766      | -3                   | 3626304766   | -2.913            | 3.01 |
| 3626304767      | -3                   | 3626304767   | -3.0101           | 3.21 |
| 3626304767      | -3                   | 3626304767   | -2.96155          | 3.41 |
| 3626304767      | -3                   | 3626304767   | -3.05865          | 3.61 |
| 3626304767      | -3                   | 3626304767   | -3.1072           | 3.81 |
| 3626304767      | -3                   | 3626304767   | -3.25285          | 4.01 |
| 3626304768      | -3                   | 3626304768   | -3.3014           | 4.21 |
| 3626304768      | -3                   | 3626304768   | -3.3014           | 4.41 |
| 3626304768      | -3                   | 3626304768   | -3.15575          | 4.61 |

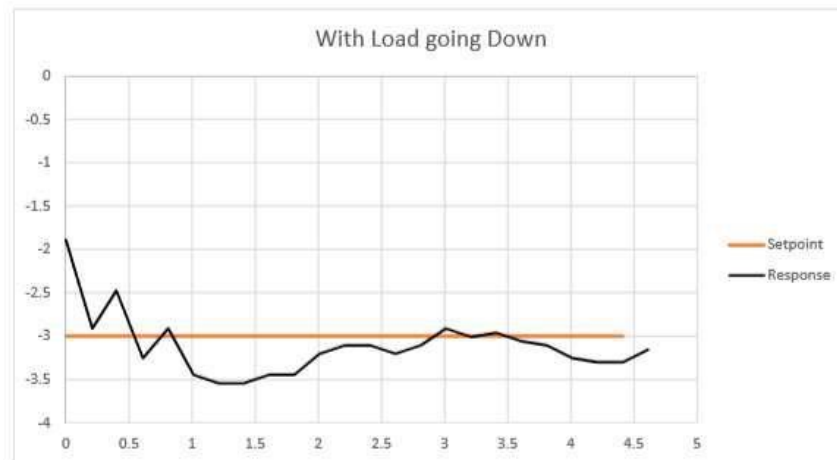


Figure J2

For Figure J1, %OS = 8.3%,  $T_s = 2.6$  s,  $T_r = 1.4$ s, and an  $E_{ss} = .14$ .

For Figure J2, %OS = 16%,  $T_s = 2.6$  s,  $T_r = 1.4$ s, and an  $E_{ss} = .3$

## Appendix J Continued

| Time - Setpoint | Amplitude | Time - Speed | Amplitude - Speed | Time |
|-----------------|-----------|--------------|-------------------|------|
| 3626304139      | 3         | 3626304139   | 2.2333            | 0    |
| 3626304139      | 3         | 3626304139   | 2.3304            | 0.2  |
| 3626304139      | 3         | 3626304139   | 2.57315           | 0.4  |
| 3626304139      | 3         | 3626304139   | 2.7188            | 0.6  |
| 3626304139      | 3         | 3626304139   | 2.76735           | 0.8  |
| 3626304140      | 3         | 3626304140   | 2.913             | 1    |
| 3626304140      | 3         | 3626304140   | 3.0101            | 1.2  |
| 3626304140      | 3         | 3626304140   | 3.1072            | 1.4  |
| 3626304140      | 3         | 3626304140   | 3.05865           | 1.6  |
| 3626304140      | 3         | 3626304140   | 3.05865           | 1.8  |
| 3626304141      | 3         | 3626304141   | 2.96155           | 2    |
| 3626304141      | 3         | 3626304141   | 3.0101            | 2.2  |
| 3626304141      | 3         | 3626304141   | 2.96155           | 2.4  |
| 3626304141      | 3         | 3626304141   | 2.913             | 2.61 |
| 3626304141      | 3         | 3626304141   | 2.86445           | 2.8  |
| 3626304142      | 3         | 3626304142   | 3.0101            | 3.01 |
| 3626304142      | 3         | 3626304142   | 2.913             | 3.2  |
| 3626304142      | 3         | 3626304142   | 2.96155           | 3.4  |
| 3626304142      | 3         | 3626304142   | 2.96155           | 3.6  |
| 3626304142      | 3         | 3626304142   | 2.96155           | 3.81 |
| 3626304143      | 3         | 3626304143   | 2.86445           | 4    |
| 3626304143      | 3         | 3626304143   | 2.96155           | 4.2  |
| 3626304143      | 3         | 3626304143   | 2.913             | 4.41 |
| 3626304143      | 3         | 3626304143   | 2.913             | 4.61 |

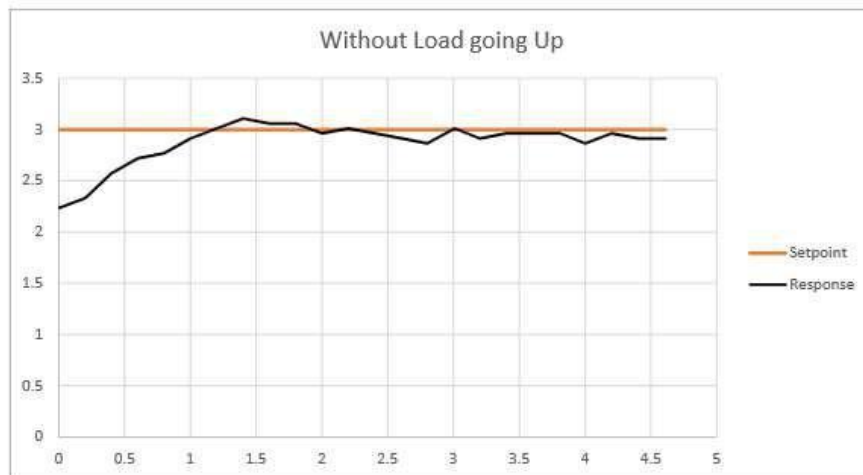


Figure J3



## Appendix J Continued

| Time - Setpoint | Amplitude | Time - Speed | Amplitude - Speed | Time  |
|-----------------|-----------|--------------|-------------------|-------|
| 3626304399      | -3        | 3626304399   | 0                 | -0.14 |
| 3626304399      | -3        | 3626304399   | -0.6797           | 0     |
| 3626304399      | -3        | 3626304399   | -2.18475          | 0.21  |
| 3626304400      | -3        | 3626304399   | -2.5246           | 0.4   |
| 3626304400      | -3        | 3626304400   | -2.6217           | 0.61  |
| 3626304400      | -3        | 3626304400   | -2.86445          | 0.81  |
| 3626304400      | -3        | 3626304400   | -2.913            | 1.01  |
| 3626304400      | -3        | 3626304400   | -3.05865          | 1.21  |
| 3626304401      | -3        | 3626304400   | -2.96155          | 1.41  |
| 3626304401      | -3        | 3626304401   | -3.05865          | 1.61  |
| 3626304401      | -3        | 3626304401   | -3.0101           | 1.81  |
| 3626304401      | -3        | 3626304401   | -3.0101           | 2.01  |
| 3626304401      | -3        | 3626304401   | -2.96155          | 2.21  |
| 3626304402      | -3        | 3626304401   | -3.1072           | 2.41  |
| 3626304402      | -3        | 3626304402   | -3.0101           | 2.61  |
| 3626304402      | -3        | 3626304402   | -3.05865          | 2.81  |
| 3626304402      | -3        | 3626304402   | -3.05865          | 3.01  |
| 3626304402      | -3        | 3626304402   | -3.1072           | 3.21  |
| 3626304403      | -3        | 3626304402   | -3.1072           | 3.41  |
| 3626304403      | -3        | 3626304403   | -3.0101           | 3.61  |
| 3626304403      | -3        | 3626304403   | -3.05865          | 3.81  |
| 3626304403      | -3        | 3626304403   | -3.05865          | 4.01  |
| 3626304403      | -3        | 3626304403   | -3.05865          | 4.21  |
| 3626304404      | -3        | 3626304403   | -3.05865          | 4.41  |
| 3626304404      | -3        | 3626304404   | -3.05865          | 4.61  |

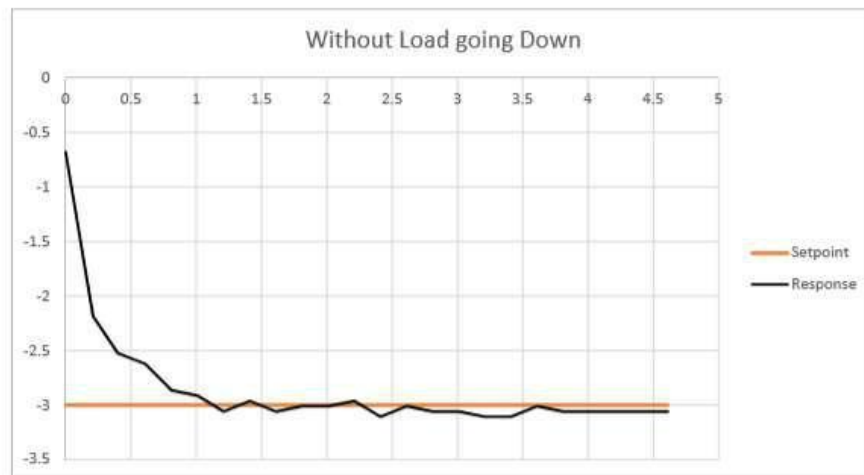


Figure J4

For Figure J3, %OS = 3.3%, Tr = 2.6 s, Ts = 1.4, and an Ess = .087.

For Figure J4, %OS = 2%, Tr = 1.6 s, Ts = 1.4, and an Ess = .06.



## Appendix J Continued

This is the data for the PID tuner parameters.

| Time - Speed | Amplitude - Speed | Time - Speed | Amplitude - Speed | Time   |
|--------------|-------------------|--------------|-------------------|--------|
| 3626350915   | 0.647333          | 3626351054   | -0.712067         | 139.08 |
| 3626350915   | 0.712067          | 3626351054   | -0.7768           | 139.23 |
| 3626350915   | 0.712067          | 3626351054   | -0.7768           | 139.38 |
| 3626350915   | 0.647333          | 3626351055   | -0.841533         | 139.53 |
| 3626350916   | 0.841533          | 3626351055   | -1.10047          | 139.68 |
| 3626350916   | 1.10047           | 3626351055   | -1.42413          | 139.83 |
| 3626350916   | 1.3594            | 3626351055   | -1.5536           | 139.98 |
| 3626350916   | 1.61833           | 3626351055   | -1.81253          | 140.13 |
| 3626350916   | 1.7478            | 3626351055   | -1.942            | 140.28 |
| 3626350916   | 1.942             | 3626351055   | -2.1362           | 140.43 |
| 3626350916   | 2.07147           | 3626351056   | -2.20093          | 140.58 |
| 3626350917   | 2.1362            | 3626351056   | -2.3304           | 140.73 |
| 3626350917   | 2.3304            | 3626351056   | -2.45987          | 140.88 |
| 3626350917   | 2.3304            | 3626351056   | -2.58933          | 141.03 |
| 3626350917   | 2.45987           | 3626351056   | -2.58933          | 141.18 |
| 3626350917   | 2.5246            | 3626351056   | -2.7188           | 141.33 |
| 3626350917   | 2.5246            | 3626351056   | -2.7188           | 141.48 |
| 3626350918   | 2.58933           | 3626351057   | -2.7188           | 141.63 |
| 3626350918   | 2.58933           | 3626351057   | -2.78353          | 141.78 |
| 3626350918   | 2.7188            | 3626351057   | -2.78353          | 141.93 |
| 3626350918   | 2.65407           | 3626351057   | -2.84827          | 142.08 |
| 3626350918   | 2.7188            | 3626351057   | -2.84827          | 142.23 |
| 3626350918   | 2.78353           | 3626351057   | -2.913            | 142.38 |
| 3626350918   | 2.78353           | 3626351058   | -2.913            | 142.53 |
| 3626350919   | 2.78353           | 3626351058   | -2.84827          | 142.68 |
| 3626350919   | 2.78353           | 3626351058   | -2.84827          | 142.83 |
| 3626350919   | 2.78353           | 3626351058   | -2.97773          | 142.98 |
| 3626350919   | 2.84827           | 3626351058   | -2.913            | 143.13 |
| 3626350919   | 2.84827           | 3626351058   | -2.97773          | 143.28 |
| 3626350919   | 2.913             | 3626351058   | -2.97773          | 143.43 |
| 3626350920   | 2.78353           | 3626351059   | -2.913            | 143.58 |
| 3626350920   | 2.913             | 3626351059   | -2.97773          | 143.73 |
| 3626350920   | 2.913             | 3626351059   | -2.913            | 143.88 |

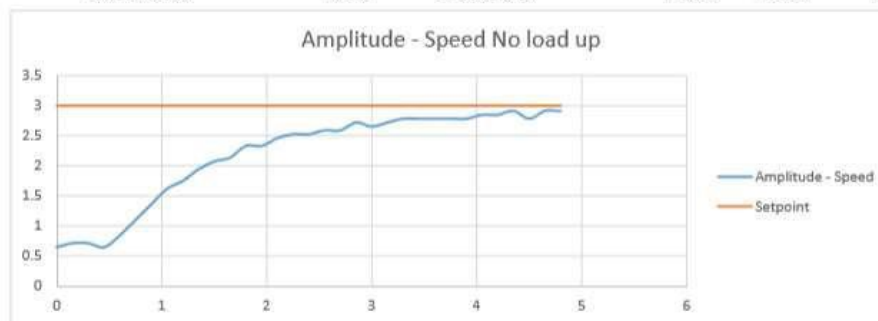


Figure J5

## Appendix J Continued

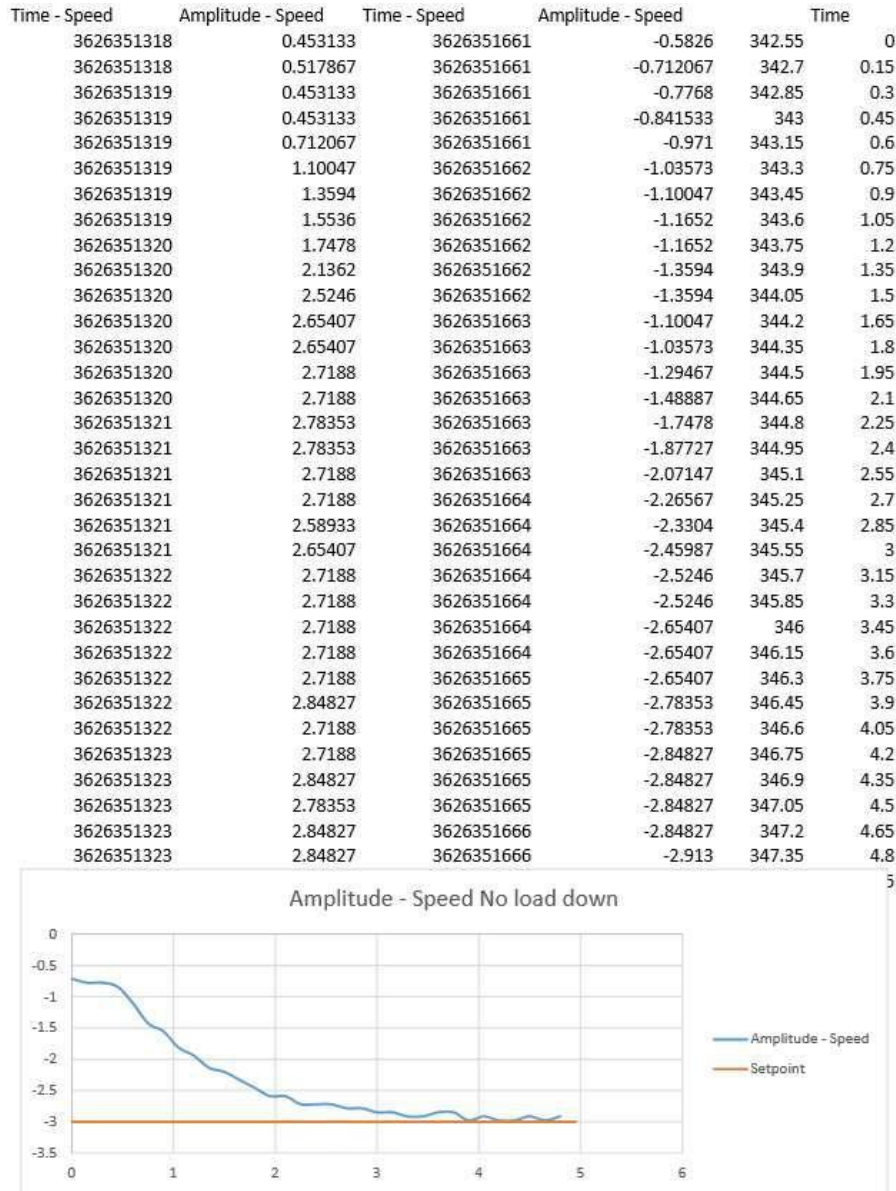


Figure J6

## Appendix J Continued

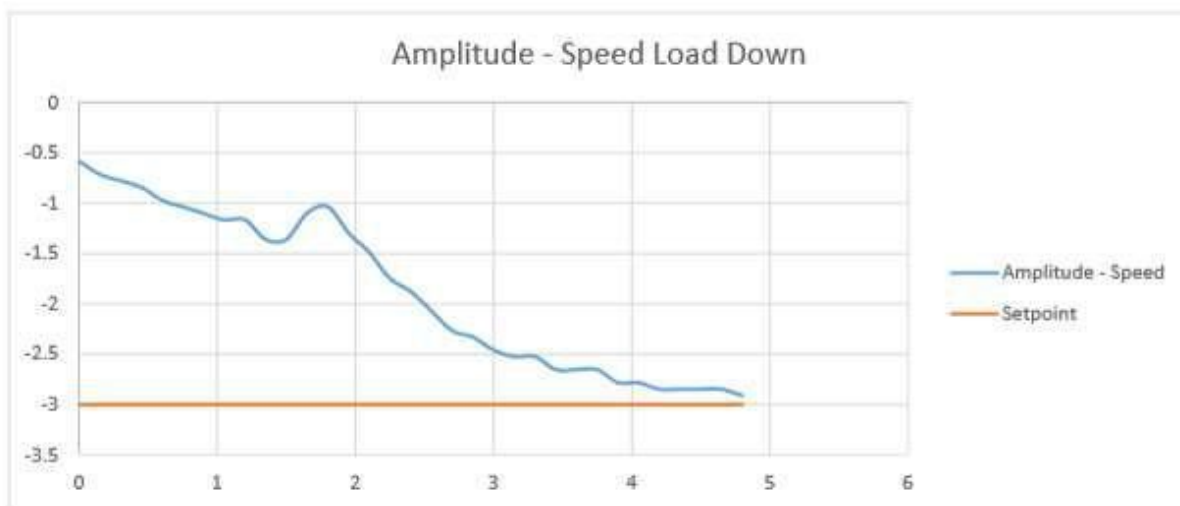


Figure J7

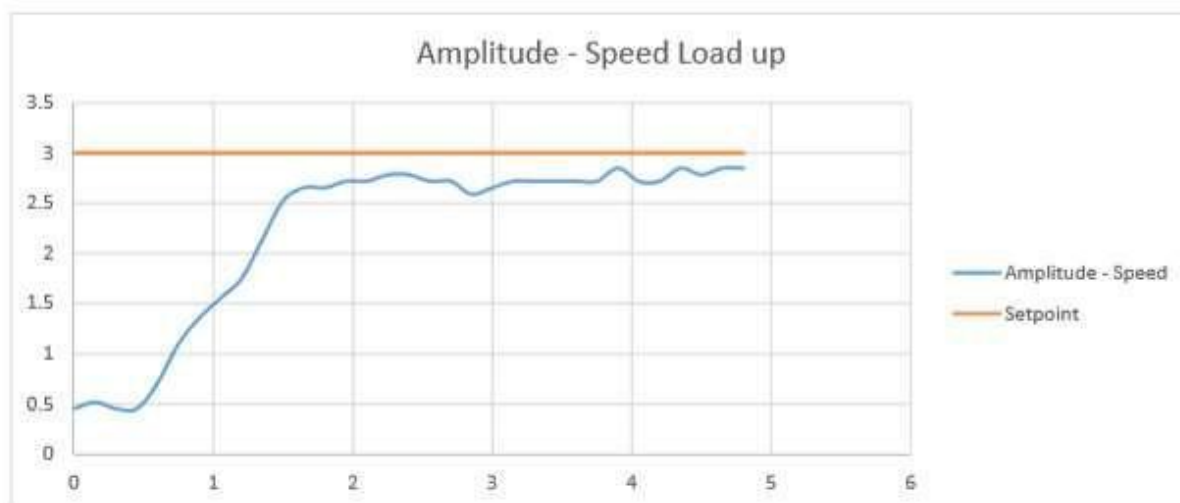


Figure J8

For Figure J5, %OS = 0%,  $T_r = 4$  s,  $T_s = 2.8$  s, and an  $E_{ss} = .087$ .

For Figure J5, %OS = 0%,  $T_r = 3.4$  s,  $T_s = 2.4$  s, and an  $E_{ss} = .087$ .

For Figure J5, %OS = 0%,  $T_r = 5$  s,  $T_s = 2.8$  s, and an  $E_{ss} = .087$ .

For Figure J5, %OS = 0%,  $T_r = 4.1$  s,  $T_s = 1.7$  s, and an  $E_{ss} = .016$ .

## Appendix J Continued

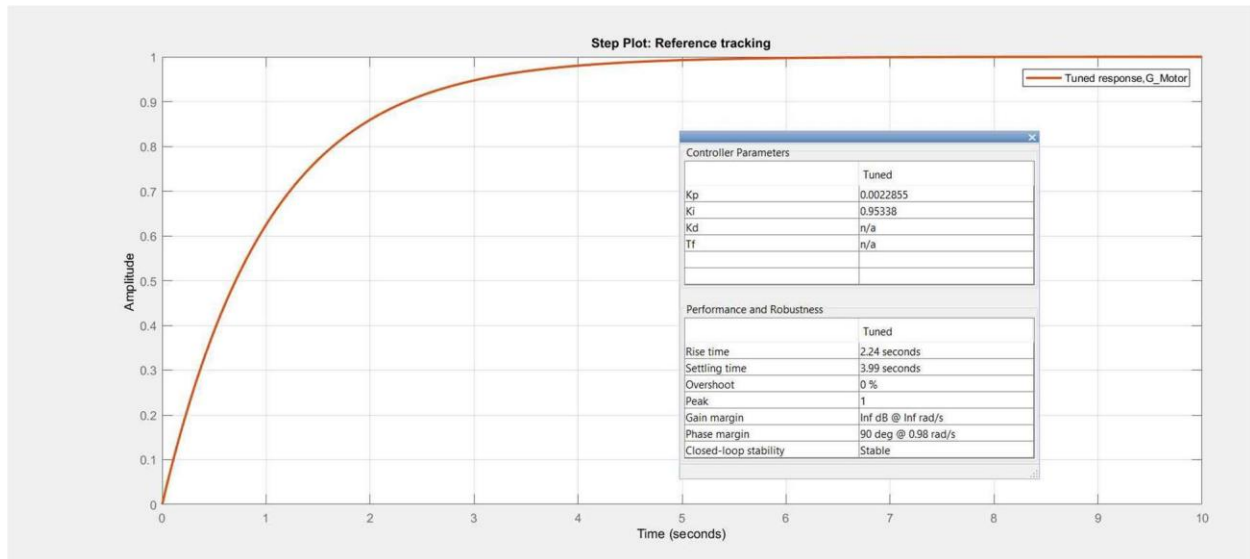


Figure J9

## Appendix K: Accumulated Grades

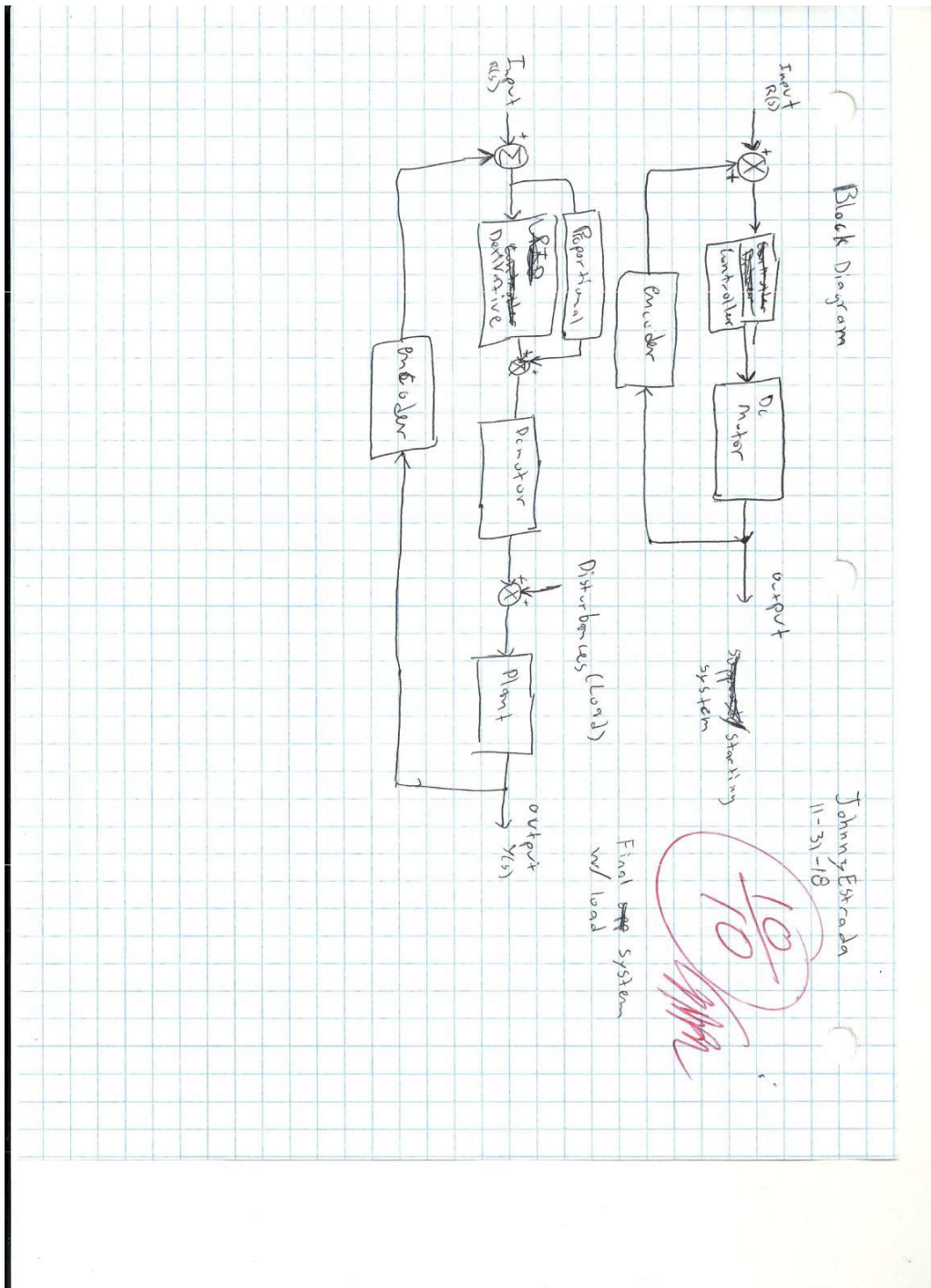


Figure K1

## Appendix K Continued

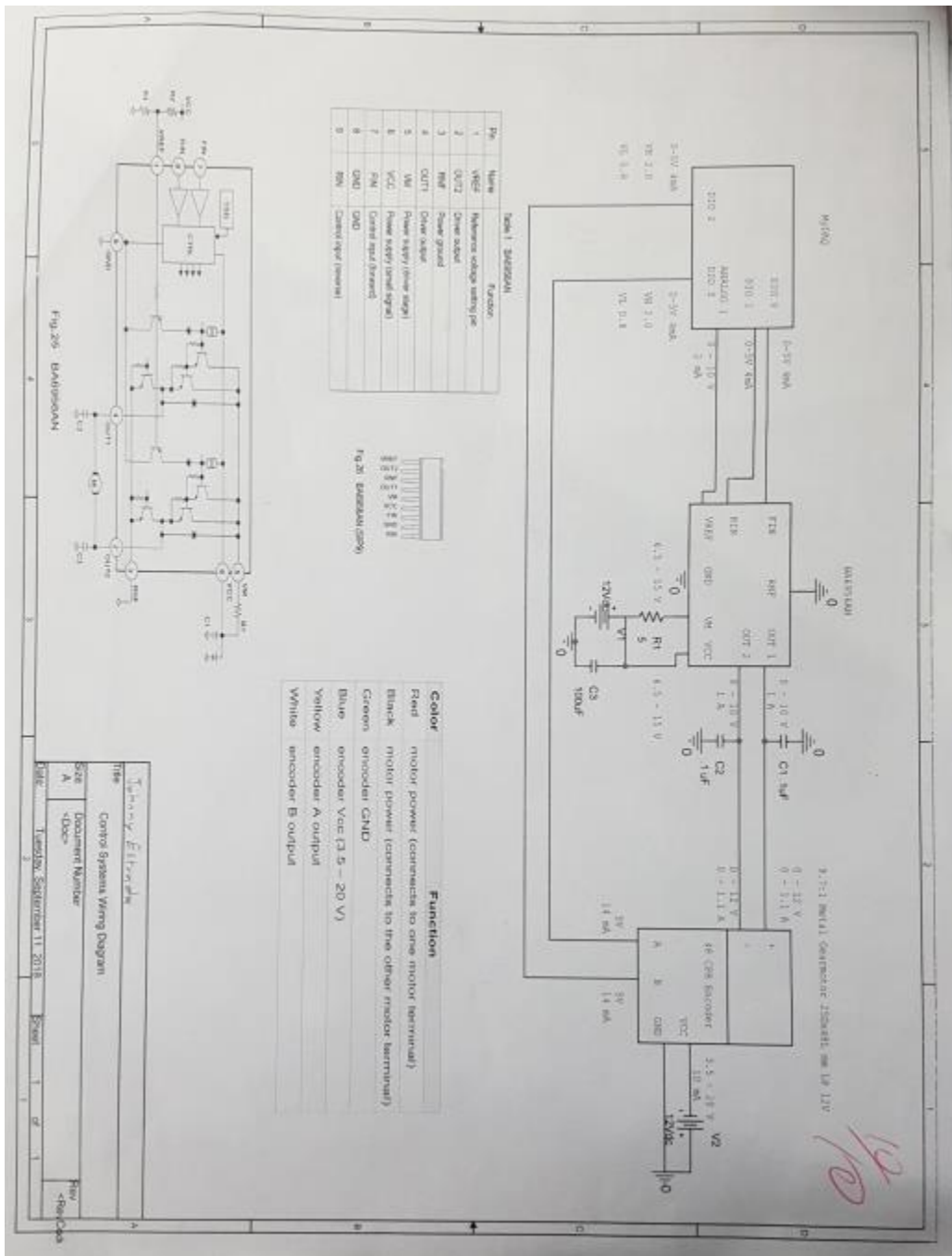


Figure K2



## Appendix K Continued

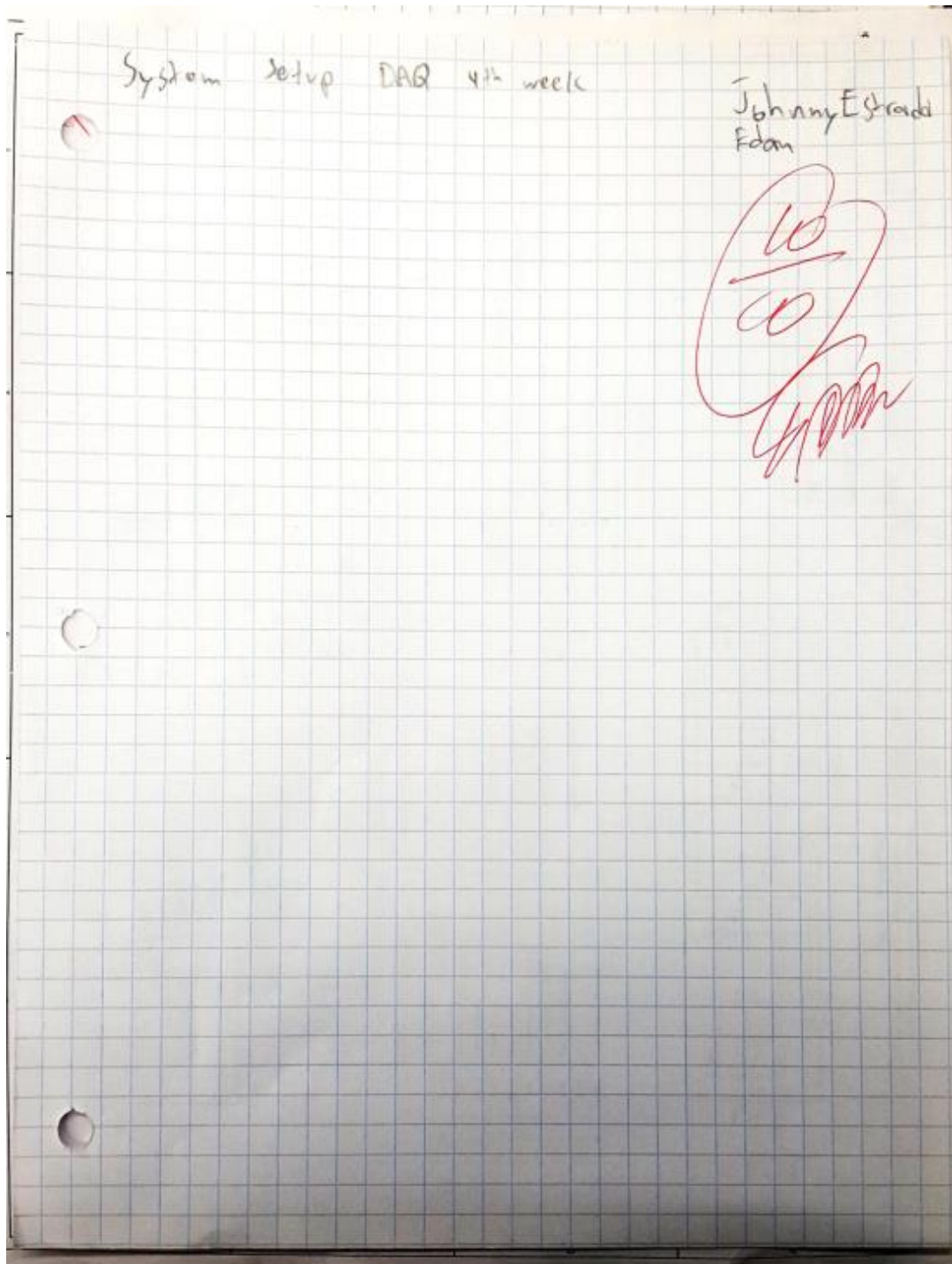


Figure K3

## Appendix K Continued

| Time - Setpoint | Amplitude - Setpoint | Time - Speed | Amplitude - Speed |
|-----------------|----------------------|--------------|-------------------|
| 3621516186      | 1                    | 3621516186   | 1.02291           |
| 3621516186      | 1                    | 3621516186   | 0.987636          |
| 3621516187      | 2                    | 3621516187   | 0.987636          |
| 3621516187      | 2                    | 3621516187   | 1.30509           |
| 3621516187      | 2                    | 3621516187   | 1.48145           |
| 3621516188      | 2                    | 3621516188   | 1.62255           |
| 3621516188      | 2                    | 3621516188   | 1.69309           |
| 3621516188      | 2                    | 3621516188   | 1.76364           |
| 3621516188      | 2                    | 3621516188   | 1.83418           |
| 3621516189      | 2                    | 3621516189   | 1.86945           |
| 3621516189      | 2                    | 3621516189   | 1.90473           |
| 3621516189      | 2                    | 3621516189   | 1.90473           |
| 3621516189      | 2                    | 3621516189   | 1.94              |
| 3621516190      | 2                    | 3621516190   | 1.97527           |
| 3621516190      | 2                    | 3621516190   | 1.97527           |
| 3621516190      | 2                    | 3621516190   | 1.97527           |
| 3621516191      | 2                    | 3621516191   | 1.97527           |
| 3621516191      | 2                    | 3621516191   | 1.97527           |
| 3621516191      | 2                    | 3621516191   | 2.01055           |

%OS= 0

Ess= .03

Ref=2

Rise time = ~2s — rise time less than or

Transient Response ~4s

settles less than 3s

Link →

[mathworks.com/discovery/pid-control.html](https://mathworks.com/discovery/pid-control.html)

<sup>K</sup> P-Gain = .103  
<sup>K</sup> I-Gain = 1.06

transfer Fraction

$$\frac{.103s + 1.06}{s}$$

Conti-time PID Controller

Figure K4



## Appendix K Continued

$Torque = J \times \alpha$   
 $J = D \times L \times .077 \times 10^{-6} = [kg \cdot m^2]$   
 $\downarrow \quad \downarrow$   
 $4mm \quad 12.5mm$   
 $.004m \cdot .0125m \cdot .077 \times 10^{-6} = 3.85 \times 10^{-12}$   
 $\frac{1}{2} m r^2 = \frac{1}{2} (.095 kg)$   
 $.00126385 \text{ mass } [kg] \text{ using density of steel}$   
 $2.5277 \times 10^{-9} = J$   
 $r = .2 \text{ cm}$

$P(s) = \frac{\theta(s)}{V(s)} = \frac{K}{(Js+b)(Ls+R)+K^2} \left[ \frac{rad/sec}{V} \right]$   
 $b = .047$   
 $J = 2.5277 \times 10^{-9}$   
 $L = 20.4 \times 10^{-3} \text{ H}$   
 $R = 8.5 \Omega$   
 $-6$

$b. \quad T = bW$   
 $.009627 = b(.2046)$   
 $b = 1.047$

$s = \frac{b}{J}$   
 $121 - 143$

$(2.5277 \times 10^{-9} s + .047)$   
 $\times (20.4 \times 10^{-3} s + 8.5)$   
 $5.15651 \times 10^{-11} s^2 + 9.5882148 \times 10^{-4} s$   
 $5.15651 \times 10^{-11} s^2 + 9.5882148 \times 10^{-4} s$   
 $4.4209$   
 $W_n = .648$




Figure K5

## Appendix K Continued

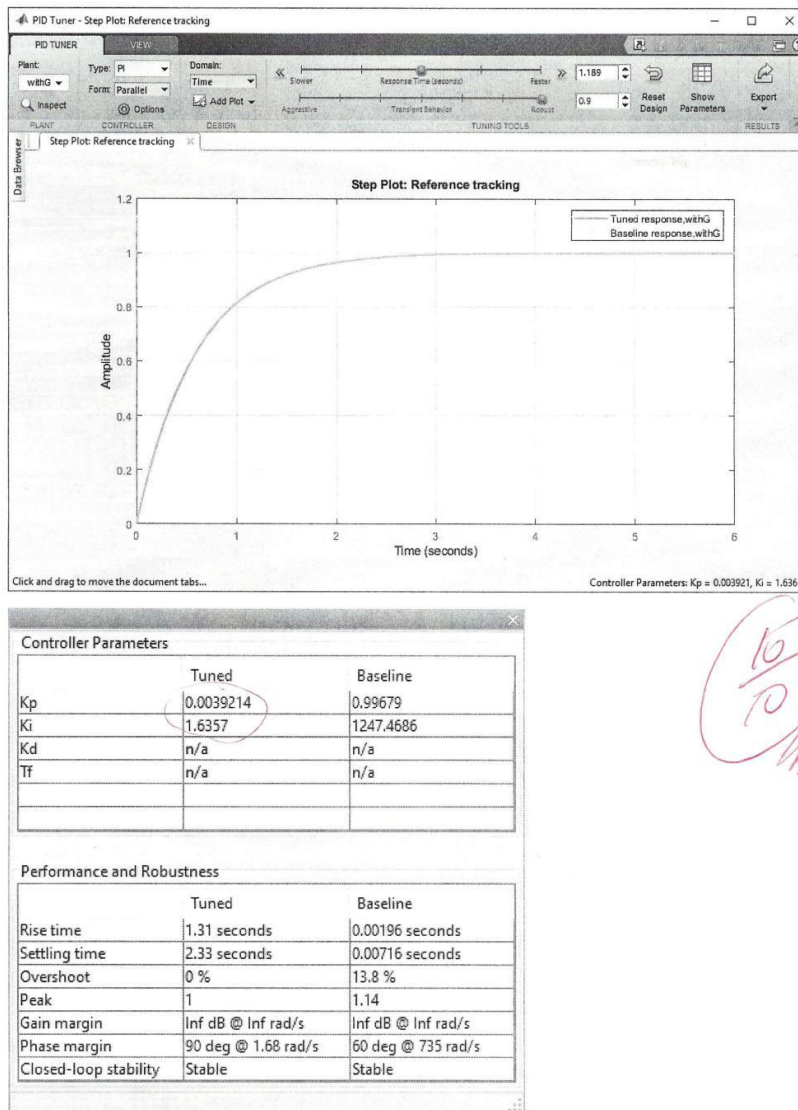


Figure K6

## Appendix K Continued

b.c.  
2/2

| Time (sec) | Time - Setpoint | Amplitude - Setpoint | Amplitude - Speed |
|------------|-----------------|----------------------|-------------------|
| 0.340      | 3625149972      | 2                    | 0.971             |
| 0.540      | 3625149973      | 2                    | 1.2623            |
| 0.740      | 3625149973      | 2                    | 1.4565            |
| 0.940      | 3625149973      | 2                    | 1.60215           |
| 1.140      | 3625149973      | 2                    | 1.7478            |
| 1.340      | 3625149973      | 2                    | 1.8449            |
| 1.540      | 3625149974      | 2                    | 1.89345           |
| 1.740      | 3625149974      | 2                    | 1.942             |
| 1.940      | 3625149974      | 2                    | 1.89345           |
| 2.140      | 3625149974      | 2                    | 1.99055           |
| 2.340      | 3625149974      | 2                    | 1.99055           |
| 2.540      | 3625149975      | 2                    | 1.99055           |
| 2.740      | 3625149975      | 2                    | 1.99055           |
| 2.940      | 3625149975      | 2                    | 1.99055           |
| 3.140      | 3625149975      | 2                    | 1.99055           |
| 3.340      | 3625149975      | 2                    | 1.99055           |
| 3.540      | 3625149976      | 2                    | 1.99055           |
| 3.740      | 3625149976      | 2                    | 1.99055           |
| 3.940      | 3625149976      | 2                    | 2.0391            |
| 4.140      | 3625149976      | 2                    | 1.99055           |
| 4.340      | 3625149976      | 2                    | 1.99055           |
| 4.540      | 3625149977      | 2                    | 1.99055           |
| 4.740      | 3625149977      | 2                    | 1.99055           |
| 4.940      | 3625149977      | 2                    | 2.0391            |
| 5.140      | 3625149977      | 2                    |                   |

System design parameters  
first run through

Figure K7

## Appendix K Continued

October 31, 2018

Johnny Estrada  
Edan Nankin

Time constant =  $\frac{1}{\sigma}$

Settling time =  $4 \frac{1}{\sigma}$

$\frac{d^2 y}{dt^2} + 3 \frac{dy}{dt} + 2y = 0$

$(s^2 + 3s + 2) = \text{characteristic eq}$

$\Rightarrow (s^2 + 2\zeta\omega_n s + \omega_n^2)$

$\omega_n = \sqrt{2}$

$\zeta = 3$

1) How do we control

$7 = 2\zeta\omega_n$

location

$\Rightarrow \frac{R}{L} = \frac{8.5}{20.4 \times 10^{-3}}$

$\frac{1}{2.4 \times 10^{-3}} =$

$T_{\text{unst}} = \frac{1}{R/L} = 1(2.4 \times 10^{-3})$

$T_{\text{settle}} = 9.6 \times 10^{-3} \text{ s}$

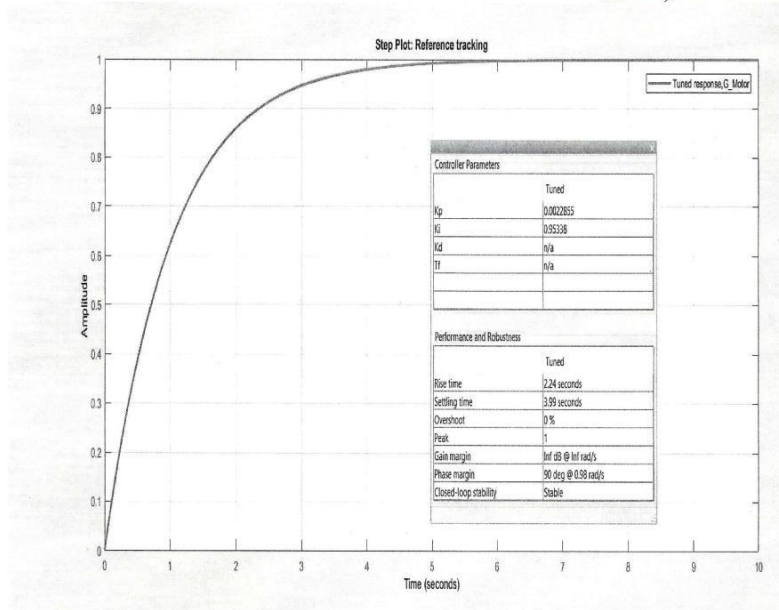
$\omega_n = \sqrt{.4209} = .649$

$T_{\text{settle}} \text{ is } (T_{\text{unst}} \times 4)$

Figure K8

## Appendix K Continued

Edan Nankin  
Johnny Estrada

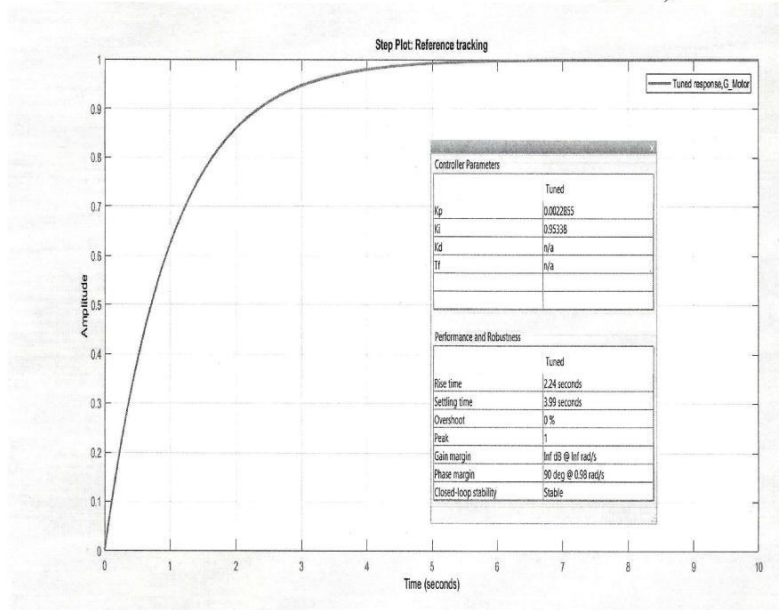


10  
10  
10

Figure K9

## Appendix K Continued

Edan Nankin  
Johnny Estrada



10  
10  
10

Figure K9

## References

1. Nise, Norman S. Control Systems Engineering. Wiley, 2015. Nise, Norman S. Control Systems Engineering. Wiley, 2015.
2. “DC Motor Speed: System Modeling.” Control Tutorials for MATLAB and Simulink - Motor Speed: System Modeling,  
[ctms.engin.umich.edu/CTMS/index.php?example=MotorSpeed&ion=SystemModeling](http://ctms.engin.umich.edu/CTMS/index.php?example=MotorSpeed&ion=SystemModeling).
3. “DC Motor Speed: Frequency Domain Methods for Controller Design.” Control Tutorials for MATLAB and Simulink - Motor Speed: Frequency Domain Methods for Controller Design,  
[ctms.engin.umich.edu/CTMS/index.php?example=MotorSpeed&ion=ControlFrequency](http://ctms.engin.umich.edu/CTMS/index.php?example=MotorSpeed&ion=ControlFrequency).
4. “Functions - By Category.” MATLAB - MATLAB & Simulink,  
[www.mathworks.com/help/matlab/functionlist.html](http://www.mathworks.com/help/matlab/functionlist.html).

