

$$L = 220 \text{ mH}$$

$$C = 10 \text{ nF}$$

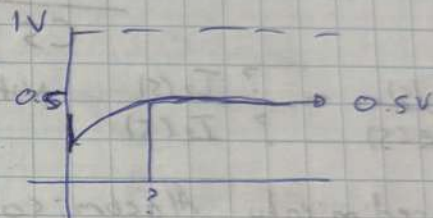
$$R = 22 \text{ k}\Omega$$

Ecuaciones principales

$$V_e(t) = R i_1(t) + L \frac{d[i_1(t) - i_2(t)]}{dt} + R [i_1(t) - i_2(t)]$$

$$L \frac{d[i_1(t) - i_2(t)]}{dt} + R [i_1(t) - i_2(t)] = R i_2(t) + R i_2(t) + \frac{1}{C} \int i_2(t) dt$$

$$V_s = R i_2(t) + \frac{1}{C} \int i_2(t) dt$$



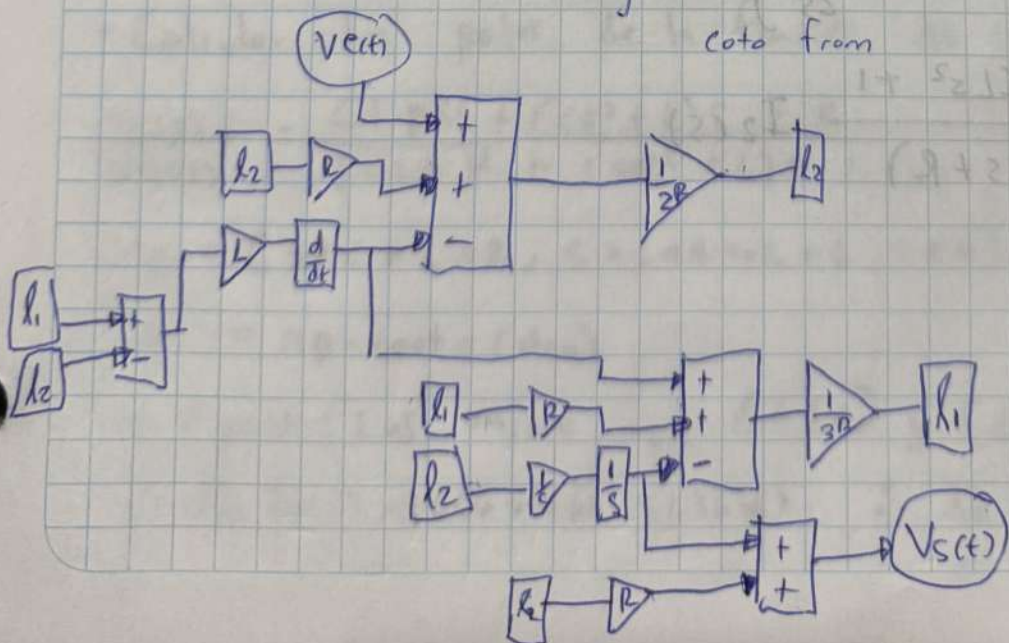
Modo de ecuaciones integral - diferencial

$$i_1(t) = \left[ V_e(t) - L \frac{d[i_1(t) - i_2(t)]}{dt} + R i_2(t) \right] \frac{1}{2R}$$

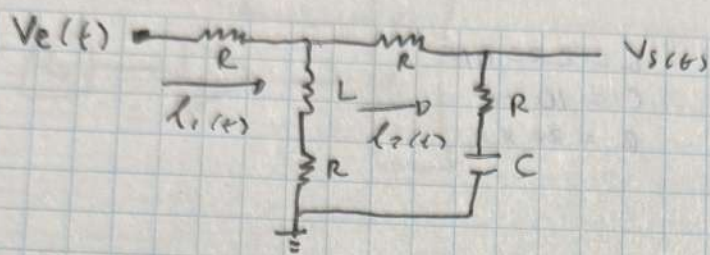
$$i_2(t) = \left[ L \frac{d[i_1(t) - i_2(t)]}{dt} + R i_1(t) - \frac{1}{C} \int i_2(t) dt \right] \frac{1}{3R}$$

$$V_s(t) = R i_2(t) + \frac{1}{C} \int i_2(t) dt$$

data from







Transformada de Laplace

$$V_e(s) = R I_1(s) + L s [I_1(s) - I_2(s)] + R [I_1(s) - I_2(s)]$$

$$L s [I_1(s) - I_2(s)] + R [I_1(s) - I_2(s)] = R I_2(s) + R I_2(s) + \frac{I_2(s)}{C s}$$

$$V_s = R I_2(s) + \frac{I_2(s)}{C s} = \frac{(R s + 1)}{C s} I_2(s)$$

$$\frac{V_s(s)}{V_e(s)} = \frac{I_2(s)}{I_1(s)} \quad \text{Nota: No debe haber terminos negativos}$$

Procedimiento Algebrico

$$V_e(s) = (R + L s + R) I_1(s) - (L s + R) I_2(s)$$

$$= (L s + 2R) I_1(s) - (L s + R) I_2(s)$$

$$L s I_1(s) - L s I_2(s) + R I_1(s) - R I_2(s) = 2R I_2(s) + \frac{I_2(s)}{C s}$$

$$L s I_1(s) + R I_1(s) = 3R I_2(s) + L s I_2(s) + \frac{I_2(s)}{C s}$$

$$(L s + R) I_1(s) = \left( 3R + L s + \frac{1}{C s} \right) I_2(s)$$

$$I_1(s) = \frac{3R s + C L s^2 + 1}{C s (L s + R)} I_2(s)$$



$$V_e(s) = \frac{(Ls + 2R)(CLs^2 + 3CRs + 1)}{Cs(Ls + R)} I_2(s) - (Ls + R) I_2(s)$$

$$= \left[ \frac{(Ls + 2R)(CLs^2 + 3CRs + 1) - (Cs(Ls + R)(Ls + R))}{Cs(Ls + R)} \right] I_2(s)$$

$$CL^2s^3 + 3CLRs^2 + Ls + 2CRs^2 + 6CR^2s + 2R$$

$$- CL^2s^3 - 2CLRs^2 - CR^2s$$

$$3CLRs^2 + Ls + 5CR^2s + 2R$$

$$V_e(s) = \frac{3CLRs^2 + (5CR^2 + L)s + 2R}{Cs(Ls + R)}$$

$$V_s(s) = \frac{CRs + 1}{Cs} I_2(s)$$

$$\frac{3CLRs^2 + (5CR^2 + L)s + 2R}{Cs(Ls + R)} I_2(s)$$

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$$\frac{V_s(s)}{V_e(s)} = \frac{CLRs^2 + (CR^2 + L)s + R}{3CLRs^2 + (5CR^2 + L)s + 2R}$$

Estabilidad de lazo abierto

- Calcular los polos de la función de transferencia

$$\frac{V_s(s)}{V_e(s)} = \frac{CLRs^2 + (CR^2 + L)s + R}{3CLRs^2 + (5CR^2 + L)s + 2R}$$

$$\text{den} = [3 * C * L * R, 5 * C * R^2 + L, 2 * R]$$

$$L = \text{np.roots}(\text{den})$$

→ Fprint: Los raíces son  $\{L[0]\}$  y  $\{L[1]\}$

$$\therefore \lambda_1 = -1.6666666666666667 \quad \therefore \lambda_2 = -1.8181818181818182$$



Error en estado estacionario

$$\begin{aligned}
 e(s) &= \lim_{s \rightarrow 0} s V_e(s) \left[ 1 - \frac{V_s(s)}{V_e(s)} \right] \\
 &= \lim_{s \rightarrow 0} s \cdot \frac{1}{s} \left[ 1 - \frac{(Ls^2 + (CR^2 + L)s + R)}{3CLs^2 + (5CR^2 + L)s + 2R} \right] \\
 &= \frac{R}{2R}
 \end{aligned}$$

$$e(t) = \frac{1}{2} V$$

El sistema presenta una respuesta estable y sobre amortiguada

