

Deliverables Lesson 6

Sistemas Operativos

Grado en Ingeniería Informática

Departamento de Ingeniería Informática

Universidad de Cádiz

Consider a system with a physical memory of 512 MiB. The operating system occupies 512 KiB. Which will be the maximum size of a process in each of the following types of memory allocation schemes?

- 1 A fixed partitioning system where all partitions have the same size: 256 KiB.
- 2 A dynamic partitioning system.
- 3 A buddy system with a minimum partition size of 64 KiB.
- 4 A virtual memory system with 32-bit logical addresses.

Deliverable 6.1 Solution

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- 1 *The size of the partition limits the size of the process. Thus, the maximum size of the process is 256 KiB.*
- 2 *The operating system occupies 512 KiB, therefore we have (512 MiB - 512 KiB) available for processes. This is the maximum size of a process.*
- 3 *To allocate memory to the operating system, the partition of 512 MiB will be divided in two partitions of 256 MiB. One of these will be subdivided until a partition of 512 KiB for hosting the operating system. The other partition could be allocated to a process. Therefore the maximum size of a process is 256 MiB.*
- 4 *The size of the process depends on the logical address, so that the maximum size is 2^{32} bytes.*

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Consider a paged virtual memory system with 32 bits logical addresses and a physical memory of 1 GiB. The page size is 8 KiB and page table and frame table entry sizes are 64 bits. Calculate:

- 1 The maximum size of a process in this system.
- 2 The size of the page table.
- 3 The size of the frame table.
- 4 When we have 10 active processes in the system, how many page tables are there in the system? And how many frame tables?

Deliverable 6.2 Solution

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Physical memory = 1 GiB, Page size = 8 KiB

- 1 Process max. size = Logical Address Space
Process max. size = 2^{32} B = 4 GiB
- 2 Page Table Size = Max. number pages of process \times Entry Size PT
Max. number pages of process = Process max. size / Page Size
Max. number pages of process = 2^{32} B / 2^{13} B = 2^{19} pages
PT Size = $2^{19} \times 2^3$ B = 2^{22} B
- 3 Frame Table Size = Number of physical memory frames \times Entry FT Size
Number of physical memory frames = Physical Memory / Frame Size
Number of physical memory frames = 2^{30} B / 2^{13} B = 2^{17} frames
Frame Table Sizes = $2^{17} \times 2^3$ B = 2^{20} B = 1 MiB
- 4 10 frame tables, one per process. Only one frame table.

Deliverable 6.3 Exercise 1

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Bit maps

- 1 Consider a system with 8GiB of main memory where the size of the asignation unit is 8 KiB. The free-space management is made through a bit map. Calculate the size of the bit map.

Deliverable 6.3 Exercise 1 Solution

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Bit maps

- 1 Consider a system with 8GiB of main memory and the size of the asignment unit is 8 KiB. The free-space management is made through a bit map. Calculate the size of the bit map.

No. bits in the bit map = Main memory size / Asignment unit size

No. bits in the bit map = 8 GiB / 8 KiB =

$$2^3 \times 2^{30} \text{ B} / 2^3 \times 2^{10} \text{ B} = 2^{20}$$

$$\text{Bit map size} = 2^{20} \text{ bits} / 2^3 \text{ bits/B} = 2^{17} \text{ B} = 128 \text{ KiB}$$

Deliverable 6.3 Exercise 2

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Paged virtual memory

2 A virtual memory system has the followings characteristics:

- Logical addresses: 64 bits
- Physical addresses: 30 bits
- Page size: 4 KiB
- Entry page-table size: 32 bits
- Entry frame-table size: 32 bits

Answer these questions:

- 1 Physical memory size.
- 2 Size of the logical address space.
- 3 Frame table size.
- 4 Page table size.

Deliverable 6.3 Exercise 2 Solution

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A paged virtual memory system:

- Logical addresses: 64 bits
- Physical addresses: 30 bits
- Page size: 4 KiB
- Entry page-table size: 32 bits
- Entry frame-table size: 32 bits

1 Physical memory size.

Physical address = 30 bits \rightarrow Physical memory = 2^{30} B = 1 GiB

2 Size of the logical address space.

Logical address = 64 bits \rightarrow Logical address space = 2^{64} B

3 Frame table size.

Frame Table size = No. frames \times Entry FT size

No. Frames = Physical memory / Frame size

Frame Table size = $(2^{30}$ B / 4 KiB) \times 4 B = $(2^{30}$ B / 2^{12} B) \times 2^2 B = 2^{20} B

4 Page table size.

Page table size = No. pages \times Entry PT size

No. pages = Virtual address space / Page size

No. pages = 2^{64} B / 4 KiB = 2^{64} B / 2^{12} B = 2^{52}

Page table size = $2^{52} \times 2^2$ B = 2^{54} B

Format of memory addresses

- ③ Consider a paged virtual memory system with 32 bits logical address and a physical memory of 1 MiB. The page size is 2 KiB. Calculate:
 - ① Logical address format, expressing the size (in bits) of each element.
 - ② Physical address format, expressing the size (in bits) of each element.
- ④ Consider a segmented virtual memory system with 32 bits logical addresses and where the maximum size of segment is 16 KiB. Calculate the logical address format, expressing the size (in bits) of each element.

Deliverable 6.3 Exercise 3 - Solution

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Logical Address Size = 32 bits, Physical Memory = 1 MiB, Page Size = 2 KiB

① Logical Address Format:

p	d
---	---

If Page Size = 2 KiB = 2^{11} B \rightarrow d = 11 bits

If Logical Address Size = p + d = 32 bits \rightarrow p = 21 bits

② Physical Address Format:

m	d (11 bits)
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If Physical Memory = 1 MiB = 2^{20} B \rightarrow Physical Address Size = 20 bits

If Physical Address Size = m + d = 20 bits \rightarrow m = 9 bits

Logical Address Size = 32 bits, Maximum Segment Size = 8 KiB

Logical Address Format:

s	d
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If Maximum Segment Size = 16 KiB = 2^{14} B \rightarrow d = 14 bits

If Logical Address = s + d = 32 bits \rightarrow s = 18 bits

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Consider a paged virtual memory system where:

- Logical address size: 32 bits
- Page size: 4 KiB
- Page Table entry size: 32 bits

The system uses two-level page tables. Determine the format of logical addresses specifying the size (in bits) of each component.

Deliverable 6.4 - Solution

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Logical Address Format:

p1	p2	d
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Logical Address Size = $p1 + p2 + d$

Page Size = 4 KiB = 2^{12} B \rightarrow Offset = $d = 12$ bits

Entries in a Page Table = Page Size / Entry Size

Entries in a Page Table = 2^{12} B / 2^2 B = 2^{10} entries \rightarrow We need 10 bits for p1 and 10 bits for p2.

Logical Address Format:

10	10	12
----	----	----

Deliverable 6.5 Exercise 1

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Multilevel page tables

1 Consider a virtual memory system which uses two-level page tables:

- Logical address size: 32 bits
- Page size: 8 KiB
- Page table entry size: 32 bits

Calculate logical address format considering second level page tables don't show internal fragmentation.

Deliverable 6.5 Exercise 1 - Solution

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Multilevel page tables

1 Consider a virtual memory system which uses two-level page tables:

- Logical address size: 32 bits
- Page size: 8 KiB
- Page table entry size: 32 bits

Calculate logical address format considering second level page tables don't show internal fragmentation.

- Page size = 8 KiB = 2^{13} B, then **d=13 bits**
- $p_1 + p_2 + d = 32 \rightarrow p_1 + p_2 = 32 - 13 = 19$ bits
- No. entries in a PT = Page size / Entry PT size = 2^{13} B / 4 B = 2^{11} entries
- $p_1 \leq 11$ bits and $p_2 \leq 11$ bits
- If second level page tables don't show internal fragmentation, then the component **p2 = 11 bits**
- Therefore $p_1 = 19 - p_2 \rightarrow$ **p1 = 8 bits**

Multilevel page tables

2 Consider a paged virtual memory system which uses three-level page tables:

- Logical addresses: 32 bits
- Physical addresses: 24 bits
- Page size: 2 KiB
- Page table entry size: 32 bits

Calculate:

- 1 Number of bits for offset.
- 2 Maximum number of entries in a page table.
- 3 Maximum number of bits for each pagination component.
- 4 Logical address format considering first and second level page tables don't show internal fragmentation.
- 5 Internal fragmentation in this system.

Deliverable 6.5 Exercise 2 - Solution

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Logical address = 32 bits, Physical address = 24 bits, Page size = 2 KiB, PT Entry = 32 bits, three-level PT

- ① Page size = 2 KiB = 2^{11} B \rightarrow **d = 11 bits**
- ② The size of all page tables is one page, then
No. entries in a PT = Page Size / PT entry size = 2 KiB / 32 bits
= 2^{11} B / 4 B = 2^9 entries
- ③ To address 2^9 entries we need **9 bits**.
- ④ If first and second level page tables don't show internal fragmentation, \rightarrow the components $p1 = p2 = 9$ bits. The logical address is:

p1 (9 bits)	p2 (9 bits)	p3	d (11 bits)
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$$p3 = (32 - p1 - p2 - d) \text{ bits} = \mathbf{3 \text{ bits}}$$

Deliverable 6.5 Exercise 2 - Solution

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Logical address = 32 bits, Physical address = 24 bits, Page size = 2 KiB, PT Entry = 32 bits, three-level PT

⑤ Internal Fragmentation = Intern. Frag. 1-level PT + Intern. Frag. 2-level PT + Intern. Frag. 3-level PT

Internal Frag. N-level = No. N-level PT \times Internal Frag. N-level PT

Internal Frag. N-level PT = Page Size - $2^{pN} \times$ PT entry size

No. N-level PT = $2^{p1} \times 2^{p2} \times \dots \times 2^{p(N-1)}$

Therefore, in this system:

Intern. Frag. 1-level PT = Intern. Frag. 2-level PT = 0

No. 3-level PT = $2^9 \times 2^9 = 2^{18}$ PT

Int. Frag. 3-level PT = 2^{11} B - (2^3 entries \times 4 B/entry) = 2^{11} B - 2^5 B = 2016 B

Total Fragmentation = 2^{18} TP \times 2016 B = 528.482.304 B

Deliverable 6.5 Exercise 3

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Inverted page table

8 Consider a paged virtual memory system which uses inverted page table:

- Logical addresses = 32 bits
- Physical addresses = 24 bits
- Page size = 2 KiB
- Page table entry size = 32 bits

- 1 Calculate the size of inverted page table.
- 2 How many inverted page tables are there?

Deliverable 6.5 Exercise 3 - Solution

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Logical address = 32 bits, Physical address = 24 bits, Page size = 2 KiB, PT entry size = 32 bits, inverted PT

① Physical address format

m	d (11 bits)
---	-------------

24 bits = m + d

m = (24 - 11) bits = 13 bits

Inverted PT Size = 2^m entries \times PT Entry Size

Inverted PT Size = 2^{13} entries \times 4 B/entry = 2^{15} B = 32 KiB

Another way to obtain the solution:

Physical address = 24 bits \implies Physical Memory = 2^{24} B

No. frames = Physical Memory / Frame size

No. frames = 2^{24} B / 2 KiB = 2^{24} B / 2^{11} B = 2^{13} frames

Inverted PT size = No. frames \times TP entry size

Inverted PT size = 2^{13} frames \times 2^2 B = 2^{15} B = 32 KiB

② Only one inverted page table is needed in the system.