Higgs boson production at the Large Hadron Collider: accurate theoretical predictions at higher orders in QCD

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Outline

- Introduction to QCD
 - A historical approach
 - Asymptotic freedom and pQCD
- QCD and collider physics
 - QCD Factorization
 - Partonic cross section and perturbative QCD
- All order perturbative resummation
 - Higher order radiative corrections
 - Resummation of large logarithmic corrections
 - Resummed, asymptotic and fixed-order
- Precise and fast predictions for Higgs boson physics
 - Higgs production at the LHC
 - HTurbo numerical code
 - Preliminary results & Conclusions

Part I QCD and collider physics

Introduction

QCD and the strong interactions

- QCD is the theory of the strong interactions
- Sector of the Standard describing fundamental interactions at the TeV scale
- Fundamental objects described as homogeneous field with quantum mechanical behavior $U(1)\times SU(2)\times SU(3)$

Introduction

QCD and the strong interactions

How to explore proton's inner structure?





?

- At different scales, hadrons show different behavior
- From point-like to complex internal dynamics
- Scattering experiments (DIS) and hadronic physics (LHC)

"A way of describing high energy collisions is to consider any hadron as a composite object of point-like constituents \longrightarrow partons" R.Feynman, 1969

Asymptotic freedom and pQCD



- Parton model as LO approximation to QCD
- Real QCD coupling strength changes with energy
- At high energies the hadron involves extremely complex internal dynamics

QCD is strongly coupled at large scales / low energies \longrightarrow confinement

Non-perturbative physics

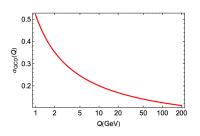
Asymptotic freedom and pQCD

Running coupling given by Renormalization Group Equation (RGE)

$$\mu \frac{d\alpha_s(\mu)}{d\mu} = \beta(\alpha_s(\mu)) = -\sum_{n=0}^{\infty} \beta_n \left(\frac{\alpha_s}{\pi}\right)^{n+1}$$

- ullet Coupling $lpha_s$ evolves with scale μ as given by RGE o LO behavior driven by eta_0
- $\beta_0^{\rm QED} < 0 \implies$ strongly coupled at large energies, UV divergent
- $\beta_0^{\rm QCD} > 0 \implies$ weakly coupled at large energies, IR divergent

Asymptotic freedom and pQCD



 Running coupling given by Renormalization Group Equation (RGE)

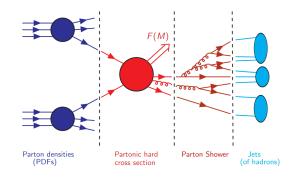
$$lpha_s(\mu) = rac{1}{eta_0 \log \left(rac{\mu^2}{\Lambda_{ ext{QCD}}^2}
ight)}$$

- β_0 LO of the β function, is > 0
- $\Lambda_{\rm QCD},$ parameter that defines value of the coupling at large scales

QCD is weakly coupled for $\mu >> \Lambda_{\rm QCD} \longrightarrow$ asymptotically free

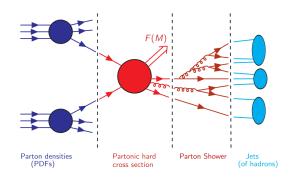
Perturbative Quantum Chromodynamics (pQCD)

Hadronic processes and factorization



- LHC physic rely on hadronic collisions → pQCD
- ullet Compute cross section \longrightarrow probability for a given process

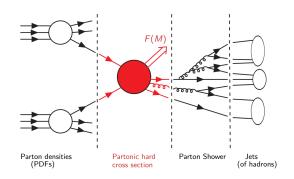
Hadronic processes and factorization



Compute hadronic cross sections is a hard problem --> QCD Factorization

$$\sigma^{F}(p_{1}, p_{2}) = \int_{0}^{1} dx_{1} dx_{2} f_{\alpha}(x_{1}, \mu_{F}^{2}) * f_{\beta}(x_{2}, \mu_{F}^{2}) * \hat{\sigma}_{\alpha\beta}^{F}(x_{1}p_{1}, x_{2}p_{2}, \alpha_{s}(\mu_{R}^{2}), \mu_{F}^{2})$$

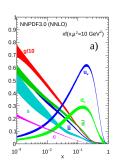
Hadronic processes and factorization



- Parton densities (PDFs) $f_{\alpha}(x_i, \mu_F^2)$: non perturbative but universal
- Partonic cross section $\hat{\sigma}_{\alpha\beta}^{\rm F}$: process dependent but computable as perturbative series in α_s

Parton densities

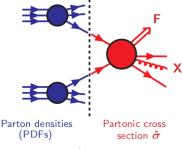
Parton Distribution Functions: probability distribution of finding a particular parton (u, d, ..., g) carrying a fraction x of the proton's momentum



- Each parton has a different PDF $\longrightarrow u(x), d(x), ..., g(x)$
- PDFs can not predicted and yet can not measured → extracted from data (MSTW, CTEQ, NNPDF collaborations)
- The N3PDF project: Machine Learning for PDFs determination [Urtasun-Elizari et al.] ref. at 1910.07049

Partonic cross section and pQCD

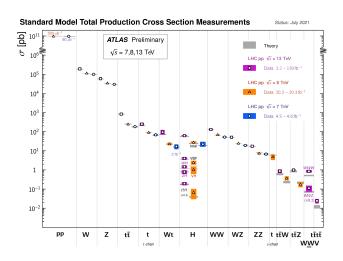
- Born cross section is the leading-order (LO) term of the perturbative series
- $\sigma^{(1)}, \sigma^{(2)}, \sigma^{(3)}$ are the NLO, NNLO, N³LO corrections



$$\hat{\sigma} = \sigma^{\mathtt{Born}} \Big(1 + \alpha_{\mathtt{s}} \sigma^{(1)} + \alpha_{\mathtt{s}}^2 \sigma^{(2)} + \alpha_{\mathtt{s}}^3 \sigma^{(3)} + \ldots \Big)$$

Lower order predictions strongly depend on the auxiliary / unphysical scales Need higher order corrections to increase theoretical accuracy!

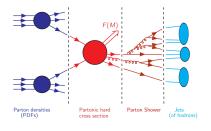
LHC phenomenology



LHC phenomenology

Main processes studied in hadronic physics

- Deep Inelastic Scattering (DIS)
- Drell-Yan lepton pair production
- Higgs boson production

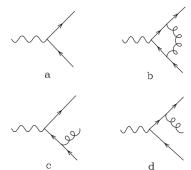


Focus on Higgs production through gluon fusion

Part II All order resummation

Higher order corrections - need for resummation

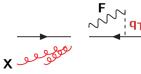
- Calculation of higher order corrections is not an easy task due to infrared (IR) soft and collinear singularities
- ② Final state singularities cancel by combining real and virtual contributions → KLN theorem
- Initial state collinear singularities factorized inside the PDFs



Cancellation only works in completely inclusive final states!

 q_{\perp} resummation

- Describing exclusive final states
- Study the differential q_{\perp} distribution $h_1(p_1) + h_2(p_2) \longrightarrow F(M, q_{\perp}) + X$



$$\int_0^{Q_\perp^2} \ dq_\perp^2 \frac{d\hat{\sigma}}{dq_\perp^2} \sim c_0 + \alpha_s (c_{12}L^2 + c_{11}L + c_{10}) + ..., \quad \text{where} \quad L = \ln(M^2/q_\perp^2)$$

$\alpha_{S}L^{2}$	$\alpha_{\mathcal{S}}L$	 $\mathcal{O}(\alpha_{\mathcal{S}})$
$\alpha_S^2 L^4$	$\alpha_S^2 L^3$	 $\mathcal{O}(\alpha_S^2)$
$\alpha_S^n L^{2n}$	$\alpha_S^n L^{2n-1}$	 $\mathcal{O}(\alpha_S^n)$
dominant logs		

Truncated fixed-order predictions \rightarrow enhanced $\alpha_s^n \ln^m(M^2/q_\perp^2)$ appear

 q_{\perp} resummation

Separate partonic q_{\perp} distribution as follows

$$\frac{d\hat{\sigma}_{ab}}{dq_{\perp}^{2}} = \left[\frac{d\hat{\sigma}_{ab}^{(\mathrm{res.})}}{dq_{\perp}^{2}}\right]_{\mathrm{l.a.}} + \left[\frac{d\hat{\sigma}_{ab}^{(\mathrm{fin.})}}{dq_{\perp}^{2}}\right]_{\mathrm{f.o.}} , \quad \text{such that}$$

$$\int_{0}^{q_{\perp}^{2}} dq_{\perp}^{2} \frac{d\hat{\sigma}_{ab}^{(\mathrm{res.})}}{dq_{\perp}^{2}} \sim \sum \alpha_{s}^{n} \log^{m} \left(\frac{M^{2}}{q_{\perp}^{2}}\right) \quad \text{for} \quad q_{\perp} \to 0$$

$$\lim_{n \to \infty} \int_{0}^{q_{\perp}^{2}} dq_{\perp}^{2} \frac{d\hat{\sigma}_{ab}^{(\mathrm{fin.})}}{dq_{\perp}^{2}} = 0$$

Resummed and finite components can be matched (LL+LO, NLL+NLO, NNLO+NNLL, ...) to have uniform accuracy in a wide range of q_{\perp}

Resummed component

Resummation holds in impact parameter space b

$$\frac{d\hat{\sigma}_{ab}^{(\mathrm{res.})}}{dq_{\perp}^{2}} = \frac{\mathit{M}^{2}}{\hat{s}} \int db \; \frac{b}{2} \; J_{0}(bq_{\perp}) \; \mathcal{W}_{ab}(b, M)$$

with \mathcal{W}_{ab} also expressed in Mellin space (with respect to $z=M^2/\hat{s})$

$$W_N(b, M) = \mathcal{H}_N(\alpha_s) \times \exp\{\mathcal{G}_N(\alpha_s, L)\}$$
 being $L \equiv \log(M^2 b^2)$

- Large logarithms exponentiated in the universal Sudakov form factor $\mathcal{G}_N(\alpha_s, L)$
- Constant (b-independent) terms factorized in the process dependent hard factor $\mathcal{H}_N(\alpha_s)$

Resummed component

Sudakov factor \mathcal{G}_N and hard coefficient \mathcal{H}_N can be expanded as perturbative series in $lpha_s$

$$\mathcal{G}_{N}(\alpha_{s}, L) = L g^{(1)}(\alpha_{s}L) + g^{(2)}(\alpha_{s}L) + \frac{\alpha_{s}}{\pi} g^{(3)}(\alpha_{s}L) + \dots$$
$$\mathcal{H}_{N}(\alpha_{s}) = 1 + \alpha_{s}\mathcal{H}^{(1)} + \alpha_{s}^{2}\mathcal{H}^{(2)} + \dots$$

For each new order implement a factor of \mathcal{G}_N and Hard \mathcal{H}_N

LL(
$$\sim \alpha_s^n L^{n+1}$$
): $g^{(1)}$, $\hat{\sigma}^{(0)}$
NLL($\sim \alpha_s^n L^n$): $g^{(2)}$, $\mathcal{H}^{(1)}$
NNLL($\sim \alpha_s^n L^{n-1}$): $g^{(3)}$, $\mathcal{H}^{(2)}$

Each term $g^{(i)}$ and $\mathcal{H}^{(i)}$ in the series becomes increasingly complicated

Current codes able to produce only up to NNLL predictions!

Finite component

Finite component by fixed-order truncation of the resummed cross section

$$\frac{d\hat{\sigma}_{ab}^{(\mathrm{fin.})}}{dq_{\perp}^{2}} = \left[\frac{d\hat{\sigma}_{ab}}{dq_{\perp}^{2}}\right]_{\mathrm{f.o.}} + \left[\frac{d\hat{\sigma}_{ab}^{(\mathrm{res.})}}{dq_{\perp}^{2}}\right]_{\mathrm{f.o.}}$$

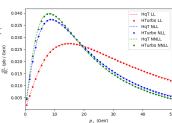
the truncation of the resummed cross section is written in terms of the Σ coefficients

$$\mathcal{W}_{a,b}(b,M) = \sigma^{(0)} \times \mathcal{H}_N(\alpha_s) \times \alpha_s^n \Sigma^n(z,L)$$
 being $L \equiv \log(M^2 b^2)$

Part III HTurbo numerical implementation

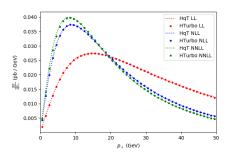
Resummation for Higgs differential distribution

- Fast and accurate predictions for Higgs boson production cross section
- ullet Predictions for differential cross section $d\sigma^{
 m H}/dq_{\perp}^2$
- Numerical implementation of resummed and finite components



Predictions for Higgs q_{\perp} distribution

- q_⊥ resummation implemented in numerical codes HRes, HRes, HNNLO [Catani, de Florian, Ferrera, Grazzini, Tommasini]
- Higher order accuracy require high computation times



Codes producing fast and accurate predictions are needed for precision era of the LHC

Starting point: DYTurbo

Numerical code **DYTurbo** [Camarda et al.] ref. at 1910.07049, fast and precise q_{\perp} resummation and several improvements for Drell-Yan $(h_1h_2 \rightarrow V + X \rightarrow I^+I^- + X)$

First goal: set up a numerical code for Higgs boson production starting from DYTurbo

- Set LO amplitude $gg \rightarrow H$
- Set Sudakov and Hard coefficients for resummed component
- Set Σ coefficients for asymptotic term
- Implement MC producing the LO and NLO H+jet cross sections
- Compare with HRes and HqT

Final goal: extend theoretical accuracy up to N³LL+N³LO

Implementation of Higgs boson factors

Sudakov factor \mathcal{G}_N and hard coefficient \mathcal{H}_N can be expanded as perturbative series in $lpha_s$

$$\mathcal{G}_{N}(\alpha_{s}, L) = L g^{(1)}(\alpha_{s}L) + g^{(2)}(\alpha_{s}L) + \frac{\alpha_{s}}{\pi} g^{(3)}(\alpha_{s}L) + \dots$$
$$\mathcal{H}_{N}(\alpha_{s}) = 1 + \alpha_{s}\mathcal{H}^{(1)} + \alpha_{s}^{2}\mathcal{H}^{(2)} + \dots$$

For each new order implement a factor of \mathcal{G}_N and Hard \mathcal{H}_N

LL(
$$\sim \alpha_s^n L^{n+1}$$
): $g^{(1)}$, $\hat{\sigma}^{(0)}$
NLL($\sim \alpha_s^n L^n$): $g^{(2)}$, $\mathcal{H}^{(1)}$
NNLL($\sim \alpha_s^n L^{n-1}$): $g^{(3)}$, $\mathcal{H}^{(2)}$

Start by building predictions up to NNLO+NNLL, then add N^3LO+N^3LL

Code optimization

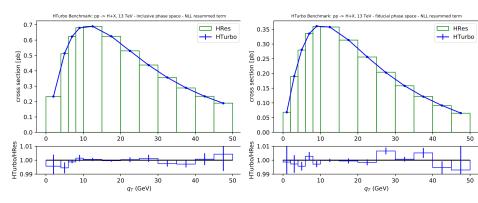
Optimized reimplementation of HqT, HRes and HNNLO for q_T -resummation

- C++ structure with Fortran interfaces → Multi-threading
- Optimization in the integration routines / integral transforms
 - Factorize boson and decay kinematics
 - Gauss-Legendre quadrature rules (1-dim.)
 - Vegas/Cuhre through **Cuba** (multi-dim.)

Comparison HRes and HTurbo - speed performance

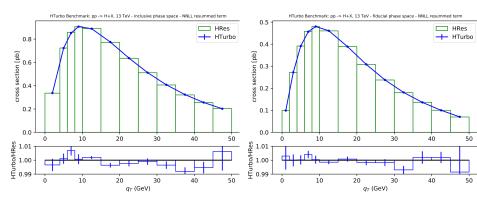
Predictions	HRes	HTurbo
resummed NNLL	10h	10'
combined NNLO+NNLL	48h	2h

Comparison HTurbo and HRes - NLL resummed



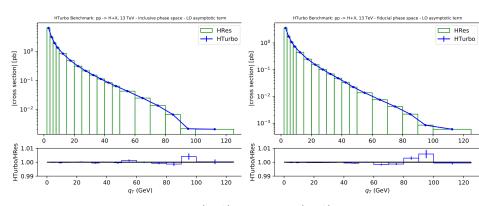
- ullet Cross section for fully inclusive (LHS) and fiducial (RHS) phase space \checkmark
- CM energy $\sqrt{s} = 13$ GeV and PDF set NNPDF31_nlo_as_0118 PDF set

Comparison HTurbo and HRes - NNLL resummed



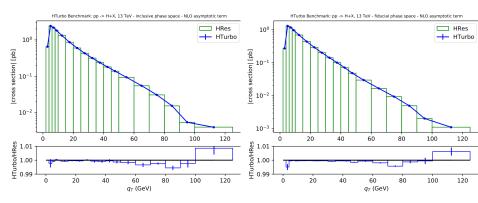
- Cross section for fully inclusive (LHS) and fiducial (RHS) phase space √
- CM energy $\sqrt{s} = 13$ GeV and PDF set NNPDF31_nnlo_as_0118 PDF set

Comparison HTurbo and HRes - LO asymptotic



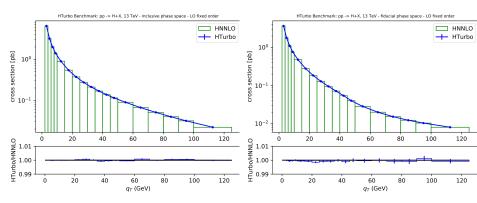
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Comparison HTurbo and HRes - NLO asymptotic



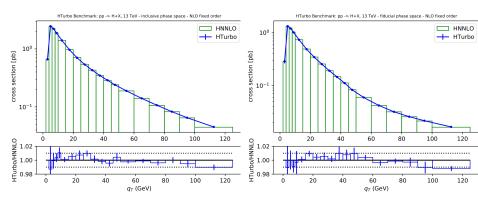
- Cross section for fully inclusive (LHS) and fiducial (RHS) phase space √
- CM energy $\sqrt{s} = 13$ GeV and PDF set NNPDF31_nnlo_as_0118 PDF set

Comparison HTurbo and HRes - LO fixed-order



- Cross section for fully inclusive (LHS) and fiducial (RHS) phase space √
- CM energy $\sqrt{s} = 13$ GeV and PDF set NNPDF31_nlo_as_0118 PDF set

Comparison HTurbo and HRes - NLO fixed-order



- Cross section for fully inclusive (LHS) and fiducial (RHS) phase space √
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Summary & Conclusions

- Fast and accurate predictions are needed towards the precision era of the LHC
- ② Developing a novel numerical code, **HTurbo**, which implements q_{\perp} resummation for Higgs boson production
- 4 HTurbo is faster than any of the existing codes
- Outlook of thesis work:
 - Add N³LO+N³LL prediction
 - Perform phenomenological studies comparing with LHC data

Discussion & next steps

- Fast and accurate predictions are needed towards the precision era of the LHC
- ② Developing a novel numerical code, **HTurbo**, which implements q_{\perp} resummation for Higgs boson production
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Thank you!



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Back up

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