

Higgs boson production at the Large Hadron Collider: accurate theoretical predictions at higher orders in QCD

Jesús Urtasun Elizari

PhD presentation - Milan, February 25th, 2022



UNIVERSITÀ
DEGLI STUDI
DI MILANO



European
Research
Council

This project has received funding from the European Union's Horizon 2020 research and innovation program under grant agreement No 740006.

Outline

- ① Introduction to QCD
 - A historical approach
 - Asymptotic freedom and pQCD
- ② QCD and collider physics
 - QCD Factorization
 - Partonic cross section and perturbative QCD
- ③ All order perturbative resummation
 - Higher order radiative corrections
 - Resummation of large logarithmic corrections
 - Resummed, asymptotic and fixed-order
- ④ Precise and fast predictions for Higgs boson physics
 - Higgs production at the LHC
 - HTurbo numerical code
 - Preliminary results & Conclusions

Introduction

Introduction

QCD - A historical approach

- The Standard Model
- QCD and the strong interactions
- Higgs boson physics and the LHC

Part I

QCD and collider physics

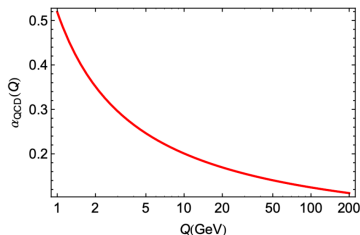
Introduction

QCD and the strong interactions

- The Standard Model
- QCD and the strong interactions
- Higgs boson physics and the LHC

QCD and collider physics

Asymptotic freedom and pQCD



- Running coupling given by Renormalization Group Equation (RGE)

$$\alpha_s(\mu) = \frac{1}{\beta_0 \log\left(\frac{\mu^2}{\Lambda_{\text{QCD}}^2}\right)}$$

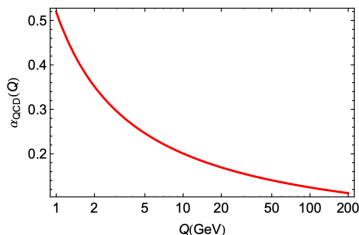
- β_0 LO of the β function, is > 0
- Λ_{QCD} , parameter that defines value of the coupling at large scales

QCD is weakly coupled for $\mu \gg \Lambda_{\text{QCD}} \rightarrow$ asymptotically free

Perturbative Quantum Chromodynamics (pQCD)

QCD and collider physics

Asymptotic freedom and pQCD



- Running coupling given by Renormalization Group Equation (RGE)

$$\alpha_s(\mu) = \frac{1}{\beta_0 \log\left(\frac{\mu^2}{\Lambda_{\text{QCD}}^2}\right)}$$

- β_0 LO of the β function, is > 0
- Λ_{QCD} , parameter that defines value of the coupling at large scales

QCD is weakly coupled for $\mu \gg \Lambda_{\text{QCD}} \rightarrow$ asymptotically free

Perturbative Quantum Chromodynamics (pQCD)

QCD and collider physics

Hadronic processes and factorization

- Hadronic processes and factorization

QCD and collider physics

The parton model

- The parton model

QCD and collider physics

Parton densities

- Parton densities

QCD and collider physics

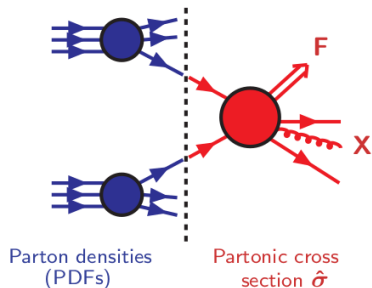
Fixed-order QCD

- Fixed-order QCD

QCD and collider physics

Perturbative QCD

- Born cross section is the leading-order (LO) term of the perturbative series
- $\sigma^{(1)}, \sigma^{(2)}, \sigma^{(3)}$ are the NLO, NNLO, N3LO corrections



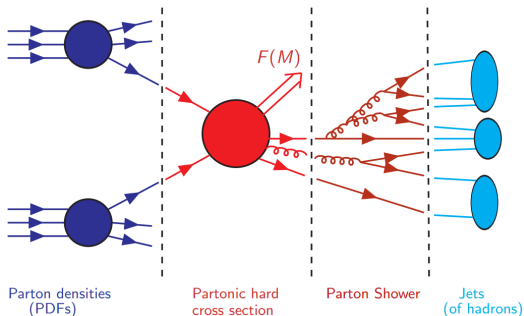
$$\hat{\sigma} = \sigma^{\text{Born}} \left(1 + \alpha_s \sigma^{(1)} + \alpha_s^2 \sigma^{(2)} + \alpha_s^3 \sigma^{(3)} + \dots \right)$$

Lower order predictions strongly depend on the auxiliary / unphysical scales

Need higher order corrections to increase theoretical accuracy!

QCD and collider physics

Factorization theorem

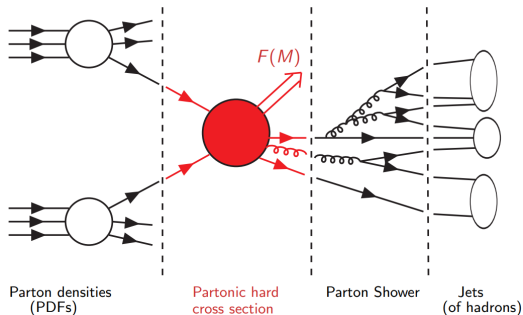


Compute hadronic cross sections is a **hard problem** \rightarrow **QCD Factorization**

$$\sigma^F(p_1, p_2) = \int_0^1 dx_1 dx_2 f_\alpha(x_1, \mu_F^2) * f_\beta(x_2, \mu_F^2) * \hat{\sigma}_{\alpha\beta}^F(x_1 p_1, x_2 p_2, \alpha_s(\mu_R^2), \mu_F^2)$$

QCD and collider physics

Partonic cross section

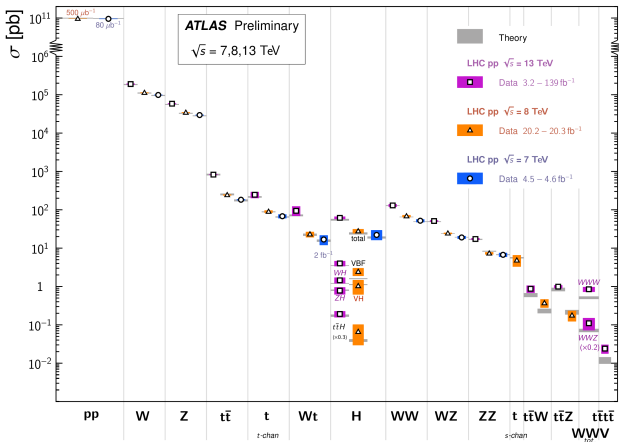


- Parton densities (PDFs) $f_a(x_i, \mu_F^2)$: non perturbative but universal
- Partonic cross section $\hat{\sigma}_{\alpha\beta}^F$: process dependent but computable as perturbative series in α_s

LHC phenomenology

Standard Model Total Production Cross Section Measurements

Status: July 2021



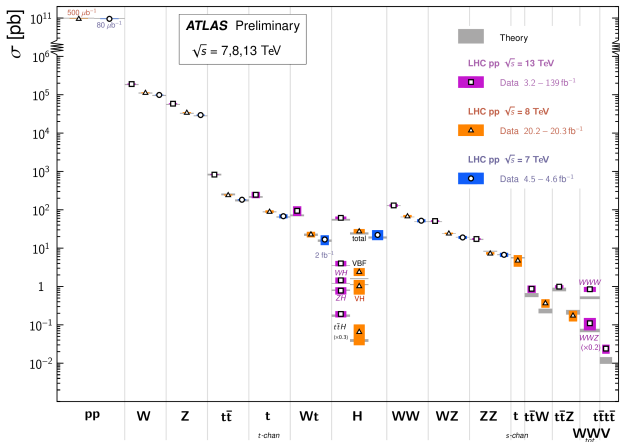
- Physics at the LHC

QCD and collider physics

LHC phenomenology

Standard Model Total Production Cross Section Measurements

Status: July 2021



Physics at the LHC

Part II

All order resummation

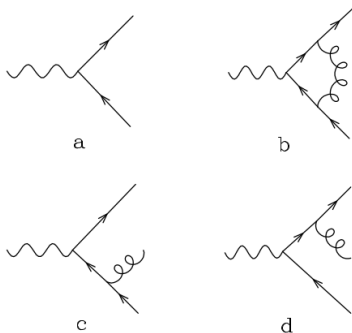
Resummation in QCD

The need for resummation

Resummation in QCD

Higher order corrections

- 1 Calculation of higher order corrections is **not an easy task** due to **infrared (IR) soft and collinear singularities**
- 2 Final state singularities **cancel** by combining real and virtual contributions
- 3 Initial state collinear singularities **factorized** inside the PDFs

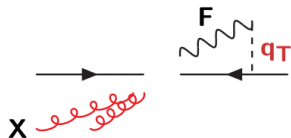


Resummation in QCD

q_\perp resummation

Study the differential q_\perp distribution

$$h_1(p_1) + h_2(p_2) \longrightarrow F(M, \mathbf{q}_\perp) + X$$



$$\int_0^{Q_\perp^2} dq_\perp^2 \frac{d\hat{\sigma}}{dq_\perp^2} \sim c_0 + \alpha_s (c_{12} L^2 + c_{11} L + c_{10}) + \dots, \quad \text{where} \quad L = \ln(q_\perp/M^2)$$

$\alpha_S L^2$	$\alpha_S L$	\dots	$\mathcal{O}(\alpha_S)$
$\alpha_S^2 L^4$	$\alpha_S^2 L^3$	\dots	$\mathcal{O}(\alpha_S^2)$
\dots	\dots	\dots	\dots
$\alpha_S^n L^{2n}$	$\alpha_S^n L^{2n-1}$	\dots	$\mathcal{O}(\alpha_S^n)$
dominant logs	\dots	\dots	\dots

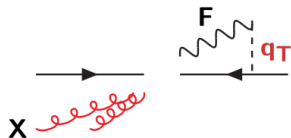
Truncated fixed order predictions \rightarrow enhanced $\alpha_s^n \ln^m(M^2/q_\perp^2)$ appear

Resummation in QCD

q_\perp resummation

Study the differential q_\perp distribution

$$h_1(p_1) + h_2(p_2) \longrightarrow F(M, \mathbf{q}_\perp) + X$$



$$\int_0^{Q_\perp^2} dq_\perp^2 \frac{d\hat{\sigma}}{dq_\perp^2} \sim c_0 + \alpha_s (c_{12} L^2 + c_{11} L + c_{10}) + \dots, \quad \text{where} \quad L = \ln(q_\perp/M^2)$$

$\alpha_S L^2$	$\alpha_S L$	\dots	$\mathcal{O}(\alpha_S)$
$\alpha_S^2 L^4$	$\alpha_S^2 L^3$	\dots	$\mathcal{O}(\alpha_S^2)$
\dots	\dots	\dots	\dots
$\alpha_S^n L^{2n}$	$\alpha_S^n L^{2n-1}$	\dots	$\mathcal{O}(\alpha_S^n)$
dominant logs	\dots	\dots	\dots

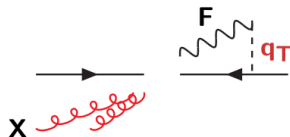
Truncated fixed order predictions \rightarrow enhanced $\alpha_s^n \ln^m(M^2/q_\perp^2)$ appear

Resummation in QCD

q_\perp resummation

Study the differential q_\perp distribution

$$h_1(p_1) + h_2(p_2) \longrightarrow F(M, \mathbf{q}_\perp) + X$$



$$\int_0^{Q_\perp^2} dq_\perp^2 \frac{d\hat{\sigma}}{dq_\perp^2} \sim c_0 + \alpha_s (c_{12} L^2 + c_{11} L + c_{10}) + \dots, \quad \text{where} \quad L = \ln(q_\perp/M^2)$$

$\alpha_S L^2$	$\alpha_S L$	\dots	$\mathcal{O}(\alpha_S)$
$\alpha_S^2 L^4$	$\alpha_S^2 L^3$	\dots	$\mathcal{O}(\alpha_S^2)$
\dots	\dots	\dots	\dots
$\alpha_S^n L^{2n}$	$\alpha_S^n L^{2n-1}$	\dots	$\mathcal{O}(\alpha_S^n)$
dominant logs	\dots	\dots	\dots

Truncated fixed order predictions \rightarrow enhanced $\alpha_s^n \ln^m(M^2/q_\perp^2)$ appear

Resummation in QCD

q_\perp resummation

Separate partonic q_\perp distribution as follows

$$\frac{d\hat{\sigma}_{ab}}{dq_\perp^2} = \left[\frac{d\hat{\sigma}_{ab}^{(\text{res.})}}{dq_\perp^2} \right]_{\text{l.a.}} + \left[\frac{d\hat{\sigma}_{ab}^{(\text{fin.})}}{dq_\perp^2} \right]_{\text{f.o.}}, \quad \text{such that}$$

$$\int_0^{q_\perp^2} dq_\perp^2 \frac{d\hat{\sigma}_{ab}^{(\text{res.})}}{dq_\perp^2} \sim \sum \alpha_s^n \log^m \frac{M^2}{q_\perp^2} \quad \text{for } q_\perp \rightarrow 0$$
$$\lim_{q_\perp \rightarrow 0} \int_0^{q_\perp^2} dq_\perp^2 \frac{d\hat{\sigma}_{ab}^{(\text{fin.})}}{dq_\perp^2} = 0$$

Resummed and finite components can be matched (LL+LO, NLL+NLO, NNLO+NNLL, ...) to have uniform accuracy in a wide range of q_\perp

Resummation in QCD

q_\perp resummation

Resummation holds in impact parameter space b

$$\frac{d\hat{\sigma}_{ab}^{(\text{res.})}}{dq_\perp^2} = \frac{M^2}{\hat{s}} \int db \frac{b}{2} J_0(bq_\perp) \mathcal{W}_{ab}(b, M)$$

with \mathcal{W}_{ab} also expressed in Mellin space (with respect to $z = M^2/\hat{s}$)

$$\mathcal{W}_N(b, M) = \mathcal{H}_N(\alpha_s) \times \exp\{\mathcal{G}_N(\alpha_s, L)\} \quad \text{being} \quad L \equiv \log(M^2 b^2)$$

- Large logarithms exponentiated in the universal Sudakov form factor $\mathcal{G}_N(\alpha_s, L)$
- Constant (b -independent) terms factorized in the process dependent hard factor $\mathcal{H}_N(\alpha_s)$

Part III

HTurbo numerical implementation

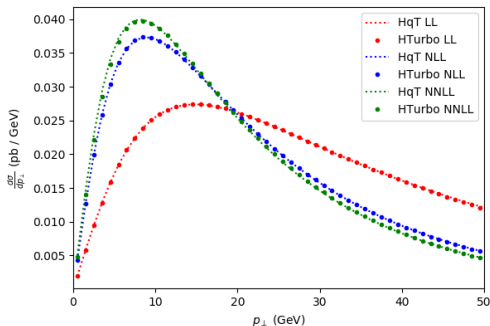
HqT and HRes

Need for fast numerical implementations

HqT and HRes

Predictions for Higgs q_{\perp} distribution

- q_{\perp} resummation implemented in numerical codes HqT and HRes
- [Catani, de Florian, Ferrera, Grazzini, Tommasini]
- Higher order accuracy require **high computation times**
- Codes producing fast and accurate predictions are needed for precision era of the LHC



HTurbo

Starting point DYTurbo

Numerical code **DYTurbo** [Camarda et al.] ref. at [1910.07049](#), fast and precise q_{\perp} resummation and several improvements for Drell-Yan ($h_1 h_2 \rightarrow V + X \rightarrow l^+ l^- + X$)

- **First goal**: set up a numerical code for Higgs boson production starting from **DYTurbo**
- Set LO amplitude $gg \rightarrow H$
- Set Sudakov and Hard coefficients for Higgs production
- Compare with **HRes** and **HqT**

Final goal: extend theoretical accuracy up to $N^3\text{LL}+N^3\text{LO}$

HTurbo

Starting point DYTurbo

Both Sudakov factor \mathcal{G}_N and hard coefficient \mathcal{H}_N can be expanded as perturbative series in α_s

$$\mathcal{G}_N(\alpha_s, L) = L g^{(1)}(\alpha_s L) + g^{(2)}(\alpha_s L) + \frac{\alpha_s}{\pi} g^{(3)}(\alpha_s L) + \dots$$

$$\mathcal{H}_N(\alpha_s) = 1 + \alpha_s \mathcal{H}^{(1)} + \alpha_s^2 \mathcal{H}^{(2)} + \dots$$

For each new order implement a factor of \mathcal{G}_N and Hard \mathcal{H}_N

$$\text{LL}(\sim \alpha_s^n L^{n+1}) : g^{(1)}, \hat{\sigma}^{(0)}$$

$$\text{NLL}(\sim \alpha_s^n L^n) : g^{(2)}, \mathcal{H}^{(1)}$$

$$\text{NNLL}(\sim \alpha_s^n L^{n-1}) : g^{(3)}, \mathcal{H}^{(2)}$$

Start by building predictions up to NNLO+NNLL, then add
N³LO+N³LL

Reimplementation of **HqT** and **HRes** for q_T -resummation

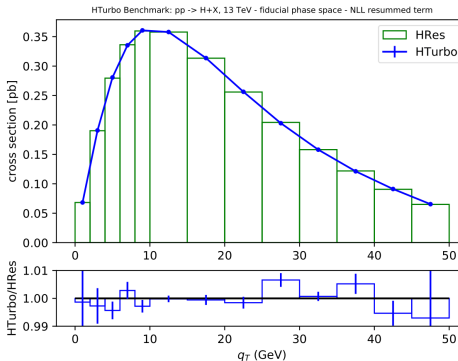
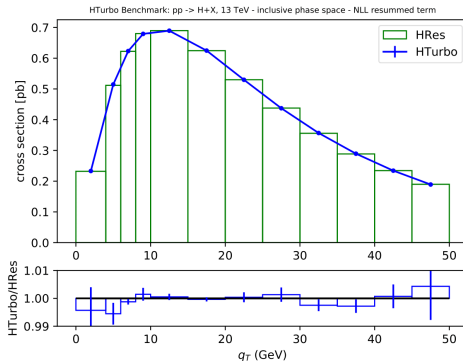
- **C++** structure with **Fortran** interfaces → Multi-threading
- Optimization in the integration routines / integral transforms
 - Factorize boson and decay kinematics
 - Gauss-Legendre quadrature rules (1-dim.)
 - Vegas/Cuhre through **Cuba** (multi-dim.)

Comparison **HRes** and **HTurbo** - speed performance

Predictions	HRes	HTurbo
resummed NNLL	10h	10'
combined NNLO+NNLL	20h	1h

Results

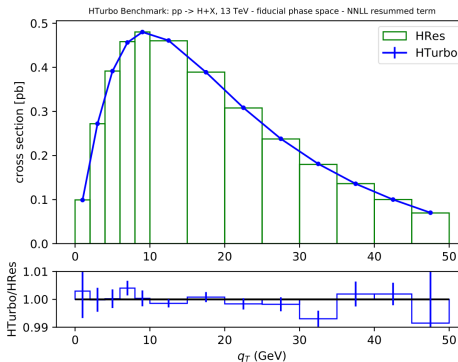
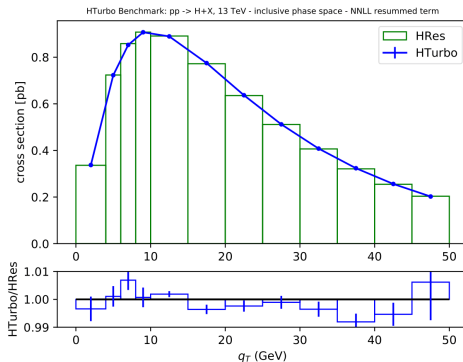
Comparison HTurbo and HRes - NLL resummed



- Represent full (LHS) and fiducial (RHS) phase space ✓
- Excellent numerical agreement at NLL

Results

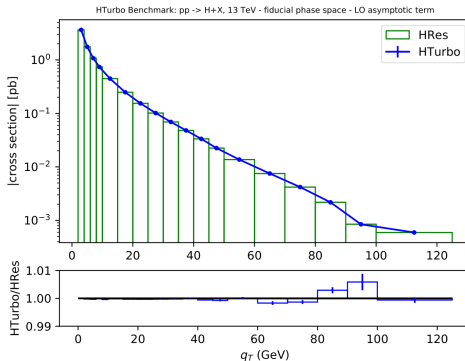
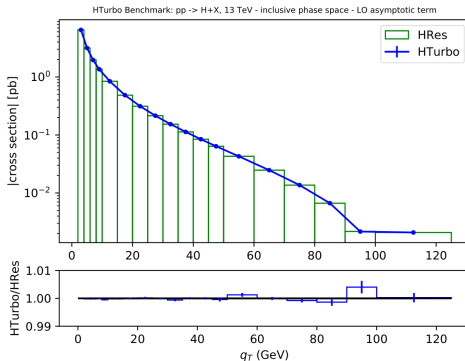
Comparison HTurbo and HRes - NNLL resummed



- Represent full (LHS) and fiducial (RHS) phase space ✓
- Excellent numerical agreement at NNLL

Results

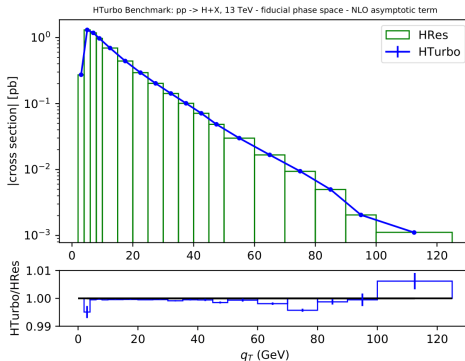
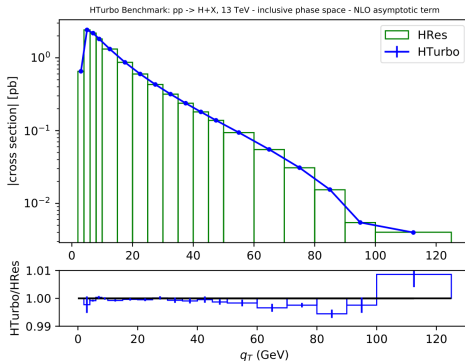
Comparison HTurbo and HRes - LO asymptotic



- Represent full (LHS) and fiducial (RHS) phase space ✓
- Excellent numerical agreement at LO

Results

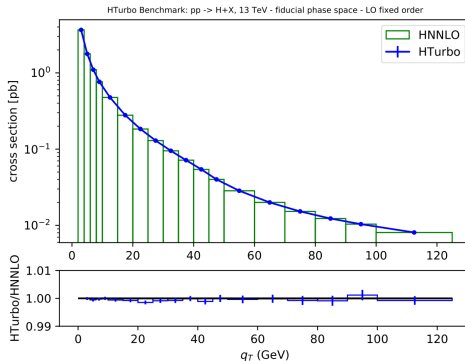
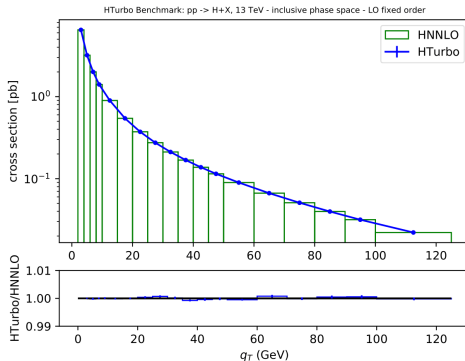
Comparison HTurbo and HRes - NLO asymptotic



- Represent full (LHS) and fiducial (RHS) phase space ✓
- Excellent numerical agreement at NLO

Results

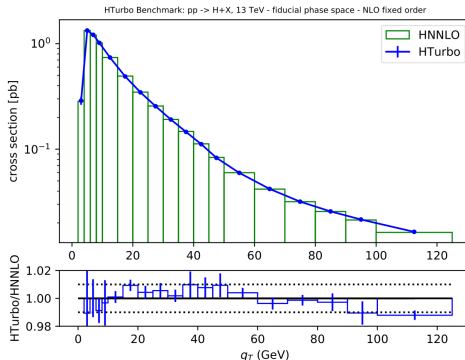
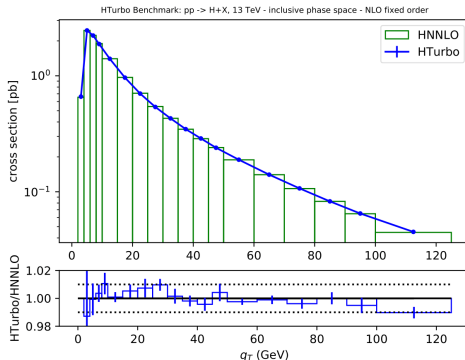
Comparison HTurbo and HRes - LO fixed-order



- Represent full (LHS) and fiducial (RHS) phase space ✓
- Excellent numerical agreement at LO

Results

Comparison HTurbo and HRes - NLO fixed-order



- Represent full (LHS) and fiducial (RHS) phase space ✓
- Excellent numerical agreement at NLO

Summary & Conclusions

- ① Fast and accurate predictions are needed towards the precision era of the LHC
- ② Developing a novel numerical code, **HTurbo**, which implements q_\perp resummation for Higgs boson production
- ③ HTurbo is faster than any of the existing codes
- ④ Outlook of thesis work:
 - Add $N^3\text{LO}+N^3\text{LL}$ prediction
 - Perform phenomenological studies comparing with LHC data

Discussion & next steps

- ① Fast and accurate predictions are needed towards the precision era of the LHC
- ② Developing a novel numerical code, **HTurbo**, which implements q_{\perp} resummation for Higgs boson production
- ③ HTurbo is faster than any of the existing codes
- ④ Outlook of thesis work:
 - Add $N^3\text{LO}+N^3\text{LL}$ prediction
 - Perform phenomenological studies comparing with LHC data

Thank you!



This project has received funding from the European Union's Horizon 2020 research and innovation program under grant agreement No 740006.