

BUSINESS ANALYTICS ASSIGNMENT -3

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R Markdown

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When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
#TASK-1
set.seed(2017)
X=runif(100)*10
Y=X*4+3.45
Y=rnorm(100)*0.29*Y+Y
head(X)

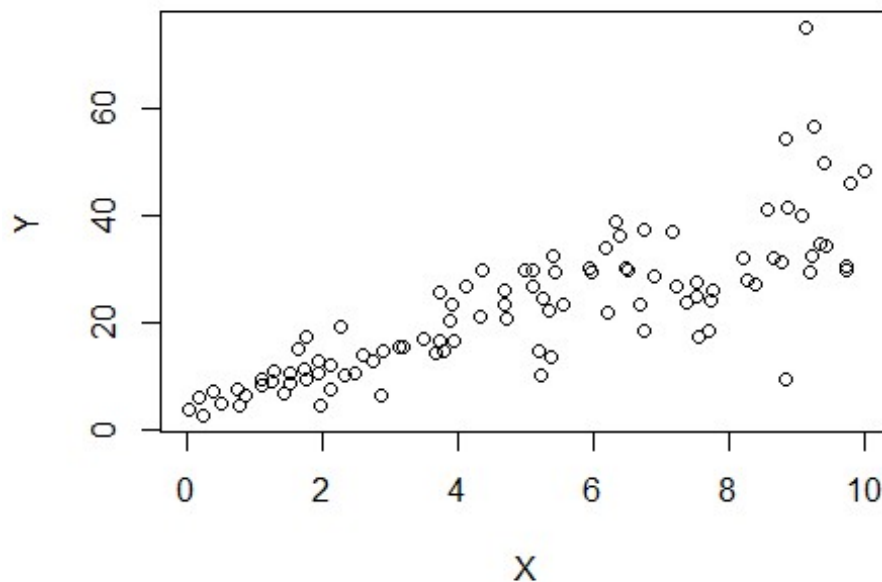
## [1] 9.242426 5.371764 4.691956 2.886262 7.700882 7.727687

head(Y)

## [1] 56.33934 13.48174 23.49129 14.90010 18.42442 24.14282

#(A)Plot Y against X. Include a screenshot of the plot in your submission.
Using the File menu you can save the graph as a picture on your computer.
Based on the plot do you think we can fit a linear model to explain Y based
on X?
plot(X, Y, main = "Scatterplot",
      xlab = "X",
      ylab = "Y")
```

Scatterplot



Yes, based on the plot we can fit a linear model to explain Y based on X

#(B)

#Construct a simple linear model of Y based on X. Write the equation that explains Y based on X. What is the accuracy of this model?

```
model= lm(Y ~ X)
summary(model)
```

```
##
## Call:
## lm(formula = Y ~ X)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -26.755  -3.846  -0.387   4.318  37.503
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   4.4655     1.5537   2.874  0.00497 **
## X             3.6108     0.2666  13.542 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.756 on 98 degrees of freedom
## Multiple R-squared:  0.6517, Adjusted R-squared:  0.6482
## F-statistic: 183.4 on 1 and 98 DF, p-value: < 2.2e-16
```

```

#The equation that explains Y based on X.
#   Y = 4.4655 + 3.6108X
#   The accuracy of the model is 0.6517 i.e, 65.17% which is good fit

#(C)
# How the Coefficient of Determination, R2, of the model above is related to
the correlation coefficient of X and Y?

cor(X,Y)^2

## [1] 0.6517187

#From the above we notice that it's exact the same value of R-squared 0.6517

#TASK-2
# We will use the 'mtcars' dataset for this question. The dataset is already
included in your R distribution. The dataset shows some of the
characteristics of different cars. The following shows few samples (i.e. the
first 6 rows) of the dataset. The description of the dataset can be found here.

head(mtcars)

##           mpg  cyl  disp  hp  drat    wt  qsec vs  am  gear  carb
## Mazda RX4      21.0   6  160 110  3.90  2.620 16.46  0   1    4    4
## Mazda RX4 Wag  21.0   6  160 110  3.90  2.875 17.02  0   1    4    4
## Datsun 710     22.8   4  108  93  3.85  2.320 18.61  1   1    4    1
## Hornet 4 Drive  21.4   6  258 110  3.08  3.215 19.44  1   0    3    1
## Hornet Sportabout 18.7   8  360 175  3.15  3.440 17.02  0   0    3    2
## Valiant        18.1   6  225 105  2.76  3.460 20.22  1   0    3    1

#(A) James wants to buy a car. He and his friend, Chris, have different
opinions about the Horse Power (hp) of cars. James think the weight of a car
(wt) can be used to estimate the Horse Power of the car while Chris thinks
the fuel consumption expressed in Mile Per Gallon (mpg), is a better
estimator of the (hp). Who do you think is right? Construct simple linear
models using mtcars data to answer the question.

model_James <- lm(hp ~ wt, data = mtcars)
summary(model_James)

##
## Call:
## lm(formula = hp ~ wt, data = mtcars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -83.430 -33.596 -13.587   7.913 172.030
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -1.821     32.325  -0.056   0.955

```

```
## wt          46.160      9.625   4.796 4.15e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 52.44 on 30 degrees of freedom
## Multiple R-squared:  0.4339, Adjusted R-squared:  0.4151
## F-statistic:    23 on 1 and 30 DF,  p-value: 4.146e-05
```

```
model_chris <- lm(hp ~ mpg, data = mtcars)
summary(model_chris)
```

```
##
## Call:
## lm(formula = hp ~ mpg, data = mtcars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -59.26 -28.93 -13.45  25.65 143.36
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   324.08      27.43   11.813 8.25e-13 ***
## mpg           -8.83       1.31   -6.742 1.79e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 43.95 on 30 degrees of freedom
## Multiple R-squared:  0.6024, Adjusted R-squared:  0.5892
## F-statistic: 45.46 on 1 and 30 DF,  p-value: 1.788e-07
```

#Based on the results, the model that predicts horsepower from mpg appears to be superior because it has a higher R-squared value (0.6024) and a smaller residual standard error (43.95) than the model that predicts horsepower from weight (R-squared = 0.4339, residual standard error = 52.44). Hence, Chris's claim that mpg is a better indicator of horsepower than James's claim that weight is a better estimator seems to be more correct.

#Therefore, Chris model's accuracy is 0.6024 which is very high than that of James i.e., 0.4339.

#(B) Build a model that uses the number of cylinders (cyl) and the mile per gallon (mpg) values of a car to predict the car HorsePower (hp). Using this model, what is the estimated Horse Power of a car with 4 calendar and mpg of 22?

```
HP<- lm(hp ~ cyl + mpg, data = mtcars)
summary(HP)
```

```
##
## Call:
## lm(formula = hp ~ cyl + mpg, data = mtcars)
##
## Residuals:
```

```
##      Min      1Q  Median      3Q      Max
## -53.72 -22.18 -10.13  14.47 130.73
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   54.067      86.093   0.628  0.53492
## cyl           23.979       7.346   3.264  0.00281 **
## mpg          -2.775       2.177  -1.275  0.21253
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 38.22 on 29 degrees of freedom
## Multiple R-squared:  0.7093, Adjusted R-squared:  0.6892
## F-statistic: 35.37 on 2 and 29 DF, p-value: 1.663e-08

predict(HP, data.frame(cyl = 4, mpg =22))

##           1
## 88.93618

HP$coefficients

## (Intercept)      cyl      mpg
##  54.066600  23.978626  -2.774769

predict_HP <- (HP$coefficients[2]*22) + (HP$coefficients[3]*4)
+ HP$coefficients[1]

## (Intercept)
##      54.0666

print(paste('The estimated horse power of a car with 4 calender and mpg of 22
is ', predict_HP))

## [1] "The estimated horse power of a car with 4 calender and mpg of 22 is
516.430701894008"

#The estimated horse power of a car with 4 calender and mpg of 22 is 88.93618

# TASK-3
# For this question, we are going to use Boston Housing data set. The data set
is in 'mlbench' package, so we first need to install the package, call the
library and the load the data set using the following commands

#install.packages("mlbench")
library(mlbench)

## Warning: package 'mlbench' was built under R version 4.2.3

data(BostonHousing)
str(BostonHousing)
```

```
## 'data.frame': 506 obs. of 14 variables:
## $ crim : num 0.00632 0.02731 0.02729 0.03237 0.06905 ...
## $ zn : num 18 0 0 0 0 12.5 12.5 12.5 12.5 ...
## $ indus : num 2.31 7.07 7.07 2.18 2.18 2.18 7.87 7.87 7.87 7.87 ...
## $ chas : Factor w/ 2 levels "0","1": 1 1 1 1 1 1 1 1 1 1 ...
## $ nox : num 0.538 0.469 0.469 0.458 0.458 0.458 0.524 0.524 0.524
0.524 ...
## $ rm : num 6.58 6.42 7.18 7 7.15 ...
## $ age : num 65.2 78.9 61.1 45.8 54.2 58.7 66.6 96.1 100 85.9 ...
## $ dis : num 4.09 4.97 4.97 6.06 6.06 ...
## $ rad : num 1 2 2 3 3 3 5 5 5 5 ...
## $ tax : num 296 242 242 222 222 222 311 311 311 311 ...
## $ ptratio: num 15.3 17.8 17.8 18.7 18.7 18.7 15.2 15.2 15.2 15.2 ...
## $ b : num 397 397 393 395 397 ...
## $ lstat : num 4.98 9.14 4.03 2.94 5.33 ...
## $ medv : num 24 21.6 34.7 33.4 36.2 28.7 22.9 27.1 16.5 18.9 ...
```

#You should have a data frame with the name of Boston Housing in your Global environment now. The data set contains information about houses in different parts of Boston. Details of the data set is explained here. Note the data set is old, hence low house prices!

#TASK-3(A)

#Build a model to estimate the median value of owner-occupied homes (medv) based on the following variables: crime rate (crim), proportion of residential land zoned for lots over 25,000 sq.ft (zn), the local pupil-teacher ratio (ptratio) and whether the tract bounds Chas River (chas). Is this an accurate model?

```
Model_Boston<-lm(formula = BostonHousing$medv ~ BostonHousing$crim +
BostonHousing$zn
+ BostonHousing$ptratio + BostonHousing$chas, data = BostonHousing)

summary(Model_Boston)
```

```
##
## Call:
## lm(formula = BostonHousing$medv ~ BostonHousing$crim + BostonHousing$zn +
## BostonHousing$ptratio + BostonHousing$chas, data = BostonHousing)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -18.282  -4.505  -0.986   2.650  32.656
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    49.91868    3.23497   15.431 < 2e-16 ***
## BostonHousing$crim -0.26018    0.04015  -6.480 2.20e-10 ***
## BostonHousing$zn    0.07073    0.01548   4.570 6.14e-06 ***
## BostonHousing$ptratio -1.49367    0.17144  -8.712 < 2e-16 ***
```

```
## BostonHousing$chas1    4.58393    1.31108    3.496 0.000514 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.388 on 501 degrees of freedom
## Multiple R-squared:  0.3599, Adjusted R-squared:  0.3547
## F-statistic: 70.41 on 4 and 501 DF,  p-value: < 2.2e-16
```

#The R-squared value for the model is 0.3599, which is low and indicates that it is not very accurate.

TASK-3(B1)

#Imagine two houses that are identical in all aspects but one bounds the Chas River and the other does not. Which one is more expensive and by how much?

```
Model_Boston1 <- lm(formula = BostonHousing$medv ~ BostonHousing$chas, data=
BostonHousing)
Model_Boston1
```

```
##
## Call:
## lm(formula = BostonHousing$medv ~ BostonHousing$chas, data =
BostonHousing)
##
## Coefficients:
##          (Intercept)  BostonHousing$chas1
##             22.094             6.346
```

#using the coefficient of the above model we can calculate the values of both the houses

#House 0 without chas and House1 with chas

```
House0<- Model_Boston1$coefficients[1]+Model_Boston1$coefficients[2]*0
House1<- Model_Boston1$coefficients[1]+Model_Boston1$coefficients[2]*1
print(paste('House with chas is more expensive and by',House1-House0))
```

```
## [1] "House with chas is more expensive and by 6.34615711252662"
```

#TASK-3(b2)

#Imagine two houses that are identical in all aspects but in the neighborhood of one of them the pupil-teacher ratio is 15 and in the other one is 18. Which one is more expensive and by how much?

```
Model_Boston2 <- lm(medv ~ ptratio, data = BostonHousing)
Model_Boston2
```

```
##
## Call:
## lm(formula = medv ~ ptratio, data = BostonHousing)
##
## Coefficients:
## (Intercept)      ptratio
##      62.345      -2.157
```

```
House15 <- predict(Model_Boston2, newdata = data.frame(ptratio = 15))
House18 <- predict(Model_Boston2, newdata = data.frame(ptratio = 18))
price_diff <- House15 - House18
print(paste('House in which pupil-teacher ratio of two houses is 15,18 and is
more expensive and by ',House15-House18))
```

```
## [1] "House in which pupil-teacher ratio of two houses is 15,18 and is more
expensive and by 6.47152588818295"
```

#TASK-3(c)

#Which of the variables are statistically important (i.e. related to the house price)? Hint: use the p-values of the coefficients to answer.

```
summary(Model_Boston)
```

```
##
## Call:
## lm(formula = BostonHousing$medv ~ BostonHousing$crim + BostonHousing$zn +
##      BostonHousing$ptratio + BostonHousing$chas, data = BostonHousing)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -18.282  -4.505  -0.986   2.650  32.656
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    49.91868    3.23497   15.431 < 2e-16 ***
## BostonHousing$crim  -0.26018    0.04015   -6.480 2.20e-10 ***
## BostonHousing$zn     0.07073    0.01548    4.570 6.14e-06 ***
## BostonHousing$ptratio -1.49367    0.17144   -8.712 < 2e-16 ***
## BostonHousing$chas1  4.58393    1.31108    3.496 0.000514 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.388 on 501 degrees of freedom
## Multiple R-squared:  0.3599, Adjusted R-squared:  0.3547
## F-statistic: 70.41 on 4 and 501 DF, p-value: < 2.2e-16
```

#As their p-values are less than 0.05. Looking at the p-values we can say that non of the independent variables are statistically significant

#TASK-3(d)

#Use the anova analysis and determine the order of importance of these four variables

```
anova(Model_Boston)
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: BostonHousing$medv
```

```
##              Df Sum Sq Mean Sq F value    Pr(>F)
```



```
## BostonHousing$crim      1  6440.8  6440.8 118.007 < 2.2e-16 ***
## BostonHousing$zn        1  3554.3  3554.3  65.122 5.253e-15 ***
## BostonHousing$ptratio   1  4709.5  4709.5  86.287 < 2.2e-16 ***
## BostonHousing$chas      1   667.2   667.2  12.224 0.0005137 ***
## Residuals               501 27344.5    54.6
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

To determine the order of importance, we can look at the magnitude of the F-values. Based on the F-values, the order of importance from highest to lowest is:

```
#crim
#ptratio
#zn
#chas
```