Discovering a motif discovering appproach

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Goal of the exercise

The goal of this exercise is to get an intuition of a motif discovery approach relying on the detection of over-represented oligonucleotides.

Our approach will be pragmatic.

We retrieved the upstream non-coding sequences of the genes involved in methionine biosynthesis and sulfur assimilation, and counted the occurrences of each hexanucleotide.

We also computed

- the relative frequencies (occurrences of each oligo / sum of all oligo occurrences) in the sequence of interest (the promoters of methionine-associated genes)
- the relative frequencies of ach hexanucleotide in the whole set of yeast promoters.

We would like to know if some 6nt are over-reprsented in promoters of methionine-associated genes relative to the occurrences that would be expected from a random selection of yeast promoters.

Create a workspace for this practical

- In your home directory, create a work directory for this practical (for example `~/LCG_BEII/practical_motif_discovery/`

```
workdir <- "~/LCG_BEII/practical_motif_discovery"
dir.create(workdir, showWarnings = FALSE, recursive = TRUE)
setwd(workdir)
```

Loading the data table

1. Download the oligonucleotide count table. Scerevisiae_MET-genes_oligos-6nt-2str-noov_occ-freq.tsv

```
oligo.url <- "http://jvanheld.github.io/LCG_BEII/practicals/motif_discovery/data/Scerevisiae_MET-genes_
oligo.file <- basename(oligo.url) ## Suppress the URL path and keep only the file name for local storag
download.file(oligo.url, destfile = oligo.file)
```

2. In **R**, open a new script or R markdown file.
3. Load the data table, print the 5 top rows and the 5 bottom rows.

```
oligo.table <- read.delim(oligo.file, header = 1, row.names = 1)
# View(oligo.table)
```

```
head(oligo.table, n = 5)
```

```
                obs_freq    exp_freq occ exp_occ
aaaaaa|tttttt 0.004592808 0.004896299  41   43.71
aaaaac|gttttt 0.001120197 0.001998518  10   17.84
aaaaag|cttttt 0.003696651 0.003604251  33   32.18
aaaaat|attttt 0.004032710 0.004160627  36   37.14
aaaaca|tgtttt 0.001344237 0.001932479  12   17.25
```

```
tail(oligo.table, n = 5)
```

```
                 obs_freq     exp_freq occ exp_occ
ttccaa|ttggaa 0.0008961577 0.0008428396   8    7.52
ttcgaa|ttcgaa 0.0001120197 0.0003224542   1    2.88
ttgaaa|tttcaa 0.0019043352 0.0019087053  17   17.04
ttgcaa|ttgcaa 0.0001120197 0.0004030214   1    3.60
tttaaa|tttaaa 0.0005600986 0.0009379354   5    8.37
```

Exploring observed and expected counts

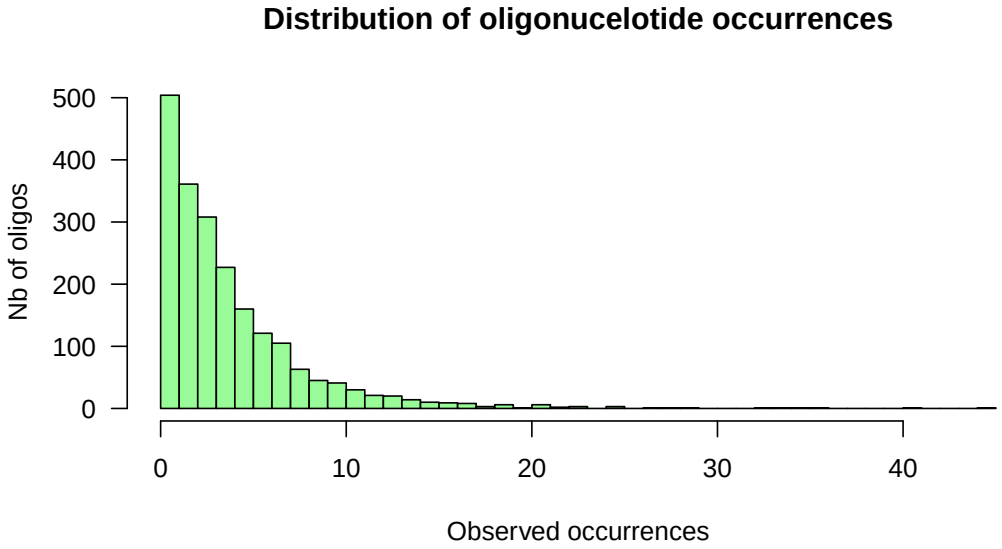
4. Draw an histogram of the observed occurrences and evaluate the spread of counts.

```
x <- oligo.table$occ
range(x)
```

```
[1]  0 45
```

```
max.x <- max(x)

hist(x, breaks = 0:max.x, col = "palegreen",
     xlab = "Observed occurrences",
     ylab = "Nb of oligos",
     las = 1,
     main = "Distribution of oligonucelotide occurrences")
```



5. Draw a scatter plot comparing the observed and expected occurrences for each hexanucleotide.

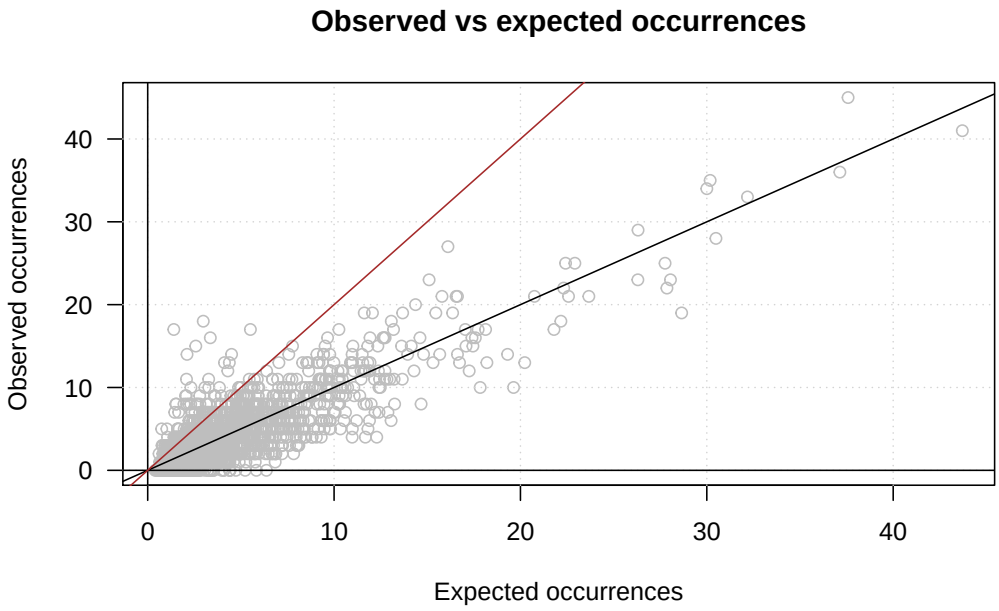


Figure 1: **Scatter plot of observed versus expected occurrences.** The black diagonal corresponds to the null hypothesis, the brown line denotes an arbitrary threshold on fold-change > 2.

```
exp.occ <- oligo.table$exp_occ

plot(exp.occ, x, col = "grey", las = 1,
     xlab = "Expected occurrences",
     ylab = "Observed occurrences",
     main = "Observed vs expected occurrences")
grid()
abline(a = 0, b = 1, col = "black")
abline(h = 0, col = "black")
abline(v = 0, col = "black")

abline(a = 0, b = 2, col = "brown")
```

6. Compute the ratio of observed / expected occurrences, and draw a scatter plot with this ratio (Y) as a function of the expected occurrences (X).

```
ratio <- (x/exp.occ)

plot(exp.occ, ratio,
     col = "grey", las = 1,
     xlab = "Expected occurrences",
     ylab = "(obs/exp) ratio",
     main = "(obs/exp) ratio")
grid()
abline(h = 1, col = "black")
abline(h = 2, col = "brown")
```

6. Compute the log-ratio of observed / expected occurrences, and draw a scatter plot with this log-ratio (Y) as a function of the expected occurrences (X).

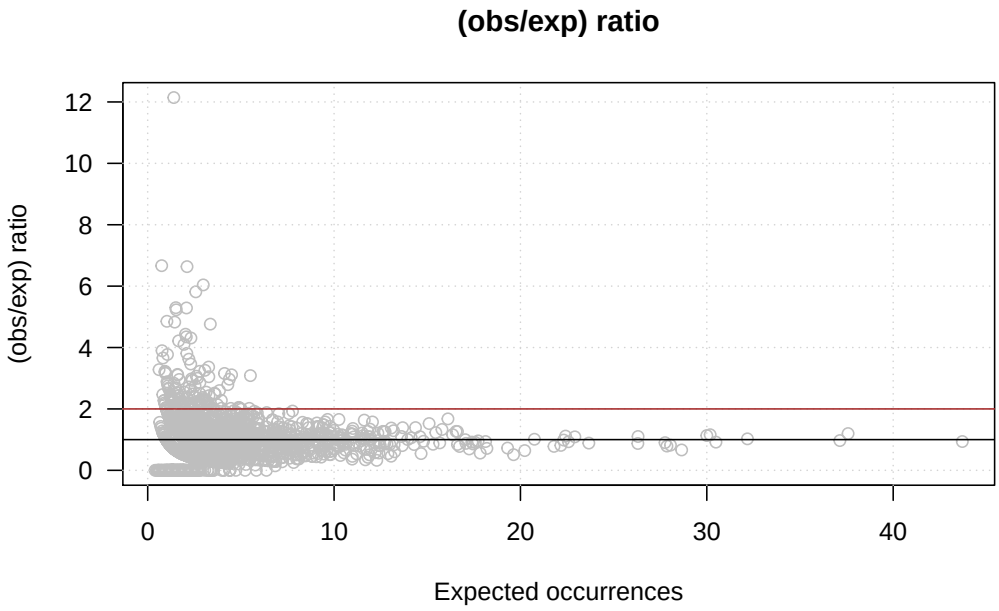


Figure 2: **Scatter plot of observed versus expected occurrences.** The black diagonal corresponds to the null hypothesis, the brown line denotes an arbitrary threshold on fold-change > 2.

```
lr <- log(x/exp.occ)

plot(exp.occ, lr,
     col = "grey", las = 1,
     xlab = "Expected occurrences",
     ylab = "log(obs/exp)",
     main = "Log-ratio")
grid()
abline(h = 0, col = "black")
abline(h =  log(2), col = "brown")
```

$$lr = log(x/ < X >)$$

7. Compute the log-likelihood ratio (llr), defined below, and draw a scatter plot with this llr as a function of the expected occurrences.

$$llr = f \cdot log(x/ < X >)$$

```
p <- oligo.table$exp_freq
llr <- p * log(x/exp.occ)

plot(exp.occ, llr,
     col = "grey", las = 1,
     xlab = "Expected occurrences",
     ylab = "llr",
     main = "Log-likelihood ratio")
grid()
abline(h = 0, col = "black")
```

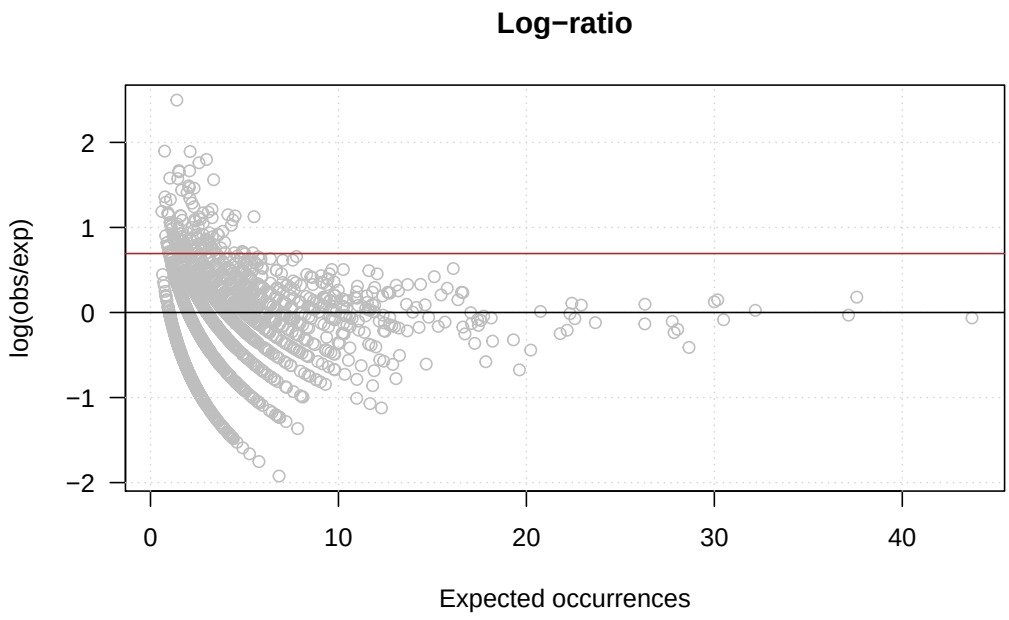


Figure 3: **Scatter plot of observed versus expected occurrences.** The black diagonal corresponds to the null hypothesis, the brown line denotes an arbitrary threshold on fold-change > 2.

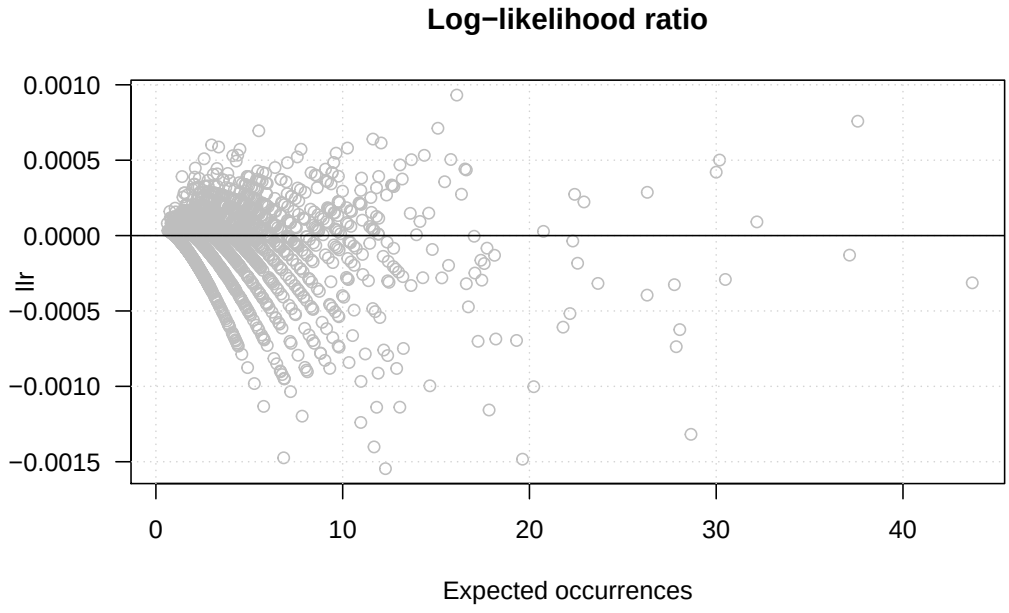


Figure 4: **Scatter plot of log-likelihood ratio (llr) versus expected occurrences.** The black line corresponds to the null hypothesis, the brown line denotes an arbitrary threshold on fold-change > 2.

```
# abline(h =  log(2), col = "brown")
```

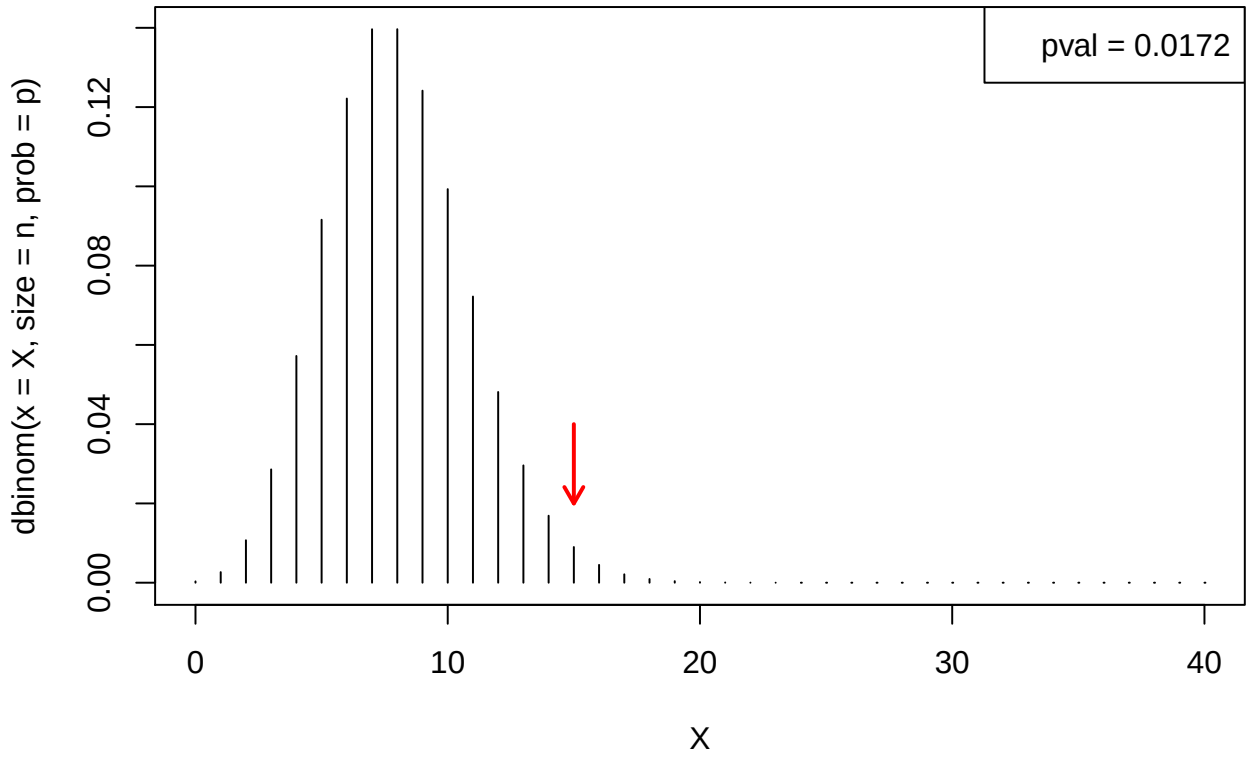
Computing over-representation significance

8. Draw a binomial distribution with parameters $n = 8000$, $p = 0.0001$.

```
n <- 8000
p <- 0.001
x <- 15# Number of successes
X <- 0:40 ## values to display

plot(X, dbinom(x = X, size = n, prob = p), type = "h")
arrows(x, 0.04, x, 0.02, lwd = 2, length = 0.1, angle = 30, col = "red")


pval <- pbinom(q = x - 1, size = n, prob = p, lower.tail = FALSE)
legend("topright", legend = paste("pval =", signif(digits = 3, pval)))
```



8. Use the binomial distribution to compute the P-value of the observed occurrences.

$$P = T(X \geq x)$$

```
x <- oligo.table$obs_freq ## Nuumber of successes
n <- sum(x)   ## Number of trials
p <- oligo.table$exp_freq ## Success probability
```

9. Draw an histogram with the P-values of all hexanucleotides, with 20 bins.

10. Draw a scatter plot with the P-value (Y) as a function of the log-ratio (X).

11. Compute the E-value, and the significance.

$$E = P \cdot N$$

$$sig = -log_{10}(E)$$

12. Draw a **Volcano plot**, with the significance as a function of the log-ratio.

13. Compute the P-value using the Poisson distribution as approximation of the binomial. Are we in suitable conditions for this approximation ? Draw a plot comparing the P-values obtained by the binomial and Poisson distributions.

14. Compute the P-value using a normal approximation of the binomial distribution.

    a. Are we in suitable conditions to approximate a binomial with a normal ?
    b. Compare the P-values obtained with the binomial and norma distrinbutions, resp.