

Exam ID: 11511

# of Questions: 15

Question #: 1

**Relational algebra [2 mark]**

Given two relational algebra expression  $E_1$  and  $E_2$ , we use the notation  $E_1 = E_2$  to indicate that the two expressions are equivalent.

Consider 5 equivalences below:

Equivalence 1	$\sigma_C(E_1 - E_2) = \sigma_C(E_1) - E_2$
Equivalence 2	$\pi_A(\pi_B(E)) = \pi_A(E)$
Equivalence 3	$\sigma_{C_1}(E_1 \bowtie_{C_2} E_2) = \sigma_{C_2}(E_1 \bowtie_{C_1} E_2)$
Equivalence 4	$(E_1 \bowtie_{C_1} E_2) \bowtie_{C_2 \wedge C_3} E_3 = E_1 \bowtie_{C_1 \wedge C_2} (E_2 \bowtie_{C_3} E_3)$
Equivalence 5	$(E_1 \bowtie E_2) \bowtie E_3 = E_1 \bowtie (E_2 \bowtie E_3)$

Which of the equivalences are true?

- A. Equivalence 1
- B. Equivalence 2
- C. Equivalence 3
- D. Equivalence 4
- E. Equivalence 5
- F. None of the above

Item Weight: 2.0

Question #: 2

**Relational algebra [2 mark]**

Consider the following relational database where the domain of each attribute is integer:

- R1 (a, b, c)
- R2 (c, d, e)
- R3 (e, f, g)

Consider the following SQL query:

```
WITH cte AS (  
  SELECT c, e FROM R1 NATURAL JOIN R2 NATURAL JOIN R3  
)  
SELECT DISTINCT c FROM cte  
WHERE e NOT IN ( SELECT e FROM R3 WHERE e >30 );
```

Consider the following four relational algebra expression below:

E1	$\pi_c(\pi_{c,e}(R1 \bowtie R2 \bowtie R3) \cup \pi_{c,e}(\sigma_{e>30}(R1 \bowtie R2 \bowtie R3)))$
E2	$\pi_c(R1 \bowtie R2 \bowtie R3) - \pi_c(\sigma_{e>30}(R1 \bowtie R2 \bowtie R3))$
E3	$\pi_c(\pi_{c,e}(R1 \bowtie R2 \bowtie R3) \cap \pi_{c,e}(\sigma_{e\leq 30}(R1 \bowtie R2 \bowtie R3)))$
E4	$\pi_c(\sigma_{e\leq 30}(R1 \bowtie R2 \bowtie R3))$

Which of the relational algebra expressions are equivalent to the SQL query above assuming that the tables are non-empty?

- A. E1
- B. E2
- C. E3
- D. E4
- E. None of the above

Item Weight: 2.0

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Question #: 3

### SQL queries [2 mark]

Consider the following relational database where the domain of each attribute is integer:

- R1 (a, b, c)
- R2 (c, d, e)
- R3 (e, f, g)

Which of the following queries may contain duplicate entries? All queries are valid queries.

- A. SELECT R1.a, R3.g  
FROM R1, R2, R3  
WHERE R1.c = R2.c AND R2.e = R3.e;

- B. SELECT R1.a, RT.g  
FROM R1, (R2 NATURAL JOIN R3) AS RT  
WHERE RT.c = RT.c;
- C. SELECT R1.a, RT.g  
FROM R1 NATURAL JOIN (R2 NATURAL JOIN R3) AS RT  
WHERE R1.c = RT.c;
- D. SELECT b, g  
FROM R1 NATURAL JOIN R2 NATURAL JOIN R3;
- E. None of the above

Item Weight: 2.0

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Question #: 4

### Functional dependencies [2 mark]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

Which of the following are parts of the prime attribute of R with respect to F?

- R1 (a, b, c)
- R2 (c, d, e)
- R3 (e, f, g)

Which of the following are parts of the prime attributes of R with respect to F?

- A. A
- B. B
- C. C
- D. D
- E. E

Item Weight: 2.0

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Question #: 5

### Functional dependencies [2 mark]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

Write down all the keys of R. You simply need to write the attributes (in uppercase) for each key without the comma. You may leave any spot blank if you feel that there are fewer than 5 keys.

The set of keys are:  $\{\{ \underline{\hspace{1cm}} 1 \}, \{ \underline{\hspace{1cm}} 2 \}, \{ \underline{\hspace{1cm}} 3 \}, \{ \underline{\hspace{1cm}} 4 \}, \{ \underline{\hspace{1cm}} 5 \}\}$

1.
2.
3.
4.
5.

Item Weight: 2.0

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Question #: 6

### Minimal cover [2 mark]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

Compute one possible minimal cover of  $F$  with respect to  $R$ . You are limited to only up to five functional dependencies in your minimal cover.

One possible minimal cover is  $G = \{ \underline{\hspace{1cm}} 1 \rightarrow \underline{\hspace{1cm}} 2, \underline{\hspace{1cm}} 3 \rightarrow \underline{\hspace{1cm}} 4, \underline{\hspace{1cm}} 5 \rightarrow \underline{\hspace{1cm}} 6, \underline{\hspace{1cm}} 7 \rightarrow \underline{\hspace{1cm}} 8, \underline{\hspace{1cm}} 9 \rightarrow \underline{\hspace{1cm}} 10 \}$

1.
2.
3.
4.
5.
6.
7.
8.
9.
10.

Item Weight: 2.0

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Question #: 7

### Armstrong's axioms [5 mark]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

Using extended Armstrong's axioms, fill in the steps to show that  $F \models CD \rightarrow ABCDE$ . You are limited to only up to five steps in the proof including the use of [Given] if necessary. Use the following example usage for your reasoning:

A  $\rightarrow$  B [Given]

B  $\rightarrow$  C [Given]

AB  $\rightarrow$  B [Reflexivity]

AC  $\rightarrow$  BC [Augmentation (1) with C]

A  $\rightarrow$  C [Transitivity (1) and (2)]

AC  $\rightarrow$  B [Decomposition of (4)]

A  $\rightarrow$  BC [Union (1,5)]

Proof:

<u>1</u>	$\rightarrow$	<u>2</u>	[ <u>3</u> ]
<u>4</u>	$\rightarrow$	<u>5</u>	[ <u>6</u> ]
<u>7</u>	$\rightarrow$	<u>8</u>	[ <u>9</u> ]
<u>10</u>	$\rightarrow$	<u>11</u>	[ <u>12</u> ]
<u>CD <math>\rightarrow</math> ABCDE [ <u>13</u> ]</u>			

1. \_\_\_\_\_
2. \_\_\_\_\_
3. \_\_\_\_\_
4. \_\_\_\_\_
5. \_\_\_\_\_
6. \_\_\_\_\_
7. \_\_\_\_\_
8. \_\_\_\_\_
9. \_\_\_\_\_
10. \_\_\_\_\_
11. \_\_\_\_\_
12. \_\_\_\_\_
13. \_\_\_\_\_

Item Weight: 5.0

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Question #: 8

### Normal forms [2 mark]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

Which of the following functional dependencies are in  $F^+$  and violates 3NF property of R?

- A.  $CE \rightarrow D$
- B.  $AE \rightarrow D$
- C.  $AD \rightarrow E$
- D.  $D \rightarrow AE$
- E.  $DE \rightarrow A$
- F.  $C \rightarrow AB$
- G. None of the above

Item Weight: 2.0

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Question #: 9

### Normal forms [4 marks]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

We consider BCNF to be better than 3NF. Consider a lossless-join and dependency-preserving decomposition that minimizes redundancies using only either Algorithm#6 for BCNF decomposition or Algorithm#7 and Algorithm#2 for 3NF decomposition.

Find the *best lossless-join and dependency-preserving* decomposition achievable by R with respect to F. You are limited to only up to 3 relations in your answer.

The best decomposition is (fill in either BCNF or 3NF) [   1   ]

The decompositions are {  $R1(\underline{\hspace{1cm}} \text{ 2 } \underline{\hspace{1cm}})$ ,  $R2(\underline{\hspace{1cm}} \text{ 3 } \underline{\hspace{1cm}})$ ,  $R3(\underline{\hspace{1cm}} \text{ 4 } \underline{\hspace{1cm}})$  }

- 1.
- 2.
- 3.
- 4.

Item Weight: 4.0

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Question #: 10

### Decomposition [2 mark]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

Which of the following decompositions are lossless-join decomposition?

- A. R1(A,B,C), R2(B,C,D), R3(C,D,E)
- B. R1(A,B,D), R2(A,C,D), R3(B,D,E)
- C. R1(A,B,E), R2(B,C,E), R3(B,D,E)
- D. R1(A,B,E), R2(A,C,D), R3(A,D,E)
- E. R1(A,B,C), R2(B,C,D), R3(C,D,E)
- F. None of the above

Item Weight: 2.0

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Question #: 11

### Decomposition [2 mark]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

Further consider the decomposed schema  $d = \{ R1(A,B,C), R2(B,C,D), R3(C,D,E) \}$ . Which of the following functional dependencies are not preserved by the decomposition?

- A.  $AB \rightarrow C$
- B.  $AC \rightarrow BD$
- C.  $C \rightarrow AB$
- D.  $D \rightarrow AE$
- E.  $BD \rightarrow AC$
- F. None of the above

Item Weight: 2.0

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Question #: 12

### Decomposition and SQL queries [2 mark]

Consider the following schema  $R(A,B,C,D,E)$  with the following set of functional dependencies  $F = \{ AB \rightarrow C, AC \rightarrow BD, C \rightarrow AB, D \rightarrow AE, BD \rightarrow AC \}$ .

Further consider the fragment  $R1(A,B,C)$  and its corresponding  $F_{R1}$ . Which of the following SQL code will correctly create the table corresponding to  $R1$  *that preserves the functional dependencies in  $F_{R1}$*  assuming that all its attributes are in the domain of integer.

- A. CREATE TABLE R1 (  
    A integer NOT NULL,  
    B integer NOT NULL,  
    C integer PRIMARY KEY,  
    UNIQUE (A, B)  
);
- B. CREATE TABLE R1 (  
    A integer,  
    B integer,  
    C integer NOT NULL,  
    PRIMARY KEY (A, B)  
);
- C. CREATE TABLE R1 (  
    A integer,  
    B integer,  
    C integer UNIQUE NOT NULL,  
    UNIQUE (A, B)  
);
- D. CREATE TABLE R1 (  
    A integer UNIQUE NOT NULL,  
    B integer UNQIUE NOT NULL,  
    C integer PRIMARY KEY  
);
- E. CREATE TABLE R1 (  
    A integer,  
    B integer,  
    C integer UNIQUE NOT NULL,  
    PRIMARY KEY (A, B)  
);
- F. None of the above

Item Weight: 2.0

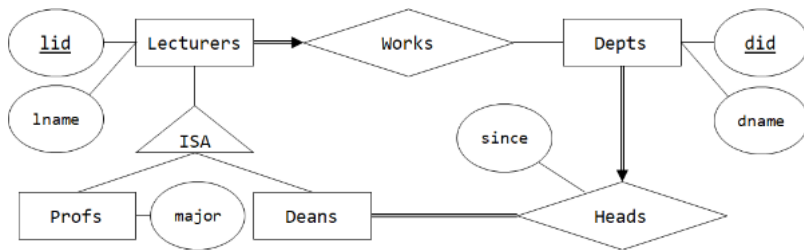
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Question #: 13

### ER diagram [3 mark]

Consider the following ER diagram where the ISA relationship satisfies both covering and overlapping constraints.





Further consider the following relational schema where we assume that all attributes are in integer domain.

```

CREATE TABLE Depts (
  did integer PRIMARY KEY,
  dname integer NOT NULL
);
CREATE TABLE Deans (
  lid integer PRIMARY KEY,
  lname integer NOT NULL,
  did integer NOT NULL REFERENCES Depts (did)
);
CREATE TABLE Profs (
  lid integer PRIMARY KEY,
  lname integer NOT NULL,
  major integer NOT NULL,
  did integer NOT NULL REFERENCES Depts (did)
);
CREATE VIEW Lecturers AS (
  SELECT lid, lname FROM Deans UNION SELECT lid, lname FROM Profs
);
CREATE TABLE Heads (
  lid integer NOT NULL REFERENCES Deans (lid),
  since integer NOT NULL,
  did integer PRIMARY KEY
);
  
```

Select all the statements that are true about the relational schema.

- A. The relational schema enforces key constraint on Lecturers with respect to Works.
- B. The relational schema enforces total participation constraint on Lecturers with respect to Works.

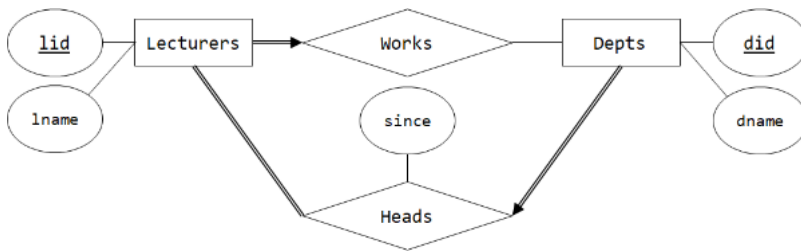
- C. The relational schema enforces key constraint on Depts with respect to Heads.
- D. The relational schema enforces total participation constraint on Depts with respect to Heads.
- E. The relational schema enforces total participation constraint on Deans with respect to Heads.
- F. The relational schema enforces covering constraint of the ISA
- G. The relational schema enforces overlap constraint of the ISA
- H. None of the above

**Item Weight:** 3.0

**Question #:** 14

**ER diagram [3 marks]**

Consider the following ER diagram where the ISA relationship satisfies both covering and overlapping constraints.



Consider the following relations

- Lecturers (lid, lname)
- Depts (did, dname)
- Works (lid, did)
- Heads (lid, did, since)

Further consider the natural join of all relations above (let's call this All (lid, lname, did, dname, since)). Which of the following functional dependencies is induced by the ER diagram on relations All? By induced, we mean the functional dependencies are the result of the ER diagram (i.e., generated by the ER diagram). As an example, the functional dependencies lid  $\rightarrow$  lname and did  $\rightarrow$  dname are both induced due to the primary key on Lecturers and Depts relations respectively.

- A. did -> lname  
B. lid -> dname

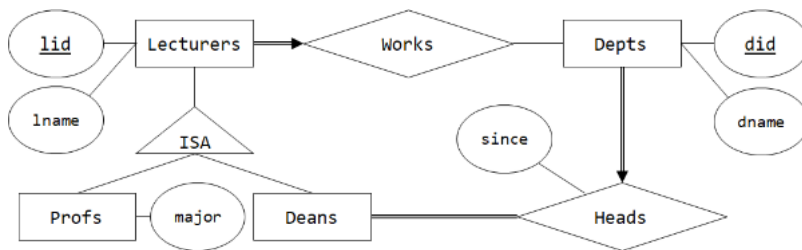
- C. did -> major
- D. lid -> major
- E. did -> since
- F. lid -> since
- G. None of the above

Item Weight: 3.0

Question #: 15

### ER diagram abd SQL query [5 mark]

Consider the following ER diagram where the ISA relationship satisfies both covering and overlapping constraints.



Further consider the following relational schema where we assume that all attributes are in integer domain.

We say that a dean is important if the dean heads a department where either:

- There are at least 20 professors working in the department excluding the dean, or
- There are at least 5 professors with different majors working in the department

Find all the non-important dean. **Your answer should not contain any CTE.**

Answer the question by creating SQL view with the schema shown below:

```
CREATE VIEW qn15(lid, lname) AS (
);
```

Your answer should include the VIEW.

Item Weight: 5.0