

Qn3a.

$F = \{ABC \rightarrow E, BD \rightarrow A, CG \rightarrow B\}$

Since $CG \rightarrow B$

By Axiom of Augmentation,

$CDG \rightarrow BD$ ----- (1)

By Axiom of Transitivity,

Since (1) and $BD \rightarrow A$,

$CDG \rightarrow A$ ----- (2)

By Axiom of Reflexivity and Transitivity,

From (1),

$CDG \rightarrow BD \rightarrow B$ ----- (3)

By Axiom of Reflexivity,

$CDG \rightarrow C$ ----- (4)

$CDGB \rightarrow AB$

From (2), (3), applying union property (proven in lecture notes),

$CDG \rightarrow AB$ ----- (5)

Applying the union property on (4) and (5),

$CDG \rightarrow ABC$ ----- (6)

By Axiom of Transitivity,

From (6) and $ABC \rightarrow E$,

$CDG \rightarrow E$ (proven)

Qn3b.

$\{CDG\}^+ = \{ABCDGE\}$

Qn3c

$\text{Keys}(R) = \{CDG\}$