

## 5.2 Generators (cont)

Friday, 11 February 2022 3:46 PM

### ★ Control of Real Power

Assumption

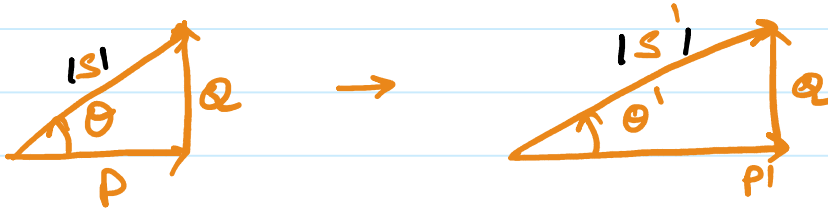
-  $|E|$  and  $|V|$  are unchanged

Changing the mech power input  
→ changes the power angle  $\delta$

→ change in current and power factor

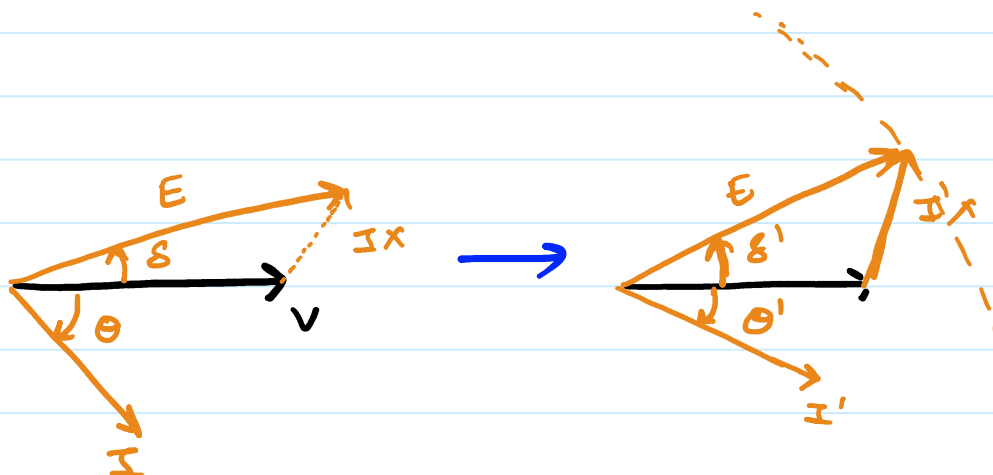
★ Changing  $P$ ,  $Q$  is kept unchanged.

$$|S| = |V||I|$$



→ If  $P' > P$  →  $\cos \theta' > \cos \theta$  [P.f. changes]  
or  $\theta' < \theta$

→  $|S'| > S$  →  $I' > I$  [current changes]

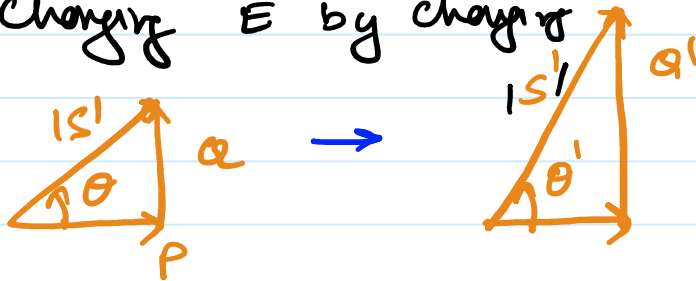


## ★ Control of Reactive power.

Assumption -  $|V|$  and  $\delta$  are unchanged.

$P$  is unchanged  $Q$  is changed.

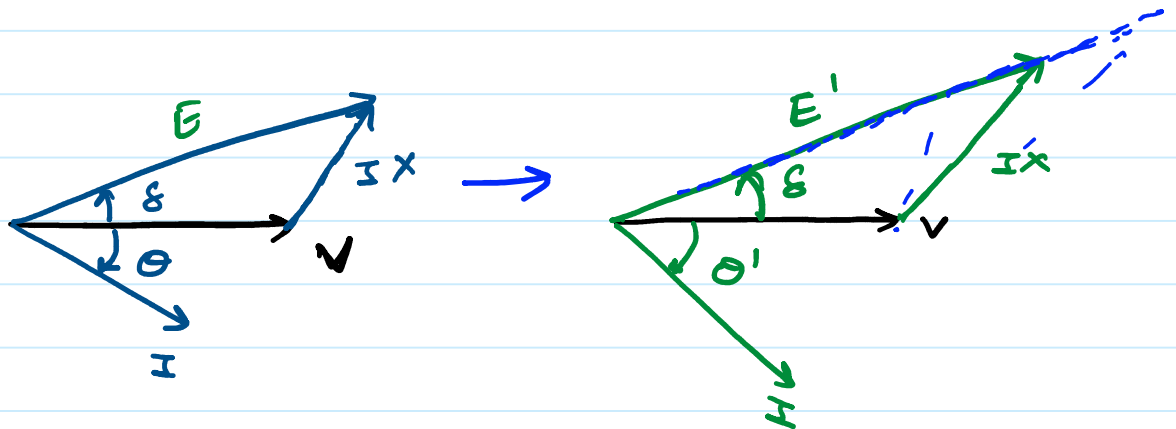
→ Changing  $E$  by changing magnetic field of rotor.



IF  $\theta' > \theta$

$\cos \theta' < \cos \theta$  [P.F. changes]  
 $\theta' > \theta$

→  $|S'| > |S| \rightarrow I' > I$   $\Sigma$  current changes



## ★ Solving Generator

- Find the Armature current from load parameters.
- Find the Excitation voltage  $E$  and power angle  $\delta$

$$E = V + I(R + jX)$$

- IF real power is changed  $\rightarrow P \rightarrow P'$   
 $\rightarrow |E| \dots \dots \dots$

c) IF real power is changed  $\rightarrow P \rightarrow P'$   
 $\rightarrow |E|$  is unchanged.  
 $\rightarrow$  New power angle  
 $- P' = \frac{3|V||E|}{|X|} \sin \delta'$

d) IF reactive power is changed  $\rightarrow Q \rightarrow Q'$   
 $\rightarrow \delta$  is unchanged  
 $\rightarrow$  New  $|E|$   
 $- Q' = \frac{3|V||E'|}{|X|} \cos \delta - \frac{3|V|^2}{|X|}$

e) Find new armature current  $I'$  and new power factor ' $\cos \theta'$ '

$$E' = V + I'(R + jX)$$

$$I' = \frac{E' - V}{R + jX}$$

(eg) 50 MVA, 30 kV, 3 $\phi$ , Wye, 60 Hz.  
 $X_s = j9 \Omega$ ,  $R = 0 \Omega$ .

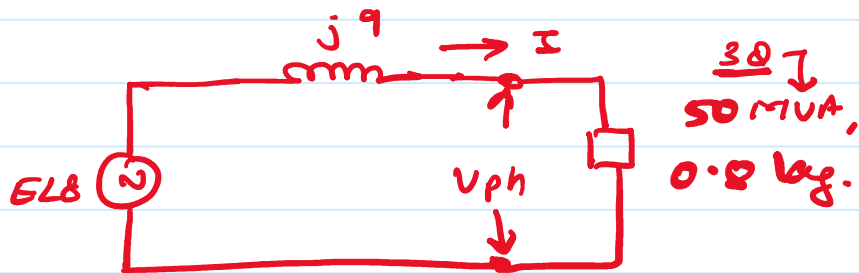
$\rightarrow$  Rated power @ 0.8 p.f. lagging.  
 $\rightarrow$  Rated terminal voltage.

$\rightarrow |S_{load}| = 50 \text{ MVA.}$   
 $\cos \theta = 0.8 \text{ lagging.}$

$V_{rms} = 30 \text{ kV}$

$$V_{line} = 30 \text{ kV}$$

$$V_{ph} = \frac{30 \text{ kV}}{\sqrt{3}} = \frac{30 \times 10^3}{\sqrt{3}} \angle 0^\circ$$



$$|S_{3\phi}| = 3 |V_{ph}| |I_{ph}|$$

$$|I_{ph}| = \frac{50 \times 10^6}{3 \times \frac{30 \times 10^3}{\sqrt{3}}} = 962.25 \text{ A.}$$

$$\theta = 36.87^\circ$$

$$a) I_{ph} = 962.25 \angle -36.87^\circ \text{ A}$$

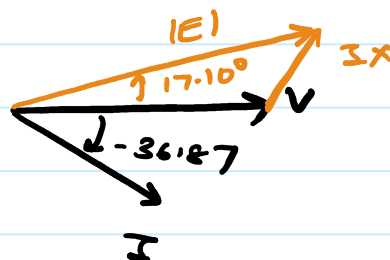
$$b) E = V + I(jX)$$

$$= \frac{30 \times 10^3}{\sqrt{3}} \angle 0^\circ + 962.25 \angle -36.87^\circ (j9)$$

$$= 23558 \angle 17.10^\circ \text{ V}$$

$$|E| = 23.558 \text{ kV}$$

$$\delta = 17.10^\circ$$



→  $|E|$  constant → Reduce torque

$$P' = 25 \text{ MW}$$

$$= \frac{3 |V| |E| \sin \delta'}{|X|}$$

$$25 \times 10^3 = \frac{3 \times \frac{30 \times 10^3}{\sqrt{3}} \times 23558}{9} \sin \delta'$$

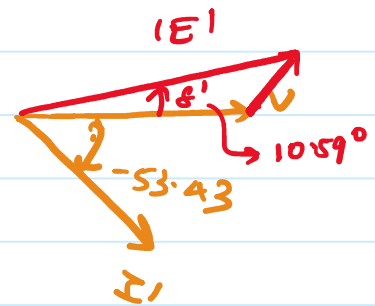
$$\sin \delta' = 0.1838 \rightarrow \delta' = 10.59^\circ$$

$$\rightarrow I' = \frac{E - V}{jX}$$

$$= \frac{|E| \angle \delta' - |V| \angle 0}{jX}$$

$$= \frac{23558 \angle 10.59 - \frac{30 \times 10^3}{\sqrt{3}} \angle 0^\circ}{j9}$$

$$= 807.46 \angle -53.43^\circ \text{ A}$$



$$|I'| = 807.46 \text{ A}$$

$$\cos \theta' = 0.596 \text{ lagging.}$$

$\rightarrow |E|$  is unchanged  $\rightarrow P_{\text{man.}}$

$$P = \frac{3 |V| |E| \sin \delta}{|X|}$$

$$\text{If } \delta = 90^\circ \quad P = P_{\text{man.}}$$

$$P_{\text{man}} = \frac{3 \times \frac{30 \times 10^3}{\sqrt{3}} \times 23558}{9} \times \sin 90$$

$$= 136.02 \text{ MW}$$