



EE2029 - Introduction to Electrical Energy Systems

Transmission Lines

Physical Components
Line Parameters
Line Modelling
Line Operations

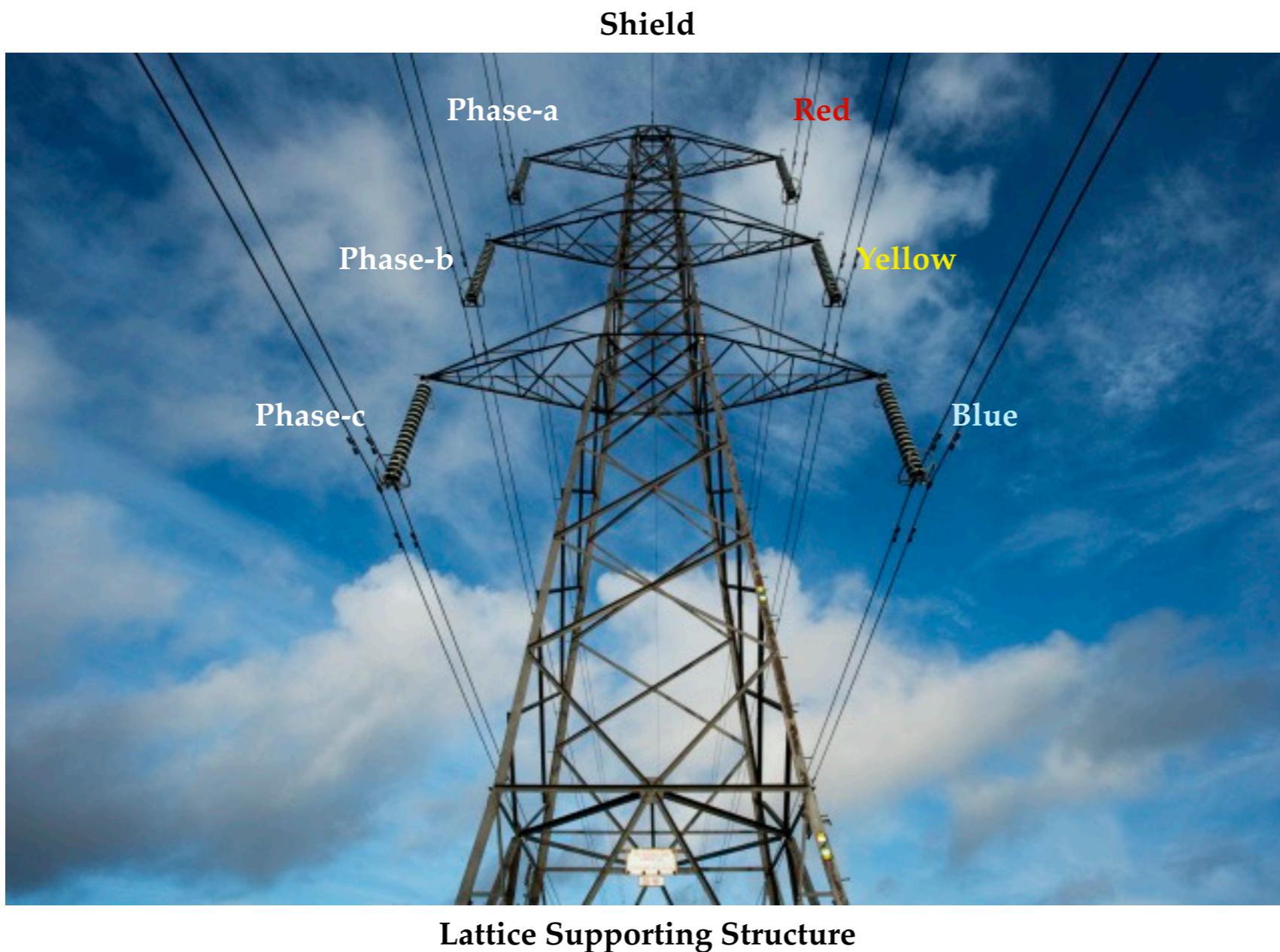
Learning Outcomes

- Able to *identify* the physical components facilitating an overhead line and underground cable.
- Able to *derive* the equivalent circuits for short and medium transmission lines.
- Able to *apply* the principles of voltage regulation and systematically *solve* the transmission efficiency of power lines.

Physical Components

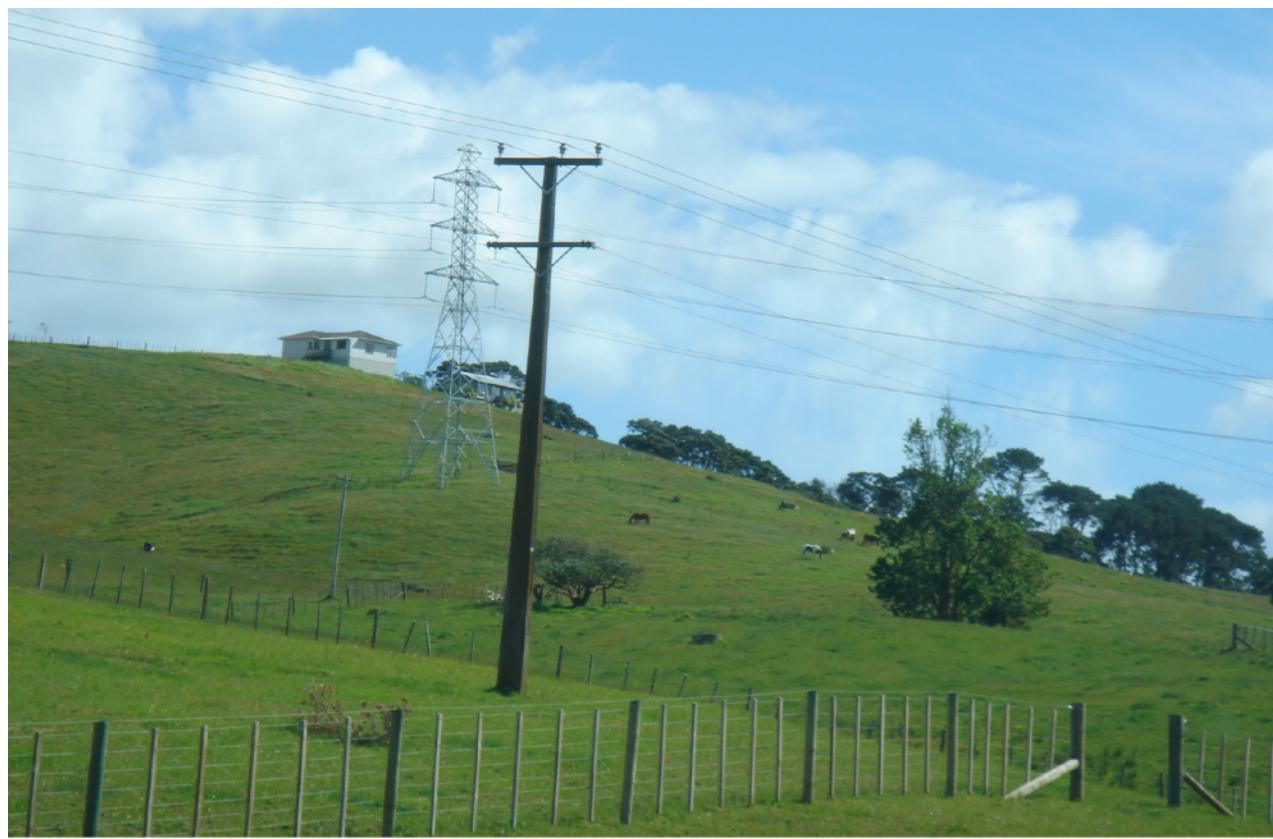
Transmission Lines

Overhead transmission infrastructure consists of **conductors**, **insulators**, **spacers**, and **supporting structure**.



Spacer - Triangular Arrangement

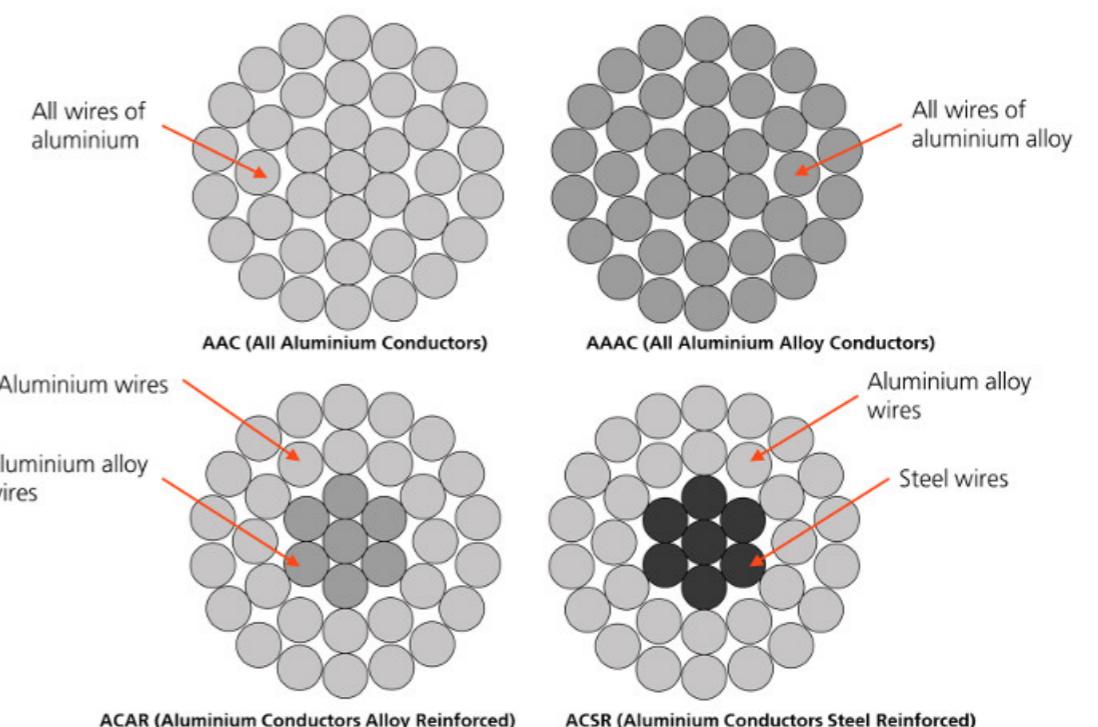




New Zealand, November 2005

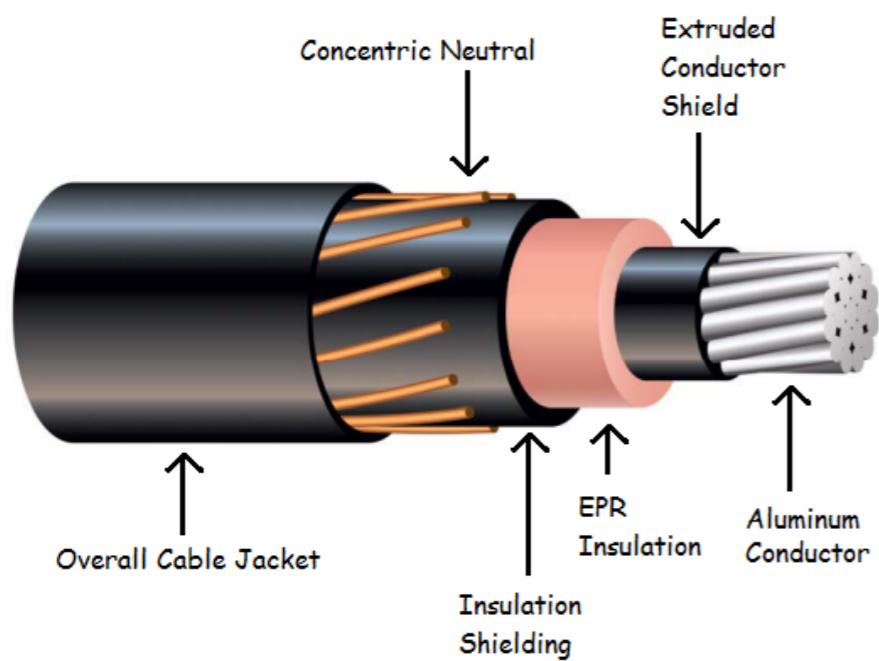
Overhead Lines

- Conductors for HV Lines are:
 - ACSR: Aluminium Conductor Steel Reinforced
 - AAC: All Aluminium Conductors
 - AAAC: All Aluminium-Alloy Conductors
 - ACAR: Aluminium Conductor Alloy Reinforced
- Each phase is usually bundled with more than one conductors using spacers.

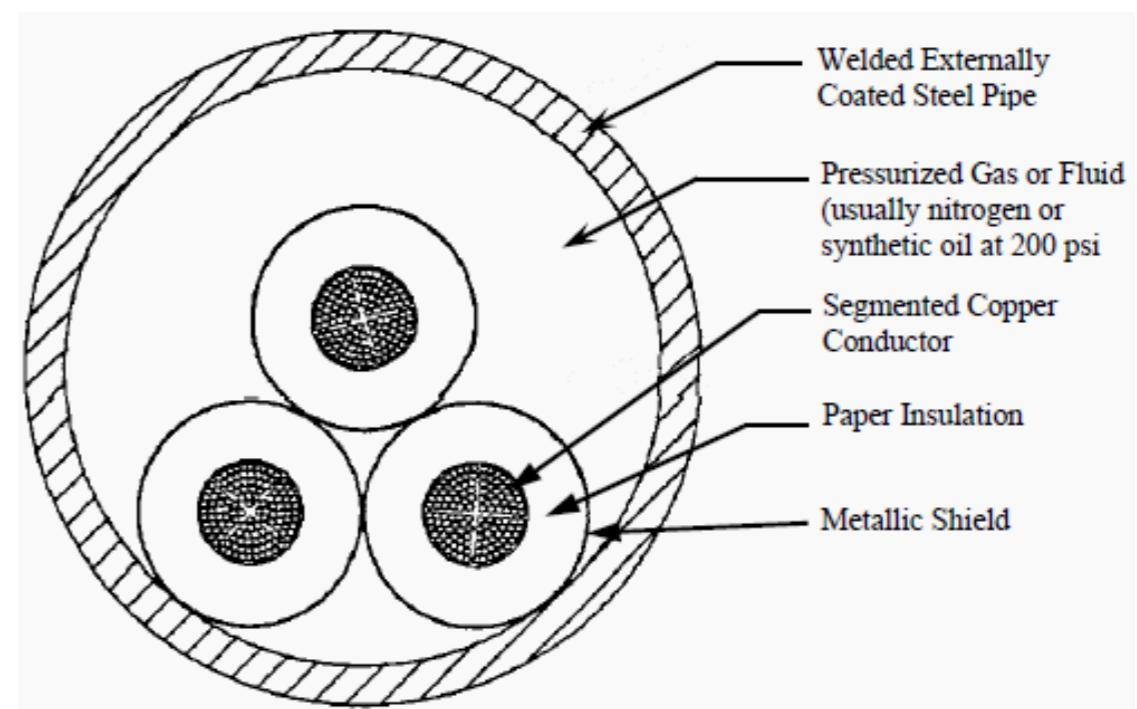
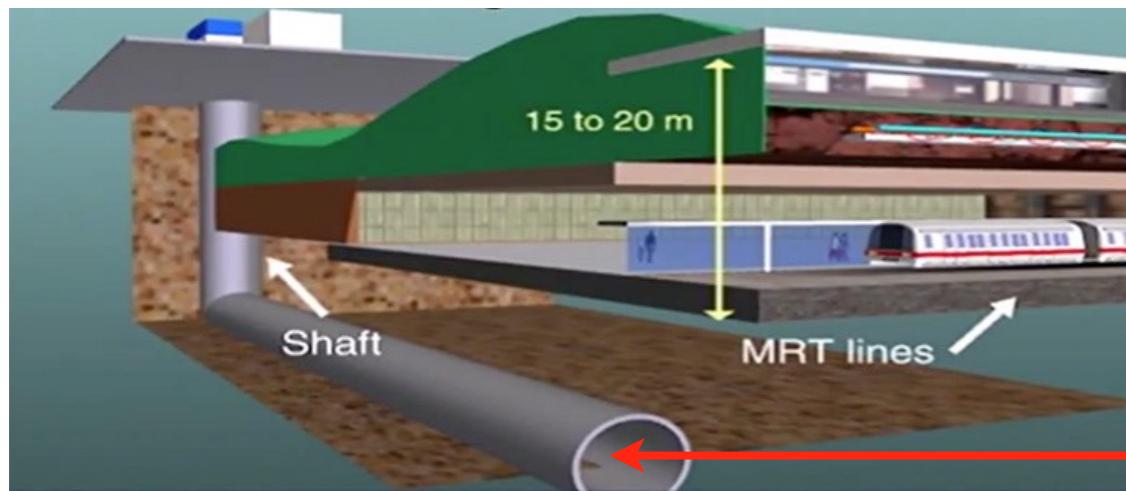


Underground Cables

- Conductors inside a cable must be insulated from the ground.



Self-contained cable



Pipe-Type cable



Types of Cable Insulation

Three main types of insulation:

1. Plastic insulation

- Solid cable, cross-linked polyethylene (XLPE)

2. Paper-Oil insulation

- High-pressure, fluid-filled pipe (HPFF)
- Self-contained fluid-filled (SCFF)

3. Paper-Gas insulation

- High-pressure, gas-filled pipe (HPGF)

- 1) High insulation resistance
-> avoid leakage current
- 2) High dielectric strength
-> avoid breakdown of cable
- 3) Should not absorb moisture from environment
-> avoid reduced lifespan

Overhead/Underground Comparison

Overhead Lines

- Lower construction cost and cable cost.
- Advantage of air for cooling and insulation of the line.
- Vulnerable to strong wind and severe weather.
- Negative visual impact.
- Easier maintenance work.
- Inductive in nature.

Underground Cables

- Expensive pipe work and cable cost.
- Expensive insulation required at high voltage.
- Immune to the severe weather because it is buried underground.
- Environment and aesthetic advantage.
- Less frequent maintenance work.
- Capacitive in nature.

Line Parameters

Resistance (R) and Conductance (G)

Resistance

$R = \text{work done} = \text{energy conversion \& consumption (heat dissipation)}$

- Responsible for transmission line loss.
- Voltage drop along the line from resistive loss can be represented by a resistor along the line.

Conductance $G = 1/R$

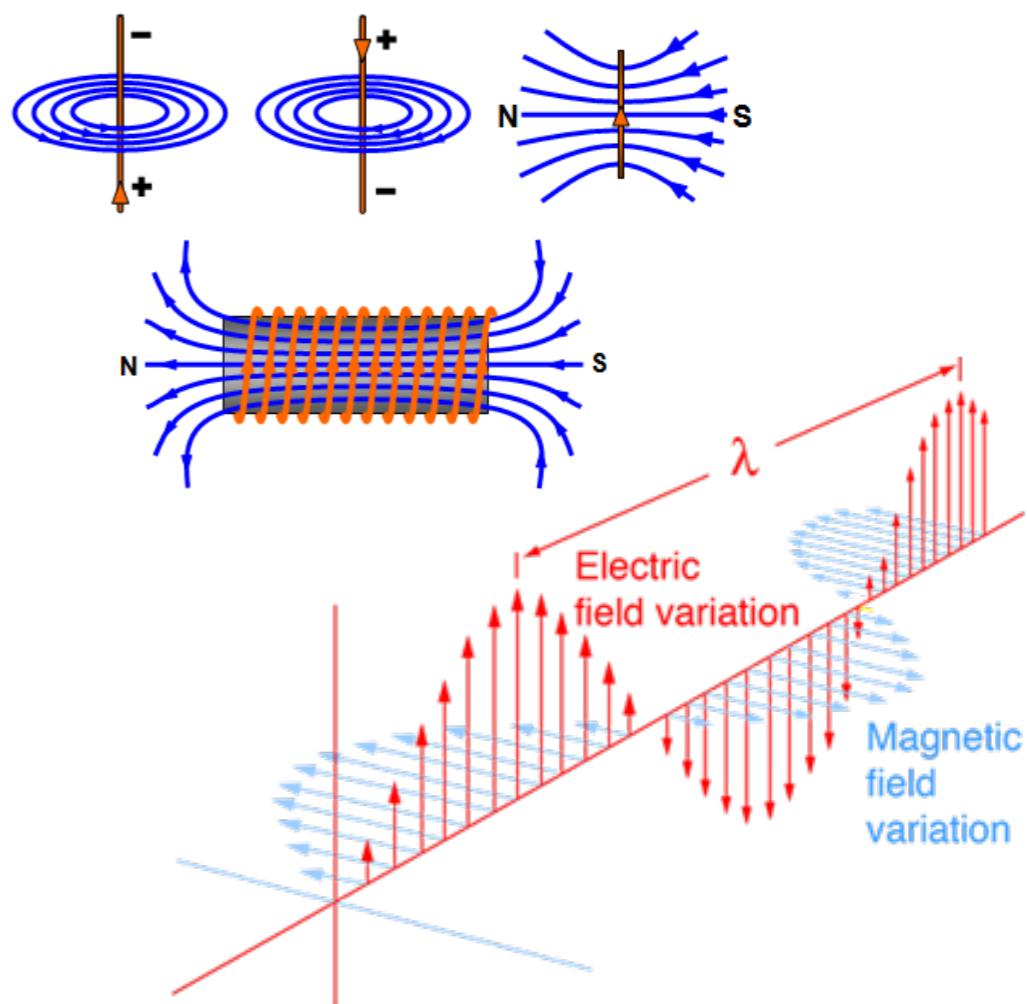
- Leakage current through insulators can be represented by a conductance from a line to the ground.
- Corona Discharge:
 - When the electric field strength is strong, air might become electrically ionised and conduct.
 - This is called a 'corona' effect and can be represented by a conductor from the line to the ground.
 - The power loss due to this effect is call corona loss.

Inductance (L) and Capacitance (C)

Ampere's Law

- Current passing through a conductor creates magnetic field around it.
- This gives inductance property.

inductors store energy in B fields
-> current leads voltage



Gauss's Law

- Electric charge is a source of electric field.
- This gives capacitance property.

capacitors store energy in E fields
-> current lags voltage

Transmission Line Parameters

- **R** from heat
 - Types, sizes of conductor determine resistance value.
- **G** from leakage current
 - Types, number of insulators determine conductance value.
- L from magnetic field
- C from electric field

All these values can be quantified!

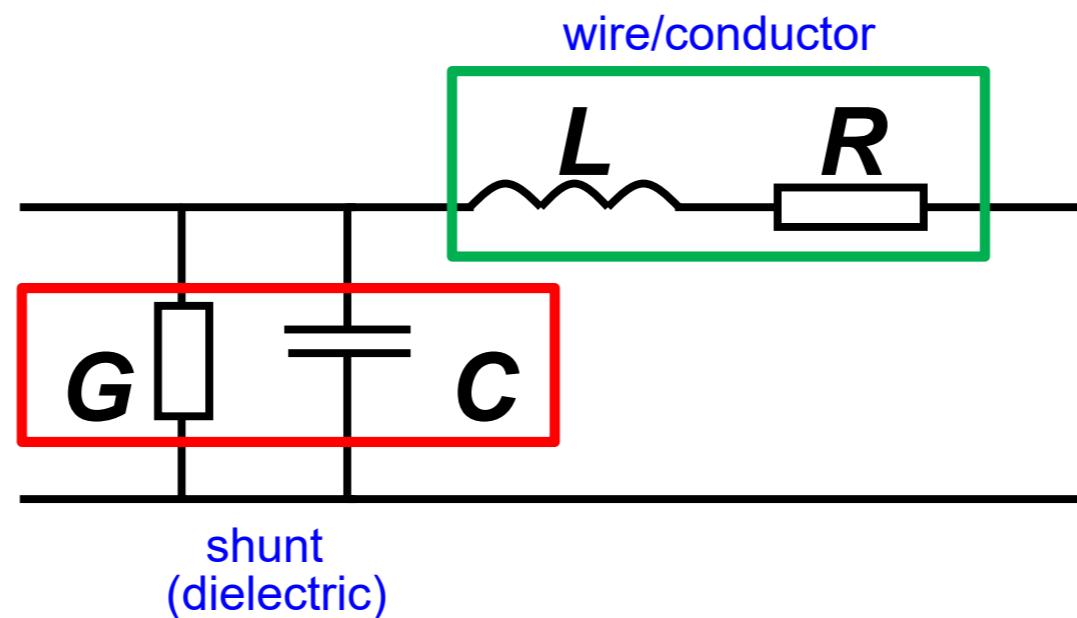
Per Phase Conductor Model

$R : \Omega / km$

$L : H / km$

$G : S / km$

$C : F / km$



$$Z_{series} = R + j\omega L$$

$$Y_{shunt} = G + j\omega C$$

- Per-phase conductor model to describe the circuit model of each phase in three-phase circuit.
- This information will be used to derive an equivalent circuit of the transmission line.

150 kV Line/Cable Parameters

Overhead Transmission Line

- $R = 0.125 \Omega/\text{km}$
- $X_L = 0.425 \Omega/\text{km}$
- $X_C = 7.7 \text{ nF/km}$ (due to Corona discharge & leakage current)
- 130 MVA rating

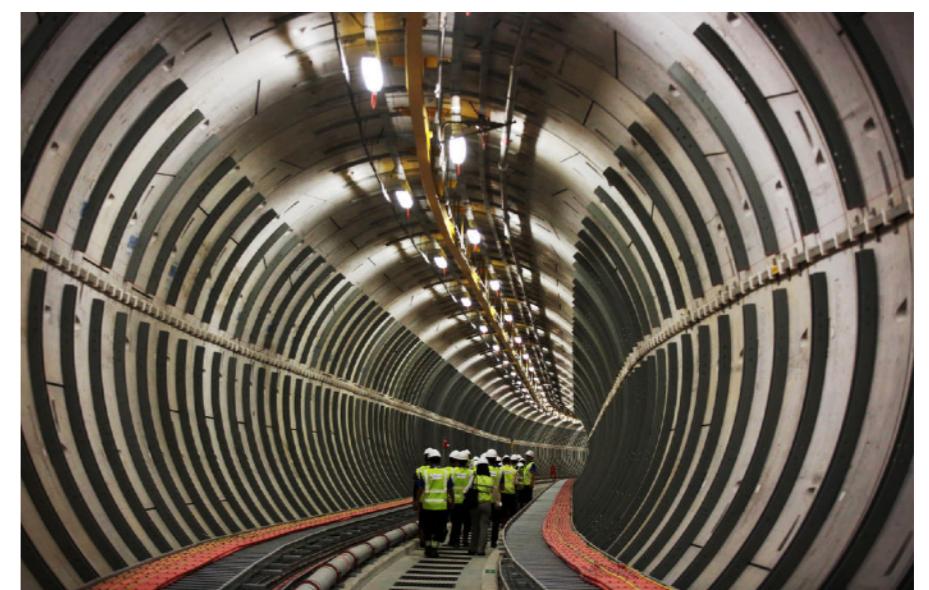
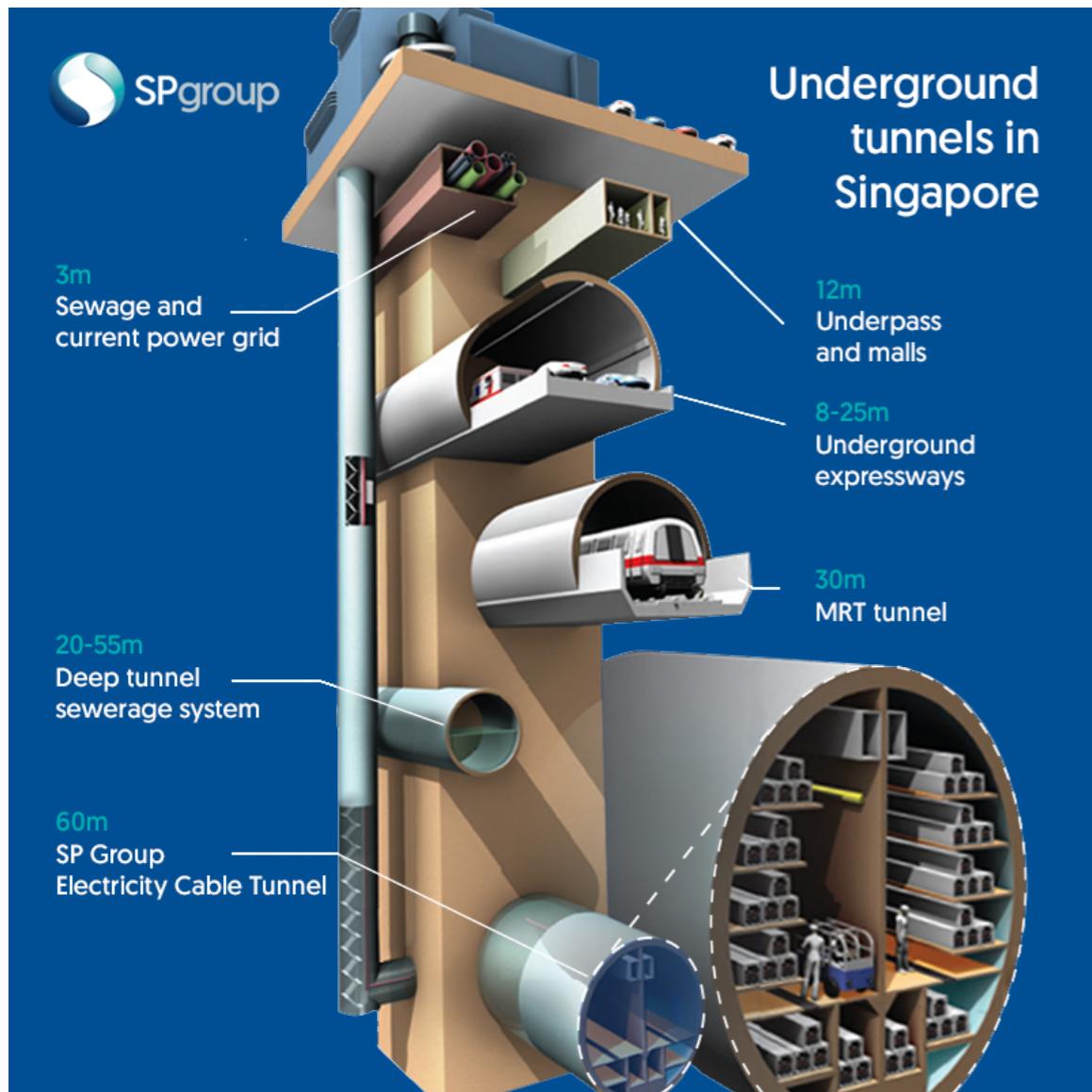
more inductive

Underground Cable

- $R = 0.12 \Omega/\text{km}$
- $X_L = 0.166 \Omega/\text{km}$
- $X_C = 210 \text{ nF/km}$
- 135 MVA rating

more conductive

Singapore 400kV Upgrade (2018)



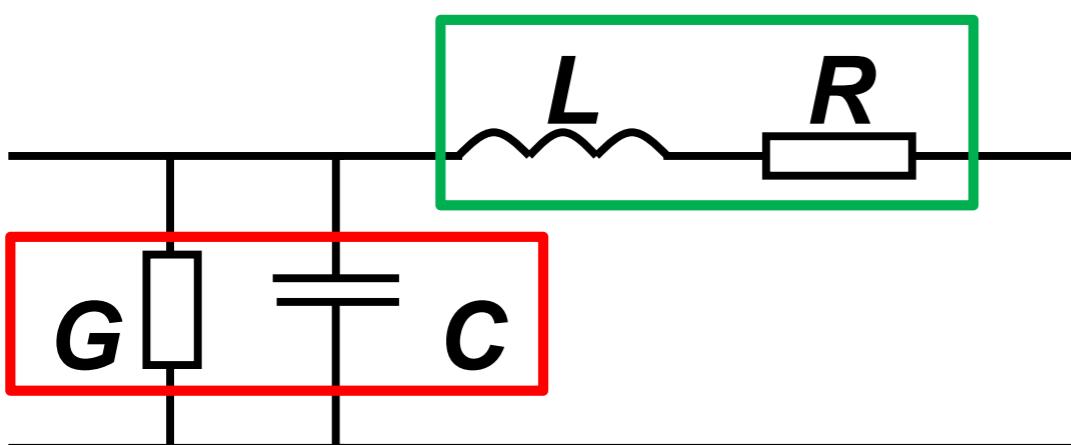
Line Modelling

Per-Phase Conductor Model

- **R** for resistive loss in the conductor
- **G** for leakage current through insulators and corona losses
- **L** to represent magnetic field
- **C** to represent electric field

Q

stores energy
-> charge/discharge over time

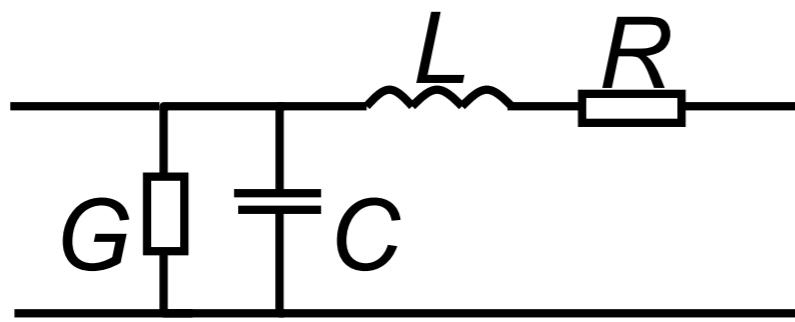


$$Z_{series} = R + j\omega L \Rightarrow \text{Series Impedance } (\Omega / m)$$

$$Y_{shunt} = G + j\omega C \Rightarrow \text{Shunt Admittance } (S / m)$$

Equivalent Circuit (Matrix Representation)

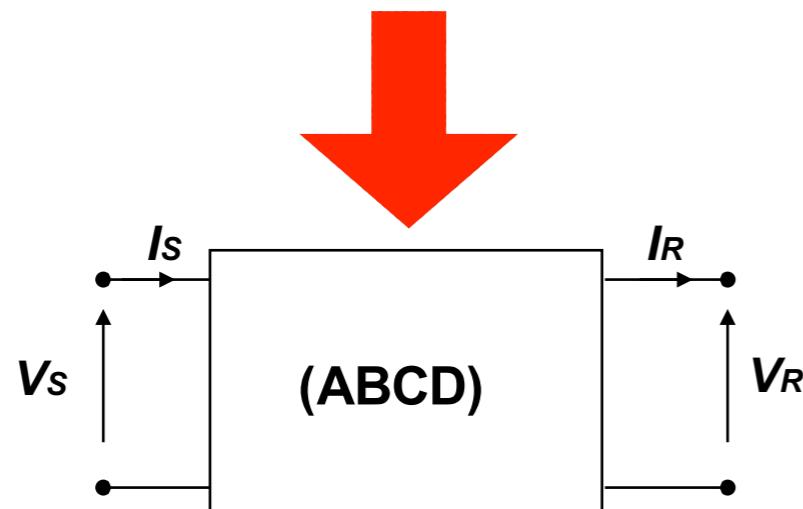
Conductor per-phase model



$$V \text{ sending-end} = V \text{ receiving-end} + V \text{ drop}$$

$$V_S = \mathbf{A}V_R + \mathbf{B}I_R$$

$$I_S = \mathbf{C}V_R + \mathbf{D}I_R$$



Two-port network model

$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{C} & \mathbf{D} \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

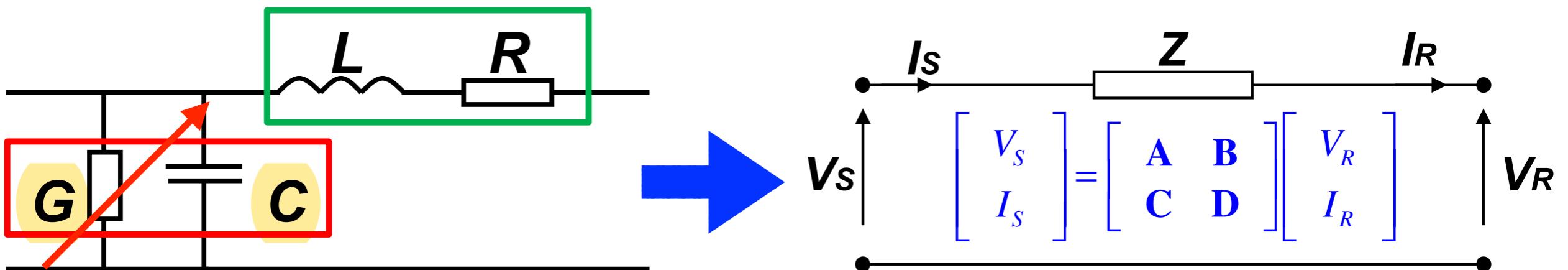
state space model of TL

Purposes of Equivalent Circuit

- To calculate the voltage at the receiving-end when the sending-end voltage is known or vice versa.
 - This is used to find the voltage difference between sending- and receiving-end.
- To find the amount of real and reactive power transfer in the line.
- To make sure the transferred power does not exceed the heating limit of the lines.
- To calculate the efficiency of the transmission line.

Short Line: A Simplified Model

- We ignore the shunt admittance and only consider series impedance.



$$V_s = V_R + I_R \cdot Z = 1 \cdot V_R + Z \cdot I_R$$

$$I_s = I_R = 0 \cdot V_R + 1 \cdot I_R$$

$$\begin{aligned} D &= 1 \\ C &= 0 \end{aligned}$$

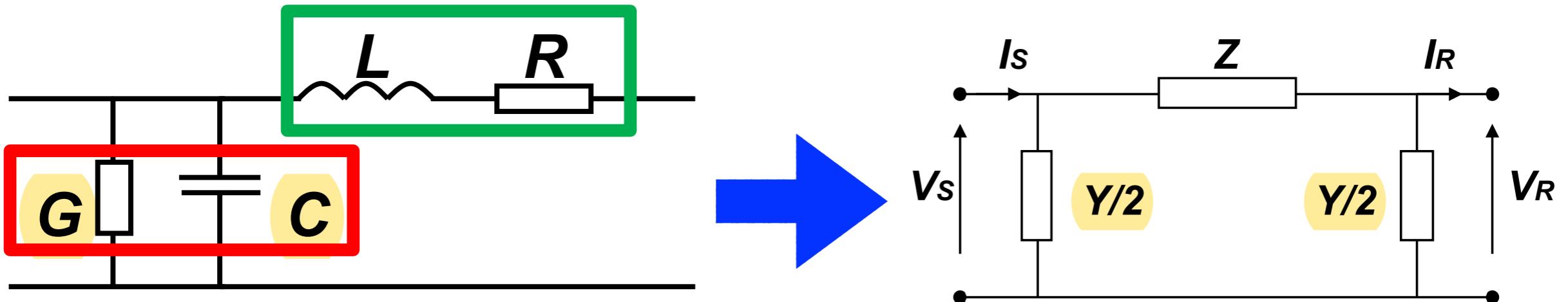
$$\begin{aligned} A &= 1 \\ B &= Z \end{aligned}$$

Example

A single-phase 50 km transmission line is supplying 8 kV to an 800 kVA, 0.9 PF lagging single-phase load. Line impedance Z is $1+j1 \Omega$. What is the sending end voltage and current of this transmission line?

Medium Line: A Lumped Model

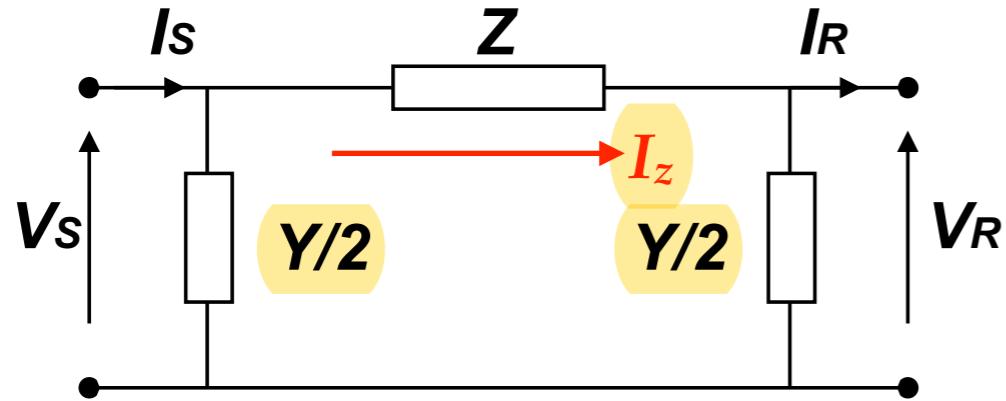
- Also known as the **nominal π -circuit**.



$$Z = R + j\omega L$$

$$Y = G + j\omega C$$

Medium Line: A Lumped Model



$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} \frac{ZY}{2} + 1 \\ Y \left(1 + \frac{ZY}{4} \right) \end{bmatrix} \frac{Z}{2} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\begin{aligned} \text{KVL: } V_S &= V_R + Z \cdot I_Z \\ &= V_R + Z \cdot \left(I_R + V_R \cdot \frac{Y}{2} \right) \\ &= \left(1 + \frac{YZ}{2} \right) V_R + Z \cdot I_R \end{aligned}$$

$$\begin{aligned} \text{KCL: } I_S &= I_Z + V_S \cdot \frac{Y}{2} \\ &= I_R + V_R \cdot \frac{Y}{2} + \left[\left(1 + \frac{YZ}{2} \right) V_R + Z \cdot I_R \right] \frac{Y}{2} \\ &= \left[\frac{Y}{2} + \frac{Y}{2} \left(1 + \frac{YZ}{2} \right) \right] V_R + \left(1 + \frac{YZ}{2} \right) I_R \\ &= \left[Y + Y \left(\frac{ZY}{4} \right) \right] V_R + \left(\frac{ZY}{2} + 1 \right) I_R \end{aligned}$$

Equivalent Models: Summary

- Short ($< 80 \text{ km}$)

$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

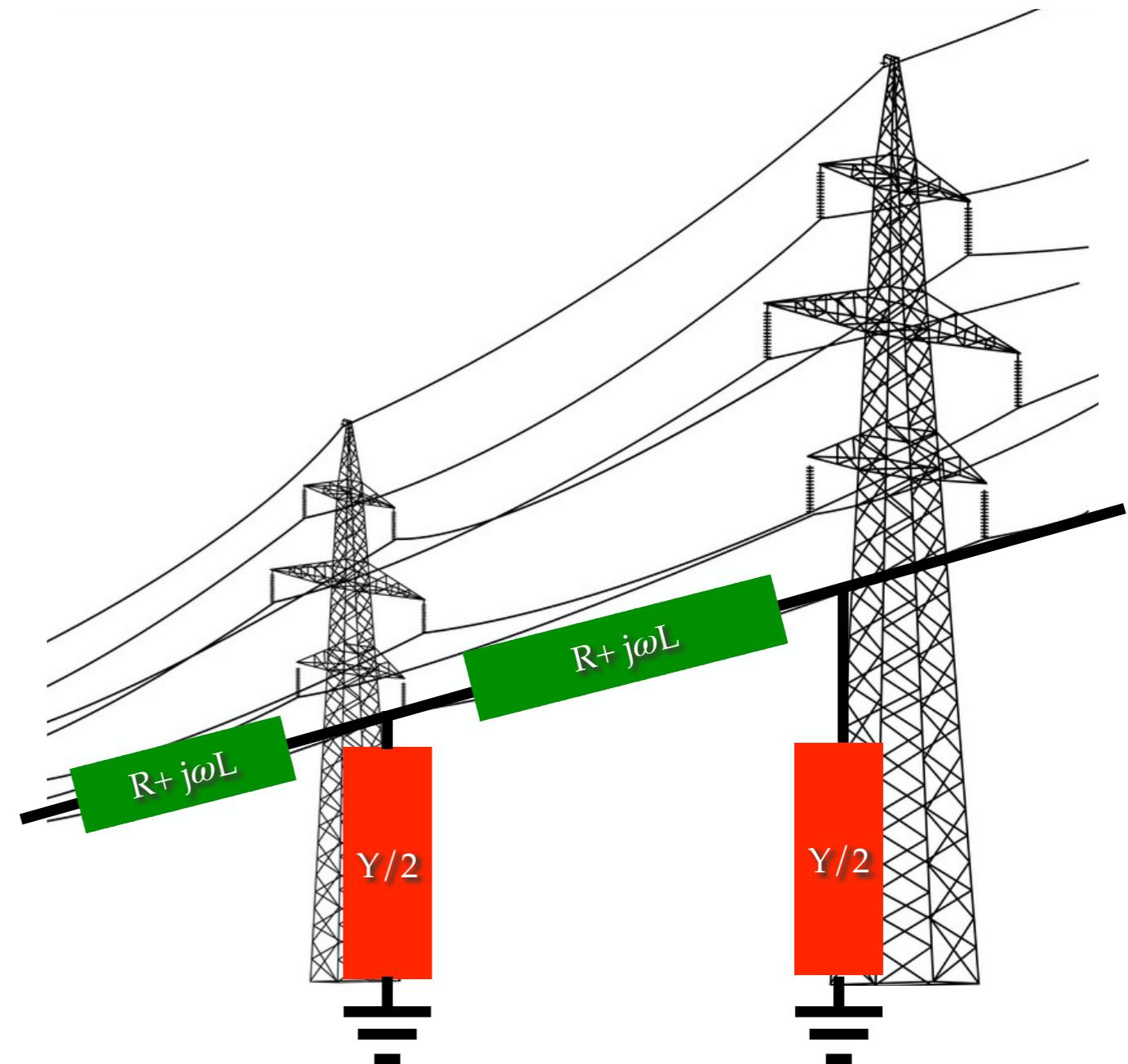
- Medium ($80 \text{ km to } 240 \text{ km}$)

$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} \frac{ZY}{2} + 1 \\ Y \left(1 + \frac{ZY}{4} \right) \end{bmatrix} \begin{bmatrix} Z \\ \frac{ZY}{2} + 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

- Long ($> 240 \text{ km}$) *X in syllabus.*

$$\cancel{X} \quad \begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} \cosh(\gamma l) & Z_c \sinh(\gamma l) \\ \frac{\sinh(\gamma l)}{Z_c} & \cosh(\gamma l) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

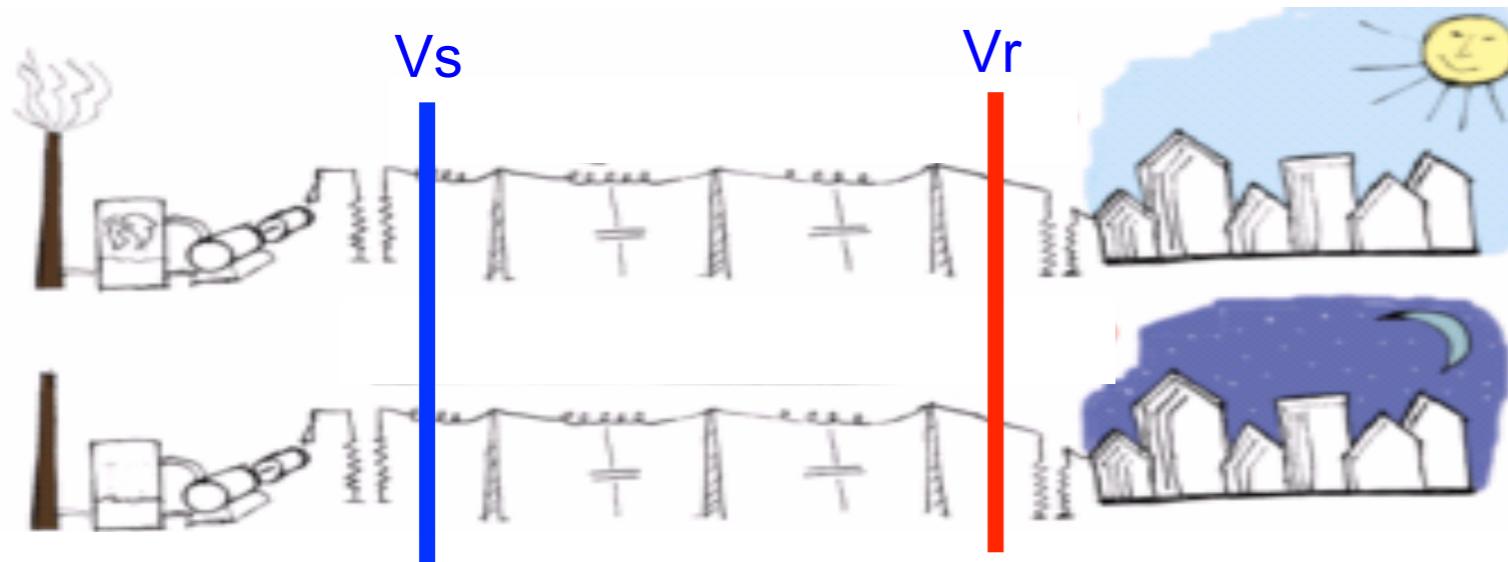
' l ' is the length of the transmission line.



Line Operation

Full Load vs No Load Conditions

To ensure that V_s & V_r are within limits in all conditions!!!



Sending end
generator

Receiving end
consumer/load

Full load condition

No load condition

If the sending-end voltage is kept constant, the receiving-end voltage will vary between full load and no load conditions.

Receiving End Voltage at No Load

$$V_s = \mathbf{A}V_R + \mathbf{B}I_R$$

$$I_S = \mathbf{C}V_R + \mathbf{D}I_R$$

$$\begin{bmatrix} V_s \\ I_S \end{bmatrix} = \begin{bmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{C} & \mathbf{D} \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

Full load condition

$$\begin{bmatrix} V_{S,FL} \\ I_{S,FL} \end{bmatrix} = \begin{bmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{C} & \mathbf{D} \end{bmatrix} \begin{bmatrix} V_{R,FL} \\ I_{R,FL} \end{bmatrix}$$

No load condition

$$\begin{bmatrix} V_{S,NL} \\ I_{S,NL} \end{bmatrix} = \begin{bmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{C} & \mathbf{D} \end{bmatrix} \begin{bmatrix} V_{R,NL} \\ 0 \end{bmatrix}$$

$$V_{S,FL} = A \cdot V_{R,NL}$$

$$|V_{R,NL}| = \left| \frac{V_{S,FL}}{A} \right|$$

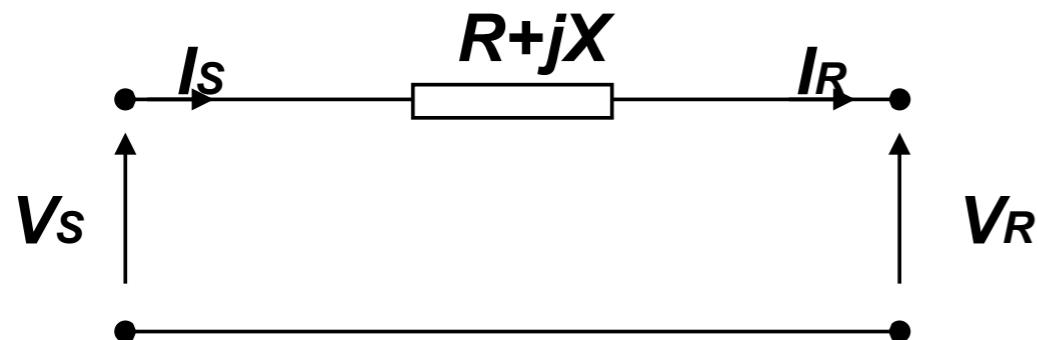
Voltage Regulation

- The variation of line voltage with different loading conditions is called ‘voltage regulation’.
- About 10% voltage change between no load and full load operation is a usual practice for reliable operation.
- Voltage regulation measures the degree of change in voltage when load varies from no-load to full load **at a specific power factor**.

$$\text{Percent Regulation} = \frac{|V_{R,NL}| - |V_{R,FL}|}{|V_{R,FL}|} \times 100\%$$

Voltage Regulation of Short Line

- For simplicity, we consider a short transmission line model.



$$\text{Percent Regulation} = \frac{|V_{R,NL}| - |V_{R,FL}|}{|V_{R,FL}|} \times 100\%$$

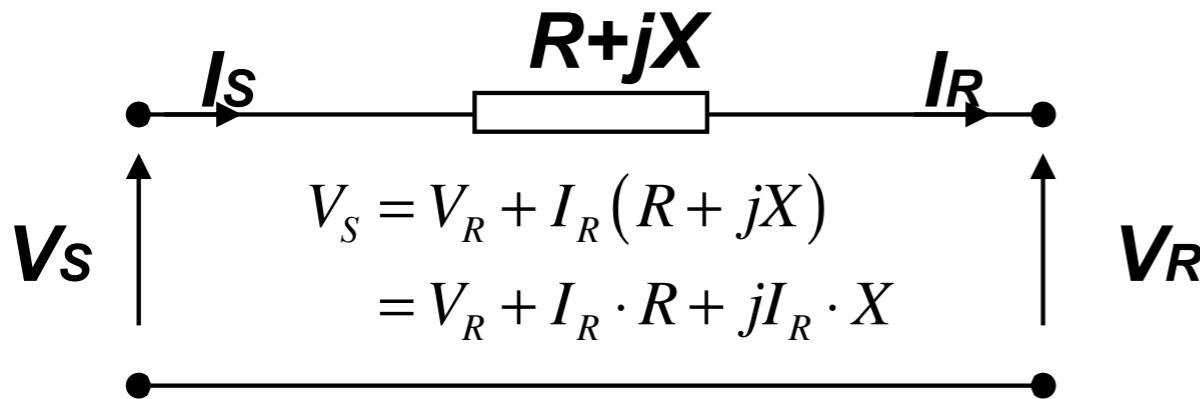
- Note that the receiving end voltage at no load condition is the same as sending end voltage at full load condition.

$$V_{R,NL} = \frac{V_{S,FL}}{A}$$

V_r no-load = V_s !
where $A = 1$, $V_{R,NL} = V_{S,FL}$

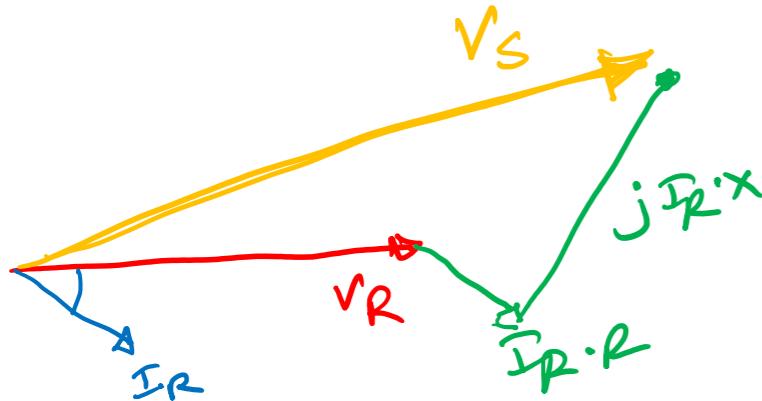
$$\text{Percent Regulation} = \frac{|V_s| / |A| - |V_{R,FL}|}{|V_{R,FL}|} \times 100\%$$

Effect of Power Factor



Percent Regulation = $\frac{|V_{R,NL}| - |V_{R,FL}|}{|V_{R,FL}|} \times 100\%$

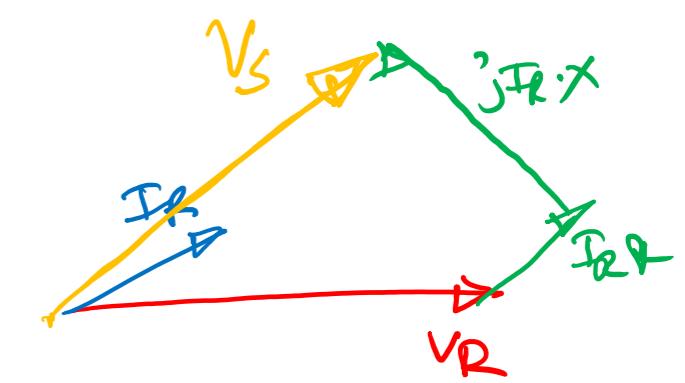
Lagging PF load



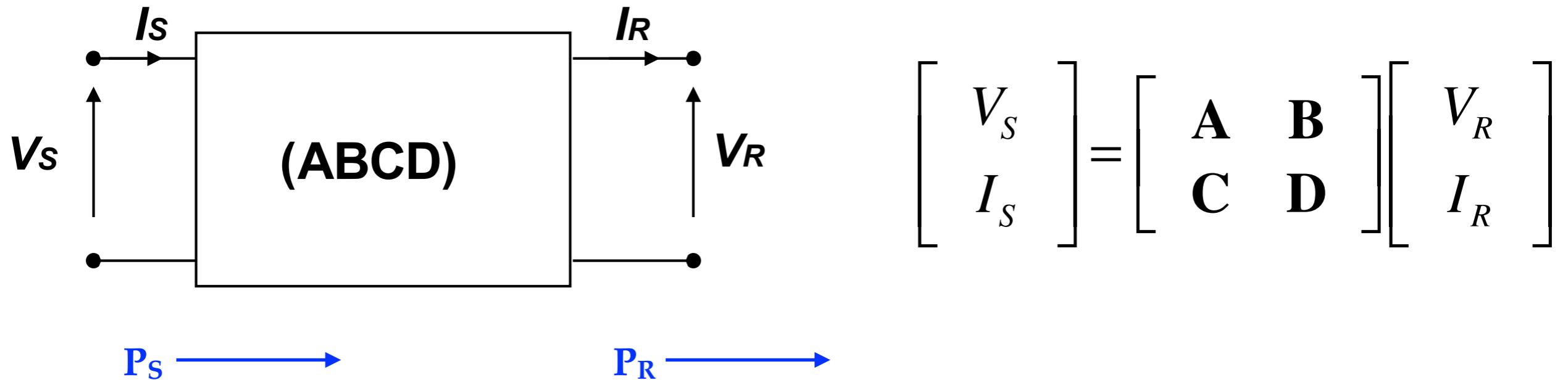
Unity PF load



Leading PF load



Transmission Efficiency



$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

Transmission Efficiency, $\eta = \frac{P_{R,3\phi}}{P_{S,3\phi}} \times 100\% = \frac{3 \times P_{R,1\phi}}{3 \times P_{S,1\phi}} \times 100\%$

Efficiency = Received / Supplied

$$\eta = \frac{\text{Re}(V_R \cdot I_R^*)}{\text{Re}(V_S \cdot I_S^*)} \times 100\%$$