

Goh Kheng Xi Jaren A01998066

Tutorial: transformers

Date

No.

1. $a = \frac{N_1}{N_2} = \frac{V_1}{V_2} = \frac{12740}{240} \approx 53$

2. $Z' = a^2 Z$

$$a = \sqrt{\frac{Z'}{Z}}$$

$$\Rightarrow \frac{N_1}{N_2} = \sqrt{\frac{Z'}{Z}}$$

$$N_2 = N_1 \sqrt{\frac{Z}{Z'}} = 400 \sqrt{\frac{6}{2000}} \approx 22$$

3. i_1 and $i_2 \Rightarrow 180^\circ$ phase difference
 i_2 and $i_3 \Rightarrow 0^\circ$ phase difference

$$Z_2' = a_{2,3}^2 (Z_3) + Z_2 = \left(\frac{1}{2}\right)^2 (8) + 3 = 5 \Omega$$

$$Z_1' = (a_{1,2})^2 (Z_2') + Z_1 = \left(\frac{2}{1}\right)^2 (5) + 5 = 50 \Omega$$

$$i_1 = \frac{200 \angle 90^\circ}{50} = 4 \angle 90^\circ \text{ A}$$

$$i_2 = (a_{1,2}) |i_1| \angle 90^\circ + 180^\circ = \frac{2}{1} (4) \angle 270^\circ = 12 \angle -90^\circ \text{ A}$$

$$i_3 = (a_{2,3}) (i_2) = \frac{1}{2} (12) \angle -90^\circ = 6 \angle -90^\circ \text{ A}$$

4. short-circuit test

Rated apparent power = 33 kVA

$$V_{1, \text{rated}} = 960 \text{ V}$$

$$I_{1, \text{rated}} = \frac{33 \times 10^3}{960} = 34.375 \text{ A}$$

$$Z_{\text{eq}} = \frac{V_{\text{means}}}{I_{1, \text{rated}}} = \frac{63}{34.375} \approx 1.833 \Omega$$

$$R_{\text{eq}} = \frac{P}{I_{1, \text{rated}}^2} = \frac{300}{34.375^2} \approx 0.25 \Omega$$

$$X_{\text{eq}} = \sqrt{Z^2 - R_{\text{eq}}^2} = \sqrt{1.833^2 - 0.25^2} \approx 1.815 \Omega$$

$$Z_{\text{eq}} = 0.25 + j1.815 \Omega$$

Open-circuit test

$$V_{2, \text{rated}} = 120 \text{ V}$$

$$V_{1, \text{rated}} = 960 \text{ V}$$

$$I_2 = 6$$

$$I_1 = 6 \left(\frac{120}{960} \right) = 0.75 \text{ A}$$

$$|Y| = \frac{I_1}{V_{1, \text{rated}}} = \frac{0.75}{960} \approx 0.00078 \text{ S}$$

$$P_2 = 320 \text{ W} = P_1$$

$$G = \frac{P_1}{V_{1, \text{rated}}^2} = \frac{320}{960^2} \approx 0.000347 \text{ S} = \frac{1}{R_m}$$

$$R_m = \frac{1}{G} = \frac{1}{0.000347} \approx 2881.8 \Omega$$

$$B = \sqrt{Y^2 - G^2} = \sqrt{0.00078^2 - 0.000347^2} \approx 0.000699 \text{ S}$$

$$X_m = \frac{1}{B} = \frac{1}{0.000699} \approx 1430.61 \Omega$$

