

1. Matric number: A0199806L

$$R = 06 = 6\Omega$$

$$C = (019) \times 2 = 38\mu F$$

a.
$$I = \frac{V}{Z} = \frac{V}{R - \frac{j}{\omega C} + j\omega L}$$

$$= \frac{230}{6 - j\left(\frac{1}{50 \times 38 \times 10^{-6}}\right) + j(50)(0.8)}$$

$$\approx \frac{230}{6 - j486.31579} \approx \frac{230 \angle 0^\circ}{486.3528 \angle -89.29314^\circ}$$

$$\approx 0.4729 \angle 89.29314^\circ$$

$$= 0.473 \angle 89.3^\circ A \text{ (3s.f.)}$$

b. $I_C = I_L = I_R = I = 0.4729 \angle 89.29314^\circ = 0.473 \angle 89.3^\circ A$

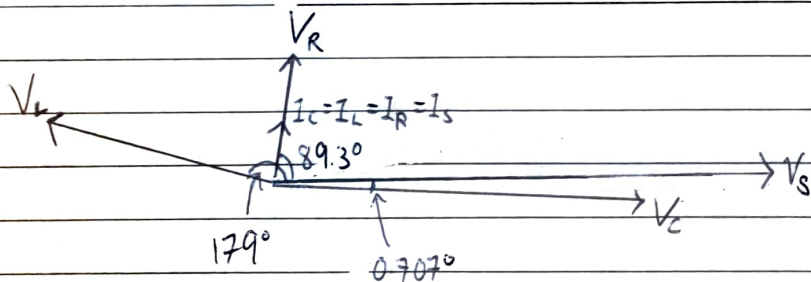
$$V_S = 230 \angle 0^\circ V$$

$$V_C = I_C \left(-\frac{j}{\omega C}\right) = (0.4729 \angle 89.29314^\circ) \left(\frac{1}{50 \times 38 \times 10^{-6}} \angle -90^\circ\right)$$

$$= 249 \angle -0.707^\circ V \text{ (3s.f.)}$$

$$V_L = I_L(j\omega L) = (0.4729 \angle 89.29314^\circ)(j50 \times 0.8) = 18.9 \angle 179^\circ V \text{ (3s.f.)}$$

$$V_R = I_R R = (0.4729 \angle 89.29314^\circ)(6) = 2.84 \angle 89.3^\circ V \text{ (3s.f.)}$$



C. I is max when Z is min and $Z = R + \frac{1}{j\omega C} + j\omega L$
is min when

$$\frac{1}{j\omega C} + j\omega L = 0$$

$$\frac{1}{j\omega C} = -j\omega L$$

$$\omega^2 LC = 1$$

$$\omega = \sqrt{\frac{1}{LC}} = \sqrt{\frac{1}{0.8(38 \times 10^{-6})}}$$
$$= 181 \text{ Hz (3 s.f.)}$$

2 Meter number: A0199806L
Nusnet id: e0406787

$$A = 87 \times 2 = 174 \text{ kW}$$

$$B = 0.7$$

a.
$$V_{\text{line-neutral}} = \frac{|V_{\text{line-line}}|}{\sqrt{3}} \angle 0^\circ = \frac{420}{\sqrt{3}} \angle 0^\circ$$
$$\approx 242.487 \angle 0^\circ \text{ V}$$

Load 1

$$Z_{y,1} = \frac{Z_{\Delta,1}}{3} = \frac{15 \angle 20^\circ}{3} = 5 \angle 20^\circ \Omega$$

$$I_1 = \frac{V_{\text{line-neutral}}}{Z_{y,1}} = \frac{242.487 \angle 0^\circ}{5 \angle 20^\circ}$$
$$= 48.4974 \angle -20^\circ \text{ A}$$

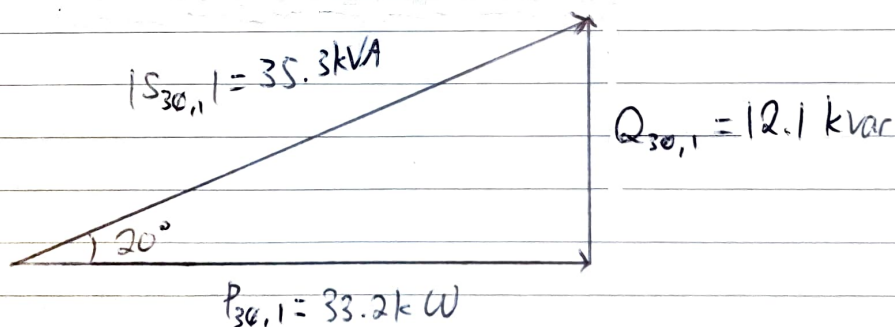
$$S_{3\phi,1} = 3(V_{\text{line-neutral}})(I_1^*) = 3(242.487 \angle 0^\circ)(48.4974 \angle 20^\circ)$$
$$\approx 35.27997 \angle 20^\circ \text{ kVA}$$

$$|S_{3\phi,1}| = 35.3 \text{ kVA (3sf.)}$$

$$\theta_1 = 20^\circ$$

$$P_{3\phi,1} = 35.27997 \cos(20^\circ) = 33.2 \text{ kW (3sf.)}$$

$$Q_{3\phi,1} = 35.27997 \sin(20^\circ) = 12.1 \text{ kvar (3sf.)}$$



Load 2

$$Z_2 = 6 + j8 \Omega \approx 10 \angle 53.13^\circ \Omega$$

$$I_2 = \frac{V_{\text{line-neutral}}}{Z_2} = \frac{242.487 \angle 0^\circ}{10 \angle 53.13^\circ}$$
$$= 24.2487 \angle -53.13^\circ \text{ A}$$

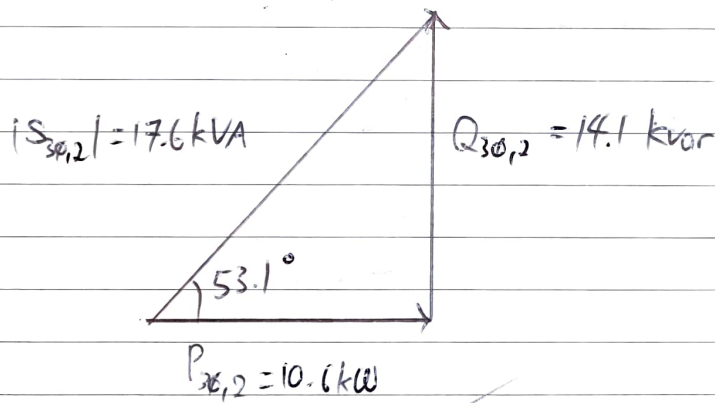
$$S_{3\phi,2} = 3 V_{\text{line-neutral}} I_2^* = 3 (242.487 \angle 0^\circ) (24.2487 \angle 53.13^\circ)$$
$$\approx 17.63998 \angle 53.13^\circ \text{ kVA}$$

$$|S_{3\phi,2}| = 17.6 \text{ kVA (3s.f.)}$$

$$\theta = 53.1^\circ \text{ (3s.f.)}$$

$$P_{3\phi,2} = 17.63998 \cos(53.13^\circ) = 10.6 \text{ kW (3s.f.)}$$

$$Q_{3\phi,2} = 17.63998 \sin(53.13^\circ) = 14.1 \text{ kvar (3s.f.)}$$



Load 3

$$P_{30,3} = 174 \text{ kW}$$

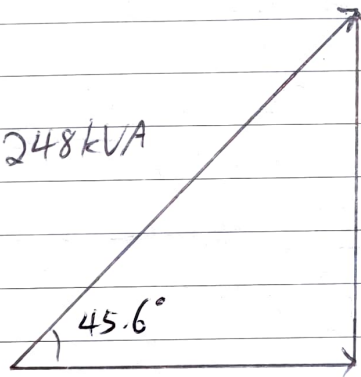
$$p.f._3 = 0.7$$

$$\theta = \cos^{-1} 0.7 \approx 45.573^\circ = 45.6^\circ \text{ (3s.f.)}$$

$$Q_{30,3} = P_{30,3} \tan \theta = 174 \tan(45.573^\circ) \\ \approx 177.5155 \text{ kvar} \\ = 178 \text{ kvar (3s.f.)}$$

$$|S_{30,3}| = \sqrt{174^2 + 177.5155^2} \\ = 248 \text{ kVA (3s.f.)}$$

$$|S_{30,3}| = 248 \text{ kVA}$$



$$P_{30,3} = 174 \text{ kW}$$

$$Q_{30,3} = 178 \text{ kvar}$$

$$b. P_s = P_{3\phi,1} + P_{3\phi,2} + P_{3\phi,3} = 33.2 + 10.6 + 174 \\ = 217.8 \text{ kW}$$

$$Q_s = Q_{3\phi,1} + Q_{3\phi,2} + Q_{3\phi,3} = 12.1 + 14.1 + 178 \\ = 204.2 \text{ kvar}$$

$$S_s = \sqrt{217.8^2 + 204.2^2} \angle \tan^{-1}\left(\frac{204.2}{217.8}\right)$$

$$\approx 298.55 \angle 43.154^\circ$$

$$= 299 \angle 43.2^\circ \text{ kVA (3s.f.)}$$

c.

Since unity, $\theta = 0^\circ$,

$$Q_{C,3\phi} = -Q_s = -204.2 \text{ kvar}$$

$$Q_{C,1\phi} = \frac{-Q_s}{3} \approx -68.06667 \text{ kvar}$$

$$X_{C,1\phi} = \frac{|V_{\text{line-line}}|^2}{Q_{C,1\phi}} = \frac{420^2}{-68.06667 \times 10^3} \approx -2.591577 \Omega$$

Assuming $\omega = 50 \text{ Hz}$,

$$|X_{C,1\phi}| = \frac{1}{\omega C}$$

$$2.591577 = \frac{1}{50 C}$$

$$C = 130 \text{ F (3s.f.)}$$

$$|P_s| = 3 |V_{\text{line-neutral}}| |I_{ph}| \cos \theta$$

$$|I_{\text{line}}| = |I_{ph}| = \frac{|P_s|}{3 |V_{\text{line-neutral}}|} = \frac{217.8 \times 10^3}{3 \left(\frac{420}{\sqrt{3}}\right)}$$

$$= 299 \text{ A (3s.f.)}$$