

EE2029: Introduction to Electrical Energy Systems

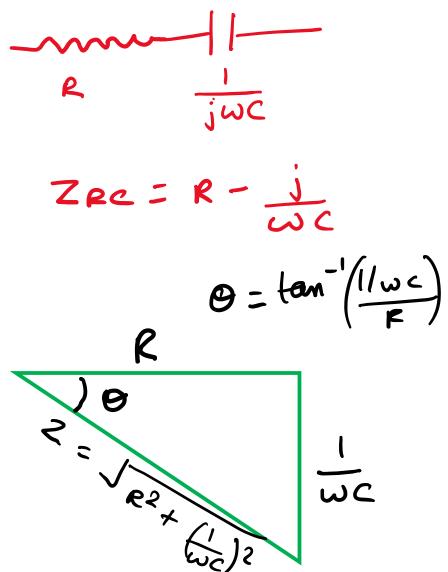
AC Power

Lecturer : Dr. Sangit Sasidhar (elesang)

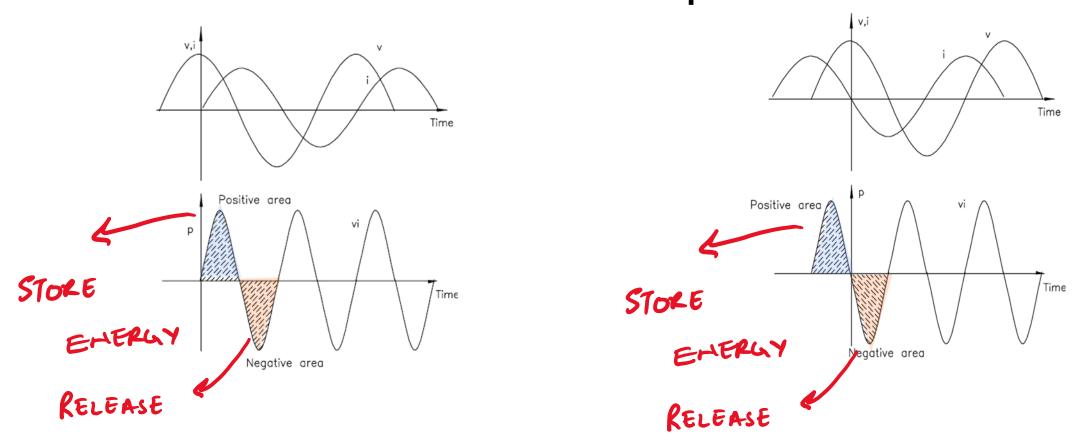
Department of Electrical and Computer Engineering

© Copyright National University of Singapore. All Rights Reserved.

Impedance Triangle

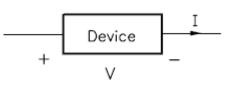


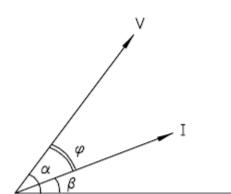
Power in Inductor and Capacitor



Both inductor and capacitor store and release energy during the AC cycle. When both the voltage and current are of the same sign, the element (L or C) draws energy equivalent to the area under the positive half cycle of p(t) from the source and stores it. When they are of opposite signs, it is returning the energy to the source.

Power in AC Circuits





$$Z = R + j X = 121L\Theta - \Omega$$

$$|Z| = \sqrt{R^2 + x^2}$$

$$V = |V|L\alpha$$

$$I = |I|L\beta$$

REAL POWER
$$P = |I|^2 R$$

$$= |I||I|R$$

$$P = \frac{|V||I|R}{|Z|} = \frac{|V|}{\sqrt{R^2 + x^2}} |I|R$$

Cos O=

Apparent Power

• We express power in d.c. and a.c. circuits as follows:

- In a.c. circuits an additional term $\cos\theta$ has occurred in the expression for Real power
- Define Apparent Power → Isl = Vrms Irms
- Units of Apparent Power → VA (VOLT AMPERES)
- So, the Real power in a.c. circuit may also be expressed in terms of apparent power as

Reactive Power

- Real Power → Power in the Resistor
- Average power in inductor or capacitor =0
- Define Reactive Power (Q) → Power stored/released by the inductor or capacitor.

$$\frac{x}{\sqrt{R^2+x^2}} = -\sin\theta$$

ORC = - Vrms Irms Sino

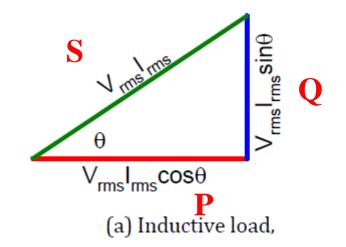
Power Triangle

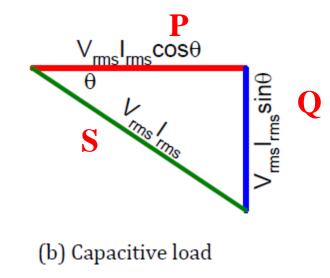
- P Real (or active) Power: Power consumed in the resistive part of the circuit
- Q Reactive Power: Power stored in the inductor or capacitor
- S Apparent Power: Combines P and Q in one quantity
 - Indication of Current the System can support

$$P = V_{rms}I_{rms}cos\theta$$

$$S = V_{rms}I_{rms}$$

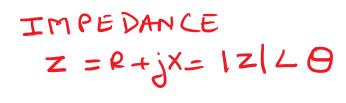
$$Q = V_{rms}I_{rms}Sin\theta$$



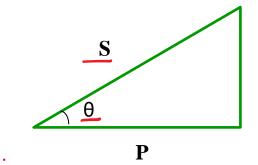


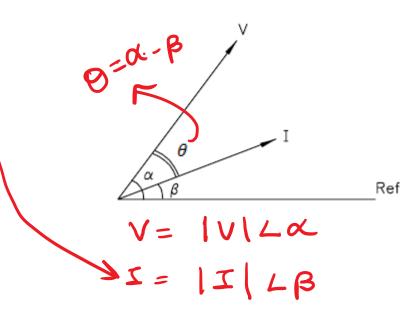
Complex Power

Define Complex Power



CONJUGATE





Power in an Inductor

IMPEDANCE OF AN INDUCTOR =
$$Z_L = j\omega L = \omega L L90^{\circ} S_L - \frac{1}{\sqrt{1 - 1}}$$

$$T = \frac{V}{Z_{L}} = \frac{|V|L0^{\circ}}{\omega L L 90^{\circ}} = \frac{|V|L0^{\circ}}{|W|L} |L-90^{\circ}| = |II|L-90^{\circ}$$

COMPLEX POWER IN AN INDULTOR SL= VIX= VLO. IL98 = ZLI.IX= jwllI|2

REAL POWER CONSUMED BY INDUCTOR = |VIII COS 90°= 0

REACTIVE POWER CONSUMED BY INDUCTOR = |VIII Sin 90°= |VIII = WLII

Power in a Capacitor

IMPEDANCE OF A CAPACITOR =
$$Z_{c} = \frac{1}{j\omega c} = \frac{1}{\omega c} 2-90^{\circ}$$
 $I = \frac{V}{Z_{c}} = \frac{IVILO^{\circ}}{\omega c} = [\omega cVIL90^{\circ} = (IIL90^{\circ})]$
 $V = IVILO^{\circ}$

COMPLEX POWER IN A CAPACITOR $S_{c} = VII^{*} = Z_{c}I \cdot I^{*} = -j\frac{|II|^{2}}{\omega c}$

REAL POWER CONSUMED BY CAPACITOR = $IVIII$ (OB $C - 90^{\circ}$) = 0

REACTIVE POWER CONSUMED BY CAPACITOR = $IVIII$ Sin $(C - 90^{\circ})$ = $-IVIII$ = $-III^{2}$
 $= -\omega c(VI)^{2}$

INDUCTANCE \Rightarrow +Ve REACTIVE POWER

CAPACITANCE -> - VE REACTIVE POWER

Complex Power of Series and Parallel Connected Loads

Series Connected Loads

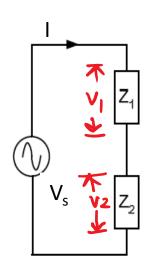
$$S = V_{S} I^{*}$$

$$V_{S} = V_{1} + V_{2}$$

$$\Rightarrow S = (V_{1} + V_{2}) I^{*}$$

$$= V_{1} I^{*} + V_{2} I^{*}$$

$$= S_{1} + S_{2}$$



Parallel Connected Loads

$$S = VI^*$$

$$I = I_1 + I_2$$

$$\Rightarrow S = V (I_1 + I_2)^*$$

$$= VI_1^* + VI_2^*$$

$$= S_1 + S_2$$

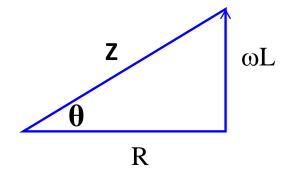
Complex Power Summary

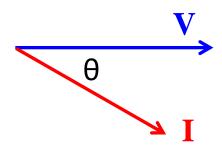
S	Complex power	VA	VI*= P+jQ
5	Apparent power	VA	151 = 1V11 = J P2+Q2
Р	Active power Average power, Real power	W	P= Re(S) = V1 Cos & = S Cos &
Q	Reactive power	VAR	Q = Im(s) = VISIND = ISISIND

© Copyright National University of Singapore. All Rights Reserved.

Power Factor

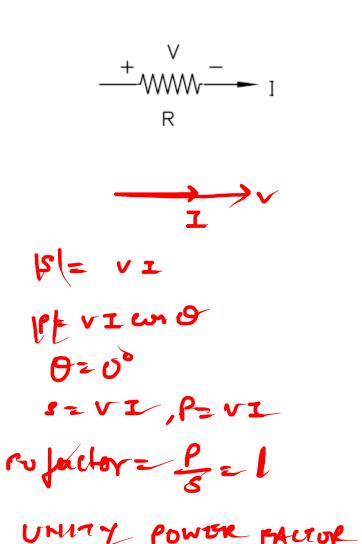
- Let us define Power Factor of an AC circuit as the ratio of the real power to the apparent power
 - Power Factor $=\frac{P}{|S|}=\frac{P}{|V||I|}=cos\theta$
 - If ' θ ' is larger, power factor ($\cos\theta$) is smaller
- Power factor angle (θ) is the same in the power triangle, impedance triangle and the angle between the voltage and the current





P

Power Factor for Resistive, Inductive and Capacitive Load



$$Z = R + j\omega L = R + jX_L = |Z| \angle \theta$$

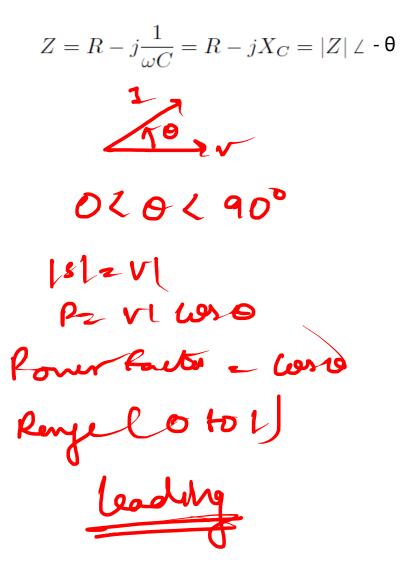
O $7 \circ 7 - 9 \circ 9$

Use VI

Pare factor 2 was θ

Range C 0 to 1)

Leggy



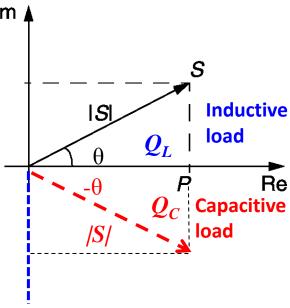
How do we Improve Poor Power Factor?

© Copyright National University of Singapore. All Rights Reserved.

Poor Power Factor

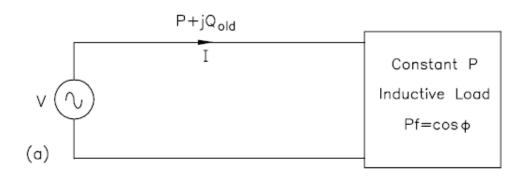
 If the power factor is poor (i.e., very low), current drawn by the load will be high.

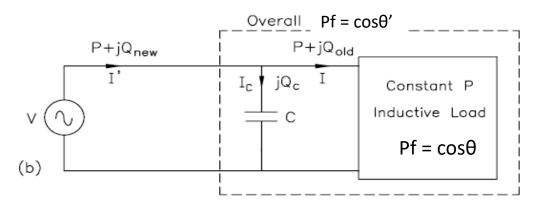
- Poor voltage regulation at the load
- Heavy transmission lines losses
- High operating cost



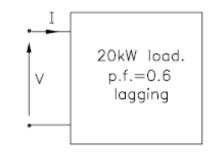
Power Factor Correction (PFC)

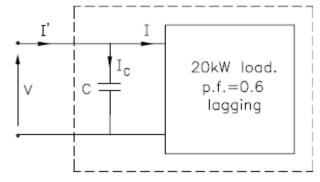
PFC: Fixed Capacitive Load → New Power Factor



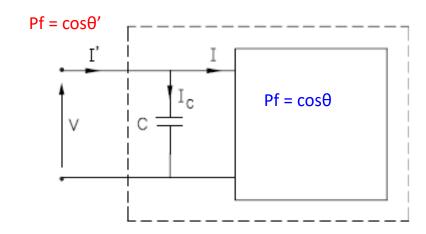


Example: A load connected across a 230V, 50HZ line draws 20kW at 0.6pf lagging. Determine the current drawn by the load. If a capacitor of 800 μF is connected in parallel with the load, what will be the current drawn from the source? Also determine the overall power factor of the system as seen by the source

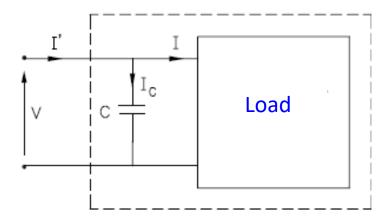




PFC: Required Power Factor → Capacitive Load



Example: A load connected across a 200 V, 50Hz line draws 10 kW at 0.5 power factor lagging. Determine the current drawn by the load. A capacitor C is now connected in parallel with the load to improve the power factor. What must be the value of C to make the overall power factor 0.9 lagging



Thank You

© Copyright National University of Singapore. All Rights Reserved.