EE2029: Introduction to Electrical Energy System

Transformers

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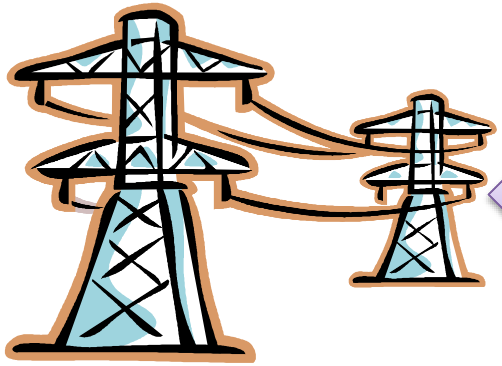
Electrical Energy Systems

Generation
(11 – 36 KV)

Large-Scale Power Plants:
Coal-fired, Hydro, Wind,
Solar, Nuclear

Transmission
(110 – 765 KV)



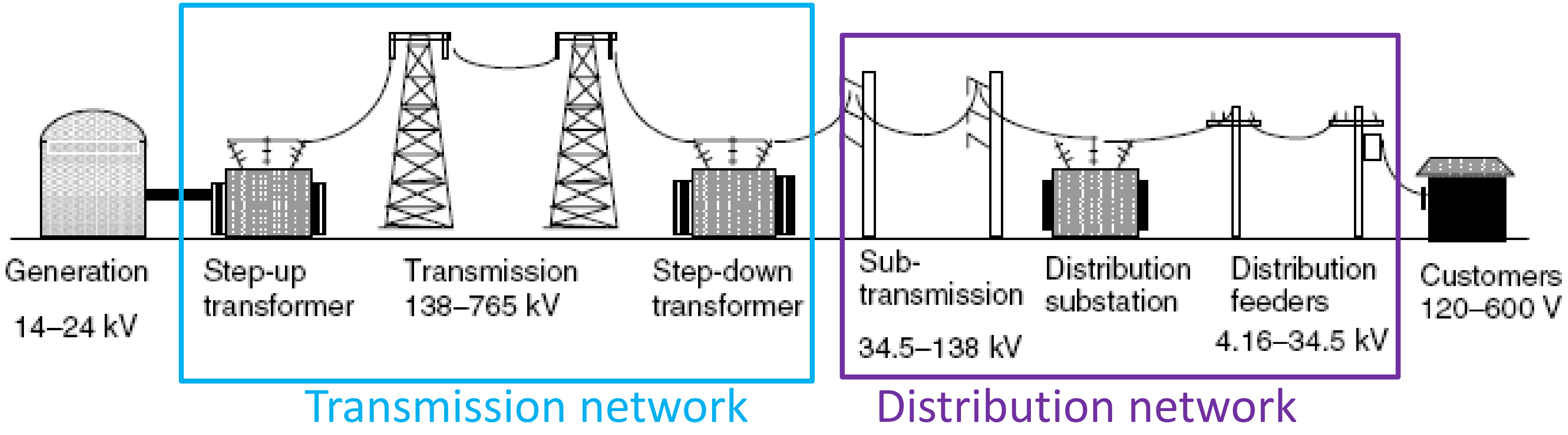
Distribution
(120/230 V – 138 KV)

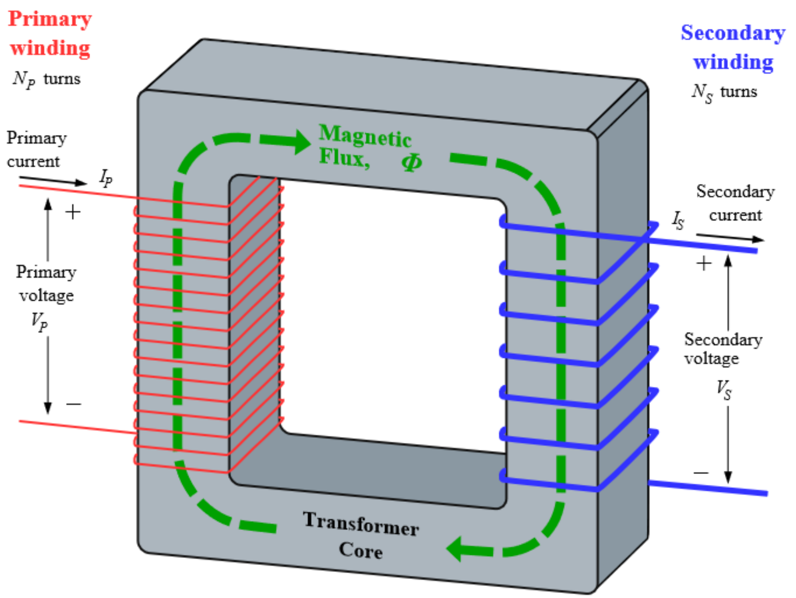
Industrial customer (23 – 138 KV)
Commercial customer (4.16 – 34.5 KV)
Residential customer (120 – 240 V)

How to connect generation (medium voltage) to transmission (high voltage) to the point of consumption (low voltage)?

Transformers

- Transformers used to step up voltages from generation units to transmission-line and to step down voltage from transmission to end users.
- Transformers are important in electrical energy systems. With transformers, the overall efficiency can be improved.
  - See this for yourself in the Lab Session 2!!



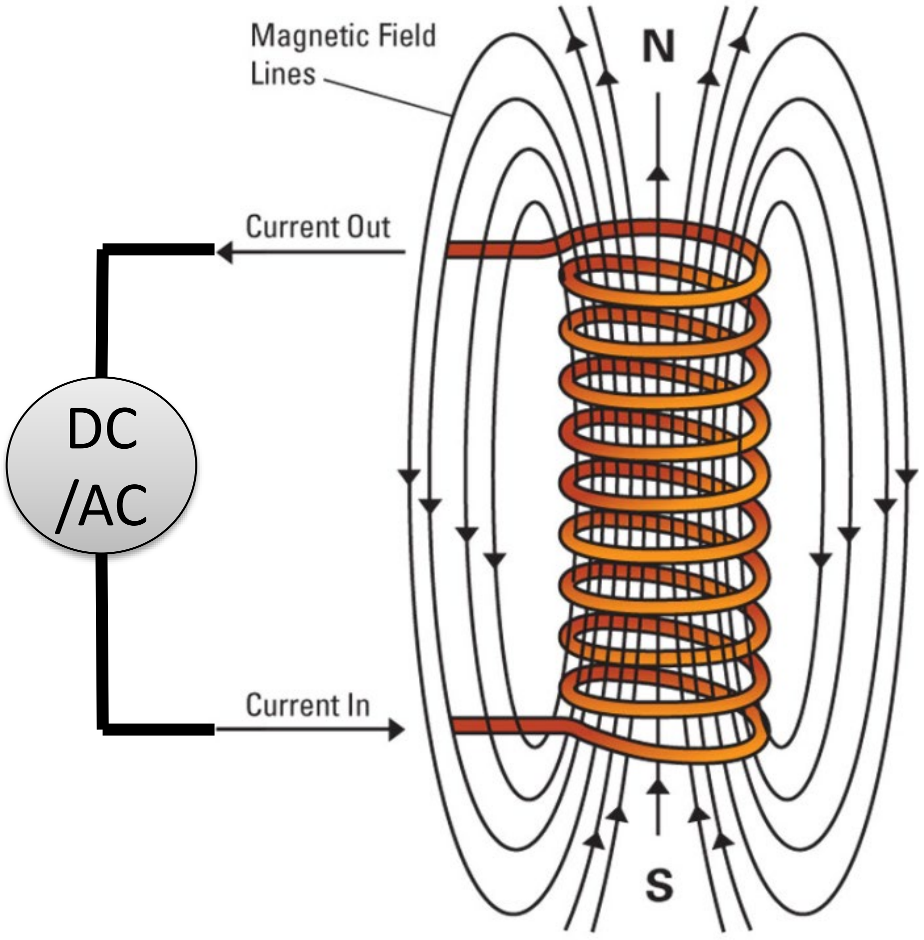


Electromagnetism
Electromagnetic induction
Dot notation
Faraday's Law
Ampere's Law

PRINCIPLE OF TRANSFORMERS

Source: "Transformer3d col3" by BillC at en.wikipedia - Own workTransferred from en.wikipedia. Licensed under CC BY-SA 3.0 via Wikimedia Commons - http://commons.wikimedia.org/wiki/File:Transformer3d_col3.svg#mediaviewer/File:Transformer3d_col3.svg

Electromagnetism and Electromagnetic Induction

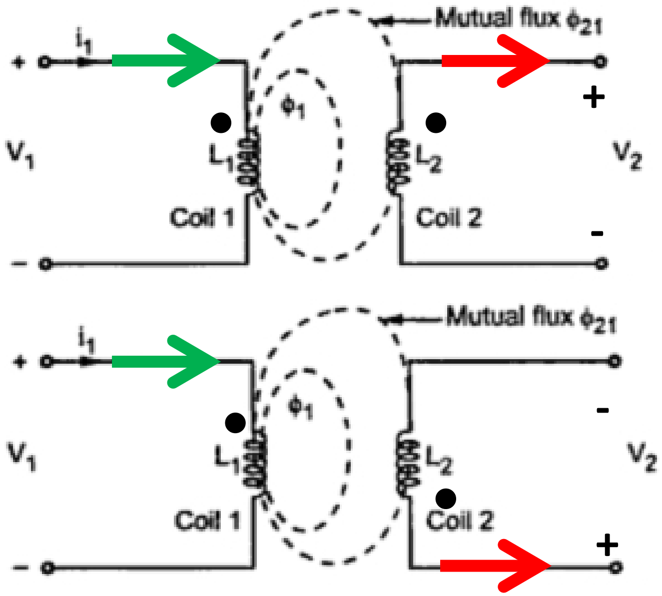


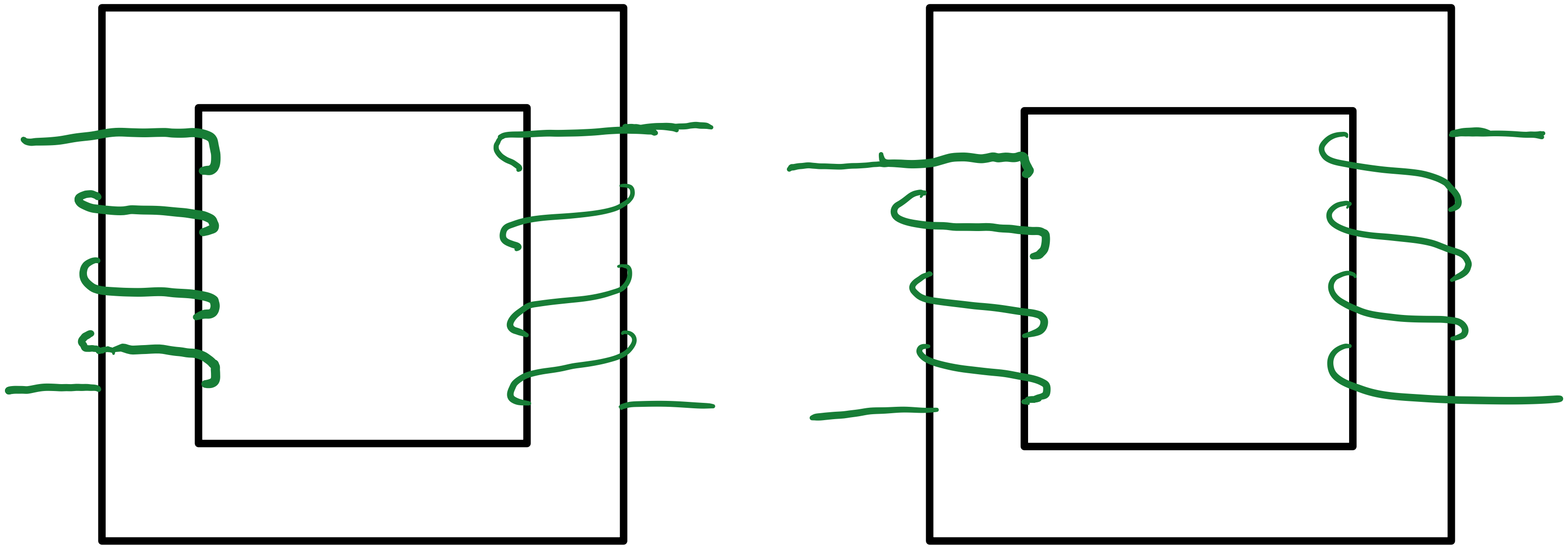
- DC source → Constant magnetic flux
- AC source → Varying magnetic flux
- *What will happen if we have another coil to link the varying magnetic flux?*
- **Faraday's Law:** $e = N\frac{d\Phi}{dt}$

Source: http://www.lanl.gov/news/index.php/fuseaction/1663.article/d/20085/id/13276

Dot Notation in Transformers

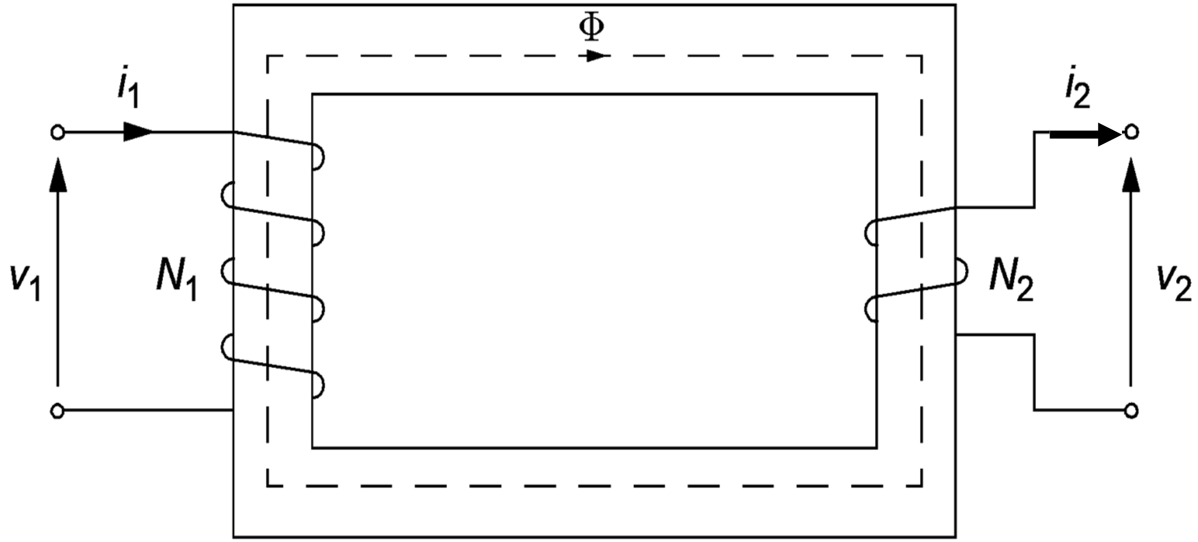
- **Dot notation** is used to indicate the direction of current out of Coil 2 in the equivalent circuit.





Magnetic Core

- We can better link the magnetic flux by using magnetic core.
- Magnetic flux "Φ" is now confined in the core and links both windings.

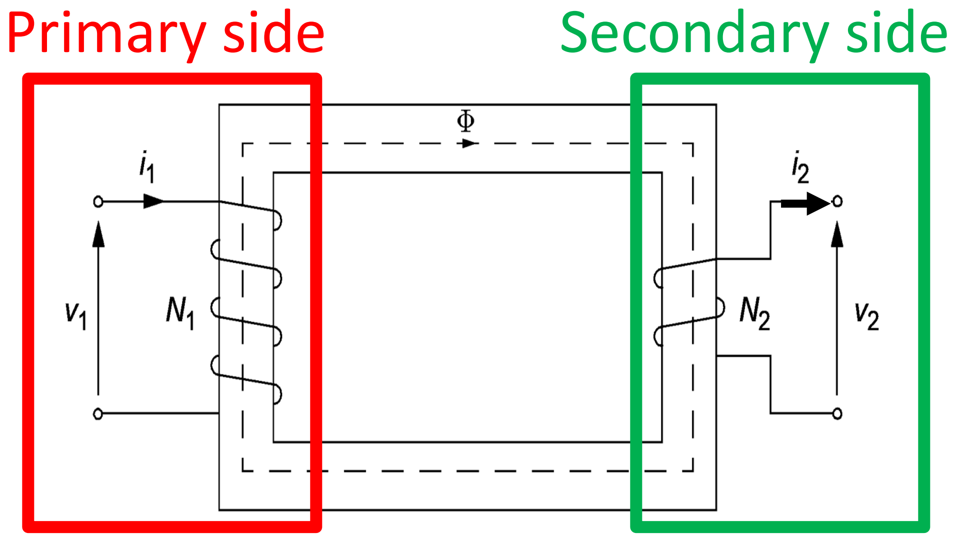


Note that 'N' refers to number of turns.

We are now interested to relate V1 and V2, and relate i1 and i2.

Ideal Transformer

1. No resistance in both windings.
2. No leakage flux around the core.
3. No core resistive loss.
4. Core permeability is infinite.

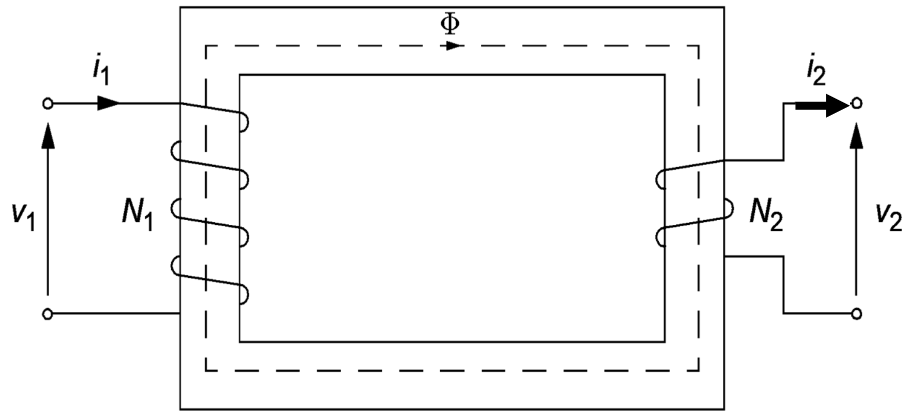


Faraday’s Law

- Recall that: $$e = N\frac{d\phi}{dt}$$

Voltage Relationship

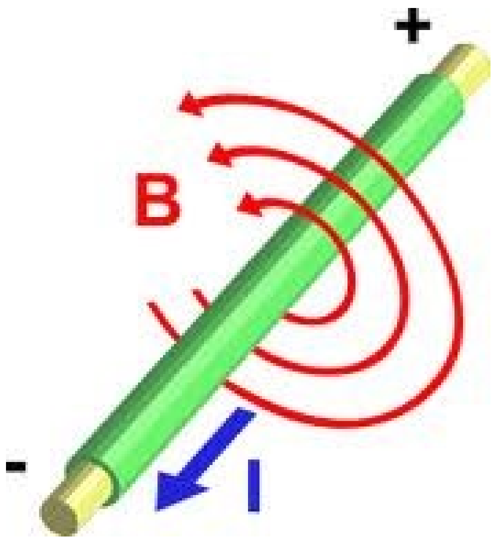
- For **ideal** transformer, we assume that the flux linkage at coil 1 and coil 2 is the same i.e. there is no flux linkage loss.
- We can now find a relationship between the voltages at two sides of the transformer as follows.



Ampere's Law

- "Current passing through a conductor creates magnetic field around it "

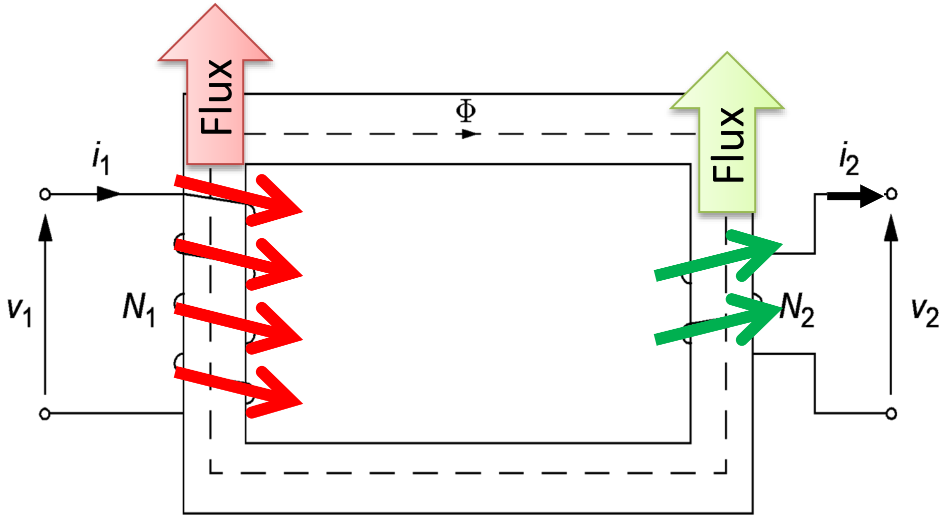
$$\oint H dl = I_{enclosed}$$



- $B = \mu H$
- B = Magnetic flux density (Weber/m² or Tesla)
- H = Magnetic field intensity (A/m)
- μ = Magnetic core permeability (H/m)

Ampere's Law Applied to Transformers

- "Magnetic flux along the path equals the net current enclosed by the path"



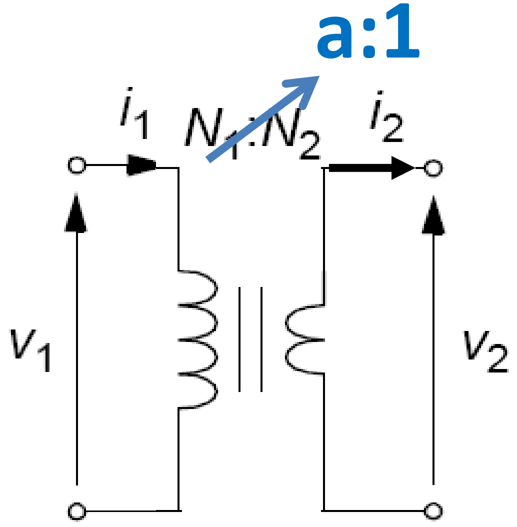
$i_1 N_1$ $-i_2 N_2$

Current Relationship

- Note that magnetic core permeability (μ) represents the degree of magnetization that the magnetic core will allow the magnetomotive force to pass through.
- For **ideal transformer**, the value of the permeability is infinity.

Transformer Equivalent Circuit

- We represent an equivalent circuit of an ideal transformer as shown below.



- Define turns ratio as:

$$a \equiv \frac{N_1}{N_2}$$

- From Faraday's and Ampere's Law:

$$\frac{V_1}{V_2} = \frac{N_1}{N_2} \qquad i_1 N_1 = i_2 N_2$$

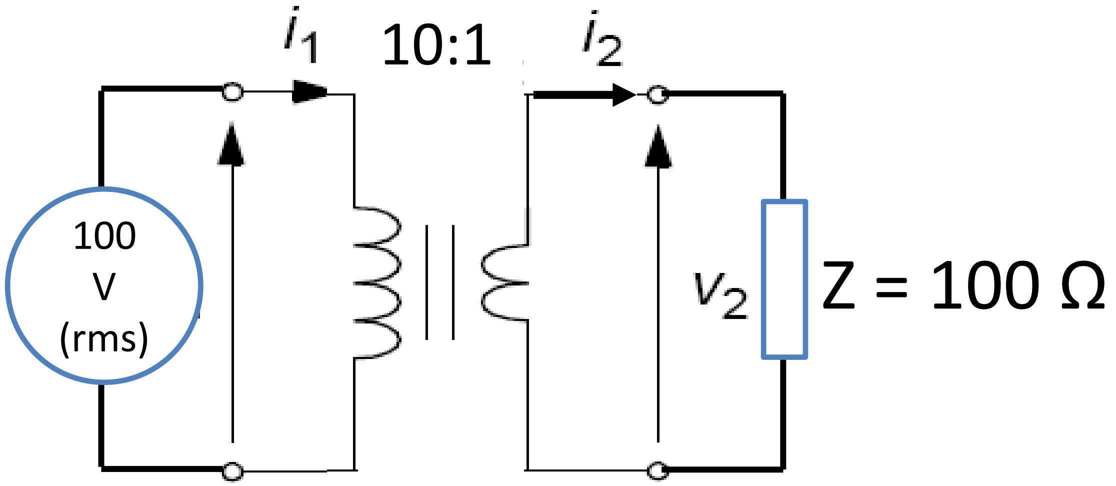
Complex Power

- Complex power *at primary side,*

- Complex Power at *secondary* side

Example 1

From the circuit below, what is the current at the secondary and primary side?



Reflected load

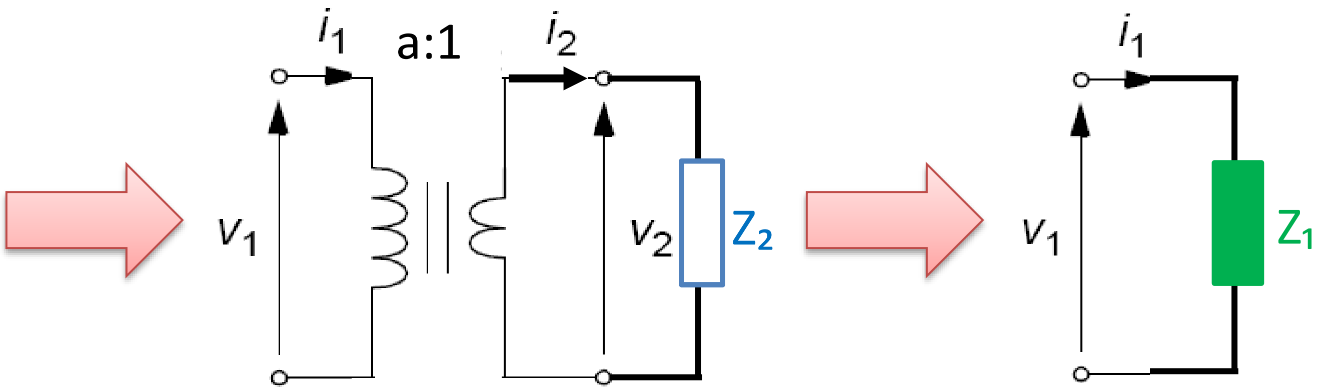
Impedance matching

APPLICATION OF TRANSFORMERS

Reflected Load

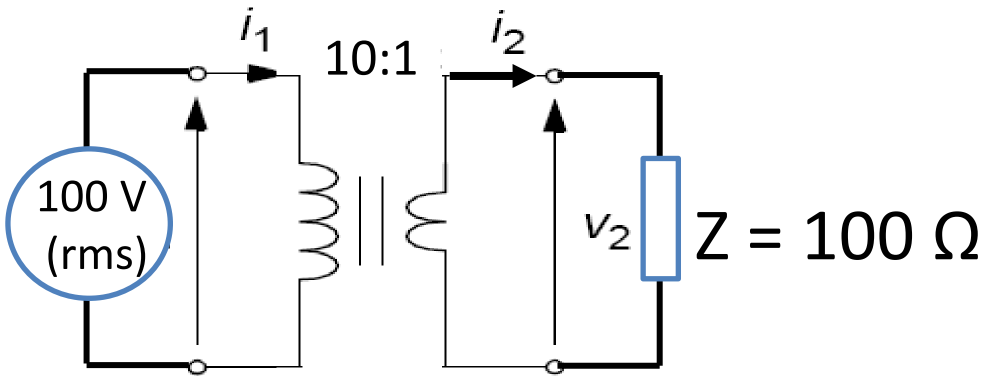
- We can reflect a load from one side of a transformer to the other side of the transformer.
- This trick allows us to combine the two separate circuits into one for easy(?) calculation.

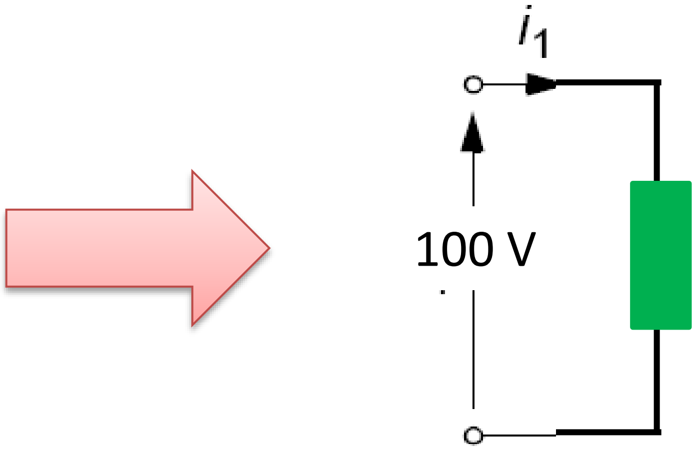
Interest to find reflected load "Z_1"



Example 2

- Find the reflected load of impedance 100 Ω seen from the primary side of the transformer.

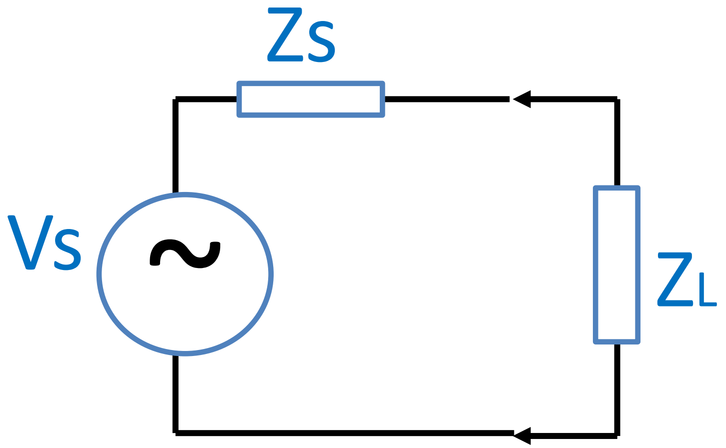




Maximum Power Transfer Theorem

- From real power expression at the load,

$$P_L = \frac{|V_S|^2}{|Z_S + Z_L|^2} \mathrm{Re}\{Z_L\}$$

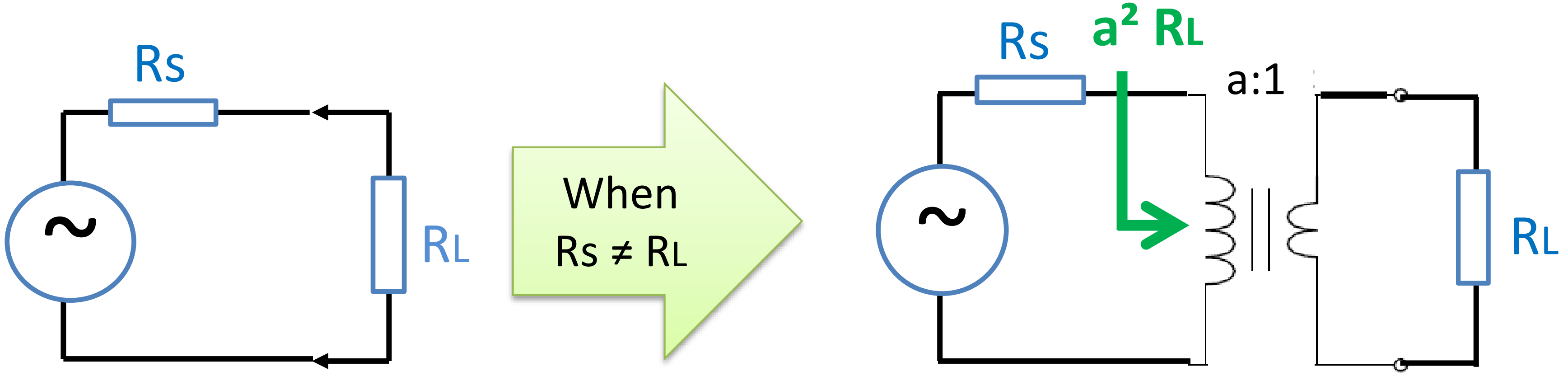


- This means that the maximum power will occur when the denominator is minimum

Maximum Power Transfer Theorem

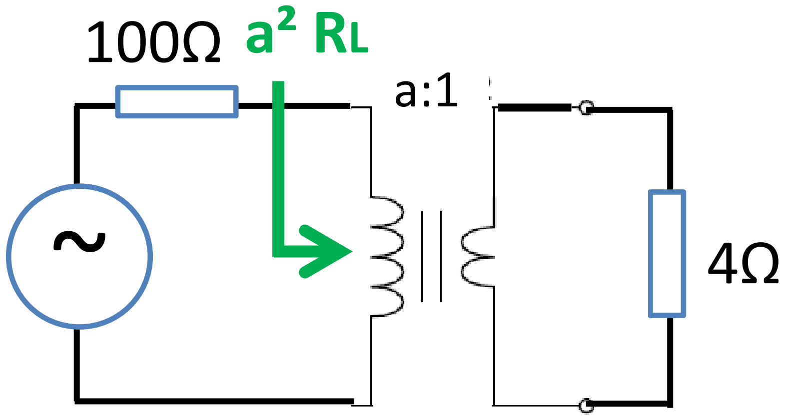
Impedance Matching for ‘R’

- Maximum power transfer occurs when $R_S = R_L$.
- In the case that we need to connect the voltage source that has internal impedance of R_S to a load R_L that does not satisfy the above condition, we can **design** a **transformer** to *match* impedance for maximum power transfer.
- To find an appropriate transformer, we let $\mathbf{R_S = a^2R_L}$ and find a transformer turns ratio.



Example 3

Given the voltage source with an internal resistance of 100 Ω. A transformer is used to connect this voltage source to the load of 4 Ω to achieve maximum power transfer at the load. What should be the turns ratio of a transformer?



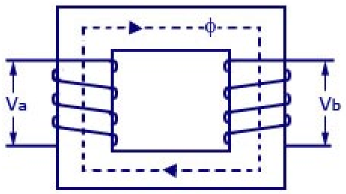
Transformer components
Losses in Transformers
Magnetizing current losses
A practical transformer model
A simplified model

PRACTICAL TRANSFORMERS

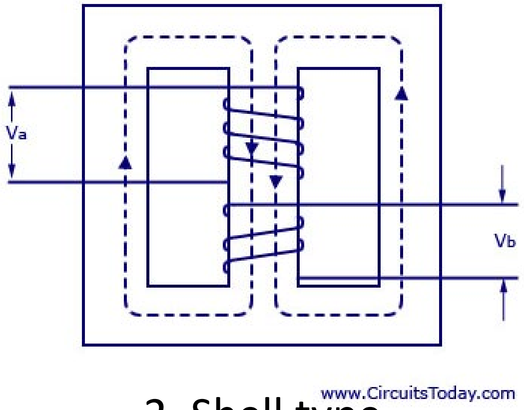
Transformer Components

Magnetic core

- Mainly two types of design.
  1. Core type – the magnetic core is surrounded by the windings.
  2. Shell type – the windings are surrounded by the core.



1. Core type



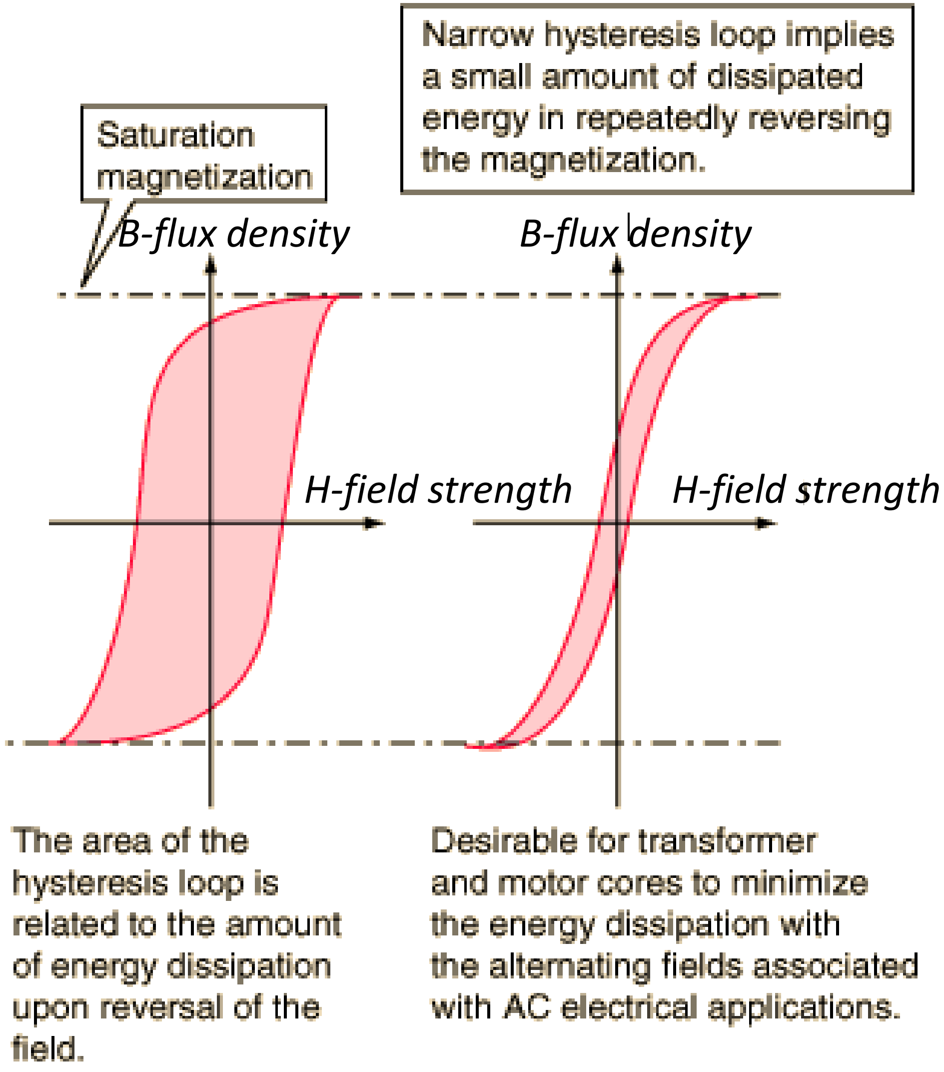
2. Shell type

Primary/Secondary winding

- Windings are placed on top of each other to reduce the amount of flux leakage losses.

Losses in Transformers: Hysteresis Losses

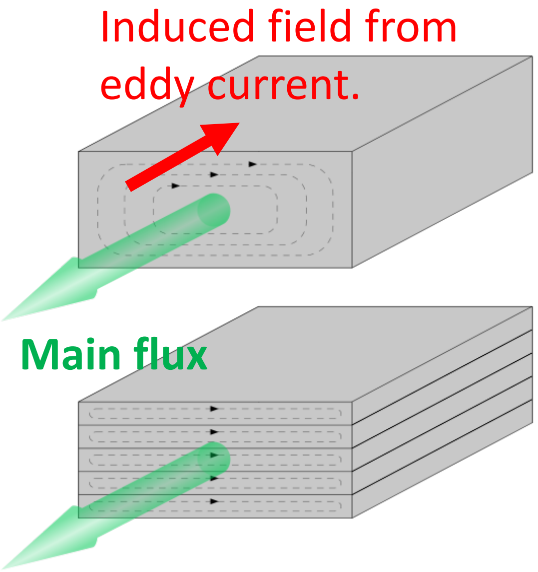
- Hysteresis loop is a characteristic of how a ferromagnetic material is magnetized.
- Each time the direction of magnetic field is reversed, some amount of energy is dissipated in the core.
- This means that <u>this loss is proportional to the frequency of electricity.</u>
- Hysteresis loss produces heat and is represented as a **resistance parallel to** the ideal transformer.



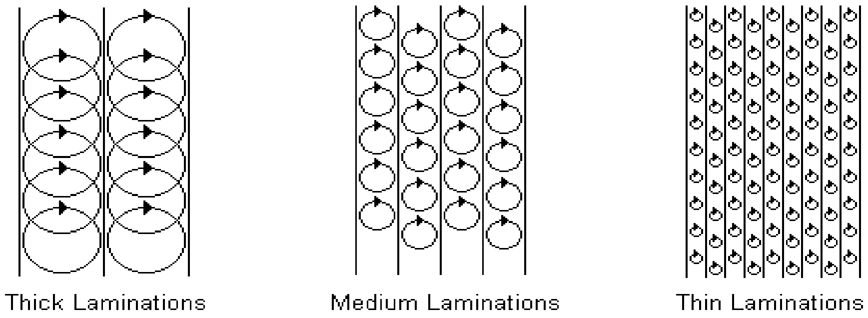
Source: http://hyperphysics.phy-astr.gsu.edu/hbase/solids/hyst.html

Losses in Transformers: Eddy Current Losses

- Eddy current refers to small circular current in the magnetic core caused by the flux that passes through the core.
- The magnitude of eddy current losses depends on the strength of the main flux, thus the voltage supplied.
- Eddy current loss produces heat and is represented as a **resistance parallel to** the ideal transformer.
- Eddy current loss can be reduced by making the cores from thin sheets of steel i.e. the core is laminated. The thinner the sheets, the smaller are the eddy current losses.



Eddy currents will induce a magnetic field that opposes to the direction of the main flux.

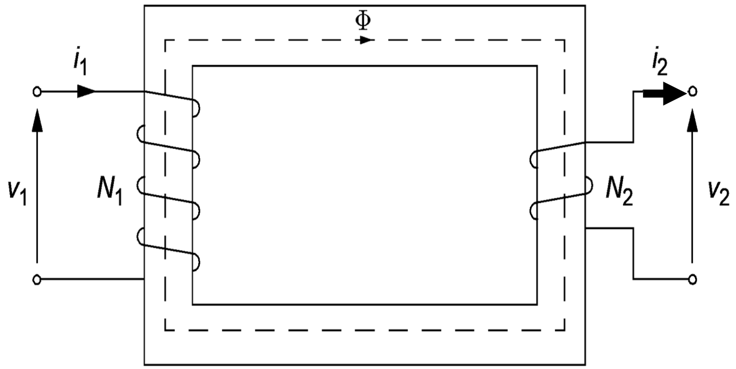


Source: http://sound.westhost.com/xfmr2.htm

Ideal VS Practical Transformer

Ideal transformer

1. Zero resistance in the both windings.
2. No leakage flux around the core.
3. No core resistive loss.
4. Core permeability is infinite



Practical transformer

1. Winding losses (copper losses) represented as ***resistance in both windings***.
2. Leakage flux around the core represented as ***inductance in both windings***.
3. Core resistive losses (hysteresis loss + eddy current loss) represented as ***resistance in parallel to the core***.
4. Magnetic core permeability is finite.

   How to represent this effect?

Finite Core Permeability

- From Ampere's law applied to transformers,

$$\frac{Bl_{path}}{\mu} = i_1N_1 - i_2N_2$$

Recall that in ideal transformer, μ is infinite so $i_1N_1 = i_2N_2$

- When the core material has finite core permeability ($\mu \neq \infty$), and $V_1 = N_1(j\omega)BA$ (Faraday's law), **assuming a constant *μ*,**

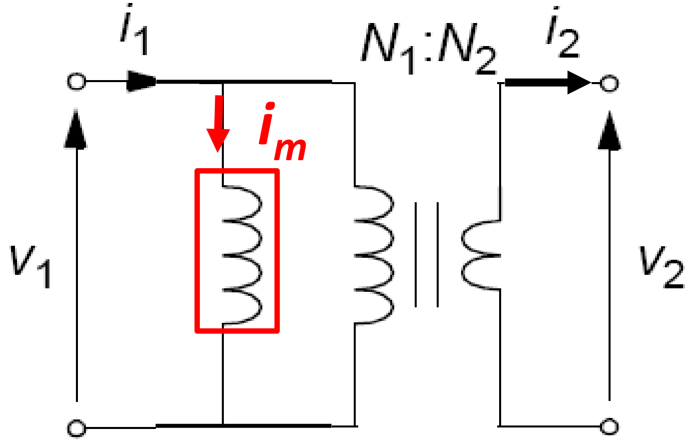
Magnetizing Current Losses

- From the magnetizing current,

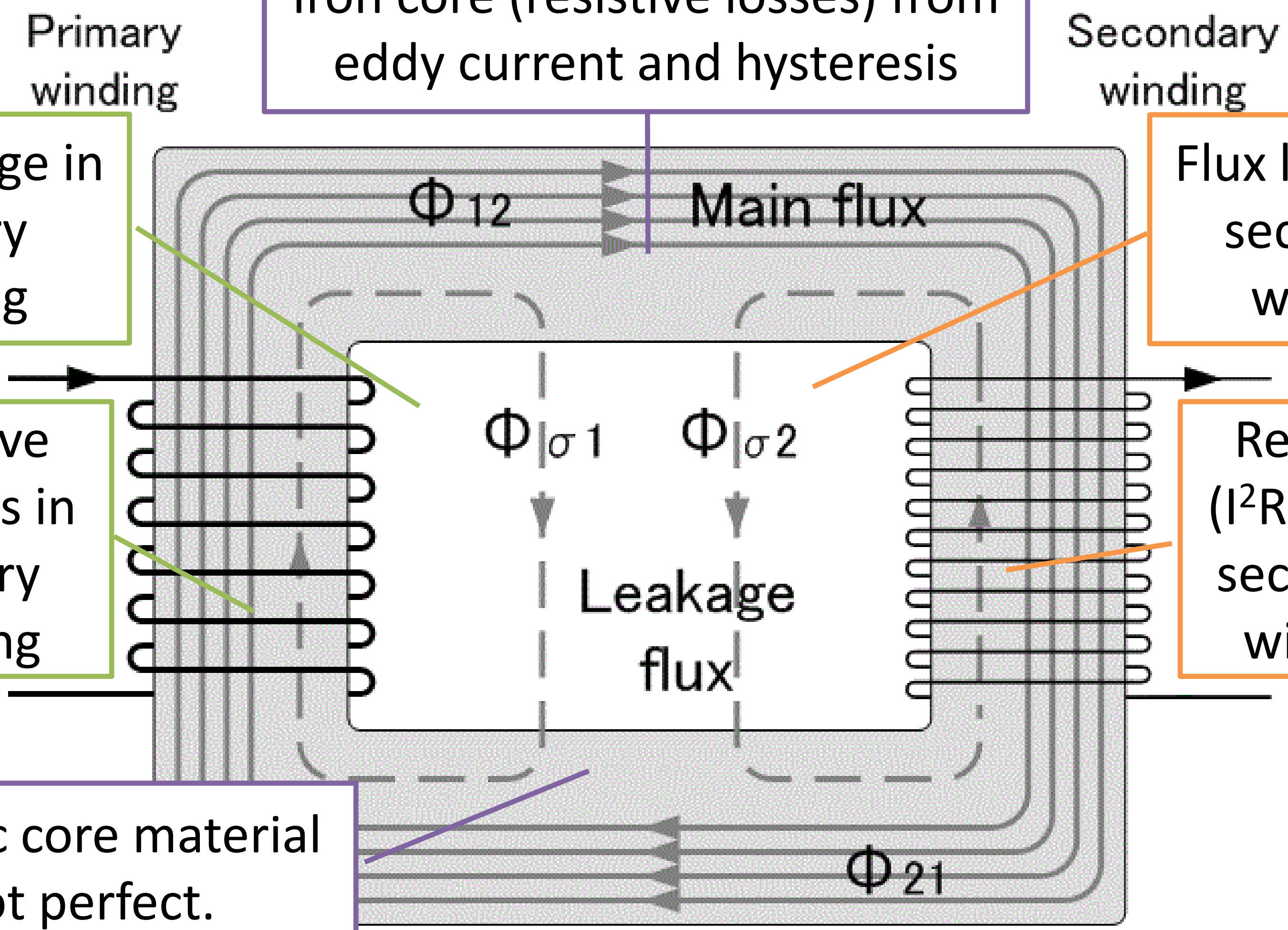
$$i_m = -j\left(\frac{l_{path}}{\omega N_1^2 A\mu}\right)V_1$$

- We find that the current lags the voltage V_1 by 90°(-j).
- As such, we can use an **inductor** to represent the effect of finite magnetic core permeability in the equivalent circuit.

$$i_1 - \left(\frac{N_2}{N_1}\right)i_2 = i_m$$



Practical Transformers



Iron core (resistive losses) from eddy current and hysteresis

Flux leakage in primary winding

Flux leakage in secondary winding

Resistive (I^2R) loss in primary winding

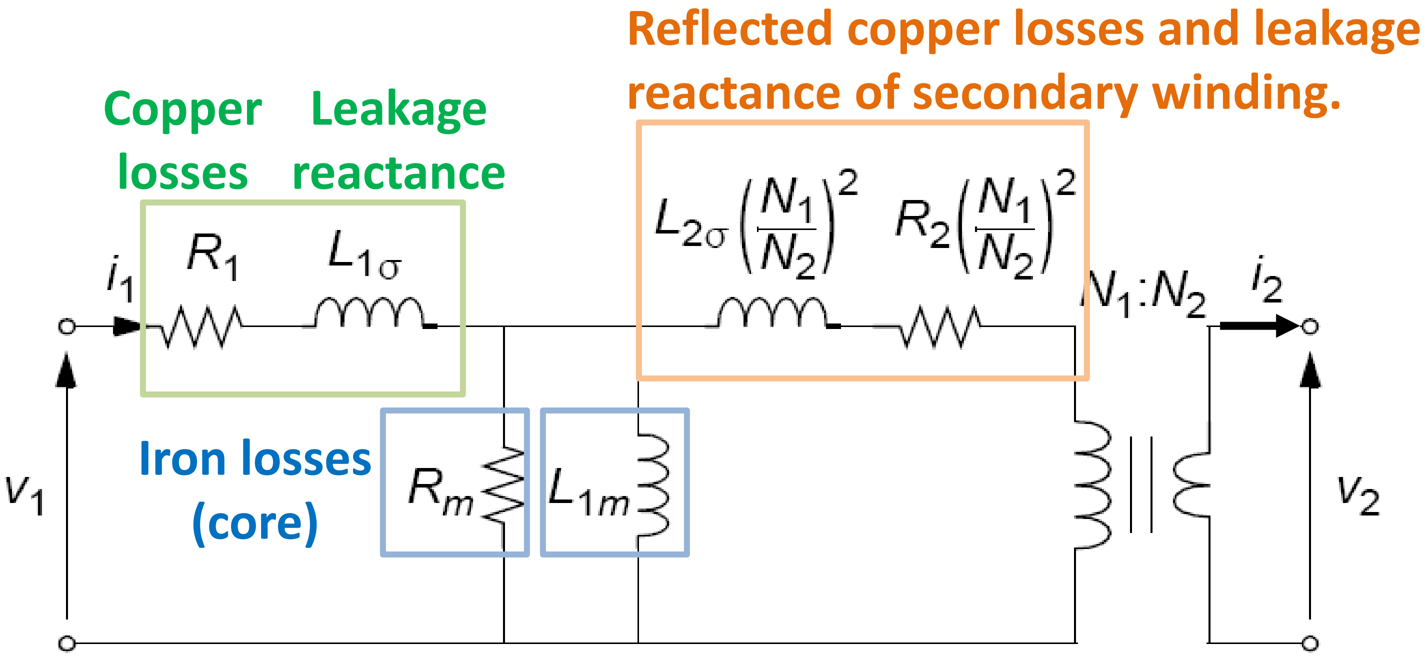
Resistive (I^2R) loss in secondary winding

Magnetic core material is not perfect.

A Practical Transformer Model

A Practical Transformer Model

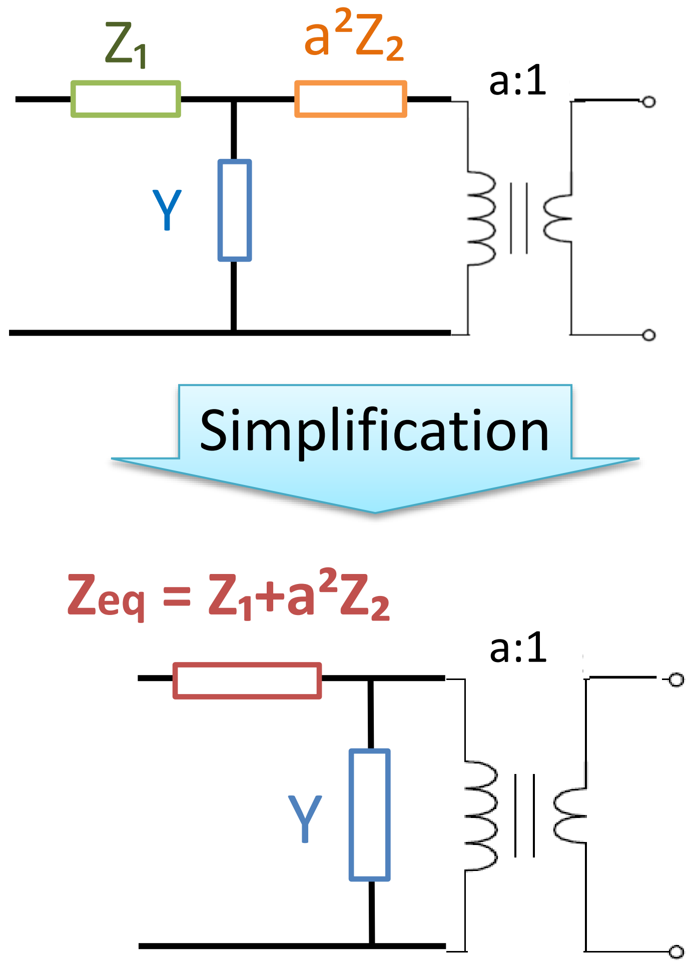
By convention, the **primary side** of transformer is the side with a **higher number** of turns.



Note that in Chapter 3 [Glover, Sarma, and Overbye, "Power System Analysis and Design"], the core losses are represented as 'shunt admittance', Y = G –jB where G and B are positive. The imaginary part is negative to represent inductive property.

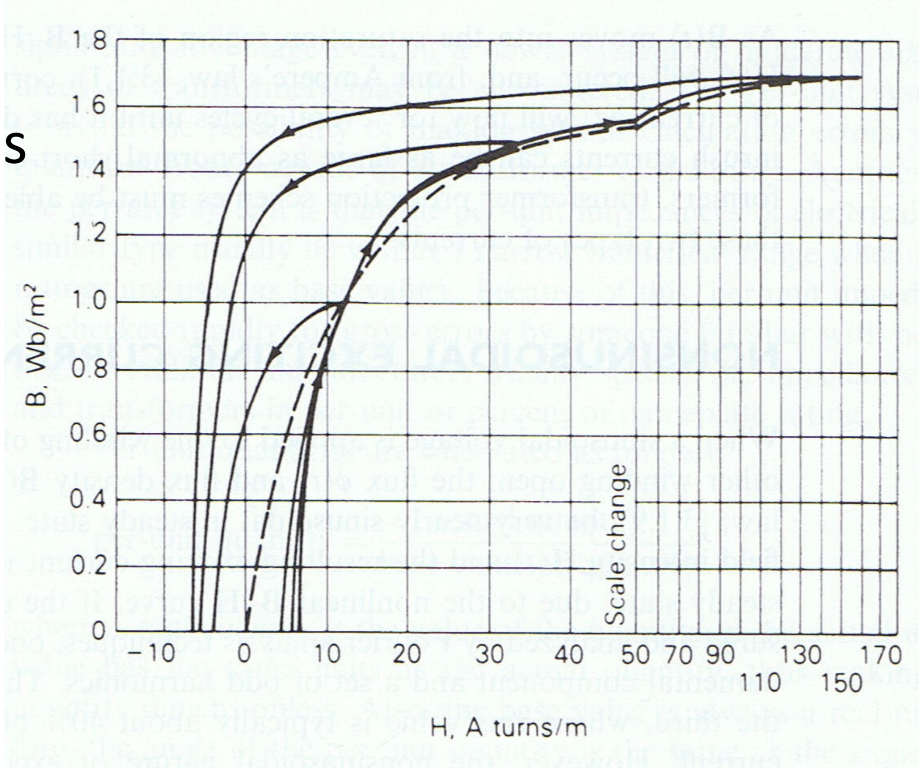
A Simplified Model

- Typically the admittance, Y, is very small i.e. resistance is very large.
- This means that the currents flowing through Z_1 and a^2Z_2 are almost the same.
- We can simply combine Z_1 and a^2Z_2 to "Z_{eq}", the equivalent series impedance.



Saturation

- In practical transformer model, we assume **a constant core permeability** thus linear relationship between B and H.
- In fact, the B-H curve for ferromagnetic materials used for transformer core is nonlinear and has multiple values.
- As H increases, the core become **saturated** i.e. the magnetic flux density B increase at a much lower rate.
- This means that there will be high magnetizing current flow making the transformer to heat up.
- This effect is **NOT included** in the equivalent circuit.



B-H curve is approximated by a dashed line.

$B = \mu H$

B = Magnetic flux density (Weber/m² or Tesla)

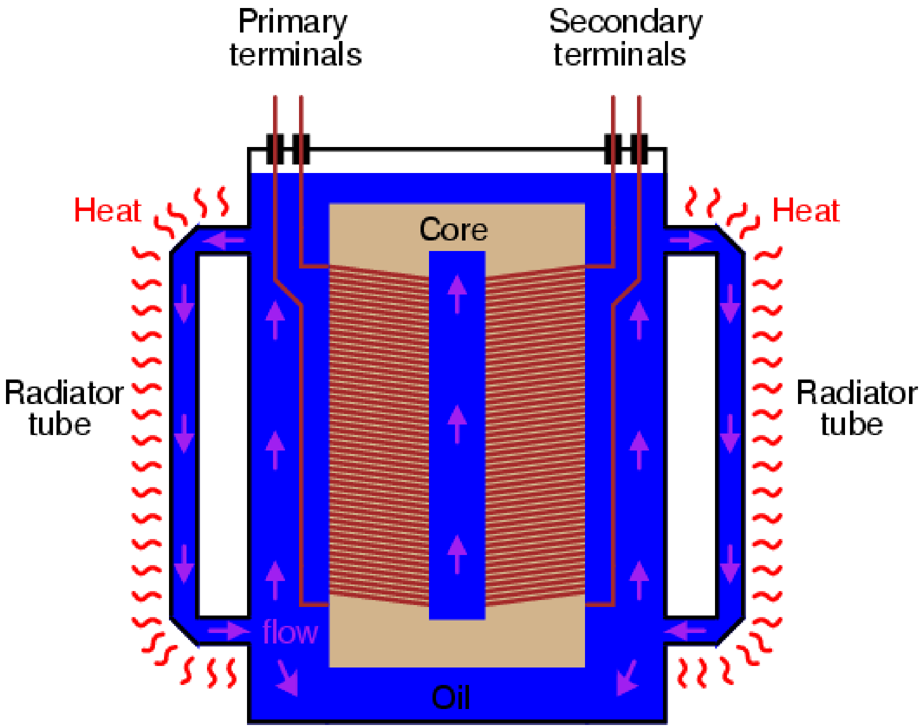
H = Magnetic field intensity (A/m)

μ = Magnetic core permeability (H/m)

Transformer Heating

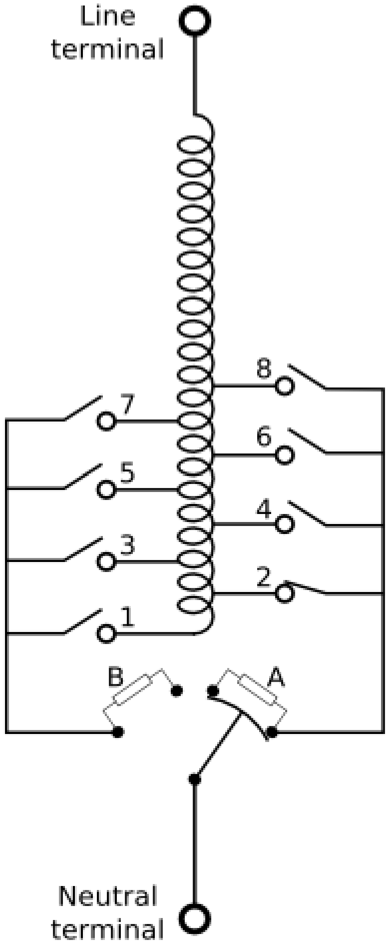
- Heating is caused by high loading of the transformer, eddy current losses, saturation.
- Heating can lead to winding insulation damage, short circuit, and even explosion.
- In order to prevent overheating, transformers are usually cooled by a fan and a convection oil to reduce heat inside the iron core.

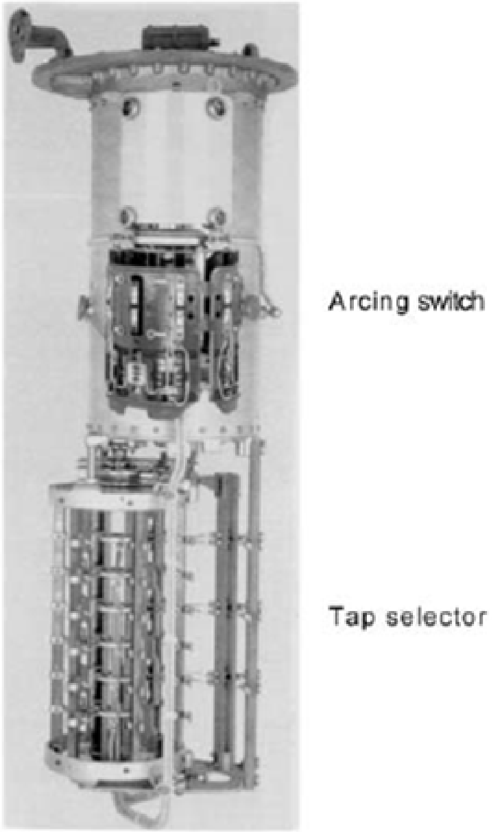
Source: abb.com



Source: http://openbookproject.net/electricCircuits/AC/AC_9.html

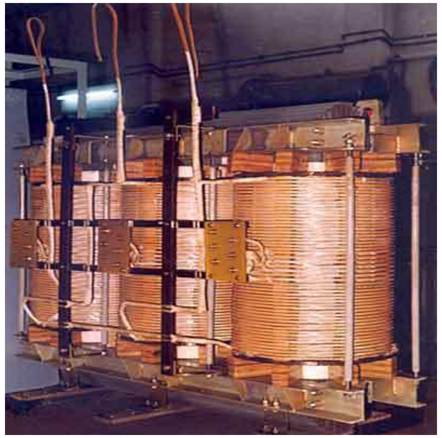
Tap Changing Transformer





Online

- Transformers with tap changer are used to adjust the voltage by changing the turns ratio.
- Tap-changing transformers are used to regulate the voltage at the end users to be at the desired value.
- This can be done both off-line and on-line.



Off-line

Source: http://en.wikipedia.org/wiki/Tap_%28transformer%29
http://www.powertransformerdesign.net

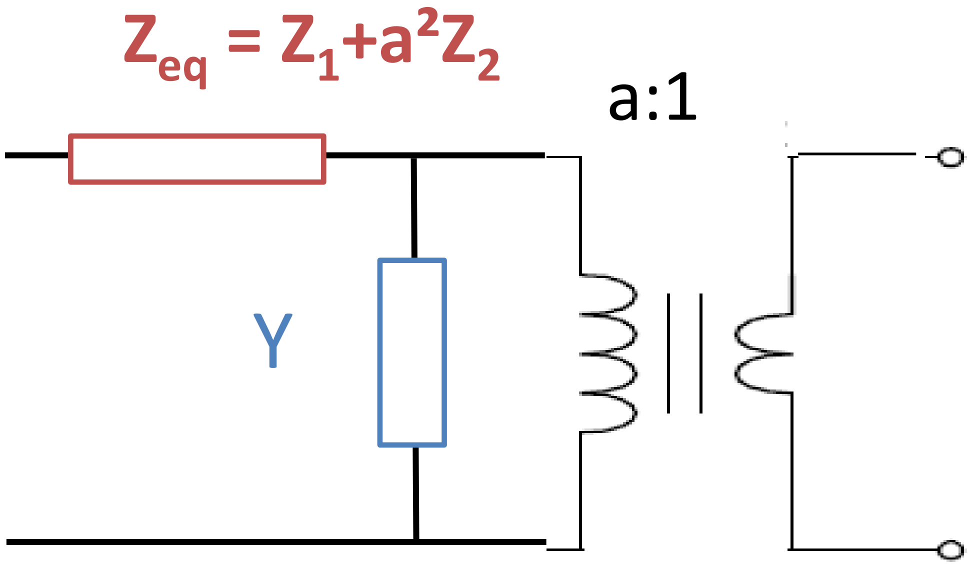
Short-circuit test

Open-circuit test

TRANSFORMER PARAMETER TESTS

Transformer Parameters

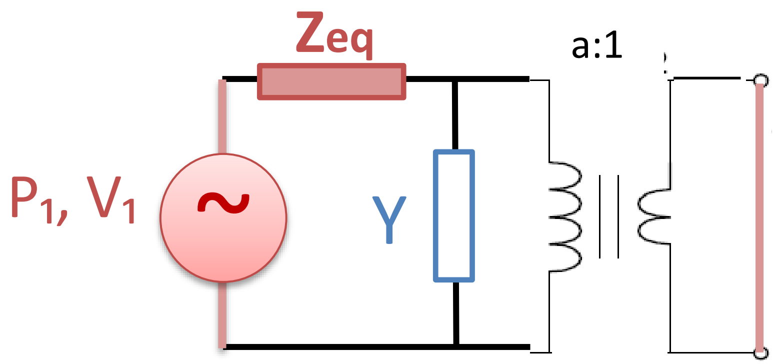
- Series impedance
  - Z_1 and Z_2 are series impedances representing the resistive loss and flux linkage loss in the two windings.
- Shunt admittance
  - Y is a shut admittance representing iron core loss and magnetizing susceptance.



Note that by convention, the primary side of a transformer is the side with a higher number of turns. This means that a > 1.

Short-Circuit Test

- To find equivalent series impedance.
- Short circuit the *secondary* side.
- Apply **rated current** (implies small voltage) at the primary side.
- Measure real power and voltage at the primary side.

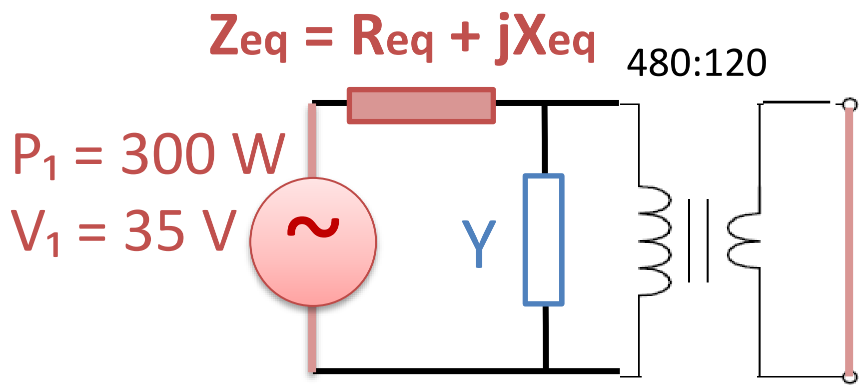


Note that we want small voltage applied to the primary side so that there will be large amount of current passing through the impedance. This will allow more accurate calculation of the series impedance

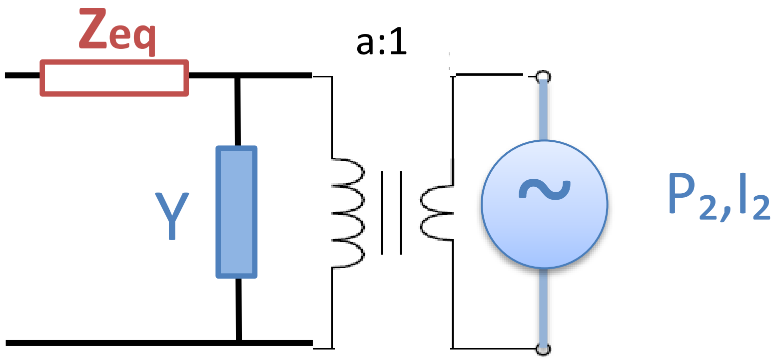
Short-Circuit Test

Example 4: Short Circuit Test

Consider a single-phase 20kVA, 480/120 V 60 Hz transformer. During short circuit test, rated current is applied to the primary side. The voltage of **35 V** and real power of **300 W** are measured. Find equivalent series impedance of this transformer.



Open-Circuit Test



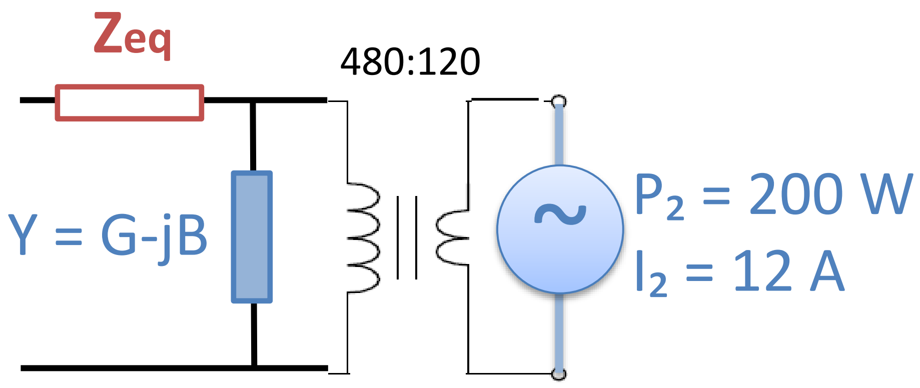
Note that we want rated voltage at the secondary side so that there will be large amount of current passing through the admittance Y (I=YV). This will allow more accurate calculation of the shunt admittance.

- To find equivalent shunt admittance.
- Open circuit the *primary* side.
- Apply **rated voltage** at the secondary side.
- Measure real power and current at the secondary side.

Open-Circuit Test

Example 5: Open Circuit Test

Consider the same transformer as Example 2. During open circuit test: rated voltage applied to secondary side, then $\mathbf{I_2 = 12\ A}$ and $\mathbf{P_2 = 200\ W}$. Find equivalent shunt admittance Y of this transformer.



QUESTIONS