EE2029 - Introduction to Electrical Energy Systems (Solution for Tutorial #2 on AC Power)

Solution Q.1

$$Z_R = 25 \Omega$$

$$Z_C = -j \frac{1}{377 \times 100 \times 10^{-6}} = -j26.52 \,\Omega$$

$$Z_{Load} = \left(\frac{1}{25} + \frac{1}{-j26.52}\right)^{-1} = 18.19 \angle -43.31^{\circ}$$

Total impedance seen by the source Z_{total} = 1 + 18.19 \angle - 43.31 o = 18.93 \angle - 41.23 $^o\Omega$

Current drawn from the source $I = \frac{230 \angle 0^o}{18.93 \angle -41.23^o} = 12.15 \angle 41.23^o A$

Load voltage $V_{load}=V_s-I\times Z_{line}=230\angle 0^o-12.15\angle 41.23^o\times 1=221\angle -2.075^o$ V

Complex power delivered to the load $S_{load}=V_{load}I^*=221 \angle -2.075^o \times 12.15 \angle -41.23^o=2685.15 \angle -43.31^o$ VA

Apparent power delivered to load $|S_{laod}| = 2685.15 VA$

Power factor of the load = $\cos(-43.31^{\circ}) = 0.728$ leading

Apparent power supplied by the source = $230 \times 12.15 = 2794.5 VA$

Solution Q.2

Current drawn by the load
$$|I_{old}| = \frac{P}{|V| \times (Power factor)} = \frac{25000}{500 \times 0.5} = 100 \text{ A}$$

$$\cos \theta = 0.5 \rightarrow \theta = \cos^{-1}(0.5) = 60^{\circ}$$

Current phasor $I = 100 \angle -60^{\circ}$ A

Complex power of the load $S_{old} = VI^* = 500 \times 100 \angle 60^\circ = 50000 \angle 60^\circ$ VA

$$Q_{old} = 50000 \sin(60^{o}) = 43301 \, VAr$$

After connecting the capacitor in parallel, new power factor =0.95 lagging

Current drawn from source
$$|I_{new}| = \frac{P}{|V| \times (Power factor)} = \frac{25000}{500 \times 0.95} = 52.63 \text{ A}$$

$$\cos \theta' = 0.5 \rightarrow \theta' = \cos^{-1}(0.95) = 18.19^{\circ}$$

Complex power drawn from the source $S_{new} = VI_{new}^* = 500 \times 52.63 \angle 18.19^o = 24999.95 + j8214.73 \text{ VA}$

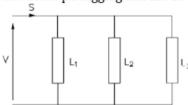
$$Q_{new} = 8214.73 \, VAr$$

Reactive power supplied by the capacitor $Q_C = 8214.73 - 43301 = -35086.27 \text{ VAr}$

The required capacitor value
$$C = \frac{Q_C}{\omega |V|^2} = \frac{35086.27}{2\pi \times 50 \times 500^2} = 446.73 \mu F$$

Solution Q3:

L1: 5 kW at 0.8 p.f. lagging, L2: 10 kW at 0.6 p.f. lagging and L3: 15 kW at 0.8 p.f. leading



The complex power consumption of the loads are computed as follows:

$$P_1 = |S_1| \times 0.8$$

 $|S_1| = 6250 \text{ VA}$
 $S_1 = 6250 \angle 36.87^\circ = 5000 + j3750$
 $P_2 = |S_2| \times 0.6$
 $|S_2| = 16666.67 \text{ VA}$
 $S_2 = 16666.67 \angle 53.13^\circ = 10000 + j13333.33$
 $P_3 = |S_3| \times 0.8$
 $|S_3| = 18750 \text{ VA}$
 $S_3 = 18750 \angle -36.87^\circ = 15000 - j11250$

Hence, overall power factor as seen by the source can be calculated as:

$$S = S_1 + S_2 + S_3$$

= 30000 + j5833.33
= 30561.87/11° VA
p.f. = $cos 11^\circ = 0.982$ lagging

Solution Q4:

As the power delivered is 10kW at 0.5 p.f. lagging,

$$|I| = \frac{P}{V\cos\phi} = \frac{10000}{200 \times 0.5} = 100 \text{ A}$$

 $I = 100/60^{\circ} = 50 - i86 \text{ 6 A}$

When a capacitor of $1000\mu F$ is connected across the supply, the capacitor current is

$$I_C = j\omega CV = j314 \times 1000 \times 10^{-6} \times 200 = j62.8 \text{ A}$$

So the total current drawn from the supply is

$$I_T = I + I_C = 50 - j23.8 = 55.38 \angle -25.45^{\circ}$$

The power factor as seen by the source is

p.f. =
$$cos(25.45^{\circ}) = 0.902$$
 lagging

Solution Q5:

Current drawn from the substation is

$$|I_1| = \frac{P}{|V|\cos\theta} = \frac{1500 \times 10^3}{500 \times 0.6} = 5000 \text{ A}$$

If the power factor could be improved to unity, then current drawn would be

$$|I_2| = \frac{P}{|V|\cos\theta} = \frac{1500 \times 10^3}{500 \times 1.0} = 3000 \text{ A}$$

The transmission line losses in both the cases are

$$P_{loss1} = R |I_1|^2 = 0.005 \times 5000^2 = 125 \text{ kW}$$

$$P_{loss2} = R |I_2|^2 = 0.005 \times 3000^2 = 45 \text{ kW}$$

So, cost of energy wasted will be high in the first case.

This example illustrates that for the same real power demand, if the power factor of the load decreases, then |I| increases, resulting in heavy transmission line losses.

A poor power factor results in higher current and hence higher power loss.