

Sizing of Electric Motors for Variable Speed Drive Applications



Learning Objectives and Outcomes

- Learning Objectives:

- Understand how to choose power rating of an electric motor optimally.
- Understand different types of losses in electrical machines: **constant losses** and **variable losses**.
- Understand what is meant by **thermal loading** of an electrical machine.
- Understand **loading capacity** of an electrical machine.
- Understand different types of **time constants** in an electric drive system.

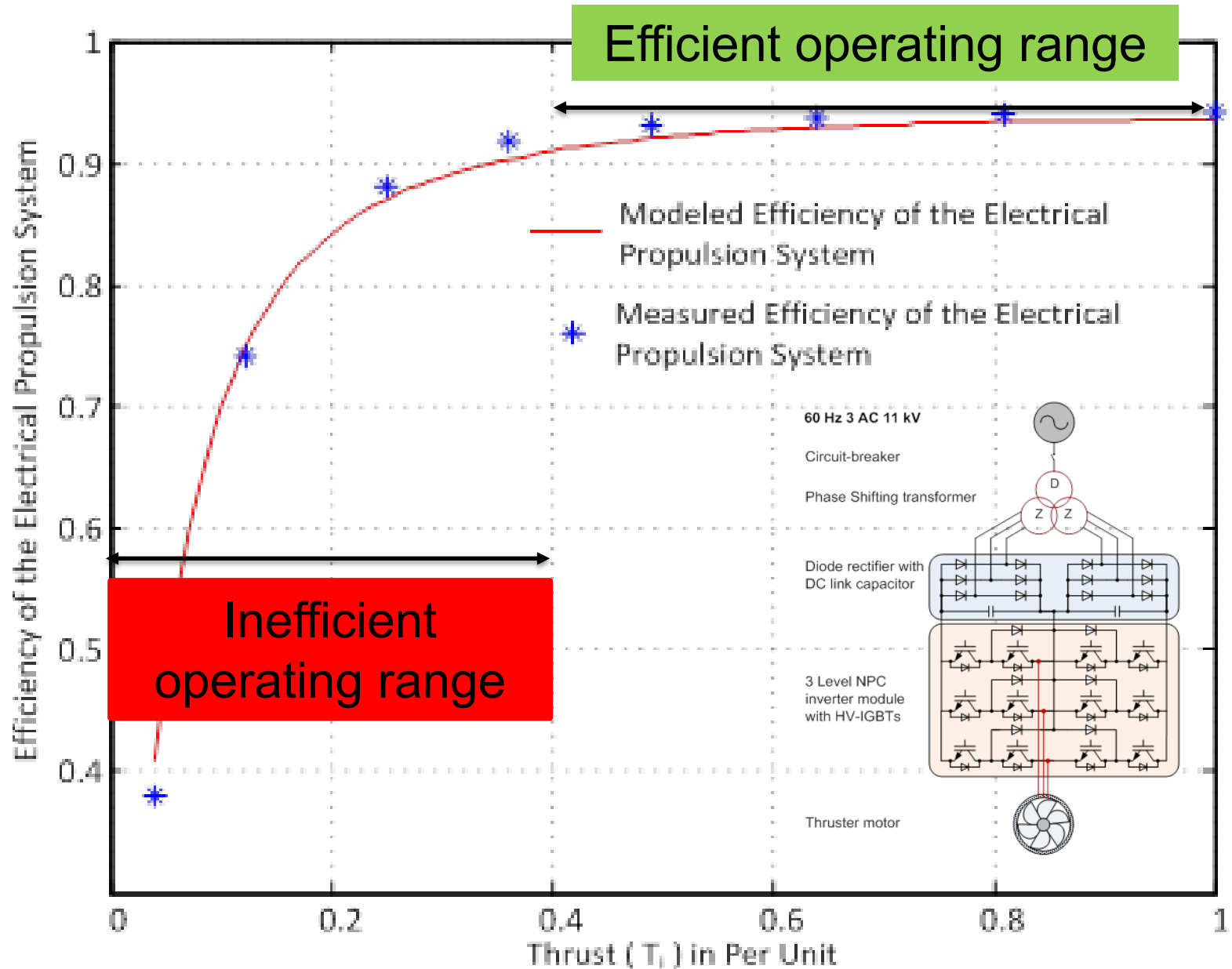
- Learning outcome

- You should be able to **specify the right sizing (power rating) of an electrical machine** for a given application and the type of the electrical machine to be used.

Selection of Motor Power Rating

- Power rating of an electric motor must be chosen carefully to make a balance between cost and reliability.
- Motors must satisfy requirements such as:
 - provide suitable torque-speed characteristics to match that of the load,
 - provide adequate output power on a sustained basis,
 - under full-load condition steady-state temperature rise of the motor windings and core must be within acceptable limit, and

- must be capable of withstanding short-term overload and have enough torque to start and accelerate the drive system from rest.
- What happens if the motor chosen is under-rated ?
 - it fails to drive the load at nominal power or
 - lowers the productivity and reliability of the drive system.
- Alternatively, if the motor chosen is over-rated ?
 - it is expensive and
 - it runs inefficiently due to operation at reduced loading.



Power Losses and Heating of Electric Motors

- During motoring operation, losses are produced which cause **winding temperature** to rise and subsequently heat is dissipated to the surrounding medium.
- Losses : **constant** and **variable** (copper) losses.

$$p = p_c + x^2 p_v \quad (2.1)$$

where p - **total loss**, p_c - **constant loss**, p_v - **variable loss at rated load** and x - **percentage of motor load in terms of rated load**.

- **Losses** \Rightarrow **temperature rise** \Rightarrow **heat outflows** \Rightarrow thermal equilibrium is reached (**heat produced = heat dissipated**, i.e. absolute temperature remains constant).
- At thermal equilibrium, temperature-rise reaches a steady-state value and is dependent on the total power loss, p which in turn is a **function** of the output power, P_{out} of the machine.
- The temperature rise of the machine has a direct relationship with the output power, P_{out} and is referred to as **thermal loading** of the machine.

- Steady-state temperature rise must always be maintained within acceptable limit of the winding insulating materials.
- Depending on the temperature rise limit, insulating materials used for windings are:
 - Class A: 105° C – cotton, synthetic, paper;
 - Class B: 130° C – resin;
 - Class H: 180° C – glass fibre, silicone rubber etc.
- Electrical machines have sufficient overload capability but thermal restriction **does not allow continuous overloading** - because losses ($p_{loss} \propto i^2$) rise more steeply than output power ($P_{out} \propto i$).

- Time lag due to thermal time constant between losses taking place and the resulting temperature rise - allows overloading of motors for short periods (of the order of few minutes) only.
- For loads operating at constant torque and speed it is easy to calculate rated output power rating of the motor ($P_{rated, output} = T_{em, rated} \times \omega_{m, rated}$).
- However, most of the motors operate with variable load (torque) and speed - it becomes difficult to calculate the power rating of the motor for such applications.

- The main objectives of our study in this chapter are:
 - to obtain a suitable thermal model of the electrical machine;
 - to categorize various types of loading into some standard form, and
 - to present methods for calculating motor power rating for various classes of duty (loading of the motor).

Thermal Model of Motor for Heating and Cooling

- Accurate prediction of heat flow and temperature distribution within the machine is very complex and extremely difficult to represent analytically.
- A simple thermal model may be obtained by assuming the machine as a homogeneous body having a uniform temperature gradient.
- Heat dissipation is assumed to be proportional to the **temperature difference** between the machine and the surrounding medium.

Heating Curve

- Let the electrical machine be considered as a homogeneous body and the cooling medium have the following parameters at any time t :

p_1 = heat developed, joule/s or watts,

p_2 = heat dissipated to the cooling medium, joule/s (W)

W = weight of the active part of the machine, kg,

h = specific heat, joule/kg/°C,

A = area of the cooling surface, m²,

d = coefficient of heat transfer, joule/s/m² °C,

θ = mean temperature rise, °C, (above ambient)

$C = W \times h$ = thermal capacity of the machine, joule /°C,

$D = d \times A$ = heat dissipation constant, watts /°C

- During a time increment dt , let the machine temperature rise (above ambient) be $d\theta$.
- The heat balance equation is given by:

$$\left[\begin{array}{c} \text{Heat} \\ \text{developed} \\ \text{in the} \\ \text{machine} \end{array} \right] = \left[\begin{array}{c} \text{Heat} \\ \text{dissipated} \\ \text{to the} \\ \text{surrounding} \\ \text{cooling medium} \end{array} \right] + \left[\begin{array}{c} \text{Heat} \\ \text{absorbed} \\ \text{or stored} \\ \text{in the} \\ \text{machine} \end{array} \right] \quad (2.2)$$

$$p_1 dt = p_2 dt + C d\theta$$

$$\frac{d\theta}{dt} + \frac{p_2}{C} = \frac{p_1}{C} [p_2 = (d \times A) \times \theta = D \times \theta]$$

$$\frac{d\theta}{dt} + \frac{D}{C} \theta = \frac{p_1}{C} \Rightarrow \frac{C}{D} \frac{d\theta}{dt} + \theta = \frac{p_1}{D}$$

$$\tau \frac{d\theta}{dt} + \theta = \theta_{ss} \quad (2.3)$$

$$\Rightarrow \theta(t) = \theta_{ss} (1 - e^{-t/\tau}) + \theta_1 e^{-t/\tau} \quad (2.4)$$

- where $\tau = C/D$, heating time constant,
- θ_1 - initial temperature rise and
- $\theta_{ss} (= p_1/D)$ - steady-state temperature rise.

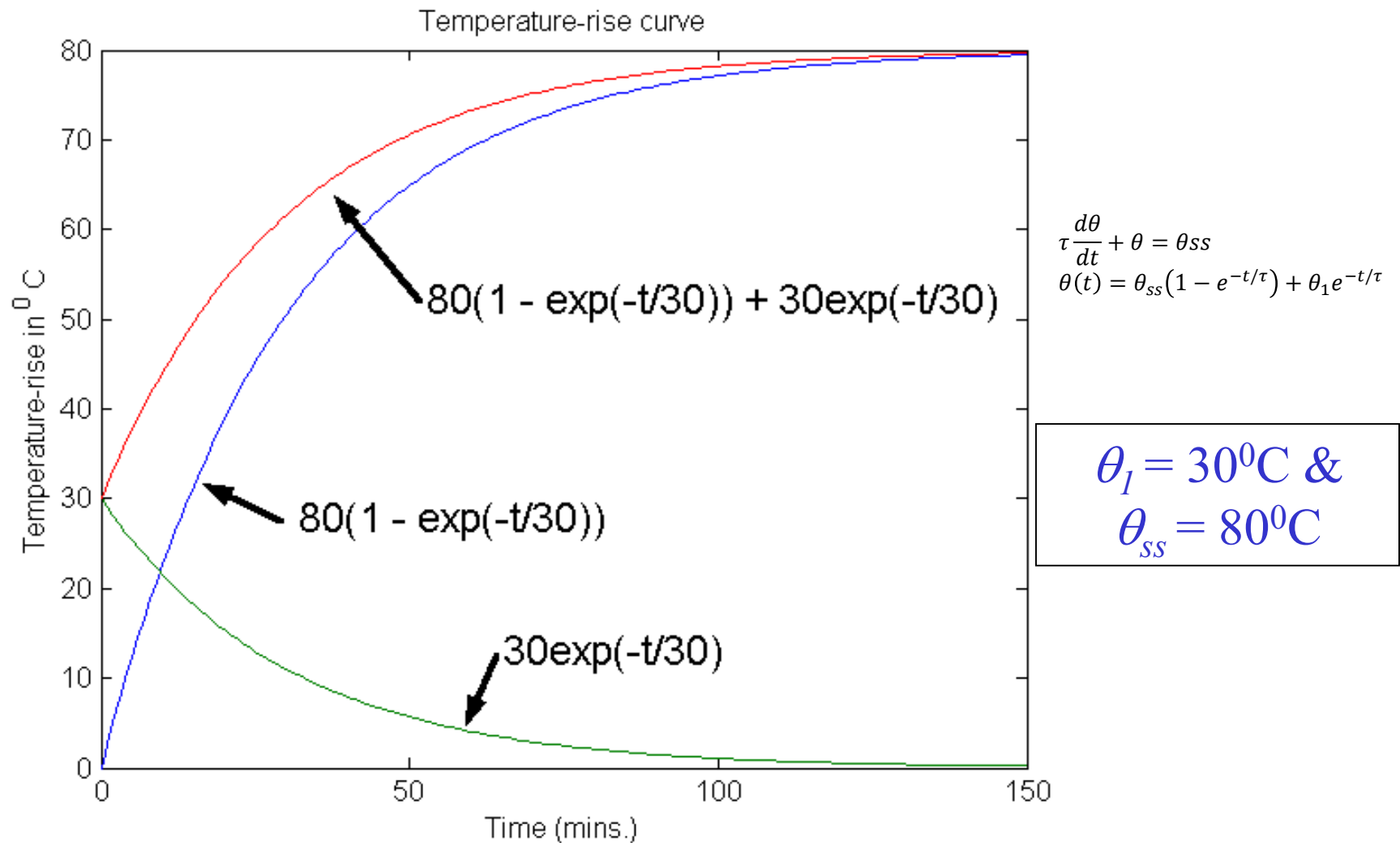


Figure 2.1: Heating temperature-rise curve of an electric motor.

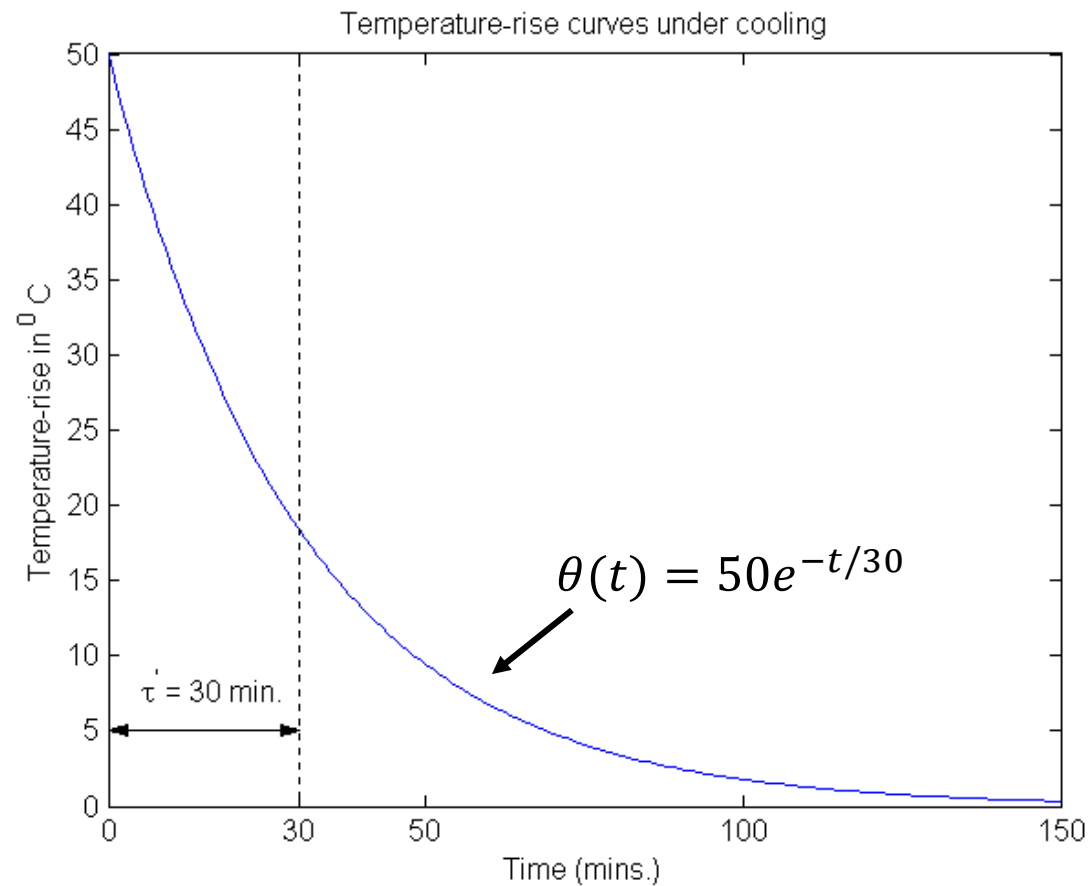
Cooling Curve

- When the machine is **switched off**, no heat is generated ($p_1 = 0$) - machine **cools down** and the temperature rise reduces to the **ambient temperature**.
- Heat balance equation 2.2:

$$0 = p_2 dt + C d\theta \rightarrow \frac{d\theta}{dt} + \frac{D'}{C} \theta = 0 \rightarrow \frac{C}{D'} \frac{d\theta}{dt} + \theta = 0 \quad (2.5)$$

$$\Rightarrow \theta(t) = \theta_2 e^{-t/\tau'} \quad (2.6)$$

where $\tau' = C/D'$ time constant during cooling and θ_2 – initial temperature rise, $D' = d' \times A$ – heat dissipation constant being different during cooling.



$$\theta_2 = 50^{\circ}\text{C}$$

Figure 2.2: Cooling curve of an electric motor switched off from the mains.

- Assume that load on the electrical machine is **reduced rather than switched off completely** so that $(p_1 > p_1' \neq 0)$.
- This causes cooling of the machine and let the new value of the heat dissipation constant be D' .

$$\frac{d\theta}{dt} + \frac{D'}{C} \theta = \frac{p_1'}{C} \rightarrow \frac{C}{D'} \frac{d\theta}{dt} + \theta = \frac{p_1'}{D'} \quad (2.7)$$

$$\Rightarrow \theta(t) = \theta'_{ss} \left(1 - e^{-\frac{t}{\tau'}}\right) + \theta_2 e^{-\frac{t}{\tau'}} \quad (2.8)$$

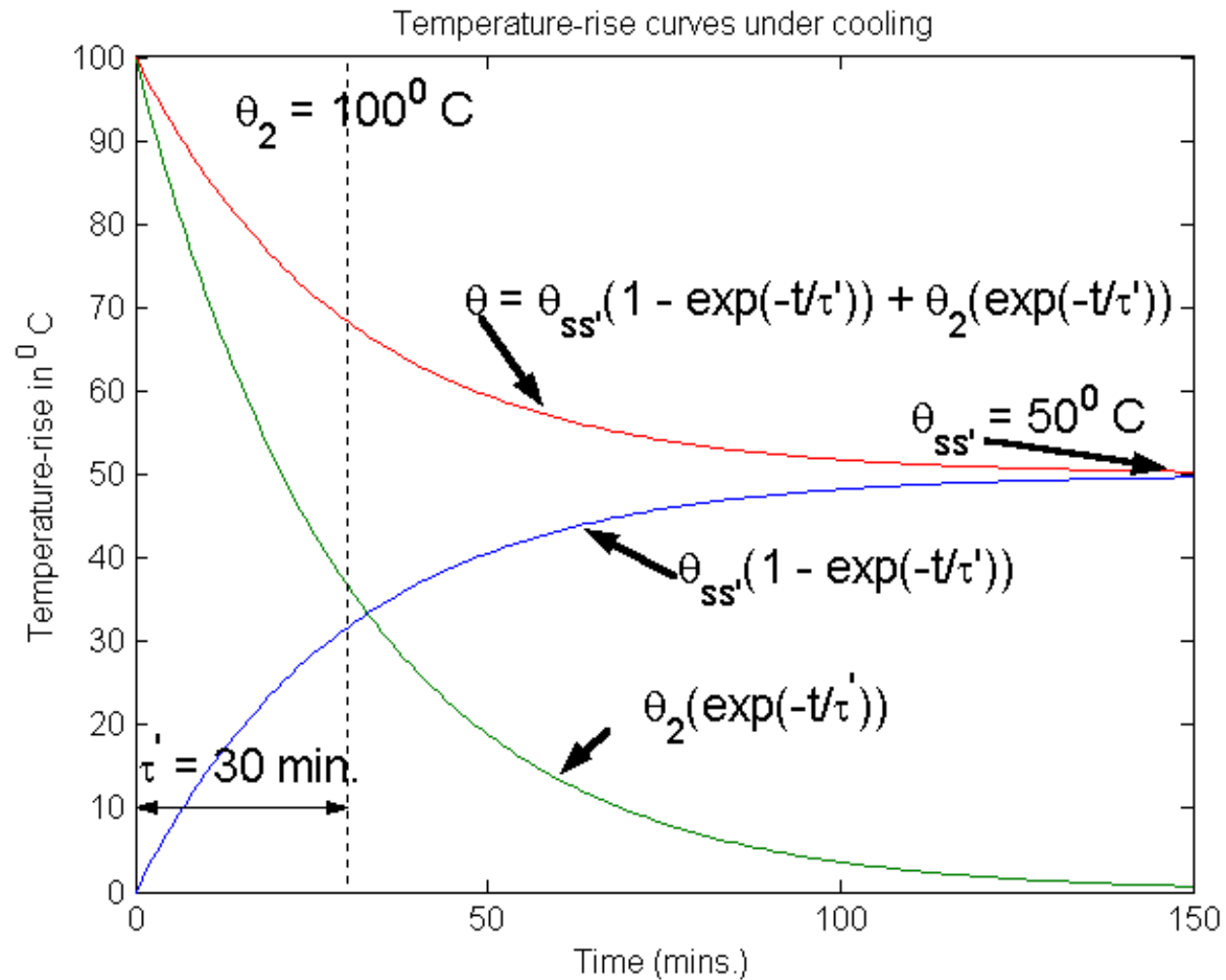


Figure 2.3: Cooling curve of an electric motor when the load is reduced but not equal to zero.

- If machine is **switched-off** from the mains supply completely then $p'_1 = 0$ and eqn. 2.8 reduces to:

$$\theta(t) = \theta_2 e^{-t/\tau'} \quad (2.9)$$

- Cooling curve shown in Fig. 2.3 can be considered as the sum of two curves:
 - heating curve as if the machine is loaded to give a maximum temperature rise of θ'_{ss} (first term of the RHS of eqn. 2.8) and
 - cooling curve as if the machine is disconnected from the mains supply when the temperature rise is θ_2 (second term of the RHS of eqn. 2.8).

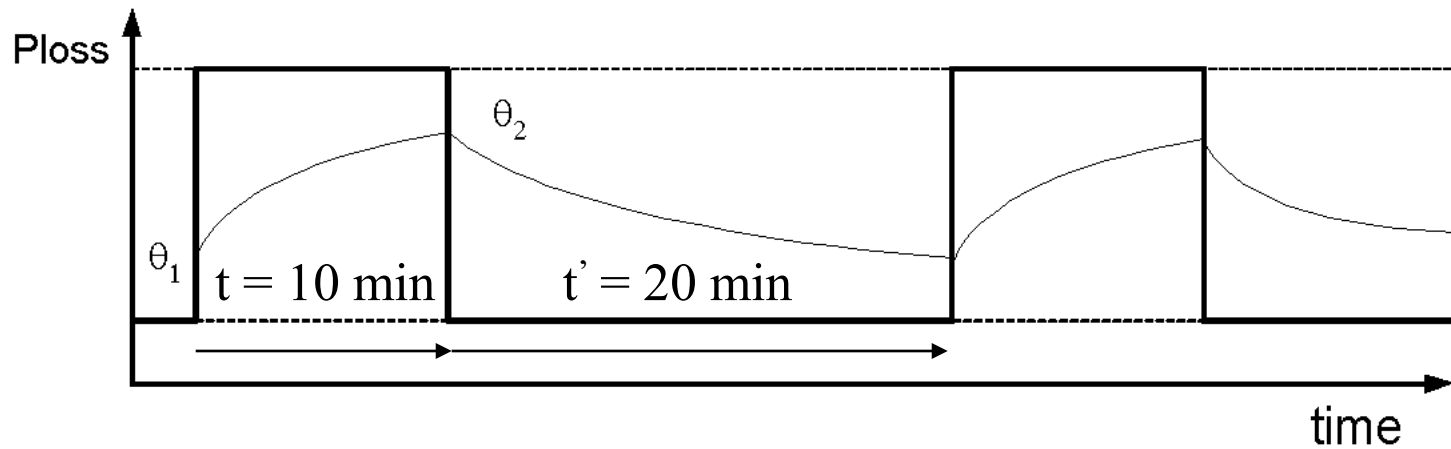
- In **self-cooled** machines heating time constant τ and cooling time constant τ' are different and it depends on the respective **heat dissipation constant, D** .
- **Thermal time constant** (of the order of mins.) is much higher usually order of magnitude larger than the **mechanical time constant** (sec), which is again order of magnitude higher than the **electrical time constant** (ms).

Electrical time constant	Mechanical time constant	Thermal time constant
0.1 – 100 ms	10 ms – 10 s	10 min – 60 min.

Example 2.1: A motor operates in a **periodic duty cycle** in which it is clutched (connected) to its load for 10 min. and de-clutched to run on no-load for 20 min. Minimum temperature rise is 40°C . Assume that heating and cooling time constants are equal and have value of 60 min. When load is de-clutched continuously the temperature rise is 15°C .

Determine:

- (a) maximum temperature during the duty cycle, and
- (b) temperature when the load is clutched continuously.



Solution: We have $\tau = \tau' = 60 \text{ min}$, $\theta_1 = 40^\circ\text{C}$, $\theta'_{ss} = 15^\circ\text{C}$.

We have $\theta_2 = 49.9^\circ\text{C}$, $\theta_{ss} = 104.5^\circ\text{C}$.

Classes of Motor Duty

- Various categories of load-time variations can be grouped into the following classes:
 - Continuous running duty
 - Short-time duty
 - Intermittent periodic duty
 - Intermittent periodic duty with high start-up torque
 - Intermittent periodic duty with high start-up torque and electrical braking

Continuous Duty

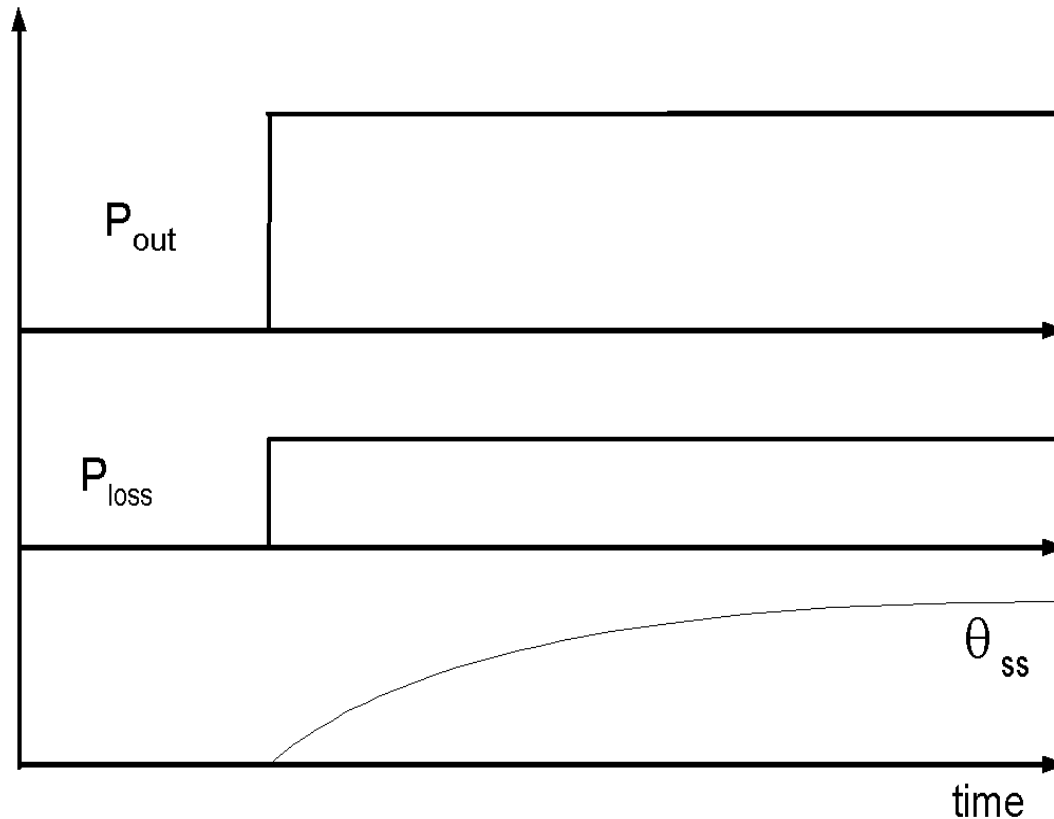


Figure 2.4: Continuous duty of a motor delivering the rated (constant) load.

- Examples - centrifugal pumps, fans and conveyors.

Short Time Duty

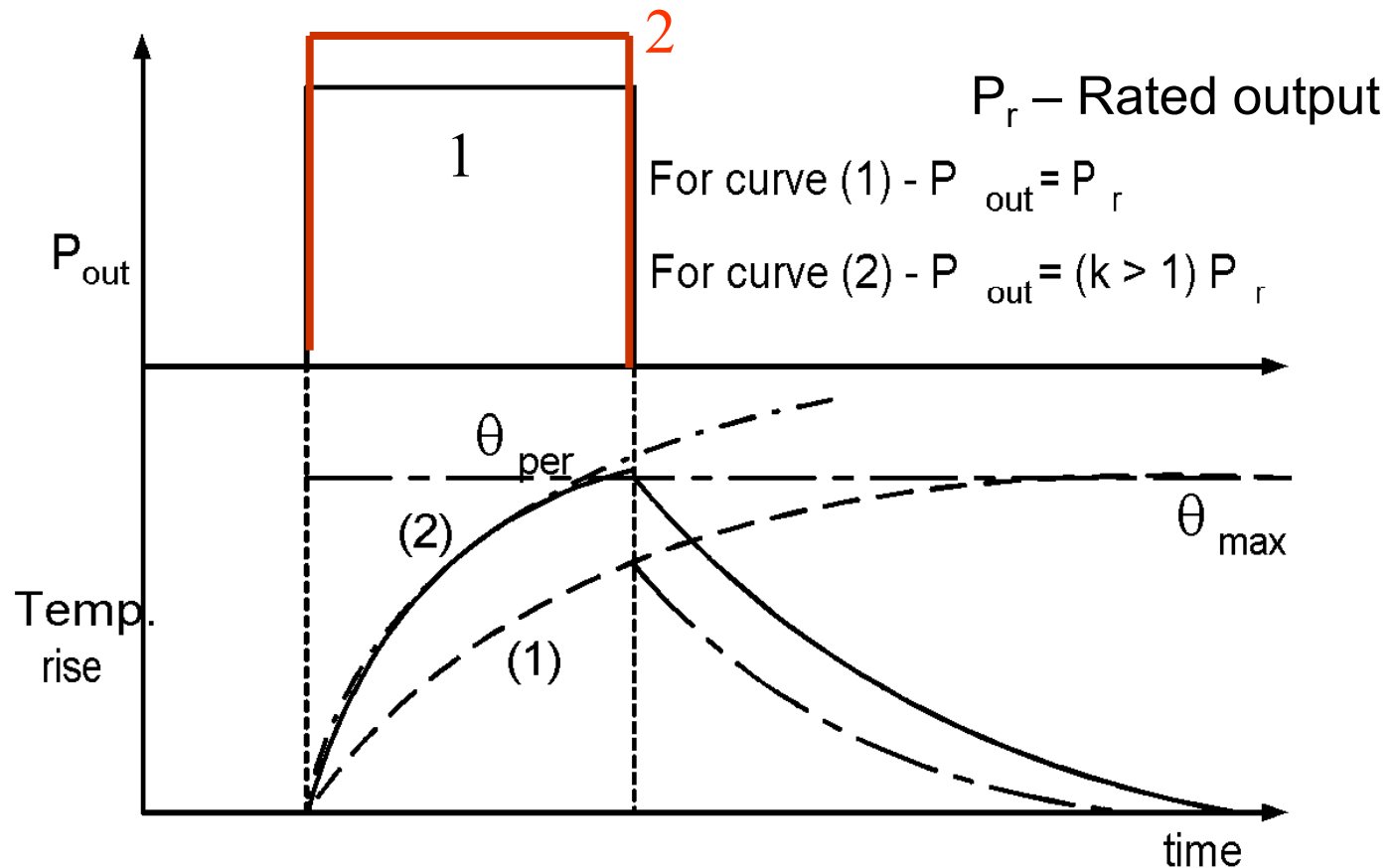


Figure 2.6: Short time duty of a motor (a) load diagram and (b) temperature rise curve.

- Examples - crane drives, household appliances, opening and closing of lock-gates and bridges etc.

Intermittent Periodic Duty

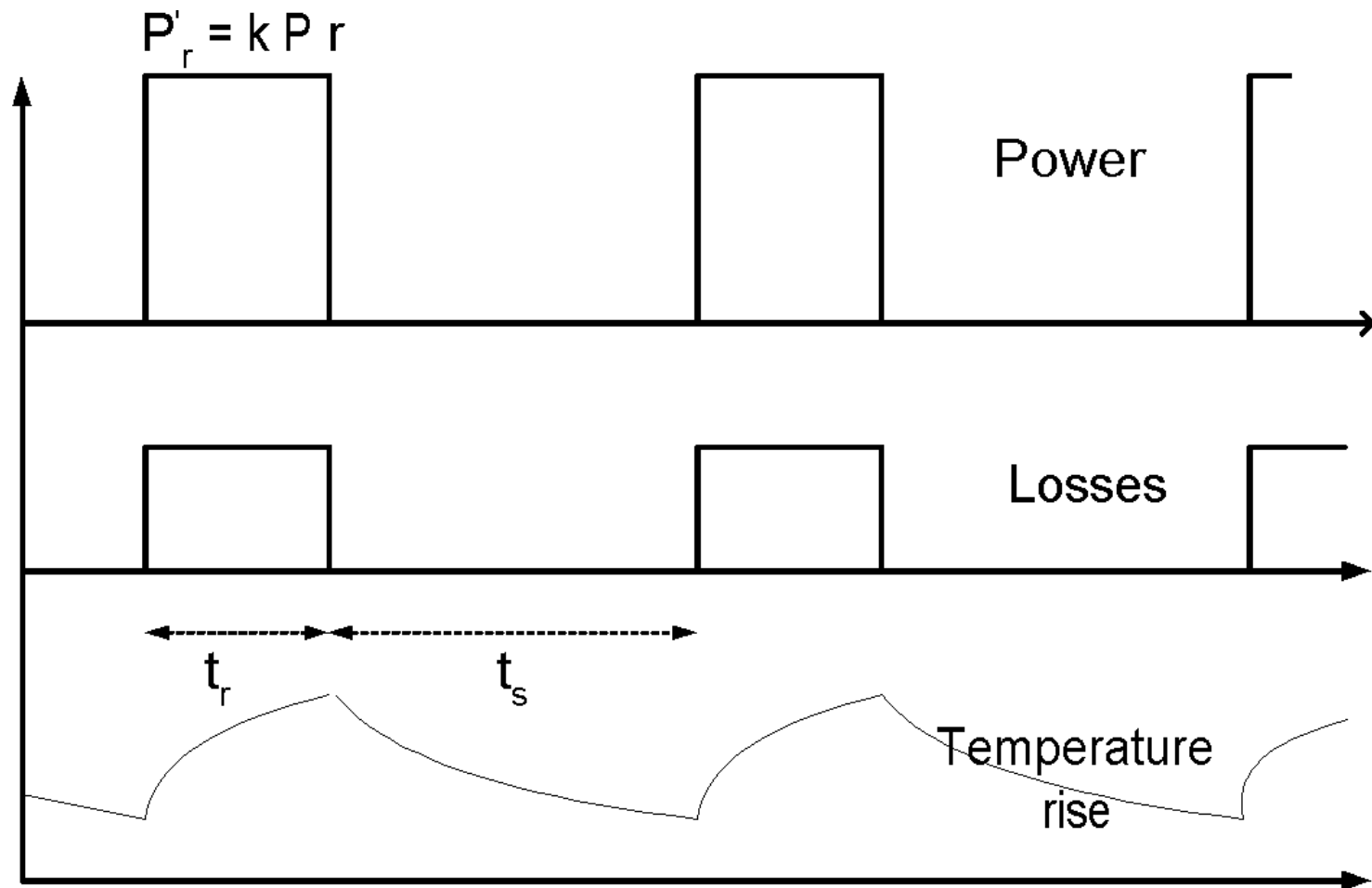


Figure 2.7: Periodic intermittent duty of a motor.

Intermittent Periodic Duty with High Start-up Torque

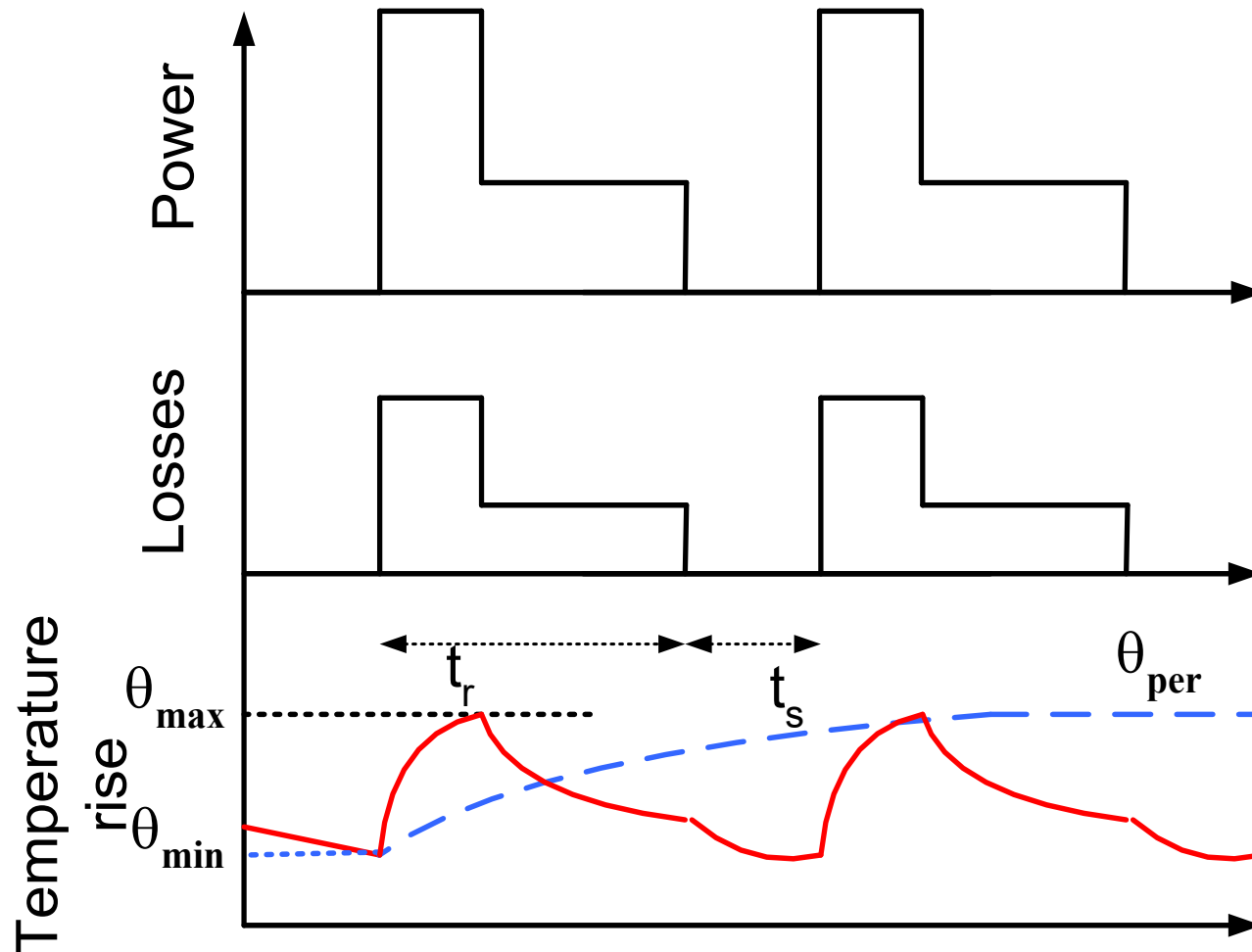


Figure 2.8: Periodic intermittent duty with starting.

Intermittent Periodic Duty with High Start-up Torque and Braking

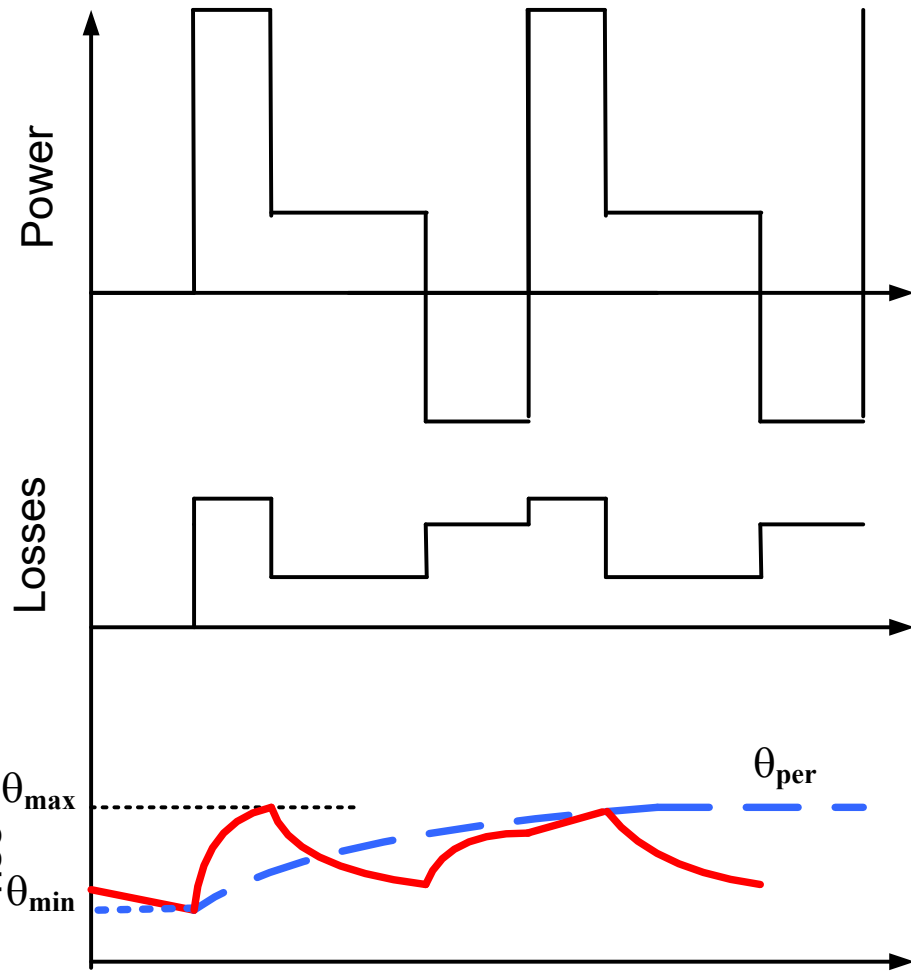


Figure 2.9: Periodic intermittent duty with starting and stopping.

Determination of Motor Power Rating

▪ Continuous Duty

- continuous duty with constant load
- continuous duty with variable load cycles

• Continuous Duty with Constant Load Cycle

- Selection of the motor rating for this type of load is straight forward.
- The maximum load (power) requirement is found and then a motor with power rating slightly higher than that of the load is chosen.

Continuous Duty – Variable Load Cycle

- The method of equivalent current criterion for selecting a motor rating for variable load is based on the principle that the actual variable i.e. **motor current** is replaced by an equivalent (rms) current i_{eq} which when flows through the motor winding would produce the same amount of motor losses as would be the case with actual motor current.
- The objective is to find i_{eq} for a given variable load (torque or current).

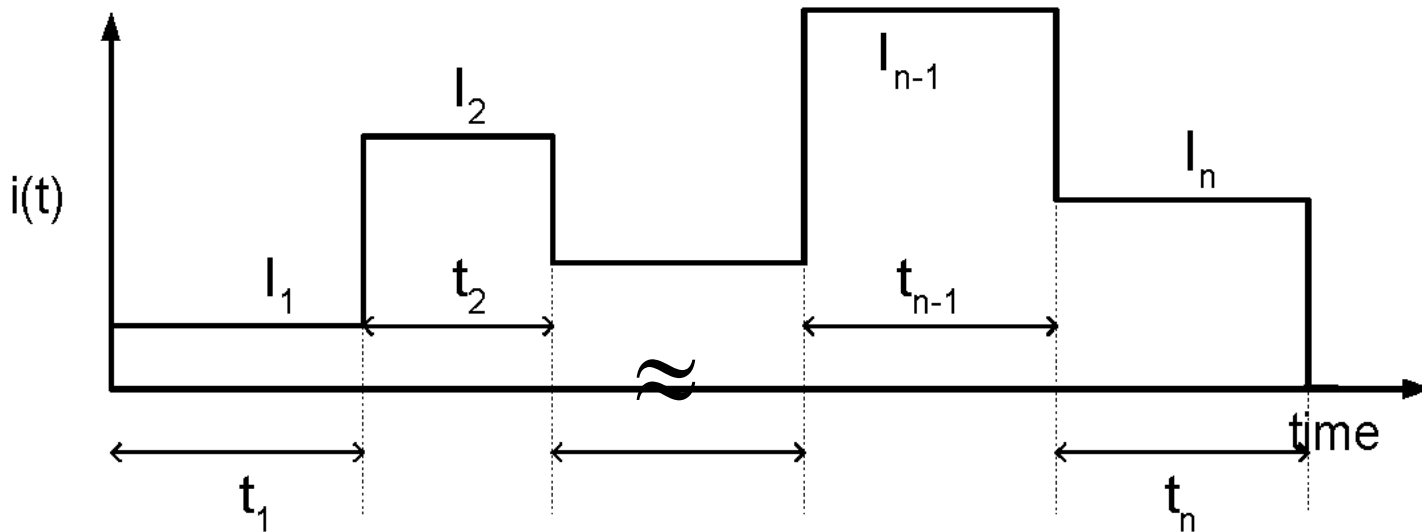


Figure 2.10: Equivalent current criterion for selecting a motor rating for variable load.

- The equivalent (rms) current i_{eq} can be calculated as

$$i_{eq} = \sqrt{\frac{I1,rms^2 \times t1 + I2,rms^2 \times t2 + I3,rms^2 \times t3 + \dots + In,rms^2 \times tn}{t1 + t2 + t3 + \dots + tn}} \quad (2.9)$$

- If the motor torque is directly proportional to the current (DC Motor) we have

$$T_{eq} = \sqrt{\frac{T1^2 \times t1 + T2^2 \times t2 + T3^2 \times t3 + \dots + Tn^2 \times tn}{t1 + t2 + t3 + \dots + tn}} [T = k\phi IA] \quad (2.10)$$

- For constant speed operation we have

$$P_{eq} = \sqrt{\frac{P1^2 \times t1 + P2^2 \times t2 + P3^2 \times t3 + \dots + Pn^2 \times tn}{t1 + t2 + t3 + \dots + tn}} [P = T \times \omega] \quad (2.11)$$

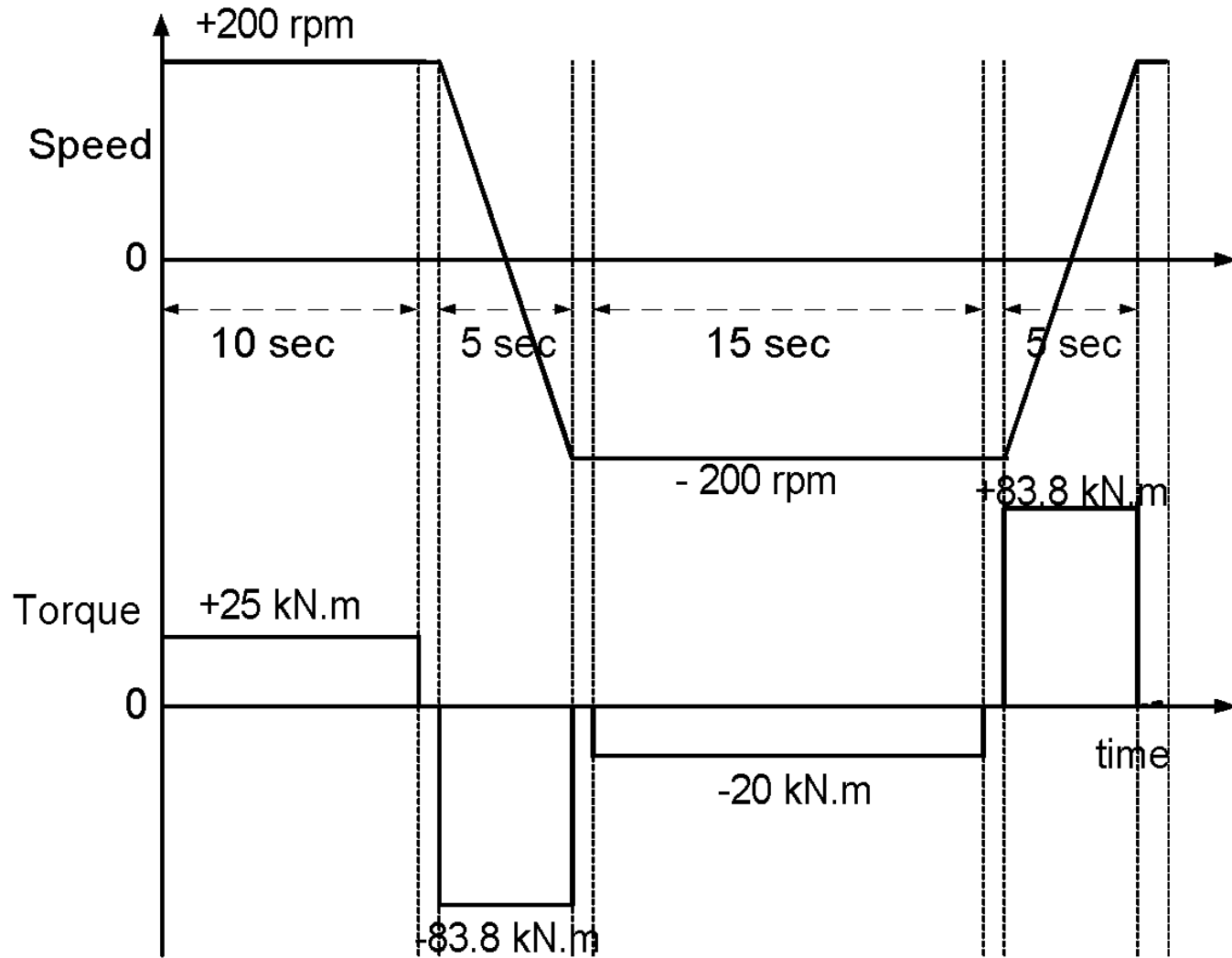
Example 2.2: A rolling mill driven by a thyristor based power converter-fed dc motor operates on a speed reversing duty cycle. Motor field current is maintained constant at the rated value. Moment of inertia referred to the rotor shaft is $10,000 \text{ kg.m}^2$. Duty cycle consists of the following intervals:

- i. Rolling at full speed of 200 rpm and at a constant torque of 25,000 N.m for 10 s.
- ii. No-load operation for 1 s at full speed.
- iii. Speed reversal from 200 rpm to -200 rpm in 5 s.
- iv. No-load operation for 1 s at full speed.
- v. Rolling at full speed and at a torque of 20,000 N.m for 15 s.
- vi. No-load operation at full speed for 1 s.
- vii. Speed reversal from -200 rpm to +200 rpm in 5 s.
- viii. No-load operation at full speed for 1 s.

Determine the torque and power ratings of the motor.

Solution: The duty cycle can be represented as follows:

Speed in RPM	Load torque in N.m	Time in sec.
$N_1 = 200$	$T_{l1} = 25,000$	$t_1 = 10$
$N_2 = 200$	$T_{l2} = 0$	$t_2 = 1$
$N_3 = +200$ to -200	$T_{l3} = 0$	$t_3 = 5$
$N_4 = -200$	$T_{l4} = 0$	$t_4 = 1$
$N_5 = -200$	$T_{l5} = -20,000$	$t_5 = 15$
$N_6 = -200$	$T_{l6} = 0$	$t_6 = 1$
$N_7 = -200$ to $+200$	$T_{l7} = 0$	$t_7 = 5$
$N_8 = +200$	$T_{l8} = 0$	$t_8 = 1$



$$T_{eq} = \sqrt{\frac{(25 \text{ kN.m})^2 \times 10 \text{ sec} + (-83.5 \text{ kN.m})^2 \times 5 \text{ sec} + (-20 \text{ kN.m})^2 \times 15 \text{ sec} + (+83.8 \text{ kN.m}^2) \times 5 \text{ sec}}{10 + 1 + 5 + 1 + 15 + 1 + 5 + 1}} = 49.975 \text{ kN.m}$$

$$T_{eq} = 45,975 \text{ N.m}$$

$$P = T_{rms} \times \omega_m = 45,975 \times \left(\frac{2\pi}{60} \times 200 \right) = 963 \text{ kW}$$

If we compare it with the peak motor power required we have,

$$P_{peak} = 83,776 \times \left(\frac{2\pi}{60} \times 200 \right) = 1755.1 \text{ kW}$$

Actual motor rating is almost half of that of peak power requirement.

Motor Rating under Short Time Duty

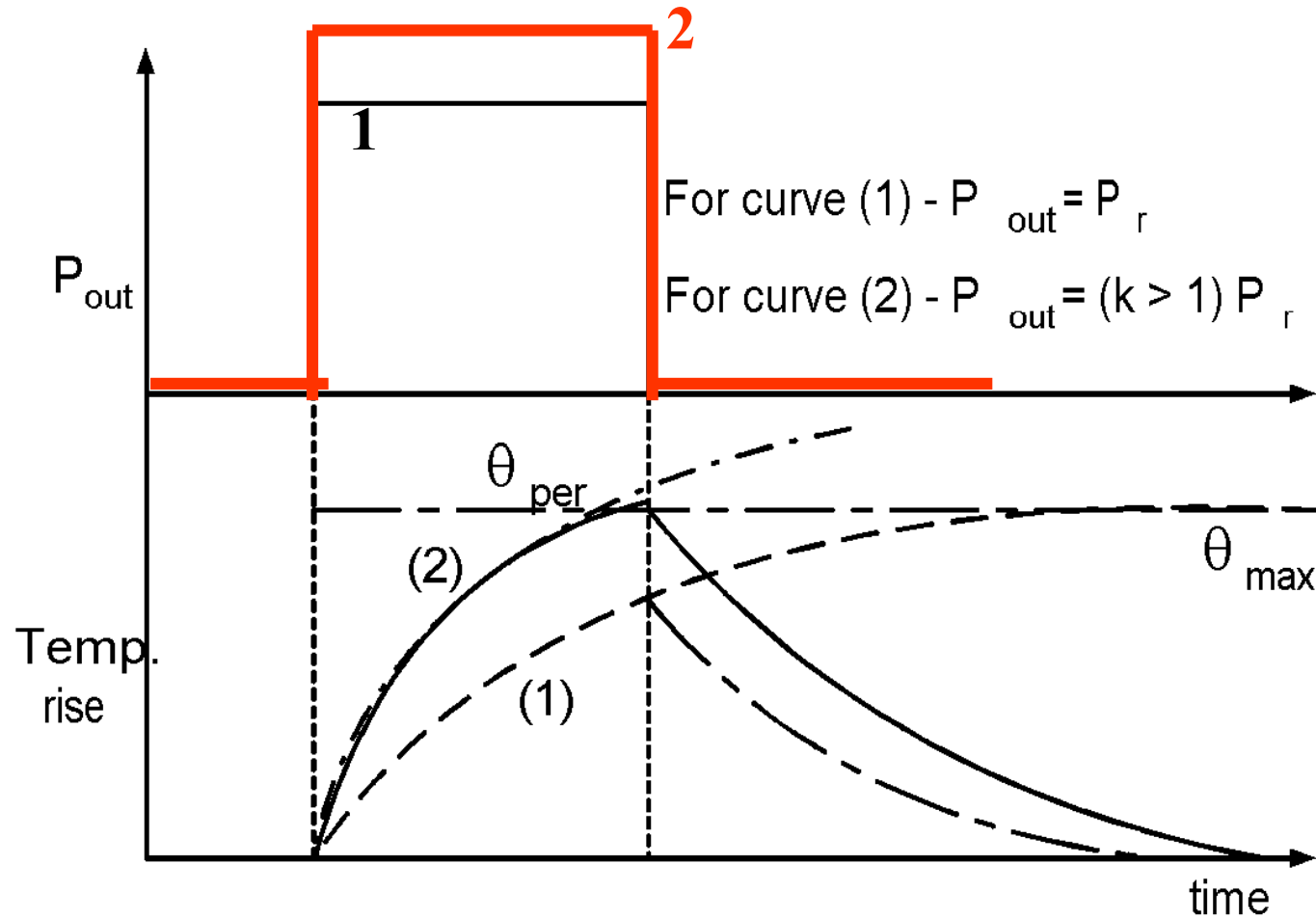


Figure 2.11: Short time duty of a motor (a) load diagram and (b) temperature rise.

- If the motor rating is chosen based on short-term load then the motor would be highly under-utilised with regard to its thermal capability (curve 1).
- Alternatively, a smaller motor is chosen and is used to supply the same load i.e. the motor is overloaded and the temperature rise curve would follow curve 2.
- The machine is effectively utilised from thermal capability point of view (curve 2).
- The motor can be overloaded by a factor of $k (> 1)$ such that $\theta_{max} = \theta_{per}$ at the end of the duty cycle.

- How to calculate the overloading factor, k ?
- Assume that motor is operating with a load of $k \times P_r$ (P_r - rated output power) for a duration t_r with initial temperature ($\theta_1 = 0$) then we have,

$$\theta_{per} = \theta_{ss}(1 - e^{-t_r/\tau}) \rightarrow \frac{\theta_{ss}}{\theta_{per}} = \frac{1}{(1 - e^{-t_r/\tau})} \quad (2.12)$$

- θ_{ss} is the steady-state temperature rise if the motor delivers output power, $(k \times P_r)$ continuously.
- θ_{per} is the steady-state temperature rise if the motor delivers output power of P_r continuously.

- Let power losses be p_{1r} and p_{1s} respectively when the motor delivers power \mathbf{P}_r and \mathbf{kP}_r continuously.

$$\theta_{per} = \frac{p_{1r}}{D} \text{ and } \theta_{ss} = \frac{p_{1s}}{D}$$

$$\text{which gives } \frac{\theta_{ss}}{\theta_{per}} = \frac{p_{1s}}{p_{1r}} = \frac{1}{(1 - e^{-t_r/\tau})} \quad (2.13)$$

$$p_{1r} = p_c + p_{cu,r} = p_{cu,r} \left(1 + \frac{p_c}{p_{cu,r}} \right)$$

$$= p_{cu,r}(1 + \alpha)$$

where $\alpha = p_c / p_{cu,r}$, p_c – constant loss and $p_{cu,r}$ – variable loss at rated condition.

$$p_{1s} = p_c + k^2 p_{cu,r} = \left(\frac{p_c}{p_{cu,r}} + k^2 \right) p_{cu,r} = p_{cu,r}(\alpha + k^2) \quad (2.14)$$

$$\frac{p_{1s}}{p_{1r}} = \frac{p_{cu,r}(k^2 + \alpha)}{p_{cu,r}(1 + \alpha)} = \frac{1}{(1 - e^{-t_r/\tau})} \rightarrow k = \sqrt{\frac{1 + \alpha}{1 - e^{-t_r/\tau}} - \alpha} \quad (2.15)$$

where $\alpha = p_c/p_{cu,r}$, t_r - time at which the temperature rise is θ_{per} and τ - heating time constant of the machine.

- Eqn. 2.15 tells us how to calculate the overloading factor, k when the constant, p_c and variables losses, p_{cu} of the motor are known separately. If unknown then assume $\alpha = p_c/p_{cu,r} = 0$.

- **Example 2.3:** An electric motor has a heating time constant of 60 min. and a cooling time constant of 90 min. When run continuously on a full load of 20 kW, the final temperature rise is 40°C.
 - What load the motor can deliver for 10 min. if this followed by a shutdown period long enough for the motor to cool down?

Solution: The following parameters are given:

$$\tau_r = 60 \text{ min}, \tau_s = 90 \text{ min}, P_r = 20 \text{ kW and } \theta_{per} = 40^\circ\text{C}$$

$$k = 2.55$$

The permitted load is **$k \times P_r = 2.55 \times 20 \text{ kW} = 51 \text{ kW}$** .

Example 2.4: Assume that half-hour rating of a motor is 100 kW, heating time constant is 80 min. and the maximum efficiency occurs at 70% of full load. Determine the continuous rating of the motor.

Solution: The parameters given are:

- $K \times P_r = 100 \text{ kW}$, $\tau = 80 \text{ min}$, η_{max} at 70% of full-load
- Let $P_r \text{ kW}$ be the continuous rating of the motor and p_c be the constant loss.
- Necessary condition for maximum efficiency is $p_c = p_{cu}$.
- At 70% of full-load when maximum efficiency occurs we have $p_c = p_{cu@70\%}$.

$$p_{cu @ 100\%rated} = \frac{p_c}{0.49}$$

$$\alpha = \frac{p_c}{p_{cu @ 100\%rated}} = \frac{p_c}{\frac{p_c}{0.49}}$$

$$= 0.49$$

$$k = \sqrt{\frac{1 + \alpha}{1 - e^{-t_r/\tau}}} - \alpha = 2.0676$$

- Thus, the continuous rating of the motor is

$$Pr = \frac{Pr'}{k} = \frac{100kW}{2.0676} = 48.37kW$$

Motor rating under Intermittent Periodic Duty

- $P_r' = kP_r$ during the period, t_r and followed by a standstill period of t_s .

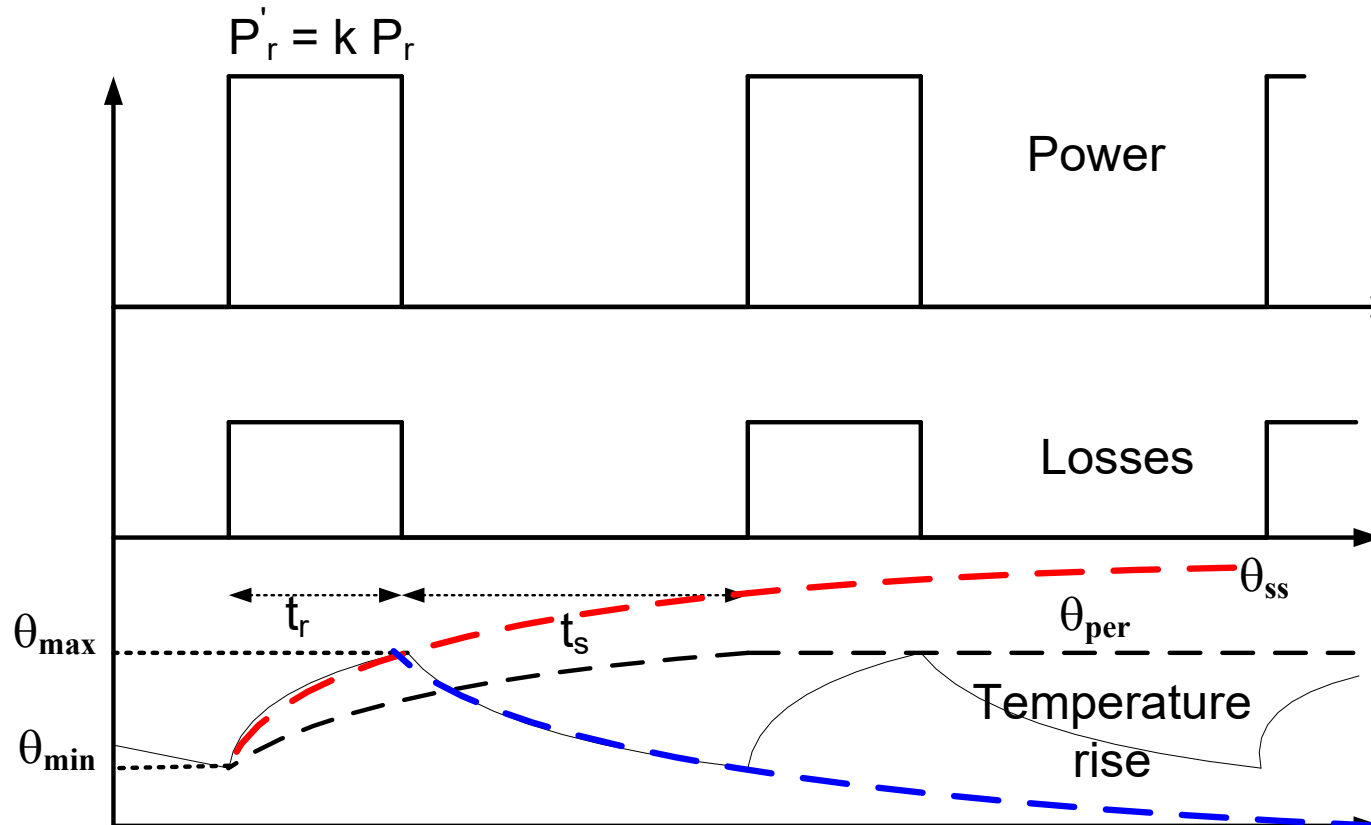


Figure 2.12:
Intermittent
periodic
load.

- The motor rating should be chosen such that $\theta_{max} \leq \theta_{per}$ where θ_{per} is the maximum temperature rise allowed when the motor is continuously operated at rated power P_r .

- During interval t_r temperature rise is given by

$$\theta(t) = \theta_{ss}(1 - e^{-t/\tau_r}) + \theta_{min} e^{-t/\tau_r} \quad (2.16)$$

- During interval t_s the temperature rise would drop and is given by

$$\theta(t) = \theta_{max} e^{-t/\tau_s} \left[\text{as } p_1 = 0, \theta_{ss'} = \frac{p_1}{D} = 0 \right] \quad (2.17)$$

- From eqns. 2.16 and 2.17 we have,

$$\frac{\theta_{ss}}{\theta_{max}} = \frac{1 - e^{-(tr/\tau_r + ts/\tau_s)}}{1 - e^{-(tr/\tau_r)}} \quad (2.18)$$

- For **proper utilisation** of the motor it is necessary that $\theta_{max} = \theta_{per}$.
- θ_{per} is the steady-state temperature rise when the machine is delivering a continuous load of **rated power, P_r** .
- If we assume that the power losses p_{1s} and p_{1r} be losses in the machine for power output of $P'_r = kP_r$ and P_r respectively then we have for ($\theta_{max} = \theta_{per}$).

$$\frac{\theta_{ss}}{\theta_{per}} = \frac{p_{1s}}{p_{1r}} = \frac{k^2 + \alpha}{1 + \alpha} = \frac{1 - e^{-(t_r/\tau_r + t_s/\tau_s)}}{1 - e^{-(t_r/\tau_r)}}$$

$$\rightarrow k = \sqrt{(\alpha + 1) \frac{1 - e^{-(t_r/\tau_r + t_s/\tau_s)}}{1 - e^{-(t_r/\tau_r)}} - \alpha} \quad (2.19)$$

Example 2.5: For the motor is Example 2.3 if we assume that the motor is on an intermittent load of 10 min followed by a 10 min. shutdown, what is the maximum value of load it can supply during the on load period?

Solution: We have $t_r = 10$ min. and $t_s = 10$ min. From Example 2.3: $\alpha = 0$, $\tau_r = 90$ min. and $\tau_s = 60$ min. Substituting in eqn. 2.19, we have

$$k = \sqrt{(\alpha + 1) \frac{1 - e^{-(t_r/\tau_r + t_s/\tau_s)}}{1 - e^{-(t_r/\tau_r)}}} - \alpha = 1.257$$

Thus, the permitted motor load is $P_r' = kP_r = 1.257 \times 20 \text{ kW} = 25.14 \text{ kW}$.

Frequency of Operation of Motors Subjected to Intermittent Loads

- In some applications, the intermittent load is applied with starting (t_{st}), braking (t_{br}), occurring quite frequently and running period, t_r and standstill period, t_s are comparable to t_{st} and t_{br} and much smaller as compared to τ_r and τ_s .
- As $t_r \ll \tau_r$ and $t_s \ll \tau_s$, we can have $e^{-x} \approx 1 - x$.

$$\frac{p_{1s}}{p_{1r}} = \frac{\theta_{ss}}{\theta_{per}} = \frac{\frac{t_r}{\tau_r} + \frac{t_s}{\tau_s}}{\frac{t_r}{\tau_r}}$$

$$p_{1s} \times t_r = p_{1r} \times t_r + p_{1r} \left\{ \left(\frac{\tau_r}{\tau_s} \right) \times t_s \right\} = p_{1r} \times \left(t_r + \left(\frac{\tau_r}{\tau_s} \right) \times t_s \right)$$

- Applying the same relationship to starting, braking and short running interval we have

$$E_{st} + p_{1s} \times t_r + E_b = p_{1r} \times (\gamma t_{st} + t_r + \gamma t_b + \beta t_s)$$

where, γ and β are some constants based on measurements.

- β varies in the range 0.3 – 0.7 and $\gamma = (1 + \beta) / 2$.
- All parameters are known except t_s that can be computed and the permissible frequency of switching per hour would be

$$f_{max} = \frac{1}{t_{st} + t_r + t_b + t_s}$$

Example 2.6: A thyristor converter-fed DC motor drive has the following specifications: rated armature current = 500 A, armature resistance = 0.01 ohm.

The drive operates in the following duty-cycles:

1. Acceleration at twice the rated armature current for 10 sec.
2. Running at full-load for 10 sec.
3. Deceleration at twice the rated armature current for 10 sec.
4. Idling interval.

The core loss is constant at 1 kW. If β has a value of 0.5, determine the maximum frequency of drive operation.

$$E_{st} = p_{1s} \times t_s = \left[\left((500 \times 2)^2 \times 0.01 \right) + 1000 \right] \times 10 \text{ sec} = 110 \text{ kW}$$

$$E_{br} = p_b \times t_b = \left[\left((500 \times 2)^2 \times 0.01 \right) + 1000 \right] \times 10 \text{ sec} = 110 \text{ kW}$$

$$p_{1s} = \left[\left((500)^2 \times 0.01 \right) + 1000 \right] = 3.5 \text{ kW}$$

$$\gamma = \frac{1 + \beta}{2} = \frac{1 + 0.5}{2} = 0.75$$

$$\begin{aligned} E_{st} + p_{1s} \times t_r + E_{br} &= (110 + 3.5 \text{ kW} \times 10 \text{ sec} + 110) \\ &= 3.5 \text{ kW} (0.75 \times 10 + 10 + 0.75 \times 10 + 0.5t_s) \Rightarrow t_s = 95.7 \text{ sec} \end{aligned}$$

$$f_{max} = \frac{3600}{t_{st} + t_r + t_b + t_s} = \frac{3600}{10 + 10 + 10 + 95.7} = 28.64 \text{ per hour}$$

Summary

- Power rating of an electric motor must be chosen carefully: **cost & reliability**.
- Losses in electrical machines: **constant losses** and **variable losses**.
- Temperature-rise is directly related to **thermal loading** of the machine.
- Electrical machines have sufficient **overloading capability** but thermal restrictions does not allow continuous overloading.
- **Electrical time constant (ms) << Mechanical time constant (sec) << Thermal time constant (mins.)**.

- Classes of motor duty: - (a) continuous, (b) short-term and (c) intermittent.
- Equivalent criterion method for selection of motor power rating for variable load.
- Calculation of motor overloading factor under: (a) Short Term Duty and (b) Periodic Intermittent Duty.

References

1. Fundamentals of Electric Drives – G K Dubey – Chapter 4.
2. Control of Electric Drives – Leonhard – Chapter 4.