# ME4252 Nanomaterials for Energy Engineering

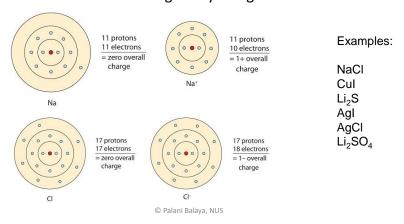
## **Ionic Conductors**

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# **Ionic Bonding**

**lonic bonding** is the complete transfer of valence electron(s) between atoms. It is a type of chemical **bond** that generates two oppositely charged **ions**. In **ionic bonds**, the metal loses electrons to become a positively charged cation, whereas the nonmetal accepts those electrons to become a negatively charged anion.



lonic Conductivity
$$\sigma = \frac{1}{k_B T} \cdot \sum_{i} (Z_i q)^2 n_i D_i$$

$$\sigma = \sum_{i} n_i q \mu_i$$

$$\frac{D}{\mu} = \frac{kT}{a}$$

- Conductivity is influenced by 1)the carrier concentration n,
   2) the carrier mobility μ
- Usually, defects act as the charge carriers
  - not many defects in most ionic solids
  - mobility is usually low at room temperature

	Material	Conductivity (S m <sup>-1</sup> )		
Ionic conductors	Ionic crystals	< 10 <sup>-16</sup> – 10 <sup>-2</sup>		
	Solid Electrolytes	10-1-103		
	Liquid electrolytes	10-1-103		
Electronic conductors	Metals	10 <sup>3</sup> -10 <sup>7</sup>		
	Semiconductors	10-3-104		
	Insulators	< 10-10		

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#### **Ionic Conduction in Solids**

$$D = D_0 \exp\left(\frac{-\Delta G}{k_{\rm B}T}\right)$$

$$= \gamma (1 - c)Za^2 \nu_0 \exp\left(\frac{\Delta S}{k_{\rm B}}\right) \exp\left(\frac{-E_{\rm m}}{k_{\rm B}T}\right)$$

$$\sigma_{ion} = n Z_i q \frac{Z_i q}{kT} D_o \exp\left(\frac{-\Delta G}{kT}\right)$$

$$\sigma_{ion} = Nc \frac{(Z_i q)^2}{kT} D_o \exp\left(\frac{-\Delta G}{kT}\right)$$

Each ion has charge of Zq  $(q = 1.6 \times 10^{-19} \text{ amp*sec})$ 

$$\begin{split} \sigma_{ion} &= Nc \; \frac{(Z_i q)^2}{kT} \gamma (1-c). Z a^2 v_o \; exp\left(\frac{\Delta S}{k}\right) exp\left(\frac{-E_m}{kT}\right) \quad (1) \\ \sigma_{ion} &= \frac{\sigma_o}{T} exp\left(\frac{-E_m}{kT}\right) \quad (2) \end{split}$$

 $\sigma_{ion} = n Z_i q \mu$ 

Where, n is the carrier density (#/cm³),  $\mu$  the mobility (cm²/Vs), and  $Z_q$  the charge ( $q = 1.6 \times 10^{-19}$  C) of the  $i^{\rm h}$  charge carrier. The huge (many orders of magnitude) differences in between metals, semiconductors and insulators generally result from differences in n rather than  $\mu$ . On the other hand, the higher conductivities of electronic versus ionic conductors are generally due to the much higher mobilities of electronic versus ionic species.

Charge number or valence of an <u>ion</u> is the coefficient that, when multiplied by the <u>elementary charge</u>, gives the ion's <u>charge</u>. For example, the charge on a <u>chloride</u> ion, Cl, is  $-1 \cdot q$ , where q is the elementary charge. This means that the charge number for the ion is -1.

#### **Ionic Conduction in Solids**

- This expression (1) shows that  $\sigma_{\text{ion}}$  is non-zero only when the product c(1-c) is non-zero. Since all normal sites are fully occupied (c=1) and all interstitial sites are empty in a perfect classical crystal, this is expected to lead to highly insulating characteristics.
- The classical theory of ionic conduction in solids is thus described in terms of the creation and motion of atomic defects or point defects, notably vacancies and interstitials.

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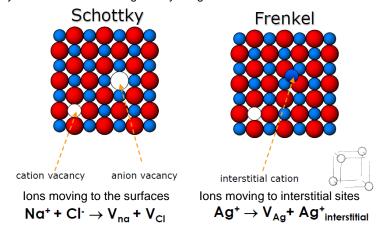
- For ionic crystals, ionic conduction is mainly intrinsic because the crystals have thermally created vacant sites in the lattice through which ions can move. The simplest types of thermally created vacant sites (lattice defects) are the well known Frenkel and Schottky defects shown in Figure (see next slide).
- Frenkel defect is formed when an ion originally at a lattice site moves to an interstitial position, which implies that this process generates two imperfections: a vacancy in the lattice and an interstitial ion.
- ➤ A Schottky defect is formed when an ion originally at a lattice site diffuses to a surface position, creating one imperfection: a vacancy in the lattice. Since the volume and the surface of a crystal must be electrically neutral, Schottky defects must be created in pairs: one vacancy created by displacing an anion and the other by displacing a cation.
- In most alkali halide ionic crystals, probability of the formation of the Schottky defects is much higher than that of the Frenkel defects. It can be imagined that in large ions, vacant lattice sites must be present for the ionic movement, whereas small ions can move through the interstitial space.
- For non-ionic solids, some structures may provide channels, which allow the ions some space to move.

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#### **Ionic Conductors: Point Defects**

A Point Defect involves missing of a single atom in the normal crystal array.

There are three types of point defects: Vacancies. Interstitial and Impurities. They may be built-in with the original crystal growth.



Schematic representations of Schottky defects and Frenkel defects

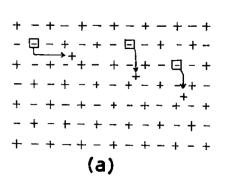
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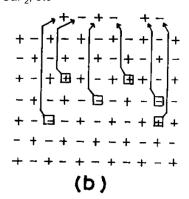
#### **Point Defects**

Point defect type of solids is further subdivided into two, according to the defect concentration.

- (a). Diluted. n <<10<sup>18</sup>/cm<sup>3</sup>, e.g.: NaCl, KCl, AgCl, etc.
- (b). Concentrated.  $n=\sim 10^{20}/cm^3$ ', e.g.:  $ZrO_2$ ,  $CaF_2$ , etc



Frenkel defects formation



Schottky defects formation

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#### Molten Sub-lattice

In molten sub-lattice type solids (with concentrated point defects), all ions are available for conductions, since the number of defects or void sites in the sub-lattice are more than the number of ions. So, ions can move freely from one position to another with low activation energy possessing high conductivity is called superionic conductors (SICS).

#### **Ionic Solids Classification**

- (i). Conventional ionic solids, in which the defect concentration is low. The numbers of mobile defects are  $-\,10^{18}$ /cm³ or less. These are same as "dilute type point defect".
- (ii) These are same as concentrated type point defect. The defect concentration is  $-10^{20}$ /cm<sup>3</sup>.
- (iii). These are the "molten sub-lattice type", in which all the ions in a sub-lattice are available for movement. The numbers of mobile ionic charge carriers are 10<sup>22</sup>/cm<sup>3</sup>

In order to increase the conductivity of an ionic solid, we need to:

- 1). Raise the temperature and so increase the number of intrinsic defects; or
- 2). Add an impurity to create vacancies or defects in the structure (extrinsic defects); or
- 3). Lower the activation energy of the jump, perhaps by creating more space in the structure.

## **Concentration of Intrinsic Defects: Schottky Defects**

Energy is required to form a defect (endothermic process)

Although there is a cost in *energy*, there is a gain in *entropy* in the formation of a defect.

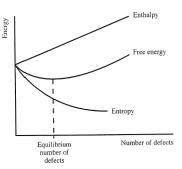
At equilibrium, the overall change in free energy of the crystal due to the defect formation is zero according to:

$$\Delta G = \Delta H - T \Delta S$$

At any temperature, there will always be an equilibrium population of defects. The number of defects (for an MX crystal) is given by:

$$n_s \approx N \exp\left(\frac{-\Delta H_s}{2kT}\right)$$

where  $n_{\rm S}$  is the number of Schottky defects per unit volume at T K, in a crystal with N cations and N anion sites per unit cell volume, and  $\Delta H_{\rm S}$  is the enthalpy required to form one defect.



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#### Recall:

What are Gibbs Free energy, Enthalpy and Entropy?

At what condition does a reaction forming a product from the reactants proceed spontaneously?

At what condition does the equilibrium exists between reactants and product?

At what condition does the reaction is non-spontaneous?

What is standard condition for thermodynamic reactions?

https://www.youtube.com/watch?v=-UI8c\_ot4j0

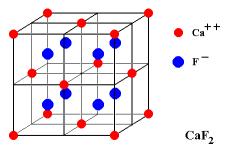
https://www.youtube.com/watch?v=XvuRJuXykyw

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#### **Anion Frenkel Defect in Fluorite**

Cation Frenkel defects are common because of the typically smaller size of a cation compared to an anion.



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#### Concentration of Defects, cont.

Consider a MX crystal, the number of Frenkel defects present in this crystal is:

$$n_f \approx (NN_i)^{1/2} \exp\left(\frac{-\Delta H_F}{2kT}\right)$$

where  $n_f$  is the number of Frenkel defects per unit volume, N is the number of lattice sites, and  $N_i$  the number of interstitial sites available., and  $\Delta H_F$  is the enthalpy of formation of one Frenkel defect.

If  $\Delta H_F$  is the enthalpy of formation of one mole of Frenkel defects:

$$n_f \approx (NN_i)^{1/2} \exp\left(\frac{-\Delta H_F}{2RT}\right)$$

Knowing the enthalpy of formation for Schottky and Frenkel defects, one can estimate how many defects are present in a crystal.

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#### **Concentration of Defects, cont.**

# Schottky Defects Frenkel Defects

	•	
Compound	ΔH (10 <sup>-19</sup> J)	ΔH (eV)
MgO	10.57	6.60
CaO	9.77	6.10
LiF	3.75	2.34
LiCl	3.40	2.12
LiBr	2.88	1.80
Lil	2.08	1.30
NaCl	3.69	2.30
KCI	3.62	2.26

Assuming  $\Delta H_s = 5 \times 10^{-19}$  J, the proportion of vacant sites  $n_s/N$  at 300 K is 6.12×10<sup>-27</sup>, whereas at 1000 K this increases to 1.37×10<sup>-8</sup>

At room temperature there are very few Schottky defects, even at 1000K there are only about 1 or 2 defects per hundred million sites.

Depending on the value of  $\Delta H$ , a Schottky or Frenkel defect may be present. The lower  $\Delta H$  Frenkel defects dominates, but in some crystals it is possible that both types of defects may be present.

Increasing temperature increase defects.

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#### **Extrinsic Defects**

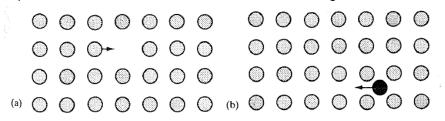
Doping with selected 'impurities' can introduce vacancies into a crystal.

Consider incorporating CaCl<sub>2</sub> into NaCl, in which each Ca<sup>2+</sup> replaces one Na<sup>+</sup> and creates one cation vacancy.

#### **Defects and Ionic Conductivity in Solids**

Defects make it possible for atoms or ions to move, by diffusion through the lattice or ionic conductivity (ions under the influence of an external electric field) through the structure.

Two possible mechanisms for the movement of ions through a lattice:

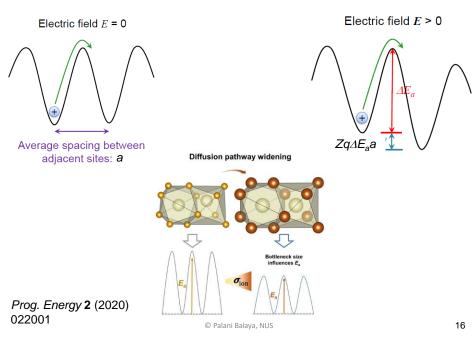


Vacancy mechanism © Palani Balaya, NUS

Interstitial mechanism

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## **Ionic Conduction: Activation Energy**



#### **Ionic Conductivity: Arrhenius Equation**

The temperature dependence of the mobility of the ions can be expressed by an Arrhenius equation.

$$\mu \propto \exp\left(\frac{-E_a}{kT}\right) \text{ or } \mu = \mu_0 \exp\left(\frac{-E_a}{kT}\right)$$

where  $\mu_o$  is a proportionality constant known as the pre-exponential factor

 $\mu_o$  depends on the attempt frequency (frequency of vibration of the lattice 10<sup>12</sup>-10<sup>13</sup> Hz), distance moved by ion, and the size of the external field.

If the external field is small (up to 300 V/cm), a temperature dependence of 1/T is present in the pre exponential factor.

An expression for the variation of ionic conductivity:  $\sigma = \frac{\sigma_0}{T} \exp\left(-\frac{\Delta E_a}{k_B T}\right)$ 

The term  $\sigma_0$  contains n and Zq as well as the attempt frequency and jump distance. Taking logs...

$$\ln \sigma T = \ln \sigma_0 - \left(\frac{E_a}{k_B T}\right)$$

Plotting  $\ln(\sigma T)$  vs 1/T should produce a straight line with a slope of  $-E_a$ .  $\ln(\sigma)$  vs 1/T is also used

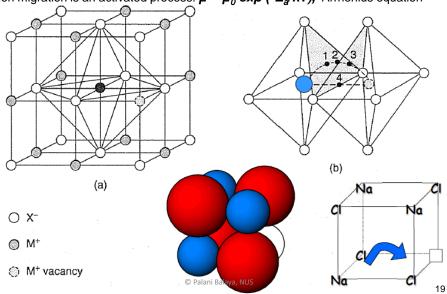
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## Ionic Conductivity in NaCl

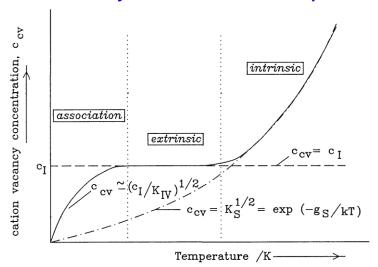
NaCl is a poor ionic conductor		Na	CL	Na	СІ	Na	
Conduction involves migration of	Na	CL	No	СІ	No	Cl	
cation vacancies	СГ	Na	CL	1	CL	Na	
Cation vacancies are present	Na	CL	Na	Cl	Na	CL	
due to	CL	Na	CL	Na	CL	Cd <sup>2+</sup>	
- doping - extrinsic defects (for example	Na+						
$Cd^{2+}$ )	Cı	Na	CL	Na	CL	Na	
- Schottky defects - intrinsic defects	Na	CL	No	СІ	No	Cl	
	CL	Na	CL	1	Cl	Na	
				/			
	Na	Cı	Na	Cl	Na	CL	

#### Ion Migration in NaCI: Schottky Defects

Na<sup>+</sup> ions move, but meet resistance in the crystal structure lon migration is an activated process:  $\mu = \mu_0 \exp(-E_a/kT)$ , Arrhenius equation



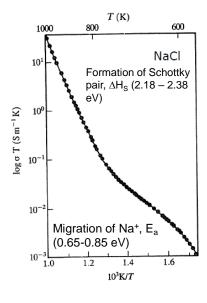
## **Cation Vacancy Concentration with Temperature**



Cation vacancy concentration in a MX crystal with Schottky disorder and doped with a divalent cation as a function of temperature.

Ionic Conduction and Diffusion in Solids, AV Chadwick

## **Temperature Dependence of Ionic Conductivity**



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## **Idealized Conductivity for NaCl**

Differences in slopes are evident, even in very pure crystals.

# Low temperature (extrinsic conductivity):

At low temperatures extrinsic vacancies are most important.

The concentration of intrinsic vacancies are so small at low temperature that they may be ignored

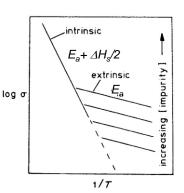
The number of vacancies will be essentially constant

 $\mu$  in the extrinsic region thus will only depend on the cation mobility due to extrinsic defects, with the temperature dependence:

$$\mu = \mu_0 \exp\left(\frac{-E_a}{kT}\right) \qquad \sigma = \frac{\sigma_0}{T} \exp\left(-\frac{\Delta E_a}{k_B T}\right)$$

Carrier concentration is fixed by doping

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#### **High Temperature (Intrinsic Conductivity)**

At high temperatures the concentration of intrinsic defects has increased so that it is similar or greater than the concentration of extrinsic defects

$$n_s \approx N \exp\left(\frac{-\Delta H_s}{2kT}\right)$$

The conductivity in this intrinsic region on the left side of the plot:

$$\sigma = \frac{\sigma'}{T} \exp\left(\frac{-E_a}{kT}\right) \exp\left(\frac{\Delta H_s}{2kT}\right)$$

A plot of  $\ln(\sigma T)$  vs 1/T gives a larger value for the activation energy ( $E_s$ ), because it depends on both the activation energy for the cation jump ( $E_a$ ) and the enthalpy of formation of a Schottky defect ( $\Delta H_s$ ).

Slope  $E_s = E_a + (1/2) \Delta H_S$ 

For a system with Frenkel defects, slope  $E_F = E_a + (1/2) \Delta H_F$ 

Activation energies typically lie in the range of 0.05 to 1.1 eV.

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## Silver Chloride, AgCl

#### **Defects in AgCI:**

The predominant defect in AgCl is cation Frenkel

Cation interstitials are more mobile than cation vacancies

Cation interstitials can migrate by one of two mechanisms

- direct movement
- indirect movement

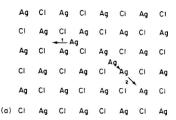
#### Migration mechanism in AgCI:

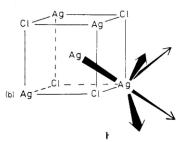
Two possible pathways for interstitial migration:

- 1) move directly from interstitial to interstitial
- 2) interstitial displaces regular cation onto interstitial position

Migration actually occurs by second pathway

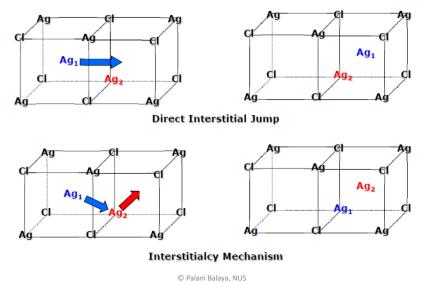
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#### **Ion Migration: Frenkel Defects**

The Frenkel defects in AgCl can migrate via two mechanisms.



## **Doping in AgCl**

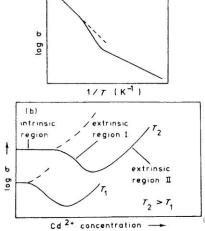
Doping AgCl with a divalent impurity like Cd<sup>2+</sup> reduces the ionic conductivity of the specimen

There is an equilibrium between cation vacancies and Ag<sup>+</sup> interstitials (prior to doping)

- doping increases vacancy concentration

AgCI / Cd 2pt

- doping decreases interstitial concentration (Cd2+ doped AgCl)



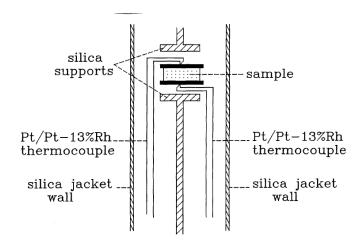
Schematic showing effect of  $Cd^{2+}$  impurity on conductivity – Presence of  $Cd^{2+}$  reduces number of  $Ag^+$  interstitials and hence lowers conductivity

Get minimum in conductivity curve when doped – at high impurity concentrations conductivity is dominated by cation vacancy migration, at low concentrations interstitial migration dominates

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## **Ionic Conductivity - Measurement**

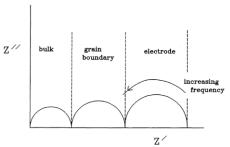


Essential features of a cell for measuring ionic conductivity of solids

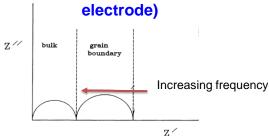
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## Impedance Measurement on Pt/AgCI/Pt (blocking electrode)

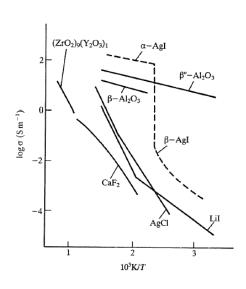


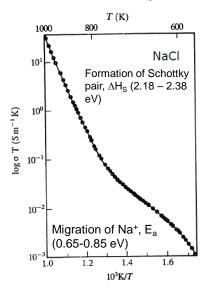
# Impedance Measurement on Ag/AgCI/Ag (non-blocking



Idealized impedance spectrum of a polycrystalline ionic conductor

#### **Temperature Dependence of Ionic Conductivity**

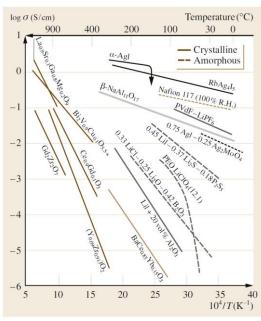




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## **Super-ionic Conductors**

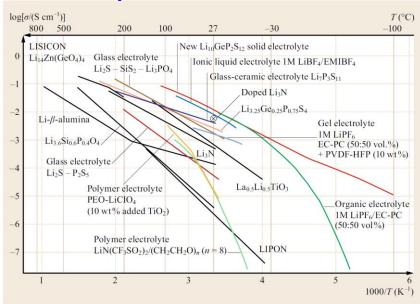


The temperature dependences of representative super-ionic conductors, including cation and anion conductors, crystalline and amorphous conductors, and inorganic and organic conductors.

H.L. Tuller: Highly conducting ceramics. In: Ceramic Materials for Electronics, 3rd edn., ed. by R.C. Buchanan (Marcel Dekker, New York 2004), p. 87

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## **Super-ionic Conductors**



The temperature dependences solid lithium ion conductors, together with representative organic liquid, ionic liquid and get electrolytes (Nat. Mater. 10, 682 (2011)

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## **Typical Applications of Ionic and Electronic Conductors**

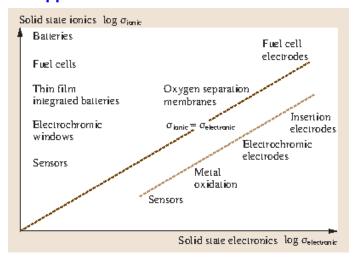


Illustration of typical applications of ionic and electronic conductors as a function of the magnitude of electrical conductivity. Applications requiring mixed ionic electronic conductivity fall within the quadrant bounded by the two axes.

H.L. Tuller: Oxygen ion conduction and structural disorder in conductive oxides, J. Phys. Chem. Solids **55**, 1393 (1994) © Palani Balaya, NUS