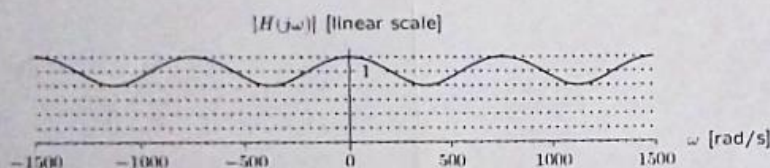
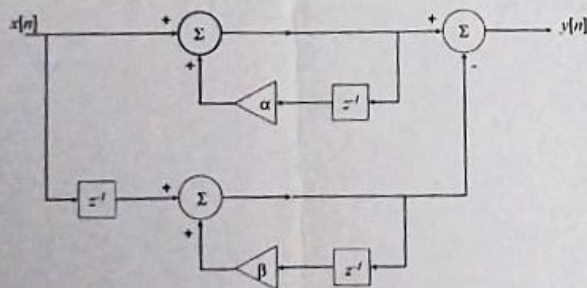


1. An LTI system is represented by $h[n] = \delta[n - n_0] + \alpha \delta[n - n_1]$ with $n_1 > n_0$. The plot below shows the magnitude of the $H(z)$ when evaluated on the unit circle, i.e. $|z| = 1$, or $z = e^{j\omega}$ where $\omega = \frac{2\pi}{T}$ is the angular frequency.
- Assume $\alpha < 1$ and sketch $h[n]$. Find the system function $H(z)$.
 - Justify the oscillatory pattern in $|H(e^{j\omega})|$ by evaluating $H(z)$ on the unit circle. Relate the variables α , n_0 , n_1 in $h[n]$ to the oscillations. If $n_0 = 0$, find n_1 and α .
 - Draw the block diagram of this system.

Bonus question (3 points): what real life problem can be modeled by this system? Explain clearly.



2. Consider the system below.

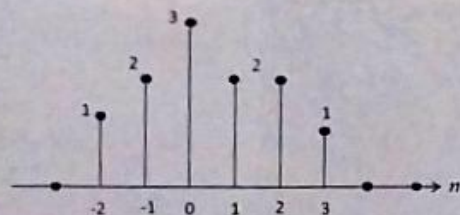


- Find the impulse response $h[n]$ and system function of this system. Plot the poles and zeros on the z -plane.
- Specify the condition on α , β and the relation between them required for
 - $h[n]$ to be of finite duration
 - System to be stable
 - System to be causal
 You can if required, give the answer 'not possible'.
- If $\alpha = \beta = 1$, describe the signal processing function done by this system.

3. An LTI system initially at rest is described by the difference equation:

$$y[n] + 2y[n-1] = x[n] + 2x[n-2].$$

- What is the impulse response of this system?
- If $x[n]$ is as shown below, find the output of this system using convolution.



4. Let $x[n] = \delta(n+3) - \delta(n+1) + 2\delta(n) + 3\delta(n-2)$ with DTFT as $X(e^{j\omega}) = X_R(e^{j\omega}) + jX_I(e^{j\omega})$ then
- Compute $X_R(e^{j\omega})$ and $\int_{-\pi}^{\pi} X_I(e^{j\omega}) d\omega$
 - $DTFT(y[n]) = X_R(e^{j\omega})e^{j2\omega} + jX_I(e^{j\omega})$, find $y[n]$ without explicitly considering DTFT?
 - Find $X_R(k)$, $0 < k < N$, which is discretized $X_R(e^{j\omega})$ at $\omega = \frac{2\pi k}{N}$ for $N = 5$
 - Compute $x_1[n] = \text{IDFT of } X_R(k)$ and find the relation between $x[n]$ and $x_1[n]$.