

# Ionizations of Liquid Water from Charged-cell Periodic Subsystem DFT and Embedded Coupled Cluster Simulations

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## Abstract

Modeling the ionization potential (IP) and electron affinity (EA) of liquid water is challenging for two reasons: (1) the bulk-like nature of the liquid imposes the use of periodic boundary conditions (PBCs), which pose roadblocks when considering charge systems; (2) quantitative electronic structure methods, such as coupled cluster, are generally not available in PBCs. In this work, we tackle both challenges by employing subsystem DFT to split the extended system into a collection of finite subsystems embedded by extended, infinite subsystem. This is achieved by an impurity model [1] where high ab initio method as coupled cluster wavefunctions can be introduced to evaluate the water molecules' energy functionals.

The liquid's electronic structure is expressed in subsystem contributions by invoking nonadditive density functionals whereby the total energy of the liquid is expressed as the sum of molecule-additive and nonadditive contributions [2]. The inter-molecular interaction is split into Coulomb interactions, and such nonadditive terms as the noninteracting kinetic energy and the noninteracting exchange-correlation [2]. These contributions represent interactions related among others to exchange, van der Waals and Pauli repulsion and are all bifunctional of the subsystem densities [1].

The final IP/EA values reproduce the experimental values to within 0.5 eV and are determined averaging over 256 water molecules (or subsystems) considered in the simulation cell, calculated by the energy difference of the neutral and the polarized system (Called SCF method) [3, 4].

## 1 Introduction

The high-accuracy calculations of ionization potentials (IPs) and electron affinities (EAs) of condensed-phase molecular systems as liquid water has represented a challenge for the last years in both experimental and computational fields [1, 5–7]. Thus, ionized states of the electrons take part in many crucial processes in electrochemistry, photochemistry as well as peculiar states of matter as excess electrons solvated in liquid water [8]. The most recent theoretical report of IP and EA values [9] shows that using quasi-particle self-consistent GW calculations and implicit vertex correction in many-body perturbation (MBPT) remarkably affect the EA of liquid water previously reported [5] by Gaiduk et al by about 1eV. Therefore, they through self-consistent GW approach with an implicit vertex correction based on the projector augmented wave (PAW) method, which is the most accurate pseudo-potential [10] (PPs available), and combined with Bethe–Salpeter equation established values of 10.2 and 1.1 eV, for IP and EA of liquid water, respectively.

Following the trend and now including the use of periodic boundary conditions (PBC) another method was introduced [1] to determine the ionization potentials (IPs) and electron affinities (EAs) of liquid water. Based on determining successfully a quantum-mechanical model for charged species in PBC which is able to face the complications related to the long-ranged nature of the Coulomb Kernel  $w(r, r') = \frac{1}{|r-r'|}$ , which decays to zero when two charges are far away in real space. Indeed, it was achieved using an impurity model with two remarkable qualities: 1) The charged periodic system is replaced by a non-periodic one which is still truly extended (ie., of infinite size) and 2) The potentials of the neutral and the charged system are pegged to a common reference.

The former requires an ad hoc mapping of the infinite system (periodic) onto finite number of finite subsystems (non-periodic subsystems) and an extended (infinite) subsystem, using a formally exact density embedding method, subsystem DFT [11]. Meanwhile, achieving the latter only requires finding a consistent choice for the  $G = 0$  component of the Coulomb Kernel in

a reciprocal space. The use of the reciprocal space is only chosen for avoiding the complication of dealing with convergent integrals [12] In addition, in PBC the physical Coulomb kernel is only the one represented in a reciprocal space  $w(G) = \frac{4\pi}{|G|^2}$  where  $G \in \mathbb{R}^3$ . Even though, when  $G = 0$  the Coulomb kernel becomes undefined the total charged density  $\rho(G)$  is zero for  $G = 0$ , which is not problematic.

Here we present an update of the current state-of-the-art of liquid water IPs and EAs base on an impurity model using an exact density embedding method, subsystem DFT which may allow us to contribute to the discussion generated by using ab initio electronic structure [5, 8] by GW approximations. We begin with a brief theoretical framework description and follow on the description of the EAs and IPs of 256 bulk liquid water.

## 2 Theoretical Background

### 2.1 Mapping a periodic system into a collection of non-periodic subsystems and one periodic subsystem

To cast DFT in a subsystem fashion, we invoke nonadditive functionals in which each energy term of the supersystem is expressed as the sum of additive and nonadditive contributions [13]. Therefore, when dealing with a finite subsystem with electron density  $\eta_I$ , and an infinite or extended subsystem with electron density  $\eta - \eta_I$ , the total energy is given by,

$$E_{tot} = E[\eta_I] + E[\eta - \eta_I] + E^{int}[\eta_I, \eta - \eta_I] \quad (1)$$

And the interaction energy can be broken down into the following contributions,

$$E^{int} = E_H^{int} + V_e^{int}N + T_s^{nad} + E_{xc}^{nad} \quad (2)$$

The two Coulombic terms  $E_H^{int}$  and  $V_e^{int}N$  are the electron-electron and electro-nuclear interactions, respectively. And the nonadditive terms  $T_s^{nad}$  and  $E_{xc}^{nad}$ , represent the noninteracting kinetic energy of the system and the noninteracting exchange-correlation functionals, respectively [2]. The two last terms represent interactions related among other to exchange, van der Waals and Pauli repulsion and are all bifunctional of the two subsystem densities.

### 2.2 Coulomb interaction energy determination

### 2.3 Embedding Scheme for the Neutral System

For the neutral system, the Coulomb interaction energy can be expressed as a potential that maps the interaction of an accurately infinitely extended environment onto and isolated subsystem  $I$ ,

$$v'_{int}[\eta](r) = v[\eta](r) - \bar{v}[\eta_I](r) \quad (3)$$

Where  $v[\eta](r)$  is the total Coulomb potential of the system and  $\bar{v}[\eta_I](r)$  the potential of the isolated subsystem  $I$ . The latter was evaluated using the Martyna-Tuckerman method whereby density  $\eta_I$  is assumed to be isolated and not periodic [13]. The embedding potential for the neutral subsystem can also be calculated directly from equation 3.

## 2.4 Impurity Model for the Ionized system

To obtain the embedding potential of a charged subsystem, we consider the system to be composed of an ionized subsystem embedded in a nonionized environment. To assemble the appropriate embedding potential, first was evaluated a screening potential,  $v^{screen}[\eta_I](r) = v[\eta_I](r) - \bar{v}[\eta_I](r)$ , for both charged and neutral subsystems (understood as a self-interaction of the charge in PBC). The embedding potential depends on three densities:  $\eta$ , the total system,  $\eta'_I$ , the neutral subsystem, and  $\eta_I$  the charged subsystem, and has the form,

$$v_{emb,imp}^I[\eta](r) = v[\eta, \eta'_I, \eta_I](r) - \bar{\eta}_I(r) \quad (4)$$

with

$$v[\eta, \eta'_I, \eta_I](r) = v[\eta](r) + \Delta v^{screen}[\eta_I, \eta'_I](r) \quad (5)$$

where  $\Delta v^{screen}[\eta_I, \eta'_I](r) = v^{screen}[\eta'_I] - v^{screen}[\eta_I]$

## 3 Computational Section

All calculations were carried out with embedded Quantum ESPRESSO (eEQ) employing ultra-soft pseudopotentials. The ground state calculation of each subsystem with the corresponding neutral and polarized embedding potential was determined through ADF [14] software. A comparison among Density Functional Theory (DFT), using GGA(PBE), Hybrid(B3LYP), Double-Hybrid (B2KPLYP, B2NCPLYP, and REVDSDBLYP) and Statistical average of orbital potentials(SOAP) models, Møller–Plesset perturbation theory (MP2) and HF methods was made, with the basis QZ4P. The final IP/EA values are calculated using an average for each of the 256 water molecules or subsystems considered in the simulation cell, calculated by the energy difference of the neutral and the polarized system (Called  $\Delta$ SCF method) [3, 4].

## 4 Results

### 4.1 IPs of Bulk water

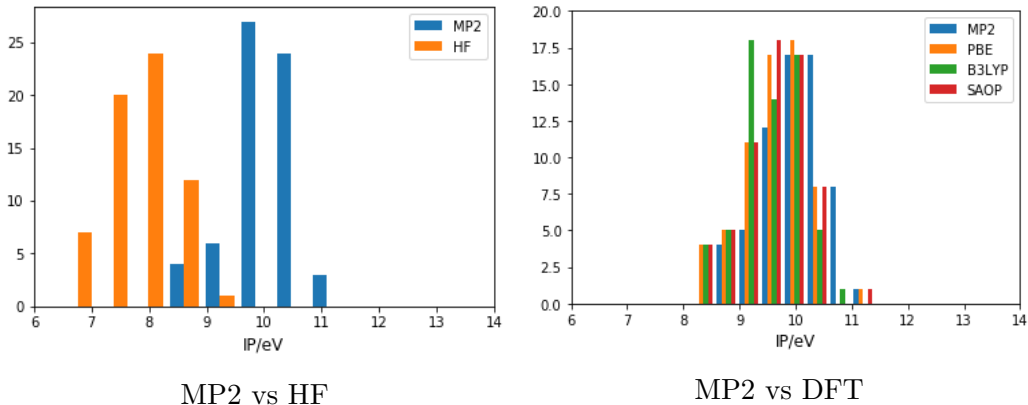


Figure 1: Distribution of IPs of bulk liquid water. The area subtended by the lines sums up to 64 (ie, the number of subsystems). Left: Comparison between MP2 and HF. Right: Comparison between MP2 and DFT

Table 1: average IPs

	IP average (eV)
MP2	9.9941
HF	7.8250
PBE	9.6089
B3LYP	9.5147
SAOP	9.5897

## 5 Conclusions

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