


EAFIT UNIVERSITY
DEPARTMENT OF INFORMATICS AND SYSTEMS
PROJECT CHOICE

Second Report
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Course: Numerical Analysis
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Repository

The repository with the evidence related to the project will be:  NumericalAnalysisProject

Description

This project aims to develop a web app to calculate data using different numerical methods as well as an API that let users make request to solve their problems. Also, the web app will have the option of visualising the data in a 2D graph.

Added Values

- The project will be done in English
- The project will have its documentation in \LaTeX
- The numerical algorithms can be found in multiple programming languages.
- The project will have extra numerical methods

Pseudocodes

1: Incremental Search

```
1: function IncrementalSearch(f,x0,delta,niter)
2:    $fx0 \leftarrow f(x0)$ 
3:   if  $fx0 = 0$  then
4:     WRITE x0 is a root
5:   else
6:      $x1 \leftarrow x0 + \text{delta}$ 
7:      $counter \leftarrow 1$ 
8:      $fx1 \leftarrow f(x1)$ 
9:     while  $fx0 * fx1 > 0$  AND  $counter < niter$  do
10:       $x0 \leftarrow x1$ 
11:       $fx0 \leftarrow fx1$ 
12:       $x1 \leftarrow x0 + \text{delta}$ 
13:       $fx1 \leftarrow f(x1)$ 
14:       $counter \leftarrow counter + 1$ 
15:   end while
16:   if  $fx1 = 0$  then
17:     WRITE x1 is a root
18:   else if  $fx0 * fx1 < 0$  then
19:     WRITE There is at least one root between x0 and x1
20:   else
21:     WRITE The method fails in niter iterations
22:   end if
23: end if
24: end function
```

2: Bisection

```

1: function Bisection(f,left,right,tol,niter)
2:    $fRight \leftarrow f(right)$ 
3:    $fLeft \leftarrow f(left)$ 
4:   if  $fRight = 0$  then
5:     WRITE right is a root
6:   else if  $fLeft = 0$  then
7:     WRITE left is a root
8:   else if  $fLeft * fRight < 0$  then
9:      $mid \leftarrow (left + right)/2$ 
10:     $fmid \leftarrow f(mid)$ 
11:     $counter \leftarrow 1$ 
12:     $error \leftarrow tol + 1$ 
13:    while  $error > tol$  AND  $fmid \neq 0$  AND  $counter < niter$  do
14:      if  $fLeft * fmid < 0$  then
15:         $right \leftarrow mid$ 
16:         $fRight \leftarrow fmid$ 
17:      else
18:         $left \leftarrow mid$ 
19:         $fLeft \leftarrow fmid$ 
20:      end if
21:       $aux \leftarrow mid$ 
22:       $mid \leftarrow (right + left)/2$ 
23:       $fmid \leftarrow f(mid)$ 
24:       $error \leftarrow |mid - aux|$ 
25:       $counter \leftarrow counter + 1$ 
26:    end while
27:    if  $fmid = 0$  then
28:      WRITE mid is a root
29:    else if  $error < tol$  then
30:      WRITE mid is an approximation with tolerance = tol
31:    else
32:      WRITE The method failed at niter iterations
33:    end if
34:  else
35:    WRITE Inappropriate interval
36:  end if
37: end function

```

3: False Rule

```

1: function falseRule(f, Xi, Xs, Tol, Iter)
2:    $Y_i \leftarrow f(X_i)$ 
3:    $Y_s \leftarrow f(X_s)$ 
4:   if  $Y_i = 0$  then
5:     WRITE Xi is a root
6:   else
7:     if  $Y_s = 0$  then
8:       WRITE Xs is a root
9:     else
10:      if  $Y_i * Y_s < 0$  then
11:         $X_m \leftarrow (X_i) - ((f(X_i) * (X_i - X_s)) / (f(X_i) - f(X_s)))$ 
12:         $Y_m \leftarrow f(X_m)$ 
13:         $Error \leftarrow Tol + 1$ 
14:         $Cont \leftarrow 1$ 
15:        while  $Y_m \neq 0$  AND  $Error > Tol$  AND  $Cont < Iter$  do
16:          if  $Y_i * Y_m < 0$  then
17:             $X_s \leftarrow X_m$ 
18:             $Y_s \leftarrow Y_m$ 
19:          else
20:             $X_i \leftarrow X_m$ 
21:             $Y_i \leftarrow Y_m$ 
22:          end if
23:           $X_{aux} \leftarrow X_m$ 
24:           $X_m \leftarrow (X_i) - ((f(X_i) * (X_i - X_s)) / (f(X_i) - f(X_s)))$ 
25:           $Y_m \leftarrow f(X_m)$ 
26:           $Error \leftarrow |X_m - X_{aux}| / X_m$ 
27:           $Cont \leftarrow Cont + 1$ 
28:        end while
29:        if  $Y_m = 0$  then
30:          WRITE  $X_m$  is a root of f
31:        else
32:          if  $Error < Tol$  then
33:            WRITE  $X_m$  is an approximation to a root with a tolerance = Tol
34:          else
35:            WRITE failure in Iter iterations
36:          end if
37:        end if
38:      else
39:        WRITE The interval is inadequate
40:      end if
41:    end if
42:  end if
43: end function

```

4: Fixed Point

```

1: function Fixed point(f, g, tol, x0, niter)                                ▷ g is the convergent form of f
2:    $fx \leftarrow f(x0)$ 
3:    $counter \leftarrow 0$ 
4:    $error \leftarrow tol + 1$ 
5:   while  $fx \neq 0$  AND  $error > tol$  AND  $counter < niter$  do
6:      $x1 \leftarrow g(x0)$ 
7:      $fx \leftarrow f(x1)$ 
8:      $error \leftarrow |x1 - x0|$ 
9:      $x0 \leftarrow x1$ 
10:     $counter \leftarrow counter + 1$ 
11:  end while
12:  if  $fx = 0$  then
13:    WRITE x1 is a root
14:  else if  $error < tol$  then
15:    WRITE x1 is a root approximation with tolerance = tol
16:  else
17:    WRITE The method failed at niter iteration
18:  end if
19: end function

```

5: Newton

```

1: function Newton(f, fder, tol, x0, niter)                                ▷ fder is the first derivative of f
2:    $fx \leftarrow f(x0)$ 
3:    $dfx \leftarrow fder(x0)$ 
4:    $counter \leftarrow 0$ 
5:    $error \leftarrow tol + 1$ 
6:   while  $error > tol$  AND  $fx \neq 0$  AND  $dfx \neq 0$  AND  $counter < niter$  do
7:      $x1 \leftarrow x0 - (fx/dfx)$ 
8:      $fx \leftarrow f(x1)$ 
9:      $dfx \leftarrow fder(x1)$ 
10:     $error \leftarrow |x1 - x0|$ 
11:     $x0 \leftarrow x1$ 
12:     $counter \leftarrow counter + 1$ 
13:  end while
14:  if  $fx = 0$  then
15:    WRITE x0 is a root of f
16:  else if  $error < tolerance$  then
17:    WRITE x1 is a root approximation with tolerance tol
18:  else if  $dfx = 0$  then
19:    WRITE x1 is a possible multiple root
20:  else
21:    WRITE The method failed at niter iteration
22:  end if
23: end function

```

6: Secant

```

1: function Secant(x0, x1, tol, iter, f)
2:    $y0 \leftarrow f(x0)$ 
3:   if  $y0 = 0$  then
4:     WRITE x0 is a root of f
5:   else
6:      $y1 \leftarrow f(x1)$ 
7:      $d \leftarrow y1 - y0$ 
8:      $error \leftarrow tol + 1$ 
9:      $cont \leftarrow 0$ 
10:    while  $y1 \neq 0$  AND  $error > tol$  AND  $cont < iter$  AND  $d \neq 0$  do
11:       $x2 \leftarrow x1 - ((y1 * (x1 - x0)) / (d))$ 
12:       $error \leftarrow |x2 - x1|$ 
13:       $x0 \leftarrow x1$ 
14:       $y0 \leftarrow y1$ 
15:       $y1 \leftarrow f(x2)$ 
16:       $x1 \leftarrow x2$ 
17:       $d \leftarrow y1 - y0$ 
18:       $counter \leftarrow counter + 1$ 
19:    end while
20:    if  $y1 = 0$  then
21:      WRITE x1 is a root of f
22:    else
23:      if  $error < tol$  then
24:        WRITE x1 is an approximation to a root with a tolerance =  $tol$ 
25:      else
26:        if  $d = 0$  then
27:          WRITE There is a multiple root
28:        else
29:          WRITE failure in  $iter$  iterations
30:        end if
31:      end if
32:    end if
33:  end if
34: end function

```

7: Multiple Root

```

1: function MultipleRoot(f,f1,f2,x0,tolerance,nMax)
2:    $xi \leftarrow x0$ 
3:    $f_{xi} \leftarrow f(xi)$ 
4:   if  $f_{xi} = 0$  then
5:     WRITE A root was found:  $xi$ 
6:   else
7:      $counter \leftarrow 0$ 
8:      $f1_{xi} \leftarrow f1(xi)$ 
9:      $f2_{xi} \leftarrow f2(xi)$ 
10:     $error \leftarrow tolerance + 1$ 
11:     $det \leftarrow (f1_{xi}^2) - (f_{xi} * f2_{xi})$ 
12:    while  $f_{xi} \neq 0$  AND  $error > tolerance$  AND  $counter < nMax$  AND  $det \neq 0$  do
13:       $xi_{Aux} \leftarrow xi$ 
14:       $x1 \leftarrow x1 - ((f_{xi} * f1_{xi}) / ((f1_{xi}^2) - (f_{xi} * f2_{xi})))$ 
15:       $f_{xi} \leftarrow f(xi)$ 
16:       $f1_{xi} \leftarrow f1(xi)$ 
17:       $f2_{xi} \leftarrow f2(xi)$ 
18:       $error \leftarrow |xi - xi_{Aux}|$ 
19:       $det \leftarrow (f1_{xi}^2) - (f_{xi} * f2_{xi})$ 
20:       $counter \leftarrow counter + 1$ 
21:    end while
22:    if  $f_{x1} = 0$  then
23:      WRITE A root was found:  $xi$ 
24:    else if  $error \leq tolerance$  then
25:      WRITE One approach is:  $xi$ 
26:    else if  $det = 0$  then
27:      WRITE Method failure
28:    else
29:      WRITE The method fails with the maximum number of iterations given
30:    end if
31:  end if
32:   $x \leftarrow xi$ 
33: end function

```

8: Simple Gauss Elimination

```

1: function GaussSimple(A,b,n)
2:    $A \leftarrow \text{Concat}(A, b)$ 
3:   for  $i \leftarrow 1, n-1$  do
4:     if  $A_{i,i} = 0$  then
5:       WRITE Mathematical Error! Stop
6:     end if
7:     for  $j \leftarrow i+1, n$  do
8:       if  $A_{j,i} \neq 0$  then
9:          $A_j \leftarrow A_j - (A_{ji}/A_{ii}) * A_i$ 
10:      end if
11:    end for
12:    display(A)
13:  end for
14:   $X_n \leftarrow A_{n,n+1}/A_{n,n}$ 
15:  for  $i \leftarrow n-1, 1, \text{step} = -1$  do
16:     $X_i \leftarrow A_{i,n+1}$ 
17:    for  $j \leftarrow i+1, n$  do
18:       $X_i \leftarrow X_i - A_{i,j} * X_j$ 
19:    end for
20:     $X_i \leftarrow X_i/A_{i,i}$ 
21:  end for
22:  WRITE "Answer vector"
23:  for  $i \leftarrow 1, n$  do
24:    WRITE  $X_i$ 
25:  end for
26: end function

```

9: Gauss Elimination with Partial Pivoting

```

1: function GaussPartial(A,b,n,delta,niter)
2:    $A \leftarrow \text{Concat}(A, b)$ 
3:   for  $i \leftarrow 1, n-1$  do
4:     WRITE changeRows(A,i)
5:     if  $A_{i,i} = 0$  then
6:       WRITE Mathematical Error! Stop
7:     end if
8:     for  $k \leftarrow 1, n+1$  do
9:        $A_{j,k} \leftarrow A_{j,k} - \text{ratio} * A_{i,k}$ 
10:    end for
11:  end for
12:   $X_n \leftarrow A_{n,n+1}/A_{n,n}$ 
13:  for  $i \leftarrow n-1, 1, \text{step} = -1$  do
14:     $X_i \leftarrow A_{i,n+1}$ 
15:    for  $j \leftarrow i+1, n$  do
16:       $X_i \leftarrow X_i - A_{i,j} * X_j$ 
17:    end for
18:     $X_i \leftarrow X_i/A_{i,i}$ 
19:  end for
20:  WRITE "Answer vector"
21:  for  $i \leftarrow 1, n$  do
22:    WRITE  $X_i$ 
23:  end for
24: end function

```


10: Gauss Elimination with Total Pivoting

```

1: function GaussTotal(A,b,n,delta,niter)
2:    $A \leftarrow \text{Concat}(A,b)$ 
3:   for  $i \leftarrow 1, n-1$  do
4:     WRITE changeRowsAndColumns(A,i)
5:     if  $A_{i,i} = 0$  then
6:       WRITE Mathematical Error! Stop
7:     end if
8:     for  $j \leftarrow i+1, n$  do
9:        $ratio \leftarrow A_{j,i}/A_{i,i}$ 
10:      for  $k \leftarrow 1, n+1$  do
11:         $A_{j,k} \leftarrow A_{j,k} - ratio * A_{i,k}$ 
12:      end for
13:    end for
14:  end for
15:   $X_n \leftarrow A_{n,n+1}/A_{n,n}$ 
16:  for  $i \leftarrow n-1, 1, step = -1$  do
17:     $X_i \leftarrow A_{i,n+1}$ 
18:    for  $j \leftarrow i+1, n$  do
19:       $X_i \leftarrow X_i - A_{i,j} * X_j$ 
20:    end for
21:     $X_i \leftarrow X_i/A_{i,i}$ 
22:  end for
23:  WRITE "Answer vector"
24:  for  $i \leftarrow 1, n$  do
25:    WRITE  $X_i$ 
26:  end for
27: end function

```

11: Steffensen

```

1: function Steffensen(f,x0,tol,n)
2:   for  $i = 1 \dots n$  do
3:      $x_1 \leftarrow f(x_0)$ 
4:      $x_2 \leftarrow f(x_1)$ 
5:      $p \leftarrow p_0 - (p_1 - p_0)^2 / (p_2 - 2 * p_1 + p_0)$ 
6:      $error \leftarrow \text{absoluteValue}(p - p_0)$ 
7:      $p_0 \leftarrow p$ 
8:      $count \leftarrow count + 1$ 
9:      $p_0 \leftarrow p$ 
10:  end for
11:  if  $f(p_0) = 0$  then
12:    WRITE  $p_0$  is a root
13:  else if  $error < tol$  then
14:    WRITE  $p_0$  is an approximation with tolerance = tol
15:  else
16:    WRITE failed to converge
17:  end if
18: end function

```

12: Aitken

```
1: function Aitken(f,x0,tol,n)
2:    $x1 \leftarrow f(x0)$ 
3:    $x2 \leftarrow f(x1)$ 
4:    $fxi \leftarrow f(x2)$ 
5:    $det \leftarrow (x2 - x1) - (x1 - x0)$ 
6:    $counter \leftarrow 4$ 
7:   while  $fxi \neq 0$  AND  $error > tol$  AND  $counter < n$  AND  $det \neq 0$  do
8:      $xi \leftarrow ((x2 - x1)^2) / det$ 
9:      $fxi \leftarrow f(xi)$ 
10:     $det \leftarrow (x2 - x2) - (x1 - x0)$ 
11:     $error \leftarrow absoluteValue(xi - x2)$ 
12:     $x0 \leftarrow xi$ 
13:     $x1 \leftarrow f(x0)$ 
14:     $x2 \leftarrow f(x1)$ 
15:     $counter \leftarrow counter + 1$ 
16:  end while
17:  if  $fxi = 0$  then
18:    WRITE "xi is a root"
19:  else if  $error \leq tol$  then
20:    WRITE "xi is an approximation"
21:  else if  $det = 0$  then
22:    WRITE "Error during method execution"
23:  else
24:    WRITE "The method fails with the maximum number of iterations"
25:  end if
26: end function
```

13: Muller

```

1: function Muller(f, x0, tol, nMax)
2:    $fx0 \leftarrow f(x0)$ 
3:    $fx1 \leftarrow f(x1)$ 
4:    $x1 \leftarrow (x0 + x1)/2$ 
5:    $fx2 \leftarrow f(x2)$ 
6:    $h0 \leftarrow x1 - x0$ 
7:    $h1 \leftarrow x2 - x1$ 
8:    $\delta0 \leftarrow (fx1 - fx0)/h0$ 
9:    $\delta1 \leftarrow (fx2 - fx1)/h1$ 
10:   $a \leftarrow (\delta1 - \delta0)/(h1 - h0)$ 
11:   $b \leftarrow a * h1 + \delta1$ 
12:   $c \leftarrow fx2$ 
13:   $xi \leftarrow x2 + (-2 * c)/(b + (b/|b|) * \text{sqrt}(b^2 - 4 * a * c))$ 
14:   $fxi \leftarrow f(xi)$ 
15:   $error \leftarrow tol + 1$ 
16:   $counter \leftarrow 0$ 
17:  while  $fx1 \neq 0$  &  $error > tol$  &  $counter < nMax$  do
18:     $x2Aux \leftarrow x2$ 
19:     $x1Aux \leftarrow x1$ 
20:     $x2 \leftarrow x1$ 
21:     $x1 \leftarrow x2Aux$ 
22:     $x0 \leftarrow x1Aux$ 
23:     $fx0 \leftarrow f(x0)$ 
24:     $fx1 \leftarrow f(x1)$ 
25:     $fx2 \leftarrow f(x2)$ 
26:     $h0 \leftarrow x1 - x0$ 
27:     $h1 \leftarrow x2 - x1$ 
28:     $\delta0 \leftarrow (fx1 - fx0)/h0$ 
29:     $\delta1 \leftarrow (fx2 - fx1)/h1$ 
30:     $a \leftarrow (\delta1 - \delta0)/(h1 - h0)$ 
31:     $b \leftarrow a * h1 + \delta1$ 
32:     $c \leftarrow fx2$ 
33:     $xi \leftarrow x2 + (-2 * c)/(b + b/|b|) * \text{sqrt}(b^2 - 4 * a * c)$ 
34:     $fxi \leftarrow f(xi)$ 
35:     $error \leftarrow tol + 1$ 
36:     $counter \leftarrow counter + 1$ 
37:  end while
38:  if  $fxi = 0$  then
39:    WRITE A root has been found it is xi
40:  else if  $error \leq tol$  then
41:    WRITE One approach has been found and it is xi
42:  else
43:    WRITE The method fails with the maximum number of iterations given
44:  end if
45: end function

```

14: Tridiagonal

```
1: function Tridiagonal(A,B,C,D)
2:    $N \leftarrow \text{lenght of D}$ 
3:    $C[0] \leftarrow C[0]/B[0]$ 
4:    $D[0] \leftarrow D[0]/B[0]$ 
5:   for  $i = 1 \dots N$  do
6:      $aux \leftarrow B[i] - (A[i] * C[i - 1])$ 
7:      $C[i] \leftarrow C[i]/aux$ 
8:      $D[i] \leftarrow (D[i] - A[i] * D[i - 1])/aux$ 
9:   end for
10:   $x \leftarrow \text{vector of lenght N}$ 
11:  for  $i = 0 \dots N$  do
12:     $x[i] \leftarrow 0$ 
13:  end for
14:   $x[n - 1] \leftarrow D[N - 1]$ 
15:  for  $i = 0 \dots N - 1$  do
16:     $x[i] \leftarrow D[i] - C[i] * x[i + 1]$ 
17:  end for
18: end function
```

15: Trisection

```

1: function Trisection(f, left, right, tol, nIter)
2:    $fRight \leftarrow f(right)$ 
3:    $fLeft \leftarrow f(left)$ 
4:    $counter \leftarrow 0$ 
5:   if  $fRight = 0$  then
6:     WRITE right is a root
7:   else if  $fLeft = 0$  then
8:     WRITE left is a root
9:   else if  $fLeft * fRight < 0$  then
10:     $xmid1 \leftarrow left + (right - left)/3$ 
11:     $xmid2 \leftarrow right - (right - left)/3$ 
12:     $fXmid1 \leftarrow f(xmid1)$ 
13:     $fXmid2 \leftarrow f(xmid2)$ 
14:     $counter \leftarrow 1$ 
15:     $error1 \leftarrow tol + 1$ 
16:     $error2 \leftarrow tol + 1$ 
17:    while  $error1 > tol \ \& \ error2 > tol \ \& \ fXmid1 \neq 0 \ \& \ fXmid2 \neq 0 \ \& \ counter < nIter$  do
18:      if  $fLeft * fXmid1 < 0$  then
19:         $right \leftarrow xmid1$ 
20:         $fRight \leftarrow fXmid1$ 
21:      else if  $fXmid1 * fXmid2 < 0$  then
22:         $left \leftarrow xmid1$ 
23:         $fLeft \leftarrow fXmid1$ 
24:         $right \leftarrow xmid2$ 
25:         $fRight \leftarrow fXmid2$ 
26:      else
27:         $left \leftarrow xmid2$ 
28:         $fLeft \leftarrow fXmid2$ 
29:      end if
30:       $xAux1 \leftarrow xmid1$ 
31:       $xAux2 \leftarrow xmid2$ 
32:       $xmid1 \leftarrow left + (right - left)/3$ 
33:       $fXmid1 \leftarrow f(xmid1)$ 
34:       $xmid2 \leftarrow right - (right - left)/3$ 
35:       $fXmid2 \leftarrow f(xmid2)$ 
36:       $error1 \leftarrow |xmid1 - xAux1|$ 
37:       $error2 \leftarrow |xmid2 - xAux2|$ 
38:       $counter \leftarrow counter + 1$ 
39:    end while
40:    if  $fXmid1 = 0$  then
41:      WRITE  $xmid1$  is a root
42:    else if  $fXmid2 = 0$  then
43:      WRITE  $xmid2$  is a root
44:    else if  $error1 < tol$  then
45:      WRITE  $xmid1$  is an approximation with tolerance tol
46:    else if  $error2 < tol$  then
47:      WRITE  $xmid2$  is an approximation with tolerance tol
48:    else
49:      WRITE The method fails in nIter iterations
50:    end if
51:  end if

```

Results

1: Incremental Search

answer =

"There is at least one root between -2.5 and -2"

matrix =

3×6 [string](#) array

| "iteration" | "x0" | "x1" | "fx0" | "fx1" | "fx0*fx1" |
|-------------|--------|--------|------------|------------|-------------|
| "1" | "-3" | "-2.5" | "-0.48028" | "-0.19386" | "0.093108" |
| "2" | "-2.5" | "-2" | "-0.19386" | "0.10258" | "-0.019886" |

2: Bisection

answer =

"0.9364 is an approach with tolerance 1e-06"

A =

21×6 [string](#) array

| "counter" | "left" | "right" | "xmid" | "fmid" | "error" |
|-----------|------------|------------|------------|----------------|---------------|
| "1" | "0" | "1" | "0.5" | "-0.29311" | "1" |
| "2" | "0.5" | "1" | "0.75" | "-0.1184" | "0.25" |
| "3" | "0.75" | "1" | "0.875" | "-0.036818" | "0.125" |
| "4" | "0.875" | "1" | "0.9375" | "0.00063392" | "0.0625" |
| "5" | "0.875" | "0.9375" | "0.90625" | "-0.017772" | "0.03125" |
| "6" | "0.90625" | "0.9375" | "0.92188" | "-0.0084866" | "0.015625" |
| "7" | "0.92188" | "0.9375" | "0.92969" | "-0.0039054" | "0.0078125" |
| "8" | "0.92969" | "0.9375" | "0.93359" | "-0.0016304" | "0.0039062" |
| "9" | "0.93359" | "0.9375" | "0.93555" | "-0.00049694" | "0.0019531" |
| "10" | "0.93555" | "0.9375" | "0.93652" | "6.8822e-05" | "0.00097656" |
| "11" | "0.935547" | "0.936523" | "0.936035" | "-0.000213974" | "0.000488281" |
| "12" | "0.936035" | "0.936523" | "0.936279" | "-7.25548e-05" | "0.000244141" |
| "13" | "0.936279" | "0.936523" | "0.936401" | "-1.86098e-06" | "0.00012207" |
| "14" | "0.936401" | "0.936523" | "0.936462" | "3.3482e-05" | "6.10352e-05" |
| "15" | "0.936401" | "0.936462" | "0.936432" | "1.58108e-05" | "3.05176e-05" |
| "16" | "0.936401" | "0.936432" | "0.936417" | "6.97501e-06" | "1.52588e-05" |
| "17" | "0.936401" | "0.936417" | "0.936409" | "2.55703e-06" | "7.62939e-06" |
| "18" | "0.936401" | "0.936409" | "0.936405" | "3.48029e-07" | "3.8147e-06" |
| "19" | "0.936401" | "0.936405" | "0.936403" | "-7.56477e-07" | "1.90735e-06" |
| "20" | "0.936403" | "0.936405" | "0.936404" | "-2.04223e-07" | "9.53674e-07" |

3: False Rule

0.936405 is an approximation to a root with a tolerance 1e-06

| Iterations | Xi | Xs | Xm | Ym | Error | |
|--------------------|----|-------------------|--------------------|-------------------|--------------------|--------------------|
| 1.0000000000000000 | | 0 | 1.0000000000000000 | 0.933940380718216 | -0.001429076703686 | 1.0000010000000000 |
| 2.0000000000000000 | | 0.933940380718216 | 1.0000000000000000 | 0.936506051665625 | 0.000058756008358 | 0.002739620254291 |
| 3.0000000000000000 | | 0.933940380718216 | 0.936506051665625 | 0.936404730742641 | 0.00000086782541 | 0.000108202062268 |
| 4.0000000000000000 | | 0.933940380718216 | 0.936404730742641 | 0.936404581100869 | 0.000000000128154 | 0.000000159804614 |

4: Fixed Point

answer =

"-0.37444 is an approximation to a root with a tolerance 1e-06"

matrix =

27×4 [string](#) array

| "iteration" | "xn" | "f(xn)" | "error" |
|-------------|-------------|----------------|---------------|
| "0" | "-0.5" | "0.20689" | "1" |
| "1" | "-0.29311" | "-0.12671" | "0.20689" |
| "2" | "-0.41982" | "0.073517" | "0.12671" |
| "3" | "-0.3463" | "-0.044654" | "0.073517" |
| "4" | "-0.39096" | "0.026553" | "0.044654" |
| "5" | "-0.36441" | "-0.016021" | "0.026553" |
| "6" | "-0.38043" | "0.0095895" | "0.016021" |
| "7" | "-0.37084" | "-0.0057689" | "0.0095895" |
| "8" | "-0.37661" | "0.0034602" | "0.0057689" |
| "9" | "-0.37315" | "-0.0020792" | "0.0034602" |
| "10" | "-0.37522" | "0.0012481" | "0.0020792" |
| "11" | "-0.373977" | "-0.00074963" | "0.00124806" |
| "12" | "-0.374726" | "0.000450082" | "0.00074963" |
| "13" | "-0.374276" | "-0.000270295" | "0.000450082" |
| "14" | "-0.374546" | "0.000162302" | "0.000270295" |
| "15" | "-0.374384" | "-9.74644e-05" | "0.000162302" |
| "16" | "-0.374482" | "5.85256e-05" | "9.74644e-05" |
| "17" | "-0.374423" | "-3.51447e-05" | "5.85256e-05" |
| "18" | "-0.374458" | "2.1104e-05" | "3.51447e-05" |
| "19" | "-0.374437" | "-1.26729e-05" | "2.1104e-05" |
| "20" | "-0.37445" | "7.60996e-06" | "1.26729e-05" |
| "21" | "-0.374442" | "-4.56974e-06" | "7.60996e-06" |
| "22" | "-0.374447" | "2.7441e-06" | "4.56974e-06" |
| "23" | "-0.374444" | "-1.64781e-06" | "2.7441e-06" |
| "24" | "-0.374446" | "9.89502e-07" | "1.64781e-06" |
| "25" | "-0.374445" | "-5.9419e-07" | "9.89502e-07" |

5: Newton

answer =

"0.9364 is a root approximation with a tolerance of 1e-06"

matrix =

6×5 [string](#) array

| "iteration" | "xn" | "f(xn)" | "f'(xn)" | "erro" |
|-------------|-----------|---------------|-----------|--------------|
| "1" | "0.5" | "-0.29311" | "0.68421" | "1" |
| "2" | "0.92839" | "-0.0046622" | "0.58461" | "0.42839" |
| "3" | "0.93637" | "-2.1913e-05" | "0.57911" | "0.0079748" |
| "4" | "0.9364" | "-4.9834e-10" | "0.57908" | "3.7839e-05" |
| "5" | "0.9364" | "-1.1102e-16" | "0.57908" | "8.6057e-10" |

6: Secant

0.936405 is an approximation to a root with a tolerance $1e-06$

| Iterations | Xn | y1 | Error |
|--------------------|--------------------|--------------------|--------------------|
| 0 | 1.0000000000000000 | 0.035366079380240 | 1.0000010000000000 |
| 1.0000000000000000 | 0.946166222306525 | 0.005619392737864 | 0.053833777693475 |
| 2.0000000000000000 | 0.935996580791173 | -0.000236322174701 | 0.010169641515352 |
| 3.0000000000000000 | 0.936407002376704 | 0.000001402235891 | 0.000410421585531 |
| 4.0000000000000000 | 0.936404581473120 | 0.000000000343716 | 0.000002420903584 |
| 5.0000000000000000 | 0.936404580879561 | -0.000000000000000 | 0.000000000593558 |

7: Multiple Roots

```
>> raicesMul(h,hder,hder2,1,tol,N)
"counter"    "xi"          "fxi"          "error"
"0"          "1"          "0.71828"      "1"
"1"          "-0.23421"    "0.025406"     "1.2342"
"2"          "-0.0084583"    "3.5671e-05"   "0.22575"
"3"          "-1.189e-05"     "7.0688e-11"   "0.0084464"
"4"          "-4.2186e-11"     "0"            "1.189e-05"
```

A root was found: $-4.21859069894e-11$

ans =

$-4.21859069893579e-11$

8: Simple Gauss Elimination

| | | | | | |
|---------|---|----|-----|-------------------|-------------------|
| Stage 1 | 2 | -1 | 0 | 3 | 1 |
| | 0 | 1 | 3 | 6.5 | 0.5 |
| | 0 | 13 | -2 | 11 | 1 |
| | 0 | 12 | -2 | -18 | -6 |
| Stage 2 | 2 | -1 | 0 | 3 | 1 |
| | 0 | 1 | 3 | 6.5 | 0.5 |
| | 0 | 0 | -41 | -73.5 | -5.5 |
| | 0 | 0 | -38 | -96 | -12 |
| Stage 3 | 2 | -1 | 0 | 3 | 1 |
| | 0 | 1 | 3 | 6.5 | 0.5 |
| | 0 | 0 | -41 | -73.5 | -5.5 |
| | 0 | 0 | 0 | -27.8780487804878 | -6.90243902439024 |

ans =

| | | | |
|--------------------|--------------------|--------------------|-------------------|
| 0.0384951881014872 | -0.180227471566054 | -0.309711286089239 | 0.247594050743657 |
|--------------------|--------------------|--------------------|-------------------|

9: Gauss Elimination with Partial Pivoting

| | | | | | |
|---------|--------------------|----------------------|--------------------|-------------------|-------------------|
| Stage 0 | 2 | -1 | 0 | 3 | 1 |
| | 1 | 0.5 | 3 | 8 | 1 |
| | 0 | 13 | -2 | 11 | 1 |
| | 14 | 5 | -2 | 3 | 1 |
| Stage 1 | 14 | 5 | -2 | 3 | 1 |
| | 0 | 0.142857142857143 | 3.14285714285714 | 7.78571428571429 | 0.928571428571429 |
| | 0 | 13 | -2 | 11 | 1 |
| | 0 | -1.71428571428571 | 0.285714285714286 | 2.57142857142857 | 0.857142857142857 |
| Stage 2 | 14 | 5 | -2 | 3 | 1 |
| | 0 | 13 | -2 | 11 | 1 |
| | 0 | 0 | 3.16483516483516 | 7.66483516483516 | 0.917582417582418 |
| | 0 | 2.22044604925031e-16 | 0.021978021978022 | 4.02197802197802 | 0.989010989010989 |
| Stage 3 | 14 | 5 | -2 | 3 | 1 |
| | 0 | 13 | -2 | 11 | 1 |
| | 0 | 0 | 3.16483516483516 | 7.66483516483516 | 0.917582417582418 |
| | 0 | 2.22044604925031e-16 | 0 | 3.96875 | 0.982638888888889 |
| ans = | 0.0384951881014873 | -0.180227471566054 | -0.309711286089239 | 0.247594050743657 | |

10: Gauss Elimination with Total Pivoting

| | | | | | |
|---------|--------------------|----------------------|--------------------|-------------------|-------------------|
| Stage 0 | 2 | -1 | 0 | 3 | 1 |
| | 1 | 0.5 | 3 | 8 | 1 |
| | 0 | 13 | -2 | 11 | 1 |
| | 14 | 5 | -2 | 3 | 1 |
| Stage 1 | 14 | 5 | -2 | 3 | 1 |
| | 0 | 0.142857142857143 | 3.14285714285714 | 7.78571428571429 | 0.928571428571429 |
| | 0 | 13 | -2 | 11 | 1 |
| | 0 | -1.71428571428571 | 0.285714285714286 | 2.57142857142857 | 0.857142857142857 |
| Stage 2 | 14 | 5 | -2 | 3 | 1 |
| | 0 | 13 | -2 | 11 | 1 |
| | 0 | 0 | 3.16483516483516 | 7.66483516483516 | 0.917582417582418 |
| | 0 | 2.22044604925031e-16 | 0.021978021978022 | 4.02197802197802 | 0.989010989010989 |
| Stage 3 | 14 | 5 | 3 | -2 | 1 |
| | 0 | 13 | 11 | -2 | 1 |
| | 0 | 0 | 7.66483516483516 | 3.16483516483516 | 0.917582417582418 |
| | 0 | 2.22044604925031e-16 | 0 | -1.63870967741936 | 0.50752688172043 |
| ans = | 0.0384951881014873 | -0.180227471566054 | -0.309711286089239 | 0.247594050743657 | |

11: Trisection

| | | | | | | | | |
|-------------|--|-------------|-------------|-------------|----------------|----------------|---------------|---------------|
| answer = | "-0.9364 is an approximation with tolerance 1e-06" | | | | | | | |
| matrix = | 15x9 string array | | | | | | | |
| "iteration" | "left" | "right" | "xmid1" | "xmid2" | "f(xmid1)" | "f(xmid2)" | "error1" | "error2" |
| "1" | "-1" | "0" | "-0.66667" | "-0.33333" | "-0.17619" | "-0.3983" | "1" | "1" |
| "2" | "-1" | "-0.66667" | "-0.88889" | "-0.77778" | "-0.028277" | "-0.099628" | "0.22222" | "0.44444" |
| "3" | "-1" | "-0.88889" | "-0.96296" | "-0.92593" | "0.01513" | "-0.0061059" | "0.074074" | "0.14815" |
| "4" | "-0.96296" | "-0.92593" | "-0.95062" | "-0.93827" | "0.0081593" | "0.0010799" | "0.012346" | "0.012346" |
| "5" | "-0.93827" | "-0.92593" | "-0.93416" | "-0.93004" | "-0.0013036" | "-0.003699" | "0.016461" | "0.0082305" |
| "6" | "-0.93827" | "-0.93416" | "-0.9369" | "-0.93553" | "0.00028672" | "-0.00050781" | "0.0027435" | "0.005487" |
| "7" | "-0.9369" | "-0.93553" | "-0.93644" | "-0.93599" | "2.2025e-05" | "-0.00024282" | "0.00045725" | "0.00045725" |
| "8" | "-0.93644" | "-0.93599" | "-0.93629" | "-0.93614" | "-6.624e-05" | "-0.00015452" | "0.00015242" | "0.00015242" |
| "9" | "-0.93644" | "-0.93629" | "-0.93639" | "-0.93634" | "-7.3953e-06" | "-3.6817e-05" | "0.00010161" | "0.00020322" |
| "10" | "-0.93644" | "-0.93639" | "-0.93643" | "-0.93641" | "1.2218e-05" | "2.4115e-06" | "3.387e-05" | "6.774e-05" |
| "11" | "-0.936409" | "-0.936392" | "-0.936403" | "-0.936397" | "-8.57402e-07" | "-4.12634e-06" | "2.25801e-05" | "1.12901e-05" |
| "12" | "-0.936409" | "-0.936403" | "-0.936407" | "-0.936405" | "1.32188e-06" | "2.32238e-07" | "3.76335e-06" | "7.52671e-06" |
| "13" | "-0.936405" | "-0.936403" | "-0.936404" | "-0.936404" | "-1.30975e-07" | "-4.94189e-07" | "2.5089e-06" | "1.25445e-06" |
| "14" | "-0.936405" | "-0.936404" | "-0.936405" | "-0.936405" | "1.11167e-07" | "-9.90421e-09" | "4.1815e-07" | "8.36301e-07" |

12: Steffensen

ans =

"-0.37445 is an approximation with tolerance 1e-06"

matrix =

7×3 string array

| "iteration" | "p" | "error" |
|-------------|------------|--------------|
| "0" | "1" | "" |
| "1" | "-1.1614" | "2.1614" |
| "2" | "-0.29639" | "0.86501" |
| "3" | "-0.37339" | "0.076997" |
| "4" | "-0.37444" | "0.0010573" |
| "5" | "-0.37445" | "1.9539e-07" |

13: Muller

| "Counter" | "xi" | "Fxi" | "Error" |
|-----------|------------------------|---------------------------|-----------------|
| "0" | "-1.5043" | "0.19094" | "1" |
| "1" | "-1.1709" | "0.11434" | "0.33342" |
| "2+0i" | "-0.72832-0.64074i" | "-0.019849+0.53616i" | "0.77873+0i" |
| "3+0i" | "-0.80786-0.054804i" | "-0.078939+0.036014i" | "0.59131+0i" |
| "4+0i" | "-0.90184-0.046692i" | "-0.019714+0.028149i" | "0.09433+0i" |
| "5+0i" | "-0.93066-0.0058347i" | "-0.0033277+0.003402i" | "0.049997+0i" |
| "6+0i" | "-0.93694-0.00081382i" | "0.00031304+0.00047096i" | "0.0080461+0i" |
| "7+0i" | "-0.93642-1.093e-06i" | "7.8828e-06+6.3292e-07i" | "0.00096849+0i" |
| "8+0i" | "-0.9364+1.9213e-08i" | "-5.1544e-09-1.1126e-08i" | "1.3667e-05+0i" |
| "9+0i" | "-0.9364-3.3272e-13i" | "6.6058e-14+1.9267e-13i" | "2.1175e-08+0i" |

An approximation has been found and is: -0.93640458088-3.32717949702e-13i

14: Aitken

```
>> aitken(f, 1, tol, N)
  "counter"  "xi"      "fxi"      "error"
  "1"        "1"      "0.035366"  "2"
  "2"        "0.035366" "-0.49875"  "0.96463"
  "3"        "-0.49875" "-0.29396"  "0.53412"
  "4"        "-1.1614"  "0.11061"  "0.66265"
  "5"        "-1.3199"  "0.16184"  "0.83202"
  "6"        "-0.25797" "-0.43694"  "0.21639"
  "7"        "-0.33039" "-0.39994"  "0.0048809"
  "8"        "-0.36486" "-0.38016"  "0.0060154"
  "9"        "-0.37176" "-0.37605"  "0.00075755"
  "10"       "-0.37375" "-0.37486"  "0.00027184"
  "11"       "-0.374259" "-0.374557" "6.50585e-05"
  "12"       "-0.374396" "-0.374475" "1.79039e-05"
  "13"       "-0.374432" "-0.374453" "4.68176e-06"
  "14"       "-0.374442" "-0.374447" "1.24684e-06"
  "15"       "-0.374444" "-0.374446" "3.29869e-07"
```

An approximation has been found and is: -0.374444108719

Members signatures


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