

C++ Assignments | Problems on sorting | Week 9

1. What is an in-place sorting algorithm?

- a) It needs $O(1)$ or $O(\log n)$ memory to create auxiliary locations
- b) The input is already sorted and in-place
- c) It requires additional storage
- d) It requires additional space

Answer:- a) It needs $O(1)$ or $O(\log n)$ memory to create auxiliary locations

2. In the following scenarios, when will you use selection sort?

- a) The input is already sorted
- b) A large file has to be sorted
- c) Large values need to be sorted with small keys
- d) Small values need to be sorted with large keys

Answer:- b) A large file has to be sorted

3. Given an integer array and an integer k where $k \leq \text{size of array}$, We need to return the k th

smallest element of the array.

Answer:- To find the k th smallest element in an array efficiently, you have several options:

- **Sorting:** Sort the array and directly access the k th element. This takes $O(n \log n)$ time complexity.
- **Min-Heap:** Use a min-heap to extract the minimum k times, which also takes $O(n \log k)$ time complexity.
- **Quickselect algorithm:** This algorithm is like quicksort but focuses on partitioning around the k th smallest element, achieving average $O(n)$ time complexity.

4. Find the minimum operations required to sort the array in increasing order. In one operation,

you can set each occurrence of one element to 0.

Answer:-

To sort the array with minimum operations where each operation sets occurrences of one element to 0, consider:

- **Counting Sort:** Count occurrences of each element and reconstruct the array. This can be done in $O(n + k)$ time, where k is the range of elements.
- **Frequency Array Approach:** Similar to counting sort, but directly operates on the original array to reduce elements to 0.

```
#include <vector>
```

```
#include <algorithm>
```

```
int findKForSortedTransformation(std::vector<int>& arr) {
```

```
    int n = arr.size();
```

```
    if (n == 0) return -1;
```

```
    std::sort(arr.begin(), arr.end());
```

```
    int medianIndex = n / 2;
```

```
    return arr[medianIndex];
```

```
}
```

5. Given an array, `arr[]` containing n integers, the task is to find an integer (say K) such that after replacing each and every index of the array by $|a_i - K|$ where ($i \in [1, n]$), results in a sorted

array. If no such integer exists that satisfies the above condition then return -1 .

To find the integer K such that replacing each element by $|a_i - K|$ results in a sorted array:

- **Middle Element:** If the array is sorted in non-decreasing order, K should ideally be the median of the array. This ensures that after transformation, the array remains sorted.

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