

A tutorial on clonal ordering and visualization using ClonEvol

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Last updated: 2017-08-14

Contents

What is ClonEvol?	3
Installation	4
Clonal evolution analysis workflow	5
Step 1: Preparing variants for clonal evolution inference	5
Step 2: Clustering variants	5
Step 3: Evaluating the variant clustering results	6
Loading ClonEvol and AML1 clustering data	6
Preparing clustering data	6
Choosing colors for the clones	7
Visualizing the variant clusters	7
Plotting pairwise VAFs or CCFs across samples	9
Plotting mean/median of clusters across samples (cluster flow)	9
Step 4: Clonal ordering with ClonEvol	9
Inferring clonal evolution trees	9
Mapping driver events onto the trees	10
Converting node-based trees to branch-based trees	10
Where are trees stored?	11

Step 5: Visualizing the results	11
Plotting multiple plots and trees together	11
Plotting trees	13
Visualizing trees predicted by other tools	13
How to obtain the best visualizations?	14
Step 6: Interpretating the results	16
Clonal mixture of individual samples	16
ClonEvol's trees	16
Clonal seedings between samples	16
Session Info	16
References	17

What is ClonEvol?

ClonEvol is a package for clonal ordering and clonal evolution visualization. It uses the clustering of heterozygous variants identified using other tools as input to infer consensus clonal evolution trees and estimate the cancer cell fraction (also called clonal frequency) of the clones in individual samples. ClonEvol can deal with statistical uncertainty and error in sequencing and data analysis that may distort the cellular prevalence estimate of individual variants.

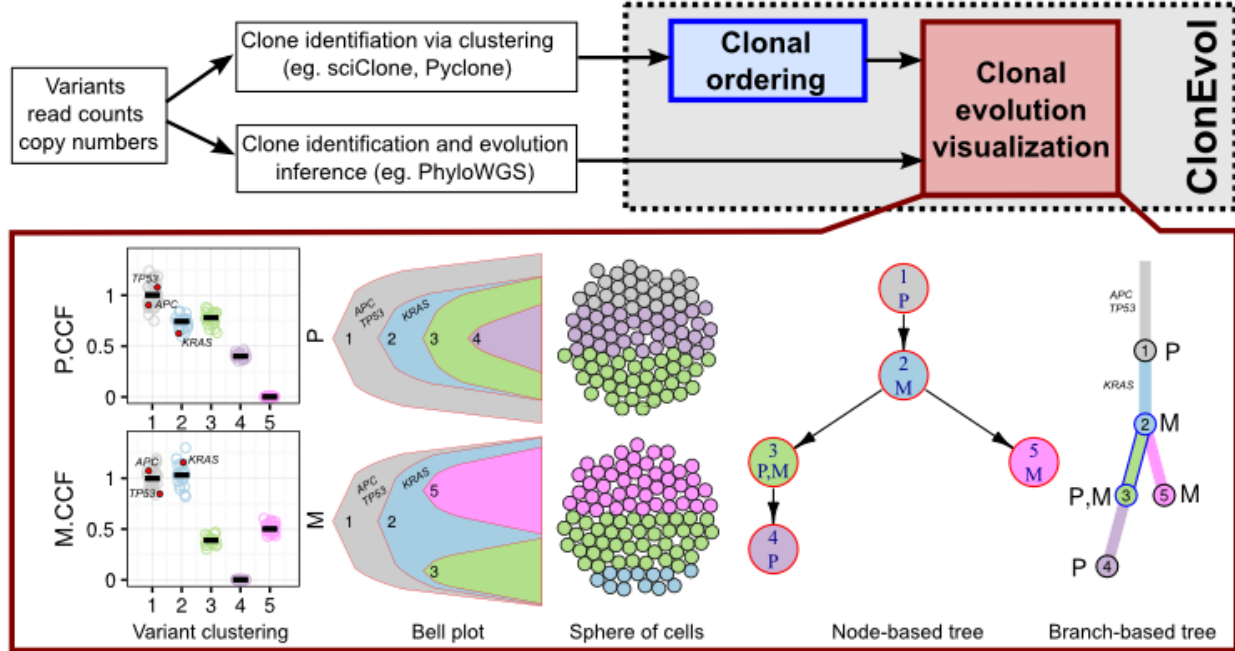


Figure 1: Overview of ClonEvol. ClonEvol infers and visualizes clonal evolution trees using variants preclustered by other methods. It can also visualizes trees identified by other methods.

ClonEvol uses a bootstrap resampling approach to estimate the cancer cell fraction (CCF) of the clones (ie. clonal frequency), given the CCF of the variants and their clusters, via the following equation (referred to as the sum rule).

$$CCF(clone Y) = CCF(cluster Y) - \sum_{X_i \in \text{all direct subclones of } Y} CCF(cluster X_i)$$

This results in a bootstrap estimate of the sampling distribution of the CCF of clone Y (given its direct subclones X_i) that can be subsequently used to estimate: (i) the confidence interval for the CCF of clone Y ; and (ii) the probability that the CCF of clone Y is negative (or non-negative).

A negative CCF estimate for a clone Y indicates that the sum rule is violated by the ordering that all clones $\{X_i\}$ are arisen directly from clone Y in a clonal evolution model. A negative

CCF estimate could also be resulted from the statistical uncertainty and errors (mentioned above) present in the cellular prevalence and clustering of variants as input to ClonEvol. Hence, the sum rule is only considered violated in ClonEvol if the confidence interval of the *CCF* of a clone is heavily shifted toward negative value, meaning the probability of negative *CCF* is high (or the probability that the *CCF* is non-negative is low).

ClonEvol evaluates the clonal ordering for all parental clones in all potential trees. A tree is reported if none of its clone violates the sum rule as described above.

ClonEvol can produce multiple visualizations (Figure 1), including:

1. Bell plots to present clonal dynamics over time (building upon the Fishplot (Ding et al. 2012))
2. Sphere of cells to present clonal subpopulations of a sample
3. Annotated node-based and branch-based trees to present clonal relationships and seeding patterns between samples.

ClonEvol is maintained at <https://github.com/hdng/clonevol>.

Installation

R requirements

ClonEvol requires R 2.15 or later. It has been tested with R versions: 2.15, 3.0.2, 3.2.1, 3.2.3, 3.3.3, 3.4.0 on MacOS and Linux.

Install from Github

```
install.packages('devtools')
library(devtools)
install_github('hdng/clonevol')
install.packages('gridBase')
install.packages('gridExtra')
install.packages('ggplot2')
install.packages('igraph')
install.packages('packcircles')
install_github('hdng/trees')
```

Install from Bioconductor

Currently unavailable

Clonal evolution analysis workflow

A typical analysis workflow for clonal evolution inference using sequencing data involves the following steps:

1. Preparing a comprehensive and reliable set of somatic mutations
2. Clustering the mutations based on cellular prevalence
3. Evaluating the clustering results
4. Inferring clonal evolution trees (ie. clonal ordering)
5. Visualizing data and clonal evolution trees
6. Interpreting the results

ClonEvol provides tools for steps 3-6 (see Figure 1). Steps 1-2 should be done prior to running ClonEvol, using other tools (briefly described below).

Step 1: Preparing variants for clonal evolution inference

The depth of sequencing, the quantity and quality of samples, and the quantity and quality of somatic variants can have a profound impact on the resulting clonal evolution models. In an ideal situation, we want:

1. Large number of samples
2. Large number of variants (exome sequencing is okay, but whole genome sequencing provides much better coverage of passenger somatic mutations)
3. Multiple time points
4. Multi-region samples (due to intra-tumor heterogeneity)
5. Deep sequencing, eg. targeted validation

This does not mean that we cannot study clonal evolution in cancer without such an ideal dataset. However, be prepared that in highly heterogeneous patients/tumors, your data may yield models that underestimate the true model.

Step 2: Clustering variants

Clustering the variants based on their cellular prevalence across samples is a critical step. The purpose of clustering variants is to identify the clones. Due to tumor heterogeneity, the cellular prevalence of distinct clones may be present at different frequency between samples (eg. sample A has 90% clone X and 10% clone Y while sample B has 50% clone X, 50% clone Y). Therefore, the clonal marker variants of a clone will show similar cellular prevalence

across samples and will likely be clustered together. The end product of a variant clustering tool is the clusters, each of them consists of the clonal marker variants of a distinct clone.

Cellular prevalence of variants used in the clustering algorithm is often measured by the variant allele frequency (*VAF*), calculated as the ratio of the number of reads carrying the variant and the total number of reads at the site. The assumption for the clustering algorithm to work is that *VAF* provides a good estimate of the cellular fraction of a variant, ie. the fraction of cells carrying the variant, which is the case with diploid heterozygous variants (copy number neutral). However, copy number variation is common in cancers, further deviating their *VAF* from actual cellular prevalence if left uncorrected. Both diploid heterozygous and copy-altered variants can be used to feed the clustering algorithms. If only diploid heterozygous variants are used, clustering can be performed using *sciClone* (Miller et al. 2014) and *VAF* can be used in *ClonEvol*. If copy-altered variants are used, clustering should be performed by copy number aware tools such as *Pyclone* (Roth et al. 2014). In the latter case, copy number corrected cellular prevalence estimate provided by the clustering tool is preferred to be used in *ClonEvol*, especially when there is bias between gain and loss events.

Step 3: Evaluating the variant clustering results

Since each cluster represents a clone, missing or incorrectly infer a cluster could hinder us from successful construction of the evolution models. Therefore, it is extremely important to obtain a good clustering result. *ClonEvol* provides a convenient visualization of variant clusters across multiple samples to help evaluate clustering results, particularly when no tree is inferred.

Assume that we already have a clustering result consisting of the cluster identity and the cellular prevalence estimate for individual variants. This can be stored as a tabular text file and read into a data frame using `read.table` function. Here we use data of a relapsed myeloid leukemia case (AML1) (Ding et al. 2012) available with *ClonEvol*. This is a simple case with two samples (a primary and a relapse) sequenced using whole genome and deep targeted validation.

Loading *ClonEvol* and AML1 clustering data

```
library(clonevol)
data(aml1)
x <- aml1$variants
```

Preparing clustering data

The clustering result as output from other tools may not be convenient for *ClonEvol* analysis and visualization. *ClonEvol* requires an input data frame consisting of at least a cluster

column and one or more variant cellular prevalence columns, each corresponds to a sample. The cluster should be named by contiguous integer numbers, starting from 1. For better visualization, the names of the cellular prevalence columns should be short.

```
# shorten vaf column names as they will be
vaf.col.names <- grep('.vaf', colnames(x), value=T)
sample.names <- gsub('.vaf', '', vaf.col.names)
x[, sample.names] <- x[, vaf.col.names]
vaf.col.names <- sample.names

# prepare sample grouping
sample.groups <- c('P', 'R');
names(sample.groups) <- vaf.col.names

# setup the order of clusters to display in various plots (later)
x <- x[order(x$cluster),]
```

Choosing colors for the clones

ClonEvol has built-in colors designed to distinguish ~20 different clones. However, users can also specify their own colors. To set up the colors for the clusters/clones that will be used throughout the visualizations, create a vector of colors as follow. In this case, we chose colors matching the original figure in Ding et al (2012).

```
clone.colors <- c('#999793', '#8d4891', '#f8e356', '#fe9536', '#d7352e')
```

If you want ClonEvol to choose colors for you, simply set it to NULL, like this.

```
clone.colors <- NULL
```

Visualizing the variant clusters

The following code will plot the clustering results for you to investigate. It will plot the cellular prevalence (CCF or VAF) of the variants across clusters and samples, using jitter, box, and violin plots to allow close investigation of the clustering. This plot is very powerful as it can visualize lots of samples and clusters at once.

```
pdf('box.pdf', width = 3, height = 3, useDingbats = FALSE, title='')
pp <- plot.variant.clusters(x,
  cluster.col.name = 'cluster',
  show.cluster.size = FALSE,
  cluster.size.text.color = 'blue',
```

```

vaf.col.names = vaf.col.names,
vaf.limits = 70,
sample.title.size = 20,
violin = FALSE,
box = FALSE,
jitter = TRUE,
jitter.shape = 1,
jitter.color = clone.colors,
jitter.size = 3,
jitter.alpha = 1,
jitter.center.method = 'median',
jitter.center.size = 1,
jitter.center.color = 'darkgray',
jitter.center.display.value = 'none',
highlight = 'is.driver',
highlight.shape = 21,
highlight.color = 'blue',
highlight.fill.color = 'green',
highlight.note.col.name = 'gene',
highlight.note.size = 2,
order.by.total.vaf = FALSE)
dev.off()

```

This should generate the jitter plot shown in Figure 2 of variants' VAF.

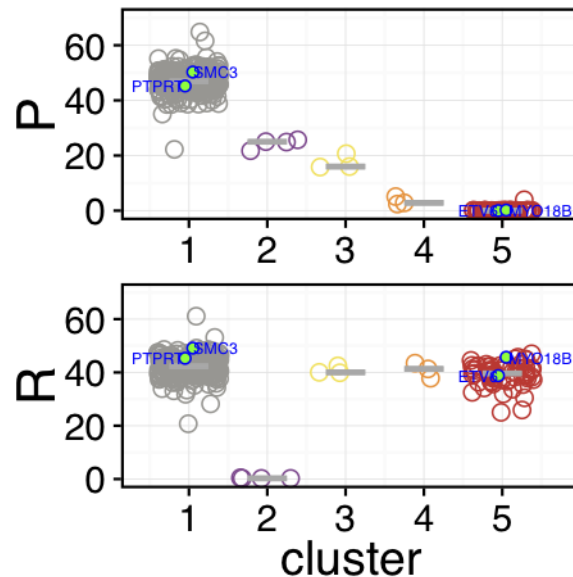


Figure 2: Visualization of multiple clusters across mutiple samples

When evaluating the clusters, look for potential outlier clusters (eg. ones with small number of variants), potential merged clusters (eg. ones that have variants with *VAF* stretching from

zero to non-zero values in multiple samples, that can be further splitted into multiple clusters), noise clusters (eg. ones that show very similar and low *VAF* across samples, indicating false variant calls). These conditions could be more relaxed with deeper sequencing as clustering can be more accurate. For AML1 case, several small clusters exists (as shown in Figure 2) but ultra-deep sequencing makes them interpretable.

Plotting pairwise VAFs or CCFs across samples

If you need to inspect variant clusters across pairs of samples, the following command is useful for pairwise plot of *VAF* or *CCF*.

```
plot.pairwise(x, col.names = vaf.col.names,  
              out.prefix = 'variants.pairwise.plot',  
              colors = clone.colors)
```

Plotting mean/median of clusters across samples (cluster flow)

```
pdf('flow.pdf', width=3, height=3, useDingbats=FALSE, title='')  
plot.cluster.flow(x, vaf.col.names = vaf.col.names,  
                  sample.names = c('Primary', 'Relapse'),  
                  colors = clone.colors)  
dev.off()
```

Step 4: Clonal ordering with ClonEvol

Inferring clonal evolution trees

At this step, we assume that you already thoroughly looked at your clustering and feel confident about it. Let's tell ClonEvol to perform clonal ordering and construct the consensus trees. In this example AML1 case, we will use *VAF* of variants. If your data contain copy-altered variants and copy number corrected *CCF* estimated by the clustering tool (eg. Pyclone), you can provide the corrected *CCF* to ClonEvol via *ccf.col.names* parameter in *infer.clonal.models* function, or calculate the equivalent copy number corrected *VAF* as half of the *CCF*.

```
y = infer.clonal.models(variants = x,  
                        cluster.col.name = 'cluster',  
                        vaf.col.names = vaf.col.names,  
                        sample.groups = sample.groups,  
                        cancer.initiation.model='monoclonal',
```

```

subclonal.test = 'bootstrap',
subclonal.test.model = 'non-parametric',
num.boots = 1000,
founding.cluster = 1,
cluster.center = 'mean',
ignore.clusters = NULL,
clone.colors = clone.colors,
min.cluster.vaf = 0.01,
# min probability that CCF(clone) is non-negative
sum.p = 0.05,
# alpha level in confidence interval estimate for CCF(clone)
alpha = 0.05)

```

The `infer.clonal.models` function takes the clustering results and evaluates all clonal orderings to reconstruct the clonal evolution trees and estimate the *CCF* of the clones in individual samples. Several important parameters are:

- `variants`: the variant clustering data frame
- `cluster.col.name`: name of cluster column
- `vaf.col.names`: names of *VAF* columns
- `sum.p`: min probability that a *CCF* estimate for a clone in a sample is non-negative in an accepted clonal ordering
- `alpha`: alpha level, or $[1 - (\text{confidence level})]$ for *CCF* estimate of a clone

Mapping driver events onto the trees

If the previous step succeeds and gives you a tree or several trees (congrats!), we can next map some driver events onto the tree to make sure they will be visualized later. For AML1 case, column `is.driver` indicates if the variant is a (potential) driver event. We will use the gene name in column `gene` to annotate the variants in the tree.

```

y <- transfer.events.to.consensus.trees(y,
  x[x$is.driver,],
  cluster.col.name = 'cluster',
  event.col.name = 'gene')

```

Converting node-based trees to branch-based trees

ClonEvol can plot both node-based tree (each clone is a node), or branch-based tree (each branch represents the evolution of a clone from its parental clone, and each node represents a point where the clone is established/founded). Before we can draw the latter tree, we need to prepare it.

```
y <- convert.consensus.tree.clone.to.branch(y, branch.scale = 'sqrt')
```

Where are trees stored?

Consensus trees are stored in `ymatchedmerged.trees`. This is a list of data frames, each describing an inferred tree with various annotations, including *CCF* estimates and graphical parameters. The trees are ranked by the probability that sum rule is not violated, hence `ymatchedmerged.trees[[1]]` is the best scoring tree. Several important columns include:

- `lab`: labels of the clones, matching with the cluster labels.
- `parent`: the parent of the clones in the tree
- `sample.with.nonzero.cell.frac.ci`: samples where clones are estimated to have positive *CCF*

The trees can be further manipulated using R, or visualized as follows.

Step 5: Visualizing the results

Plotting multiple plots and trees together

Now it is exciting time, visualizing the clonal evolution models. Let's run the following command to plot the variant clusters, the bell plots, and the clonal evolution trees.

```
plot.clonal.models(y,  
  # box plot parameters  
  box.plot = TRUE,  
  fancy.boxplot = TRUE,  
  fancy.variant.boxplot.highlight = 'is.driver',  
  fancy.variant.boxplot.highlight.shape = 21,  
  fancy.variant.boxplot.highlight.fill.color = 'red',  
  fancy.variant.boxplot.highlight.color = 'black',  
  fancy.variant.boxplot.highlight.note.col.name = 'gene',  
  fancy.variant.boxplot.highlight.note.color = 'blue',  
  fancy.variant.boxplot.highlight.note.size = 2,  
  fancy.variant.boxplot.jitter.alpha = 1,  
  fancy.variant.boxplot.jitter.center.color = 'grey50',  
  fancy.variant.boxplot.base_size = 12,  
  fancy.variant.boxplot.plot.margin = 1,  
  fancy.variant.boxplot.vaf.suffix = '.VAF',  
  # bell plot parameters  
  clone.shape = 'bell',
```

```

bell.event = TRUE,
bell.event.label.color = 'blue',
bell.event.label.angle = 60,
clone.time.step.scale = 1,
bell.curve.step = 2,
# node-based consensus tree parameters
merged.tree.plot = TRUE,
tree.node.label.split.character = NULL,
tree.node.shape = 'circle',
tree.node.size = 30,
tree.node.text.size = 0.5,
merged.tree.node.size.scale = 1.25,
merged.tree.node.text.size.scale = 2.5,
merged.tree.cell.frac.ci = FALSE,
# branch-based consensus tree parameters
merged.tree.clone.as.branch = TRUE,
mtcab.event.sep.char = ',',
mtcab.branch.text.size = 1,
mtcab.branch.width = 0.75,
mtcab.node.size = 3,
mtcab.node.label.size = 1,
mtcab.node.text.size = 1.5,
# cellular population parameters
cell.plot = TRUE,
num.cells = 100,
cell.border.size = 0.25,
cell.border.color = 'black',
clone.grouping = 'horizontal',
#meta-parameters
scale.monoclonal.cell.frac = TRUE,
show.score = FALSE,
cell.frac.ci = TRUE,
disable.cell.frac = FALSE,
# output figure parameters
out.dir = 'output',
out.format = 'pdf',
overwrite.output = TRUE,
width = 8,
height = 4,
# vector of width scales for each panel from left to right
panel.widths = c(3,4,2,4,2))

```

The output should look like Figure 3:

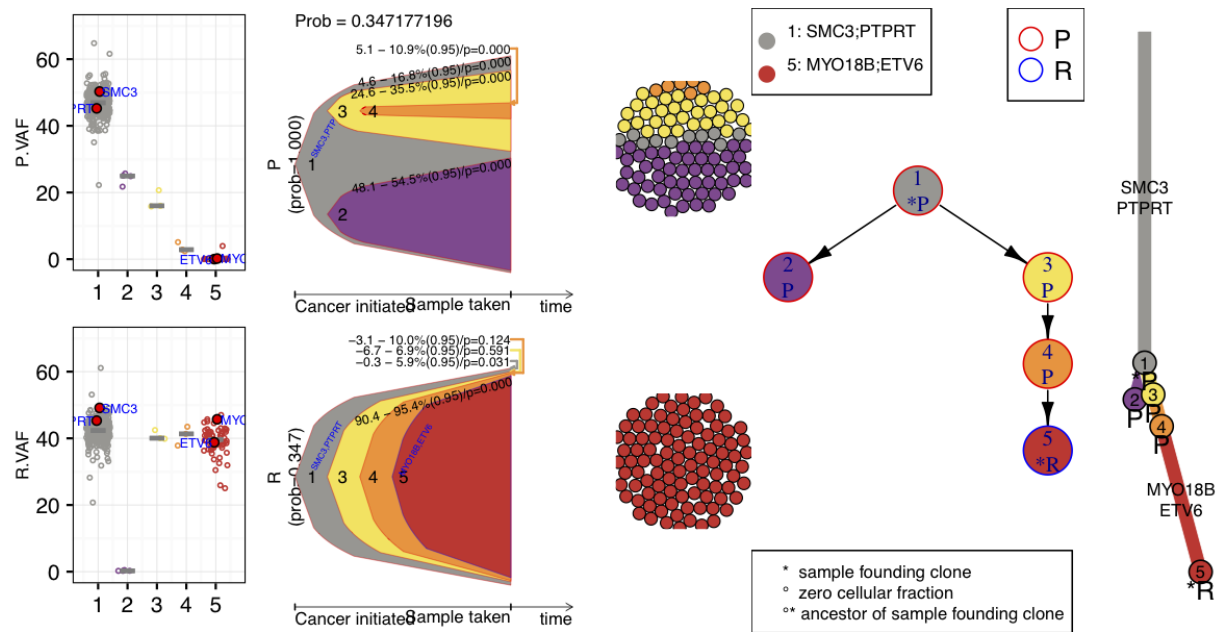


Figure 3: ClonEvol infers and visualizes clonal evolution in relapsed myeloid leukemia.

Plotting trees

If you want to plot only the trees, run this:

```
pdf('trees.pdf', width = 3, height = 5, useDingbats = FALSE)
plot.all.trees.clone.as.branch(y, branch.width = 0.5,
                               node.size = 1, node.label.size = 0.5)
dev.off()
```

Visualizing trees predicted by other tools

In order to visualize trees predicted by other tools, we need to prepare two files:

1. variants.tsv: similar to ClonEvol input, with clusters assigned by other tools
2. tree.tsv: predicted tree, consisting of:
 - a. at least 3 columns: clone, parent, sample.with.nonzero.cell.frac.ci
 - b. additional columns are: colors, events

First, read the tree and variant list from files:

```
y = import.tree('tree.tsv', 'variants.tsv')
```

Then, you can prepare annotated branch-based tree with branch length scaled to the number of clonal marker variants of the clones

```
y = convert.consensus.tree.clone.to.branch(y, branch.scale = 'sqrt')
```

You can then also map driver events onto the tree (if the variant file you prepared has ‘cluster’, ‘is.driver’, and ‘gene’ column):

```
y <- transfer.events.to.consensus.trees(y,  
  y$variants[y$variants$is.driver,],  
  cluster.col.name = 'cluster',  
  event.col.name = 'gene')
```

Now plot the tree with this:

```
pdf('imported-tree.pdf', width=3, height=5, useDingbats=F)  
plot.all.trees.clone.as.branch(y, branch.width = 0.5,  
  node.size = 1, node.label.size = 0.5)  
dev.off()
```

How to obtain the best visualizations?

ClonEvol provides default values for most parameters, and in many cases it guess the best value for the parameters for the visualizations. However, in many cases, manual intervention is required to achieve the best visualization.

Bell plots

The bell plots mimic the fishplot (Ding et al. 2012) which as a great way to present clonal dynamics over time. ClonEvol adapts the fishplot and created a simpler visualization (aka. the bell plot) to visualize clonal evolution of a single sample. The shape of the bell is controlled by several parameters in `plot.clonal.models` function.

- `bell.curve.step`: vertical distance between the end point of clone bell curve, and its mid point. Increasing this value will make the curve steeper. If it is set to equal zero, there will give no curve in the bell plot
- `clone.time.step.scale`: scaling factor for distance between the tips of the bell representing parental clone and subclones

Due to the complex clonal architecture and evolution, sometime ClonEvol places the tip of a subclone’s bell outside of the parental clone’s bell. To fix this, decrease `bell.curve.step` and/or increase `clone.time.step.scale` until a reasonable good looking bell plot is generated.

Sphere of cells

Sphere of cells is rendered partially by using the `parkcircles` package (<https://github.com/mbedward/packcircles>). ClonEvol provides several parameters to control the appearance of the subpopulation of cells drawn in a sphere of cells in the `plot.clonal.models` function, including:

- `num.cells`: total number of cells to draw (default = 100)
- `cell.border.size`: the size of border (“cell wall”) of the cells (default = 0.1)
- `cell.border.color`: the color of the border of the cells (default = ‘black’)
- `cell.size`: size of cell (default = 2)
- `clone.grouping`: how different clones are arranged (options are ‘random’, ‘horizontal’, or ‘vertical’)

Node-based trees

Node-based trees are rendered using `igraph` package (Csardi and Nepusz 2006). In order to achieve the best visualization, adjust the following parameters in the `plot.clonal.models` function.

- `merged.tree.node.size.scale`: the scaling of the size of the node (default value = 0.5)
- `merged.tree.node.text.size.scale`: the scaling of the size of the node label/annotation (default value = 1)

Branch-based trees

Branch-based trees are rendered using a modified version of the `trees` package (<https://github.com/hdng/trees> forked from <https://github.com/johnbaums/trees>). The branch-based trees are sometimes preferred as it is easier to scale the branch lengths to the number of marker variants of the corresponding clones and map the driver events onto the branches. Several important parameters that control the appearance of the branch-based trees, sometime required to be fine tuned to achieve the best tree visualization.

- `mtcab.tree.rotation.angle`: rotation angle of the tree (default = 180, top-down)
- `mtcab.tree.text.angle`: angle of the text (default = 0). When tree is rotated, text sometimes need to be rotated too.
- `mtcab.branch.angle`: the angle to draw a branch from a clone (default = 15).
- `mtcab.branch.width`: width of the branch (default = 1),
- `mtcab.branch.text.size`: text size of the events mapped onto the branches (default = 0.3)
- `mtcab.node.size`: size of clone nodes (default = 3)
- `mtcab.node.label.size`: clone label text size (default = 0.75),
- `mtcab.node.text.size`: sample label text size (default = 0.5)
- `mtcab.event.sep.char`: the character that separate events in the event string (default = “,”). Multiple events will be plot on different lines along the branches.
- `mtcab.show.event`: show driver events on branches (default = TRUE)

Putting all together in a single plot

The function `plot.clonal.models` plot all of the above plots, plus the variant jitter/box/violin plots in a single page. Therefore, arranging the plots in panels is also important to achieve the best results. This can be controlled by `panel.widths` parameter, a vector of the width scales for each panel.

Step 6: Interpretating the results

Clonal mixture of individual samples

ClonEvol estimates the confidence interval (CI) of the CCF of the clones in the samples and presents the CI alongside the visualizations (including the bell plots and trees). Only clones with positive cellular fractions, ie. there exists some cell of these clones, defined as having a high probability that their CCF is positive (see `alpha` parameter of `infer.clonal.models` function).

ClonEvol's trees

ClonEvol annotates the clones in the trees with the samples where the clones are identified to have non-zero cellular fraction. For example, if a clonal mixture of sample A contains 10% clone 1, 50% clone 3, and 40% clone 5, then sample A will appear in the annotation of clones 1, 3, and 5. A star * next to the sample name indicates that the clone is one of the founding clones of the sample, identified as the first clones with non-zero cellular fractions when traversing the tree top-down and breath-first.

Clonal seedings between samples

Clonal seeding occurs when one or more cells (homogenous, ie. monoclonal or heterogenous, ie. polyclonal) move away from a tumor site, land in a distant location in the same of different organs, survive and establish their populations and a new tumor. To understand clonal seedings, in an ideal situation, those clones that establish the first populations of cancer cells at the distant location must be identified. Given a site is presented by a sample, ClonEvol calls those clones the founding clones of the sample (annotated with a * in the tree, see above).

When two samples harbor the same clones with non-zero CCF , those clones could indicate the two samples seed each other or they were both seeded by another samples unsequenced.

Session Info

ClonEvol depends on several packages, including `ggplot2` and `igraph`. Sometimes backward compatibility is hard to maintained in newer version of packages. ClonEvol itself has changed a lot since its initial version as well and some old code might not work well using the current version. If a strange error occurs, check if you have similar versions of the packages (below), browse the past issues and Q/As (<https://github.com/hdng/clonevol/issues>), or create a new issue (<https://github.com/hdng/clonevol/issues>) and (don't forget to) attach some reproducible code and data.


```

R version 3.2.2 (2015-08-14)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Ubuntu precise (12.04.5 LTS)

attached base packages:
[1] grid      stats      graphics  grDevices  utils      datasets  methods
[8] base

other attached packages:
[1] trees_0.1.3.9000  igraph_1.0.1      packcircles_0.2.0 gridBase_0.4-7
[5] gridExtra_0.9.1   ggplot2_2.2.1     clonevol_0.99

loaded via a namespace (and not attached):
[1] Rcpp_0.12.10      plyr_1.8.4        gtable_0.1.2      magrittr_1.5
[5] scales_0.4.1      rlang_0.1          lazyeval_0.2.0     labeling_0.2
[9] tools_3.2.2       munsell_0.4.2     colorspace_1.2-4  tibble_1.3.1

```

References

- Csardi, Gabor, and Tamas Nepusz. 2006. “The Igraph Software Package for Complex Network Research.” *InterJournal, Complex Systems* 1695 (5): 1–9.
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- Miller, Christopher A., Brian S. White, Nathan D. Dees, Malachi Griffith, John S. Welch, Obi L. Griffith, Ravi Vij, et al. 2014. “SciClone: inferring Clonal Architecture and Tracking the Spatial and Temporal Patterns of Tumor Evolution.” *PLoS Computational Biology* 10 (8): e1003665. doi:[10.1371/journal.pcbi.1003665](https://doi.org/10.1371/journal.pcbi.1003665).
- Roth, Andrew, Jaswinder Khattra, Damian Yap, Adrian Wan, Emma Laks, Justina Biele, Gavin Ha, Samuel Aparicio, Alexandre Bouchard-Côté, and Sohrab P. Shah. 2014. “PyClone: statistical Inference of Clonal Population Structure in Cancer.” *Nature Methods* 11 (4): 396–98. doi:[10.1038/nmeth.2883](https://doi.org/10.1038/nmeth.2883).