



Outline

- Non-blocking send/recv
- Collective communication routines
- Lab exercise: Matrix-vector multiplication revisited
- Parallel matrix multiplication on 2D mesh/torus
- MPI Cartesian topology routines
- Homework 7

Non-Blocking Send & Receive

- MPI Functions: MPI_Isend, MPI_Irecv
- int MPI_Isend(const void* buf, int count, MPI_Datatype datatype, int dest, int tag, MPI_Comm comm, MPI_Request *request)
- int MPI_Irecv(void* buf, int count, MPI_Datatype datatype, int source, int tag, MPI_Comm comm, MPI_Request *request)
- When MPI_Isend/MPI_Irecv is called, the calling process will be not blocked and it continues to execute the subsequent instructions
- MPI_Request *request: a so called opaque object, which identifies communication operations and matches the operation that initiates the communication with the operation that terminates it

Non-Blocking Send & Receive

- MPI Functions: MPI_Test, MPI_Wait
- int MPI_Test(MPI_Request *request, int *flag, MPI_Status *status)
- int MPI_Wait(MPI_Request *request, MPI_Status *status)
- MPI_Test tests if operation finished
 - It not, the calling process will continue its execution
- MPI_Wait blocks the calling process until the non-blocking send/recv operation is finished

Non-Blocking Send & Receive

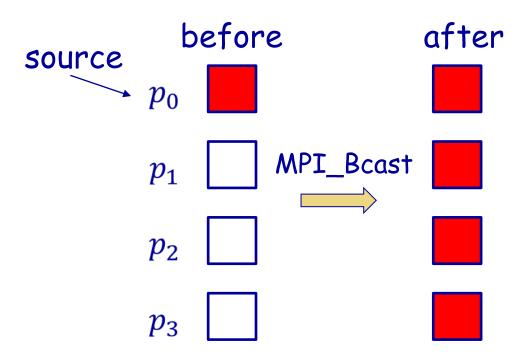
- MPI Functions: MPI_Testsome, MPI_Waitsome
- int MPI_Testsome(int incount, MPI_Request *array_of_requests, int *outcount, int *array_of_indices, MPI_Status *array_of_statuses)
- int MPI_Waitsome(int incount, MPI_Request *array_of_requests, int *outcount, int *array_of_indices, MPI_Status *array_of_statuses)
- Tests or waits until at least one of the operations associated with active handles in the list have completed
- Needs an array of requests (also indices and statuses) for multiple Isend/Irecv operations

Collective Communication

- MPI specifies a set of collective communication functions
 - One-to-All: One process contributes to the result and all processes receive the result
 - MPI_Bcast, MPI_Scatter, MPI_Scatterv, ...
 - All-to-One: All processes contribute to the result and one process receives the result
 - MPI_Gather, MPI_Gatherv, ...
 - All-to-All: All processes contribute to the result and all processes receive the result
 - MPI_Allgather, MPI_Alltoall, MPI_Allgatherv, ...
 - Other: MPI_Barrier, MPI_Reduce, MPI_Scan, ...

Broadcast

- The MPI broadcast routine (one-to-all) is:
 int MPI_Bcast(void *buf, int count, MPI_Datatype datatype,
 int source, MPI_Comm comm)
- All processes must call MPI_Bcast()



Gather

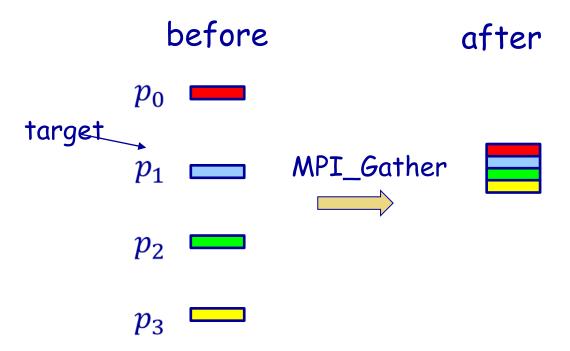
The MPI gather operation (all-to-one) is:

```
int MPI_Gather(void *sendbuf, int sendcount,

MPI_Datatype senddatatype, void *recvbuf,

int recvcount, MPI_Datatype recvdatatype,

int target, MPI_Comm comm)
```



Gather

The MPI gather operation (all-to-one) is:
 int MPI_Gather(void *sendbuf, int sendcount,
 MPI_Datatype senddatatype, void *recvbuf,
 int recvcount, MPI_Datatype recvdatatype,
 int target, MPI_Comm comm)

- sendcount number of elements each process sends
- recvcount number of elements the target process will receive from each process
- *recvbuf the length of the recvbuf must be at least recvcount times the number of processes involved in the operation

Allgather

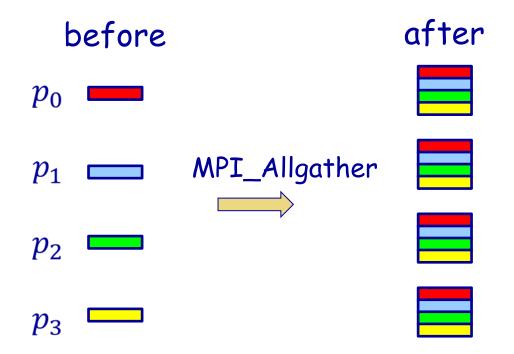
The MPI All gather operation (all-to-all) is:

```
int MPI_Allgather(void *sendbuf, int sendcount,

MPI_Datatype senddatatype, void *recvbuf,

int recvcount, MPI_Datatype recvdatatype,

MPI_Comm comm)
```



Gathery

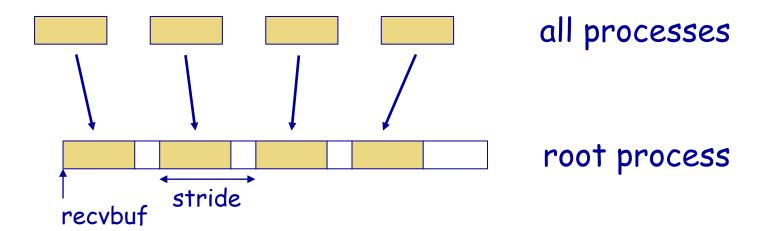
The MPI gathery operation (all-to-one) is:

```
int MPI_Gatherv(void *sendbuf, int sendcount,

MPI_Datatype sendtype, void *recvbuf,

int *recvcounts, int *displs, MPI_Datatype recvtype,

int root, MPI_Comm comm)
```

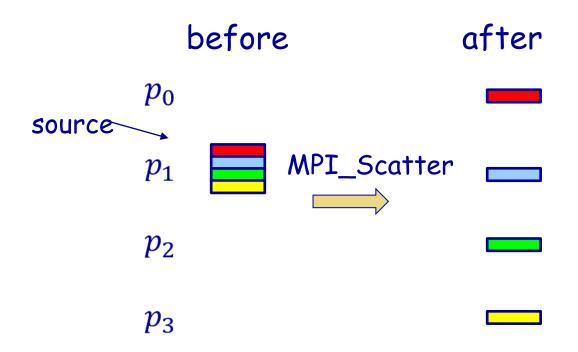


Gathery

```
    The MPI gathery operation (all-to-one) is:

    int MPI_Gatherv(void *sendbuf, int sendcount,
                  MPI_Datatype sendtype, void *recvbuf,
                  int *recvcounts, int *displs, MPI_Datatype recvtype,
                  int root, MPI_Comm comm)
 int sendarray[100];
 int stride = 150:
 int *displs, *rcounts:
 rbuf = (int *) malloc(numprocs*stride*sizeof(int));
 for (int i=0; i < numprocs; i++){
     displs[i] = i * stride;
     rcounts[i] = 100;
 MPI_Gatherv(senarray, 100, MPI_INT, rbuf, rcounts, displs, MPI_INT, root,
             MPI COMM WORLD);
```

Scatter



Scatter

- sendcount number of elements the source process will send to each process
- *sendbuf the length of the sendbuf must be at least sendcount times the number of processes involved in the operation
- recvcount number of elements each process will receive

Scattery and Alltoall

The MPI scattery operation (one-to-all) is:

The MPI all-to-all communication operation is:

 int MPI_Alltoall(void *sendbuf, int sendcount,
 MPI_Datatype senddatatype, void *recvbuf,
 int recvcount, MPI_Datatype recvdatatype,
 MPI_Comm comm)

Other Collectives

 The barrier synchronization operation: int MPI_Barrier(MPI_Comm comm)

- The MPI reduction operation (all-to-one) is:
 int MPI_Reduce(void *sendbuf, void *recvbuf, int count,
 MPI_Datatype datatype, MPI_Op op, int target,
 MPI_Comm comm)
- If the result of the reduction operation is needed by all processes, MPI provides:

int MPI_Allreduce(void *sendbuf, void *recvbuf, int count, MPI_Datatype datatype, MPI_Op op, MPI_Comm comm)

Predefined Reduction Operations

Operation	Meaning	Datatypes				
MPI_MAX	Maximum	C integers and floating point C integers and floating point				
MPI_MIN	Minimum					
MPI_SUM	Sum	C integers and floating point				
MPI_PROD	Product	C integers and floating point				
MPI_LAND	Logical AND	C integers				
MPI_BAND	Bit-wise AND	C integers and byte				
MPI_LOR	Logical OR	C integers				
MPI_BOR	Bit-wise OR	C integers and byte				
MPI_LXOR	Logical XOR	C integers				
MPI_BXOR	Bit-wise XOR	C integers and byte				
MPI_MAXLOC	Max, value-location	Data-pairs				
MPI_MINLOC	Min, value-location	Data-pairs				

Reduction Operations

- The operation MPI_MAXLOC combines pairs of values (vi, li) and returns the pair (v, l) such that v is the maximum among all vi's and l is the corresponding li (if there are more than one, it is the smallest among all these li 's)
- MPI_MINLOC does the same, except for minimum value of vi

 Value
 15
 17
 11
 12
 17
 11

 Process
 0
 1
 2
 3
 4
 5

MinLoc(Value, Process) = (11, 2)

MaxLoc(Value, Process) = (17, 1)

Reduction Operations

 MPI datatypes for data-pairs used with the MPI_MAXLOC and MPI_MINLOC reduction operations

MPI Datatype	C Datatype				
MPI_2INT	pair of ints				
MPI_SHORT_INT	short and int				
MPI_LONG_INT	long and int				
MPI_LONG_DOUBLE_INT	long double and int				
MPI_FLOAT_INT	float and int				
MPI_DOUBLE_INT	double and int				

Reduction Operations

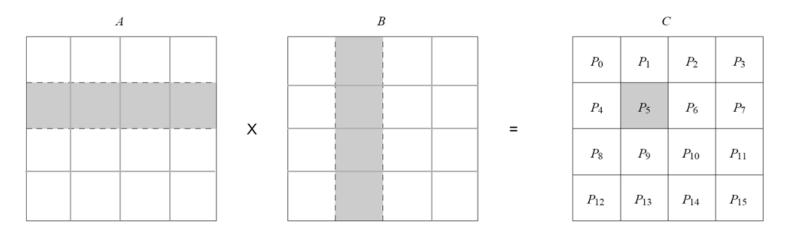
```
- Example:
  struct {
     double val;
     int rank;
  } in, out;
  in.val = ain;
  in.rank = myrank;
  MPI_Reduce(in, out, 1, MPI_DOUBLE_INT, MPI_MAXLOC, root,
comm);
  if (myrank == root) {
     aout = out.val;
     ind = out.rank;
```

Lab Exercise: Matrix-Vector Multiplication Revisited

- Modify the program for matrix-vector multiplication you did in the last lecture by using collective communication routines
- You need to consider general cases, that is, n may not divisible by p
- Thus you need to use MPI_Scatterv and MPI_Getherv functions

Parallel MM on 2D Mesh/Torus

- Use 2D partitioning and assume $p=\sqrt{p}\times\sqrt{p}$, i.e., p processes are organized as a 2D mesh/torus
- Let C(i,j) refer to a submatrix of size $n/\sqrt{p}\times n/\sqrt{p}$ and similar for A(i,j) and B(i,j)
- Each C(i,j) needs one row of A(i,j)s and one column of B(i,j)s which are held by different processes
- Communication: move A(i, j)s horizontally and B(i, j)s vertically

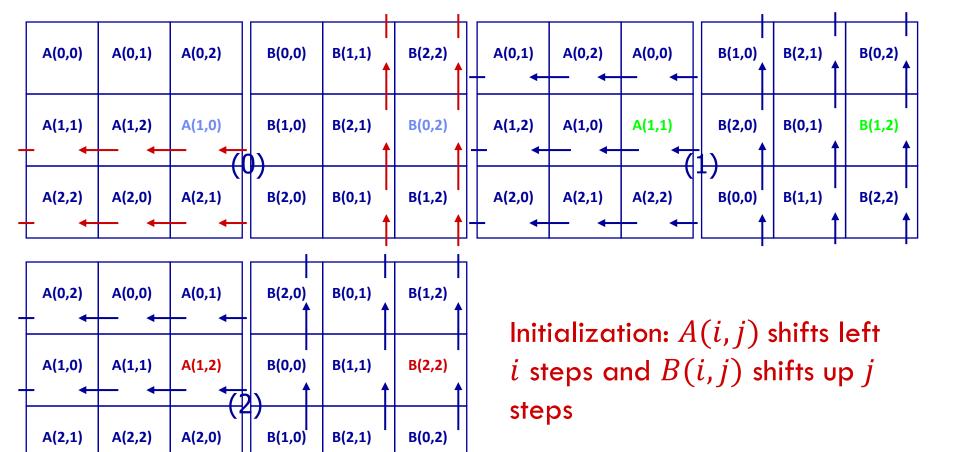


2D Algorithm 1 (Broadcast)

A(0,0)	A(0,1)	A(0,2)	B(0,0)	B(0,1)	B(0,2)	A(0,0)	A(0,0)	A(0,0)	B(0,0)	B(0,1)	B(0,2)
A(1,0)	A(1,1)	A(1,2)	B(1,0)	B(1,1)	B(1,2)	A(1,0)	A(1,0)	A(1,0)	B(0,0)	B(0,1)	B(0,2)
A(2,0)	A(2,1)	A(2,2)	B(2,0)	B(2,1)	B(2,2)	A(2,0)	A(2,0)	A(2,0)	B(0,0)	B(0,1)	B(0,2)
A(0,1)	A(0,1)	A(0,1)	B(1,0)	B(1,1)	B(1,2)	A(0,2)	A(0,2)	A(0,2)	B(2,0)	B(2,1)	B(2,2)
A(1,1)	A(1,1)	A(1,1)	B(1,0)	B(1,1)	B(1,2)	A(1,2)	A(1,2)	A(1,2)	B(2,0)	B(2,1)	B(2,2)
A(2,1)	A(2,1)	A(2,1)	B(1,0)*	B(1,1) V	B(1,2) ¥	A(2,2)	A(2,2)	A(2,2)	B(2,0)	B(2,1)	B(2,2)

$$C(1,2) = A(1,0) * B(0,2) + A(1,1) * B(1,2) + A(1,2) * B(2,2)$$

2D Algorithm 1 (Cannon)



$$C(1,2) = A(1,0) * B(0,2) + A(1,1) * B(1,2) + A(1,2) * B(2,2)$$

Parallel Matrix Multiplication

- We discussed 1D and 2D parallel algorithms for distributedmemory machines
- Question: which one performs better?
- 1D algorithm:
 - Matrices are partitioned into block rows $(n/p \times n)$
 - In one parallel step each process
 - Send one block row (B(j)) and received one block row $(\sim n^2/p)$
 - Multiplication of A(i,j) $(n/p \times n/p)$ and B(j) $(n/p \times n)$
 - Number of operations is $\sim n^3/p^2$
 - Computational intensity: $\sim n/p$
 - Number of parallel steps is p

Parallel Matrix Multiplication

- 2D algorithm:
 - Matrices are partitioned into a number of submatrices $(n/\sqrt{p}\times n/\sqrt{p})$
 - In one parallel step each process
 - Send one submatrix A(i,j) and receive one submatrix horizontally $(\sim n^2/p)$
 - Send one submatrix B(i,j) and receive one submatrix vertically $(\sim n^2/p)$
 - Multiplication of A(i,k) and B(k,j)
 - Number of operations is $\sim n^3/(p\sqrt{p})$
 - Computational intensity: $\sim n/\sqrt{p}$
 - Number of parallel steps is \sqrt{p}

Parallel Matrix Multiplication

- Although 2D algorithm requires to move both A(i,j) and B(i,j) in a parallel step, the number of operations increased by a factor of \sqrt{p}
- The computational intensity is increased by a factor of \sqrt{p}
- Since the total amount of work is fixed for a given problem, the number of parallel steps is also reduced by a factor of \sqrt{p}
 - Greatly reduced the communication overheads
- Therefore, 2D parallel algorithm for matrix multiplication

MPI Cartesian Topology Routines

- MPI allows a programmer to organize processors into logical k-D meshes
- The processor ids in MPI_COMM_WORLD can be mapped to other communicators (corresponding to higher-dimensional meshes) in many ways
- The goodness of any such mapping is determined by the interaction pattern of the underlying program and the topology of the machine

Cartesian Topologies

To create Cartesian topologies using the function:

```
int MPI_Cart_create(MPI_Comm comm_old, int ndims, int *dims, int *periods, int reorder, MPI_Comm *comm_cart)
```

- This function takes the processes in the old communicator and creates a new communicator with ndims dimensions
- Each processor can now be identified in this new cartesian topology by a vector of dimension dims

Cartesian Topologies

 To determine process coords in cartesian topology given rank in group:

```
int MPI_Cart_coord(MPI_Comm comm_cart, int rank, int maxdims, int *coords)
```

To determine process rank in communicator by its cartesian location:

int MPI_Cart_rank(MPI_Comm comm_cart, int *coords, int *rank)

Cartesian Topologies

 To find the resulting source and destination ranks, given a shift direction and amount

```
int MPI_Cart_shift( MPI_Comm comm, int direction, int displ, int *source, int *dest)
```

- MPI_Cart_sub is a collective comm routine
 - All involved processes must call

Homework 7: MPI Cartesian Topology

- Search the Internet for detailed descriptions on MPI Catesian topoloty
- Then write a simple MPI program to create 16 processes
- Use MPI cartesian routine to organize the processes into a 4 X 4
 2D ring
- Declare two integers a and b
 - Assign process's id to a and then every process shifts a to the left neighbour process using MPI send/recv
 - Assign process's id to b and then every process shifts b up to the neighbor process above also using MPI send/recv
 - Print and check the results
- Partition processes into row and column subgrids
 - For processes with column id = 0, assign it original id to a and broadcast it to the processes in the same row
 - For processes with row id = 0, assign it original id to b and broadcast it to the processes in the same column

Print and check the results



