

# NANO266 Lab 3 - Phase Stability from Quantum Mechanics

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March 26, 2016

## 1 Introduction

In this lab, we will look at predicting phase equilibrium from quantum mechanics. We will still be using QuantumEspresso. We will also introduce you to the basics of running calculations on supercomputing resources, e.g., how to submit jobs, handle queues, etc.

## 2 Initial setup

By this stage, you should already have everything set up. Make sure you are in the lab3 folder by doing:

```
cd <path/to/repo>/labs/lab3
```

## 3 Submitting jobs to the Comet queues

Comet uses the Simple Linux Utility for Resource Management (Slurm) job scheduling system. All supercomputing clusters use a job scheduler of some sort, e.g., PBS, Sun GridEngine, SLURM. They differ in some features, but work on the same basic principle. You send jobs to a queue, and they are run according to some priority system. For more information, you may read the guide at [https://www.sdsc.edu/support/user\\_guides/comet.html](https://www.sdsc.edu/support/user_guides/comet.html). For the purposes of this lab, a sample *submit\_script* has been provided. It is imperative that you understand how the script works as you will be using this for the rest of this and the next lab. Read the user guide to understand what each of the options in the preamble means. You can then modify them to suit your needs.

To submit the job, just simply run:

```
sbatch submit_script
```

You may check on the status of your job using the following command:

```
squeue -u <username>
```

If you make a mistake and need to kill a job for whatever reason. use the `scancel` command.

```
scancel <jobid>
```

## 4 Q1 (20 points): The bcc-hcp transition in iron

In this problem, you will look at the bcc to hcp transition in iron. We will be using the PBE GGA functional that we used in the earlier lab. Use an energy cutoff of 40 Ry with a charge density cutoff of 400 Ry. You will need to determine an appropriate  $k$ -point mesh for both the bcc and hcp structures. The energy differences are very small; choose parameters to converge your energies to within 1 meV.

1. Calculate the ground state energy of Fe in both the bcc and hcp structure. Two template files are provided for bcc and hcp. A `run_pw.py` file is also provided that works for bcc, but you need to modify it as appropriate to work for hcp. Optimize the lattice parameters for both bcc and hcp Fe (i.e.,  $a$  for bcc and  $a$  and  $c$  for hcp). In the case of hcp, `celldm(3)`, which is the  $c/a$  ratio, needs to be provided. Try the following values of  $c/a$  ratio: [1.72,1.73,1.74] and for each of these ratios, alter the  $a_o$  parameter to find the equilibrium structure in hcp phase. Start with an  $a_o$  value of 4.8 a.u.
2. Varying the volume of the cell, calculate the pressure at which the hcp structure becomes more favorable than the bcc one. Note that it is important when comparing energies that the  $k$ -point samplings for both systems are comparable and converged. Determine an appropriate  $k$ -point grid for both structures. Note that the  $k$ -point should be proportional to the reciprocal lattice vector length.
3. Calculate and compare the total energy for the BCC structure in the ferromagnetic, and anti-ferromagnetic states. (10 points)

Note that you will need to read the PWSCF manual to figure out how to set various options to do this work. At this stage of the course, we will not be providing all the templates and scripts and you need to work through the manuals to figure out what to do. This is part and parcel of computational modeling work.

## 5 Q2 (40 points): Stability of the $\text{PbTiO}_3$ perovskite

$\text{PbTiO}_3$  is a perovskite oxide which is ferroelectric. The ferroelectric response of  $\text{PbTiO}_3$  is the result of a displacive transition where a low temperature tetragonal phase is preferred over the cubic phase.

For this question, it is important that you note several differences in the `PbTiO3.pw.in.template` file.

- The `calculation` parameter is set to `relax`, which means we are allowing atoms to move.

- There are two additional sections: IONS section with `ion_dynamics = 'bfgs'`, and CELL section with `cell_dynamics = 'bfgs'` which chooses the quasi-Newton minimization method.
- At the end of the atomic positions for Pb and Ti, there are three additional 0s. These indicate that the Pb and Ti are not allowed to move in any of the coordinates. Conversely, no such restriction is placed on the O atoms, which are allowed to relax accordingly.

Please answer the following questions.

1. Calculate and plot the energy of cubic  $\text{PbTiO}_3$  as a function of lattice parameter. Use a  $4 \times 4 \times 4$   $k$ -point mesh with a 1, 1, 1 offset. Sample lattice parameters with a sufficiently fine grid to get a reliable value for the equilibrium lattice constant. To get an idea where to begin, note that the room-temperature experimental lattice constant is about 3.97 Å.
2. Using the equilibrium lattice parameter from part (1), plot the energy as a function of displacement of the Ti atom along one of the cubic lattice directions, allowing the O atoms to fully relax for each displacement. Report the Ti displacement at which the total energy is at a minimum. What is the energy difference between this configuration and the minimum-energy configuration from part (1)? Note that the Ti displacement will be very small.
3. Now allow both the Ti atom and the O atoms to relax and find the minimum energy structure, using the minimum-energy Ti displacement from part (B) as your starting configuration. Report the final atomic positions and final energy.
4. Which phase is the most energetically stable for  $\text{PbTiO}_3$  and how does that relate to the ferroelectric behavior of this material?

## 6 Q3 (40 points): Formation Energy of the $\text{Cu}_{1-x}\text{Au}_x$ intermetallics

In this problem, we will investigate the formation energies of the  $\text{Cu}_{1-x}\text{Au}_x$  for  $x = 0.25$ , 0.5 and 0.75. See Ozolins et al. Cu-Au, Ag-Au, Cu-Ag and Ni-Au intermetallics: First-principles study of phase diagrams and structures, Phys. Rev. B, 1997, 57, 19, doi:10.1103/PhysRevB.57.6427.

1. Calculate the ground state energy for fcc Cu, Au and  $\text{Cu}_{1-x}\text{Au}_x$ . Here, we will use PWSCF's *vc-relax* option to avoid having to manually do a equation of state analysis. Start with the end members and the CuAu ( $x = 0.5$ ) intermetallic and do a  $k$ -point convergence such that your formation energies are within 5 meV /atom. Start with a relatively small grid, e.g.,  $4 \times 4 \times 4$

2. For CuAu, you should use the L10 phase, which is a body-centered tetragonal (bct) with two atoms in the unit cell, and lattice parameters are  $a = b \neq c$ . A sample file is provided. Please note that starting configuration is a simple cubic structure with face-centered and corner lattice points occupied such that there are alternate layers of Cu and Au. You may search the internet for the experimental lattice parameters and use those to set your initial guesses for  $a = \text{celldm}(1)$  and  $c/a = \text{celldm}(3)$  (in case you start with a  $\text{ibrav} = 7$ , tetragonal structure). You should use good guesses to minimize the computational time.
3. Calculate the formation energy of  $\text{Cu}_{1-x}\text{Au}_x$  :

$$\Delta H_f(\text{Cu}_{1-x}\text{Au}_x) = E(\text{Cu}_{1-x}\text{Au}_x) - (1-x)E(\text{Cu}) - xE(\text{Au})$$

where  $E(\text{Cu})$  and  $E(\text{Au})$  are the total energies for Cu and Au in their fcc bulk phase. Note that you must normalize the energies accordingly. We want the formation energies per atom, i.e.,  $0.5 \times$  the formation energy per CuAu.

4. Repeat the calculations for  $\text{Cu}_3\text{Au}$  and  $\text{CuAu}_3$ . For both these structures, start with a fcc Cu or Au structure, and replace all corner atoms with atoms of the other type. For example, to create the  $\text{Cu}_3\text{Au}$ , you can start from the fcc Cu unit cell, and set the Cu atoms to be on the faces, which gives one Au ( $1/8 \times 8$ ) and three Cu ( $1/2 \times 6$ ). Note that in order to create this structure, you need to decrease the symmetry from the fcc to simple cubic, and then add atoms accordingly. Review your crystallography and PWSCF's input file format so that you understand how to do this.
5. Plot the formation energy of the  $\text{Cu}_{1-x}\text{Au}_x$  phases you have calculated against  $x$ . Discuss which of the ordered intermetallic structures are stable at 0K.