```
# bumpus sparrows
#HOMEWORK SECTION
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#Homework for Week 2
#Some of the following codes are adopted from sample code in class
#Bumpus_sparrows <- read_excel("Desktop/Multivariate Analysis/
Bumpus sparrows.xlsx")
Bumpus_sparrows
sparr <- Bumpus_sparrows</pre>
sparr
sparr[,-1]
#We will drop column 1 as it does not contain a number
sparr.num <- sparr[,-1]</pre>
# Computing the means of each variable in data frame sparr.num
colMeans(sparr.num)
# Covariance matrix
cov(sparr.num)
# Correlation matrix
cor(sparr.num)
# Survivorship == 'S' for survived sparrows, and "NS" for non-survived
sparrows
sparr_s <- sparr[(sparr$Survivorship == "S"),]</pre>
sparr ns <- sparr[(sparr$Survivorship == "NS"),]</pre>
# dim(sparr s)
# dim(sparr ns)
# > dim(sparr s)
# [1] 21 6
# > dim(sparr ns)
# [1] 28 6
#drop column 1 for both datasets as they does not contain a number
sparr_s.num <- sparr_s[,-1]</pre>
sparr_ns.num <- sparr_ns[,-1]</pre>
# calculate column means for both datasets
colMeans(sparr s.num)
colMeans(sparr ns.num)
# > colMeans(sparr s.num)
# Total_length Alar_extent L_beak_head L_humerous
L keel sternum
      157.38095
                   241.00000
                                  31.43333
                                                18.50000
20.80952
# > colMeans(sparr ns.num)
# Total length Alar extent L beak head L humerous
L keel sternum
      158.42857 241.57143
                                  31.47857
                                                18,44643
20.83929
```

# Column means of Total\_length and Alar\_extent for non-survived sparrows are greater than that of survived sparrows. Sparrows with longer total length and greater alar extent may have a higher chance of surviving. Means of other variables such as L\_beak\_head, L\_humerous, and L\_keel\_sternum and comparable for both groups.

```
# calculate the following for both datasets: Variance
var(sparr s.num)
var(sparr ns.num)
# > var(sparr_s.num)
                 Total length Alar extent L beak head L humerous
L keel sternum
                                    9.10
                                            1.5566667
# Total length
                    11.047619
                                                          0.8700
1.2861905
# Alar extent
                     9.100000
                                    17.50
                                            1.9100000
                                                          1.3100
0.8800000
                                     1.91
                                            0.5313333
                                                          0.1890
# L beak head
                     1.556667
0.2396667
                                     1.31
                                                          0.1760
# L humerous
                     0.870000
                                            0.1890000
0.1325000
# L keel sternum
                     1.286190
                                     0.88
                                            0.2396667
                                                          0.1325
0.5749048
# > var(sparr ns.num)
                 Total_length Alar_extent L_beak_head L_humerous
L keel sternum
                                17.190476
                                            2.2428571 1.7460317
# Total length
                    15.068783
2.9306878
# Alar extent
                    17,190476
                               32.550265
                                            3.3978836 2.9502646
4.0656085
# L beak head
                     2.242857
                                 3.397884
                                            0.7284127 0.4695503
0.5590212
# L humerous
                                 2.950265
                                            0.4695503 0.4344312
                     1.746032
0.5058862
# L keel sternum
                     2.930688
                                 4.065608
                                            0.5590212 0.5058862
1.3209921
# calculate the following for both datasets:Covariance matrix
cov(sparr s.num)
cov(sparr_ns.num)
# > cov(sparr_s.num)
                 Total_length Alar_extent L_beak_head L_humerous
L keel sternum
# Total length
                    11.047619
                                     9.10
                                            1,5566667
                                                          0.8700
1.2861905
# Alar extent
                     9.100000
                                    17.50
                                            1.9100000
                                                          1,3100
0.8800000
                                     1.91
                                                          0.1890
# L beak head
                     1.556667
                                            0.5313333
0.2396667
# L humerous
                     0.870000
                                     1.31
                                            0.1890000
                                                          0.1760
0.1325000
```

```
1.286190 0.88
# L keel sternum
                                         0.2396667
                                                      0.1325
0.5749048
# > cov(sparr ns.num)
               Total_length Alar_extent L_beak_head L_humerous
L keel sternum
                                         2.2428571 1.7460317
# Total length
                  15.068783
                             17.190476
2.9306878
# Alar extent
                  17,190476
                            32.550265
                                         3.3978836 2.9502646
4.0656085
# L beak head
                   2.242857
                              3.397884
                                         0.7284127 0.4695503
0.5590212
# L humerous
                   1.746032 2.950265
                                         0.4695503 0.4344312
0.5058862
                                         0.5590212 0.5058862
# L keel sternum
                   2.930688
                              4.065608
1.3209921
```

# The diagonal values in the covariance matrices show that the non-survived group has greater variance across all 5 variables. This increase in variance may also contribute to higher covariance between variables such as Total length and Alar extent.

```
# calculate the following for both datasets: Correlation matrix
cor(sparr_s.num)
cor(sparr ns.num)
```

```
# > cor(sparr_s.num)
                Total_length Alar_extent L_beak_head L_humerous
L_keel_sternum
                                          0.6425068 0.6239195
# Total length
                   1.0000000
                              0.6544674
0.5103557
# Alar extent
                   0.6544674
                              1.0000000
                                          0.6263698 0.7464418
0.2774378
# L beak head
                   0.6425068
                             0.6263698
                                          1.0000000 0.6180476
0.4336368
# L humerous
                   0.6239195
                             0.7464418
                                          0.6180476 1.0000000
0.4165447
# L_keel_sternum
                   0.5103557
                             0.2774378
                                          0.4336368 0.4165447
1.0000000
# > cor(sparr ns.num)
                Total length Alar extent L beak head L humerous
L keel sternum
# Total_length
                   1.0000000
                             0.7761963
                                          0.6769768 0.6824212
0.6568714
# Alar extent
                   0.7761963
                             1.0000000
                                          0.6978185 0.7845546
0.6200093
# L beak head
                   0.6769768 0.6978185
                                          1.0000000 0.8347046
0.5698878
                                          0.8347046 1.0000000
# L humerous
                   0.6824212 0.7845546
0.6677936
                   0.6568714
                             0.6200093
                                          0.5698878 0.6677936
# L keel sternum
1.0000000
```

```
# The correlation matrices are normalized by the variance of each
individual variable. The comparison of two correlation matrices shows that
in the non-survived group, the correlations between Total length &
Alar_extent and Total_length & L_keel_sternum are much higher than the
survived group. It is possible that sparrows, given the same total length,
may have a lower chance of survival if it has greater Alar_extent and
L keel sternum.
# Calculate distance for survived sparrows
distance_s = dist(scale(sparr_s.num,center = FALSE))
distance s
distance s matrix <- as.matrix(distance s)</pre>
distance_s_matrix
x <- sparr_s.num</pre>
cm <- colMeans(x)
S \leftarrow cov(x)
d s <- apply(x, MARGIN = 1, function(x)t(x - cm) %*% solve(S) %*% (x - cm))
d s
\# > d s
# [1] 3.398261 5.430132 2.761144 4.248201 2.310336 3.959346
2.220920 11.420509 5.062491 7.126981 3.495930 3.217816 4.112069
6.266423 7.583973
# [16] 1.860433 3.509591 3.456548 6.268125 6.168717 6.122055
# Calculate distance for non-survived sparrows
distance ns = dist(scale(sparr ns.num,center = FALSE))
distance ns
distance ns matrix <- as.matrix(distance ns)</pre>
distance_ns_matrix
x <- sparr_ns.num</pre>
cm <- colMeans(x)</pre>
S \leftarrow cov(x)
d ns <- apply(x, MARGIN = 1, function(x)t(x - cm) \%*\% solve(S) \%*\% (x -
cm))
d ns
# > d_ns
# [1] 3.256952 1.233208 3.801387 4.665528 6.562139 3.536768
6.679629 9.198939 3.959222 16.246076 2.227248 2.205544 10.482729
4.903730 5.065758
# [16] 5.137205 1.821819 2.468433 6.459364 5.832981 2.269359
2.136120 2.147935 1.634513 4.529446 7.868488 4.752499 3.916982
ggnorm(sparr s$Total length, main = "Total length Survive");
ggline(sparr s$Total length)
qqnorm(sparr s$Alar extent, main = "Alar extent Survive");
qqline(sparr_s$Alar_extent)
qqnorm(sparr_s$L_beak_head, main = "L_beak_head_Survive");
ggline(sparr s$L beak head)
ggnorm(sparr s$L humerous, main = "L humerous Survive");
qqline(sparr_s$L_humerous)
```

```
qqnorm(sparr_ns$Total_length, main = "Total_length_Nonsurvive");
qqline(sparr_ns$Total_length)
qqnorm(sparr_ns$Alar_extent, main = "Alar_extent_Nonsurvive");
qqline(sparr_ns$Alar_extent)
qqnorm(sparr_ns$L_beak_head, main = "L_beak_head_Nonsurvive");
qqline(sparr_ns$L_beak_head)
qqnorm(sparr_ns$L_humerous, main = "L_humerous_Survive");
qqline(sparr_ns$L_humerous)
```