

112-1 Discrete Mathematics Chapter 1-1

姓名：許嘉隆

學號：412770116

2.

- a) Is not a proposition.
- b) Is not a proposition.
- c) Is a proposition, with the truth value False.
- d) Is NOT a proposition, as its truth value Unknown.
- e) Is a proposition, with the truth value False.
- f) Is NOT a proposition, as its truth value Unknown.

12. $p = \text{"The election is decided"} , q = \text{"The votes have been counted"}$

- a) The election isn't decided.
- b) The election is decided or the votes have been counted.
- c) The election isn't decided and the votes have been counted.
- d) If the votes have been counted, the election is decided.
- e) If the votes haven't been counted, the election isn't decided.
- f) If the election isn't decided, the votes haven't been counted.
- g) The election is decided if and only if the votes have been counted.
- h) The votes haven't been counted or the election isn't decided and the votes haven't been counted.

22.

- a) It is an inclusive or, because I can experience with both of these languages.
- b) It is an exclusive or, because I can only choose one for lunch.
- c) It is an inclusive or, because I can enter the country with both of these cards.
- d) It is an inclusive or, because maybe something can publish and perish.

34.

| p | q | $\neg p$ | $\neg q$ | $p \wedge q$ | $p \vee q$ | $q \rightarrow \neg p$ | $p \leftrightarrow q$ | $(q \rightarrow \neg p) \leftrightarrow (p \leftrightarrow q)$ | $p \rightarrow \neg p$ | $\neg p \rightarrow p$ | $p \leftrightarrow \neg p$ |
|-----|-----|----------|----------|--------------|------------|------------------------|-----------------------|--|------------------------|------------------------|----------------------------|
| T | T | F | F | T | T | F | T | F | F | T | F |
| T | F | F | T | F | T | T | F | F | T | F | F |
| F | T | T | F | F | T | T | F | F | | | |
| F | F | T | T | F | F | T | T | T | | | |

| $p \leftrightarrow \neg q$ | $(p \leftrightarrow q) \oplus (p \leftrightarrow \neg q)$ | $p \oplus (p \vee q)$ | $(p \wedge q) \rightarrow (p \vee q)$ |
|----------------------------|---|-----------------------|---------------------------------------|
| F | T | F | T |
| T | T | F | T |
| T | T | T | T |
| F | T | F | T |

37.

| p | q | $\neg p$ | $\neg q$ | $p \rightarrow q$ | $p \rightarrow \neg q$ | $\neg p \rightarrow q$ | $p \leftrightarrow q$ | $\neg p \leftrightarrow q$ | $\neg p \leftrightarrow \neg q$ | $(p \rightarrow q) \vee (\neg p \rightarrow q)$ |
|-----|-----|----------|----------|-------------------|------------------------|------------------------|-----------------------|----------------------------|---------------------------------|---|
| T | T | F | F | T | F | T | T | F | T | T |
| T | F | F | T | F | T | T | F | T | F | T |
| F | T | T | F | T | T | T | F | T | F | T |
| F | F | T | T | T | T | F | T | F | T | T |

| $(p \rightarrow q) \wedge (\neg p \rightarrow q)$ | $(p \leftrightarrow q) \vee (\neg p \leftrightarrow q)$ | $(\neg p \leftrightarrow \neg q) \leftrightarrow (p \leftrightarrow q)$ |
|---|---|---|
| T | T | T |
| F | T | T |
| T | T | T |
| F | T | T |

38.

| p | q | r | $\neg r$ | $p \vee q$ | $p \wedge q$ | $(p \vee q) \vee r$ | $(p \vee q) \wedge r$ | $(p \wedge q) \vee r$ | $(p \wedge q) \wedge r$ | $(p \vee q) \wedge \neg r$ | $(p \wedge q) \vee \neg r$ |
|-----|-----|-----|----------|------------|--------------|---------------------|-----------------------|-----------------------|-------------------------|----------------------------|----------------------------|
| T | T | T | F | T | T | T | T | T | T | F | T |
| T | T | F | T | T | T | T | F | T | F | T | T |
| T | F | T | F | T | F | T | T | T | F | F | F |
| T | F | F | T | T | F | T | F | F | F | T | T |
| F | T | T | F | T | F | T | T | T | F | F | F |
| F | T | F | T | T | F | T | F | F | F | T | T |
| F | F | T | F | F | F | T | F | T | F | F | F |
| F | F | F | T | F | F | F | F | F | F | F | T |

48. a) $11000 \wedge (01011 \vee 11011) = 11000 \wedge 11011 = 11000$

b) $(01111 \wedge 10101) \vee 01000 = 00101 \vee 01000 = 01101$

c) $(01010 \oplus 11011) \oplus 01000 = 10001 \oplus 01000 = 11001$

d) $(11011 \vee 01010) \wedge (10001 \vee 11011) = 11011 \wedge 11011 = 11011$

