



How to Improve Model Robustness? A Distributional-Discrepancy Perspective

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21 November 2025



Outline

- ❑ Background
- ❑ **ICML 2025:** Sample-specific Noise Injection for Diffusion-based Adversarial Purification
- ❑ **ICML 2025:** One Stone, Two Birds: Enhancing Adversarial Defense Through the Lens of Distributional Discrepancy

What is an adversarial example (attack)?

88% Tabby Cat



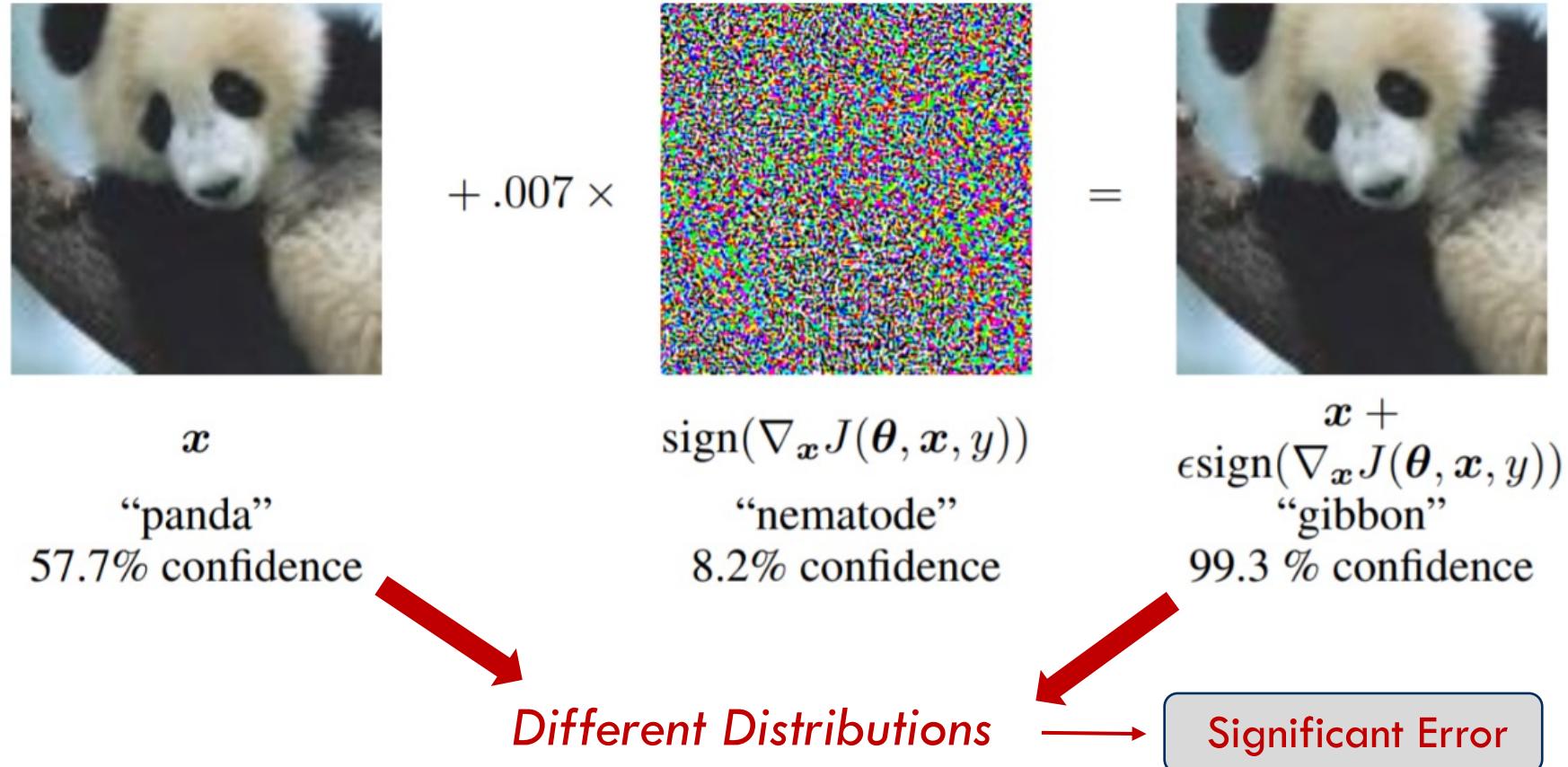
Adversarial
Perturbations

99% Guacamole

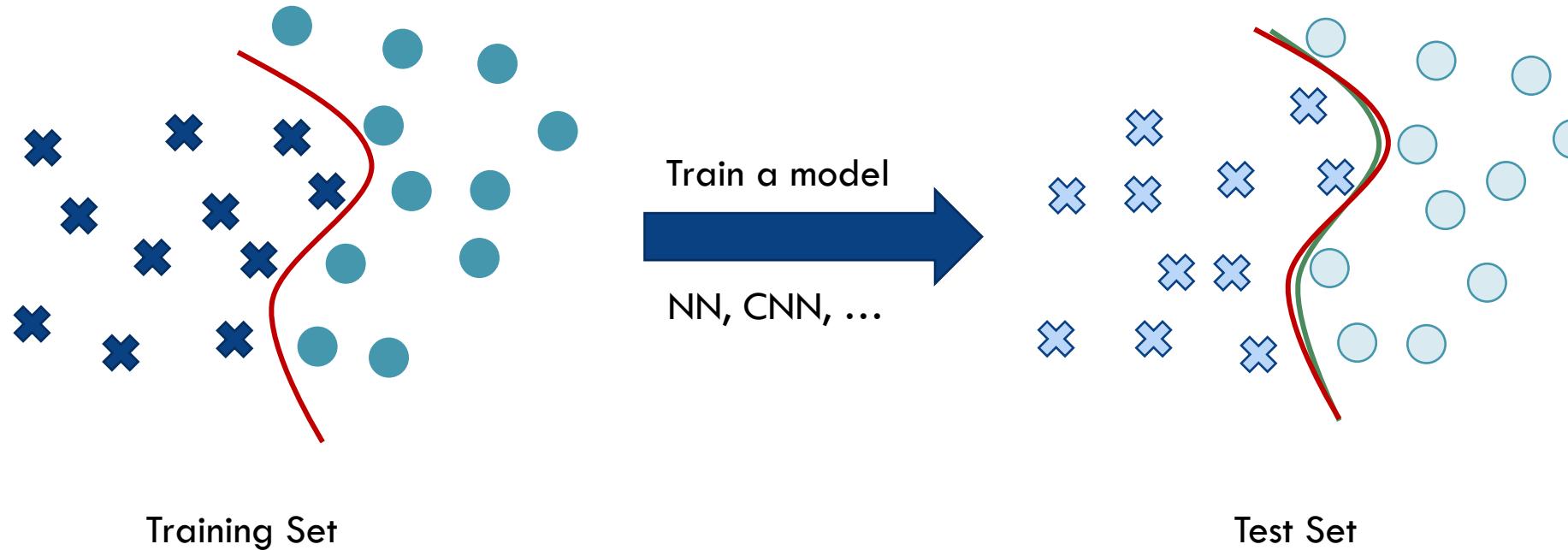


Why it works?

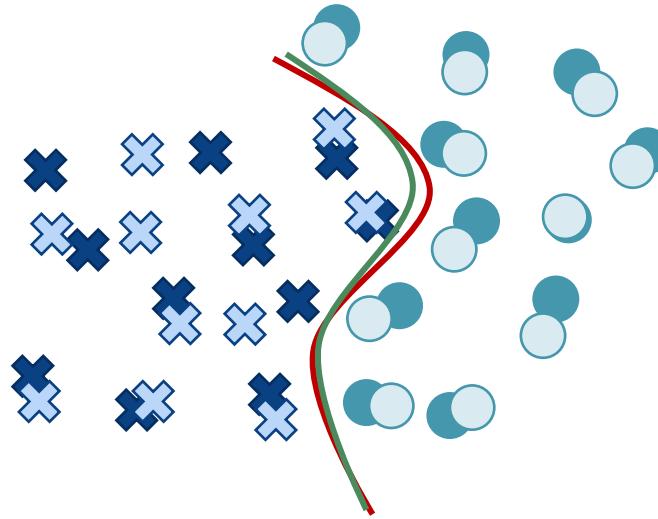
Why adversarial attack can be successful?



Basic assumption in machine learning



Basic assumption in machine learning

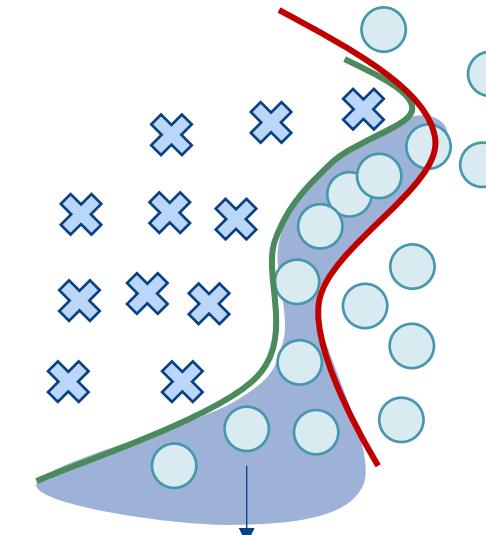


Same Distribution

Basic assumption in machine learning

Different distributions

break the assumption



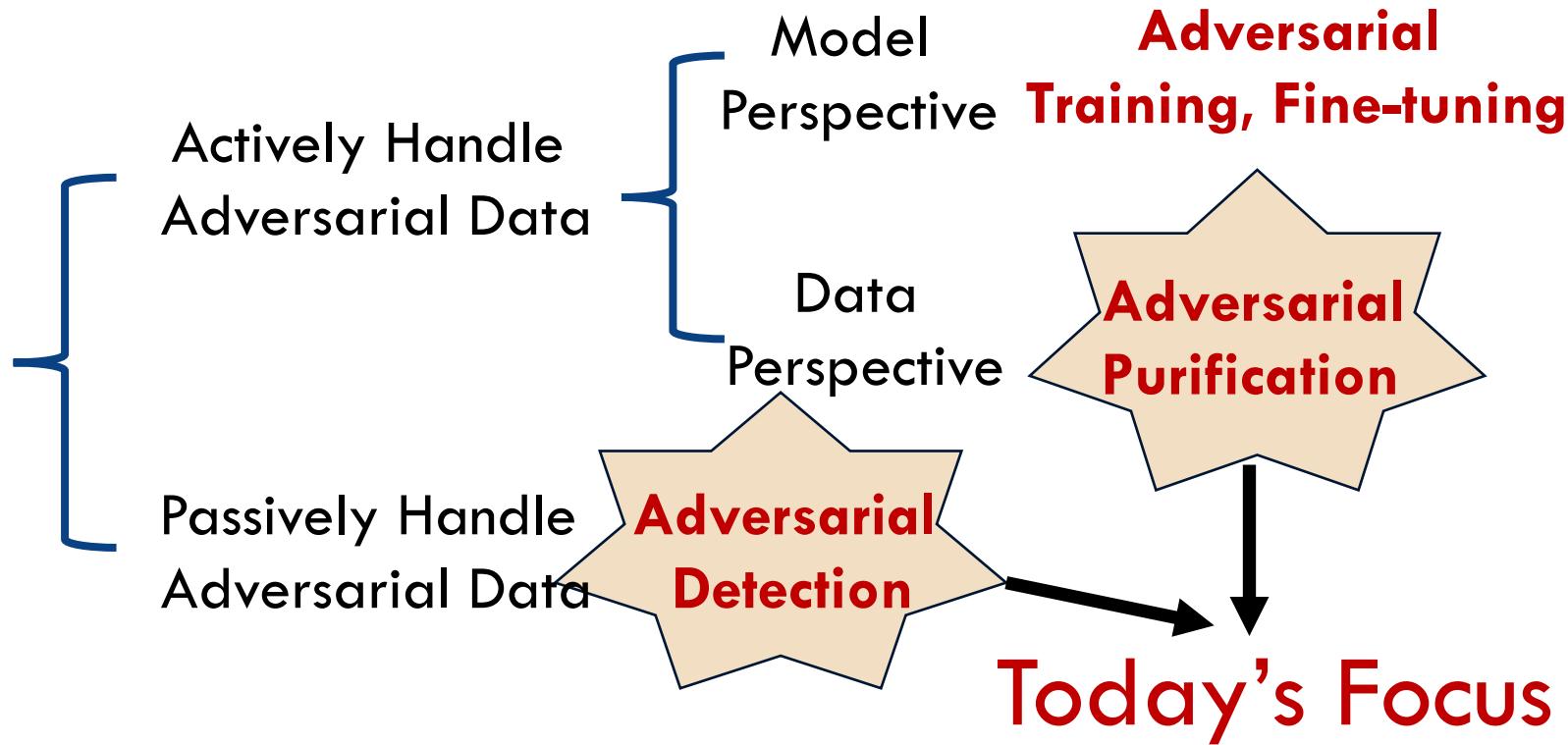
Significant Error

Break the assumption!!!

How to defend against it?

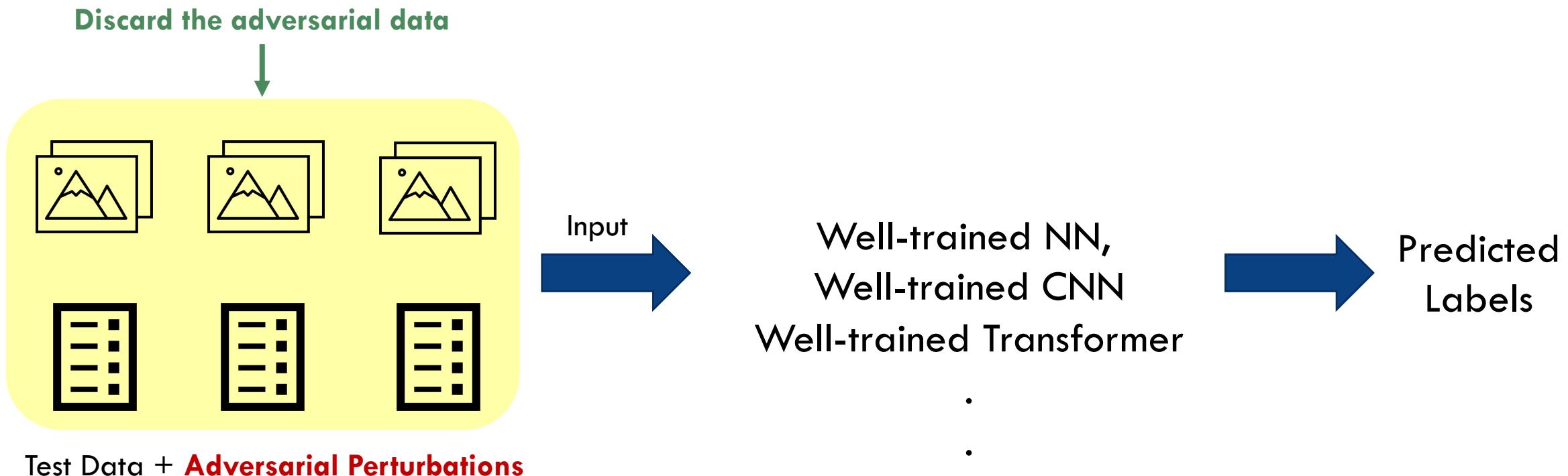
Defend against adversarial attacks

Trustworthy Machine Learning
Under Adversarial Data



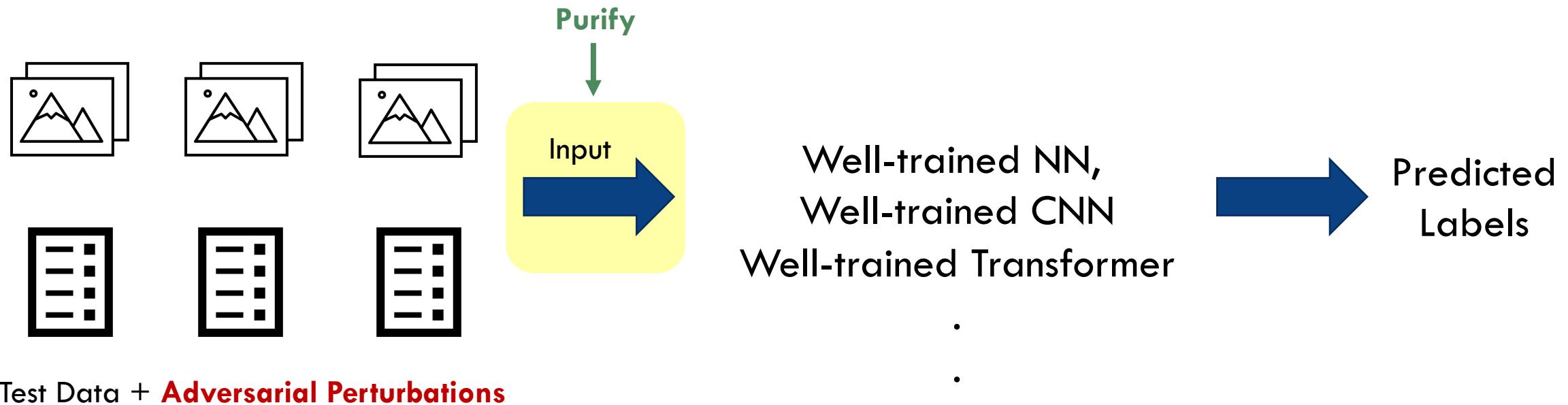
Adversarial detection

- Adversarial Detection (AD): aims to detect and discard AEs.



Adversarial purification

- Adversarial Purification (AP): aims to shift AEs back towards their natural counterparts.



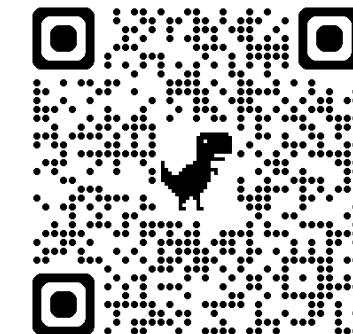
Sample-specific Noise Injection for Diffusion-based Adversarial Purification

Yuhao Sun[^], Jiacheng Zhang[^], Zesheng Ye[^], Chaowei Xiao, Feng Liu*

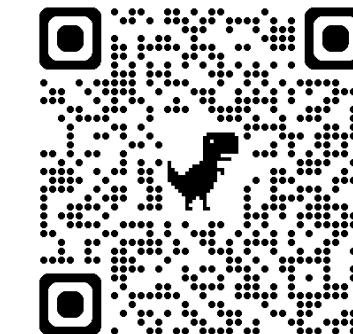
([^] Co-first authors, * Corresponding authors)

In ICML, 2025.

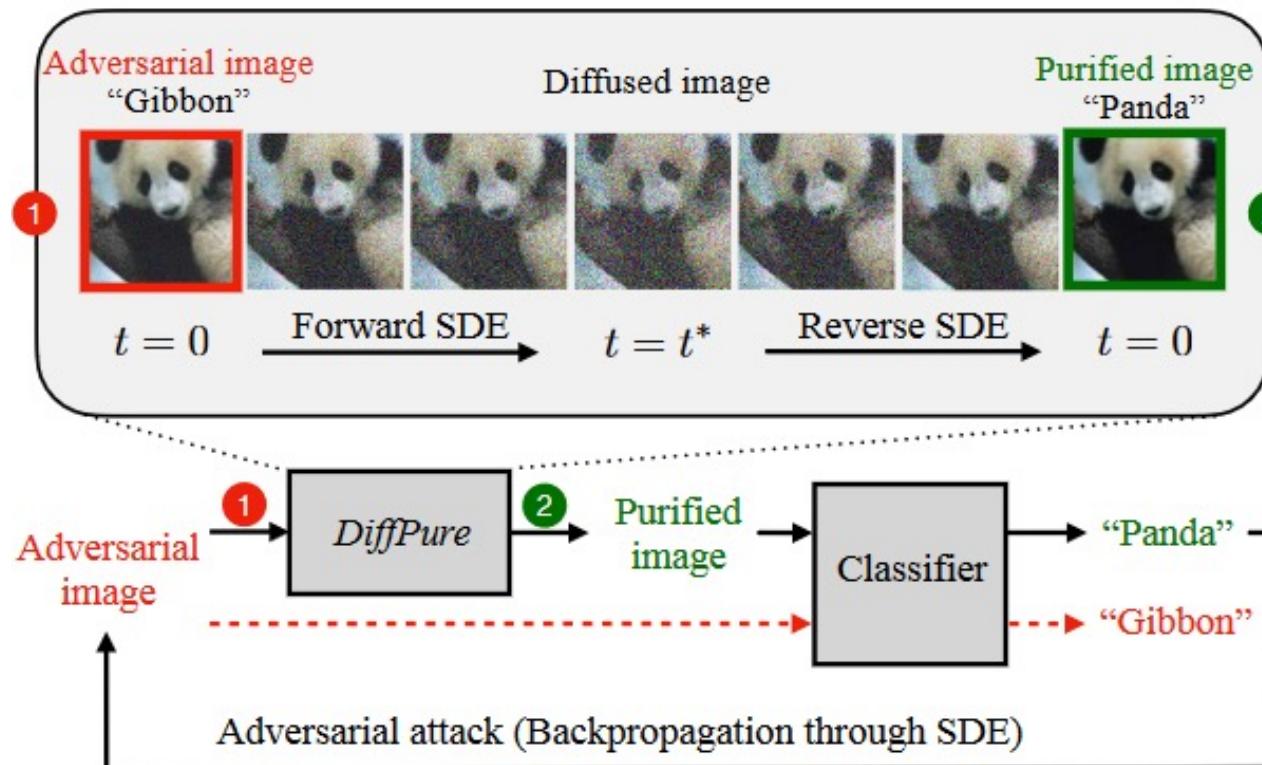
Paper



Code



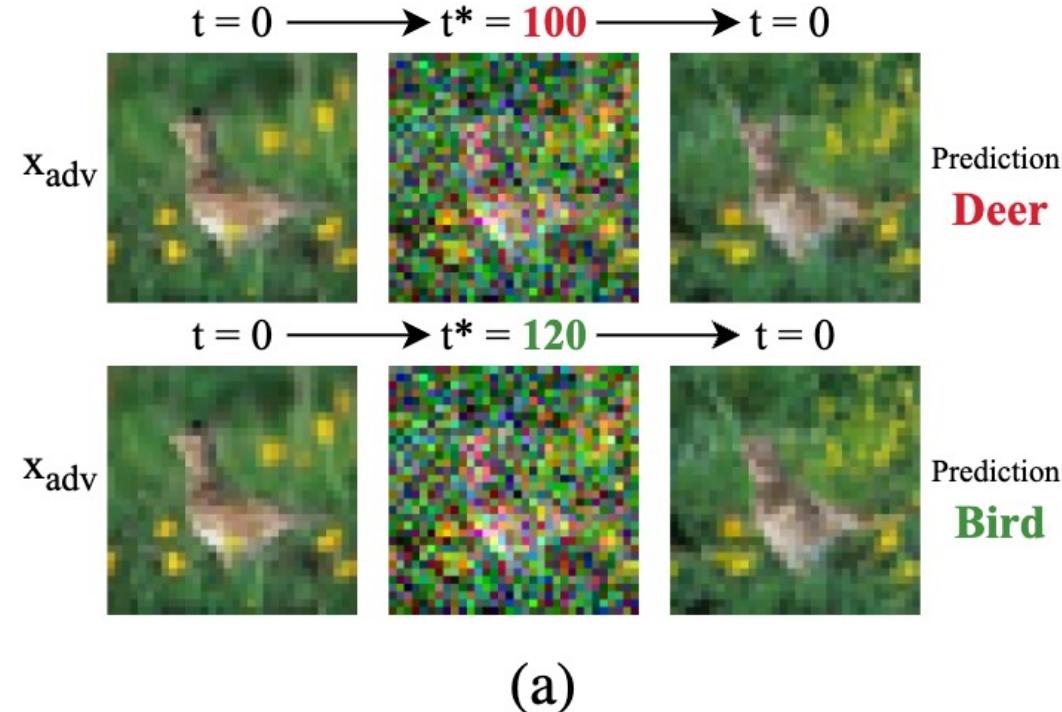
Preliminary: diffusion-based adversarial purification



A Key Challenge: The Choice of t

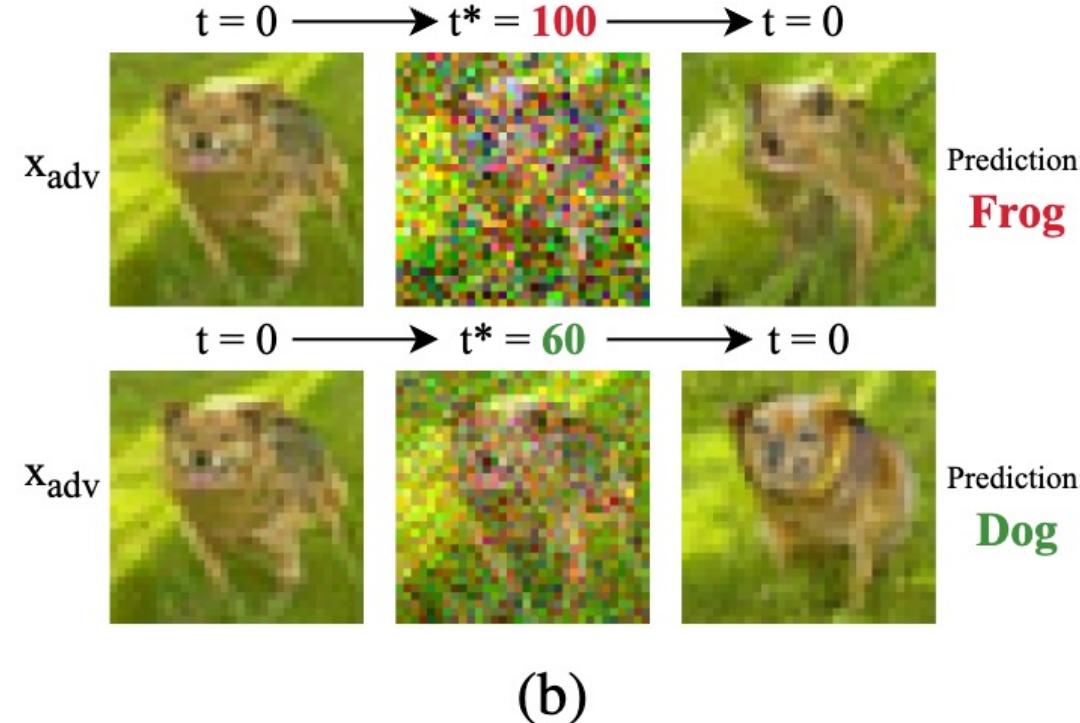
- **If t is too small**, then adversarial noise cannot be fully removed.
- **If t is too large**, then the purified image may have a different semantic meaning.
- **Research gap:** current methods empirically select a **fixed** timestep t for all images, which is **counterintuitive**.

Motivation



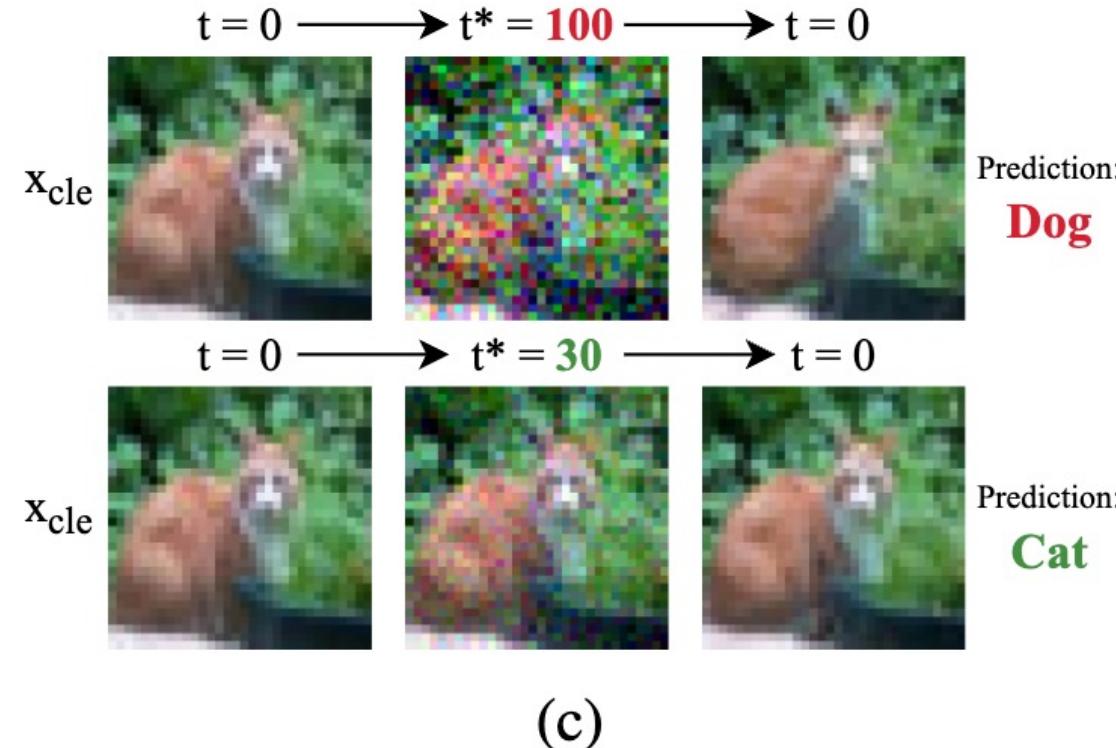
- ❑ Sample-shared noise level is sometimes **insufficient** to remove adversarial perturbations.

Motivation



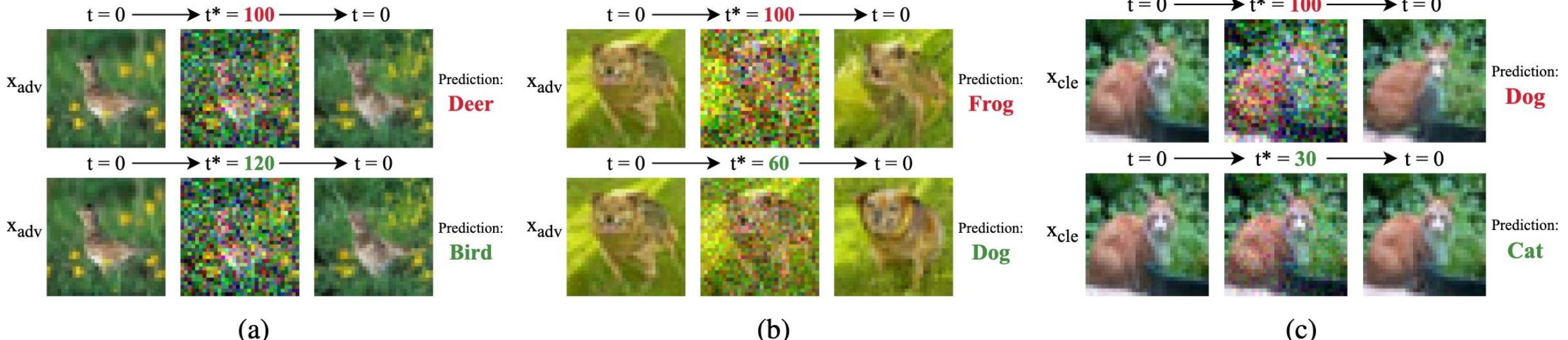
- Sample-shared noise level is sometimes too **large**, which causes excessive disruption of the sample's semantic information, making it difficult to recover the original semantics.

Motivation



- ❑ Sample-shared noise level is often too **large** for clean examples, as they do not need to be purified.

Proof-of-concept Experiment



- Sample-shared noise level *fail* to address diverse adversarial perturbations.
- These findings *highlight* the need for sample-specific noise injection levels.



What is the metric?

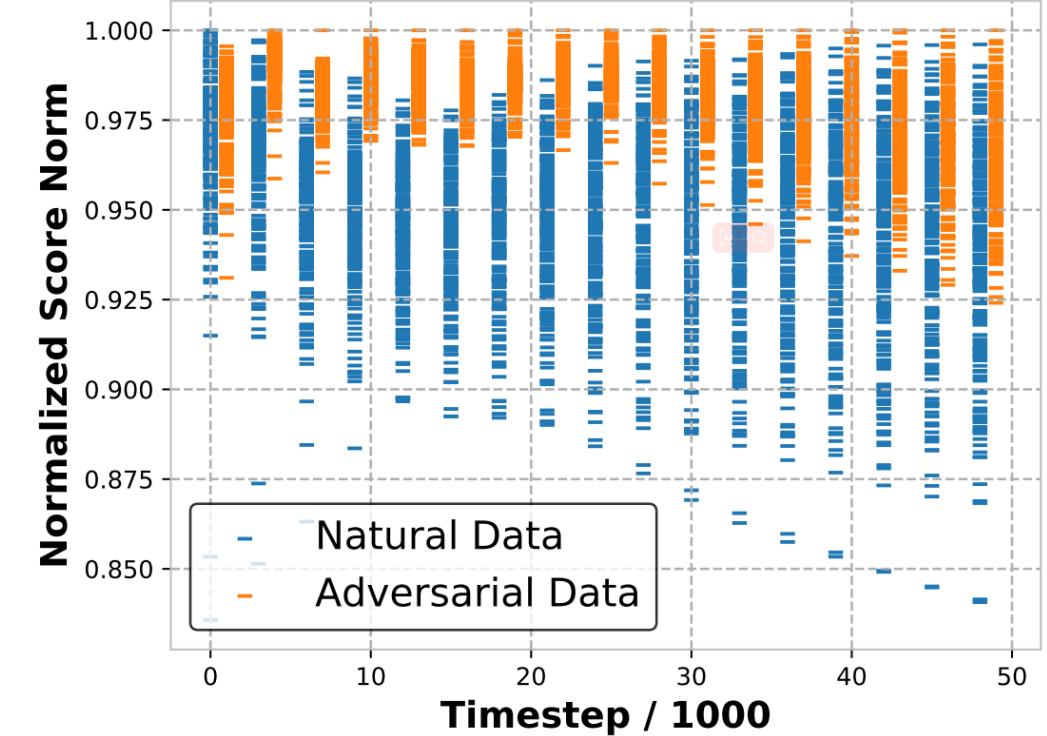
Intuition from score function

□ Intuition from score function $\nabla_x \log p(x)$

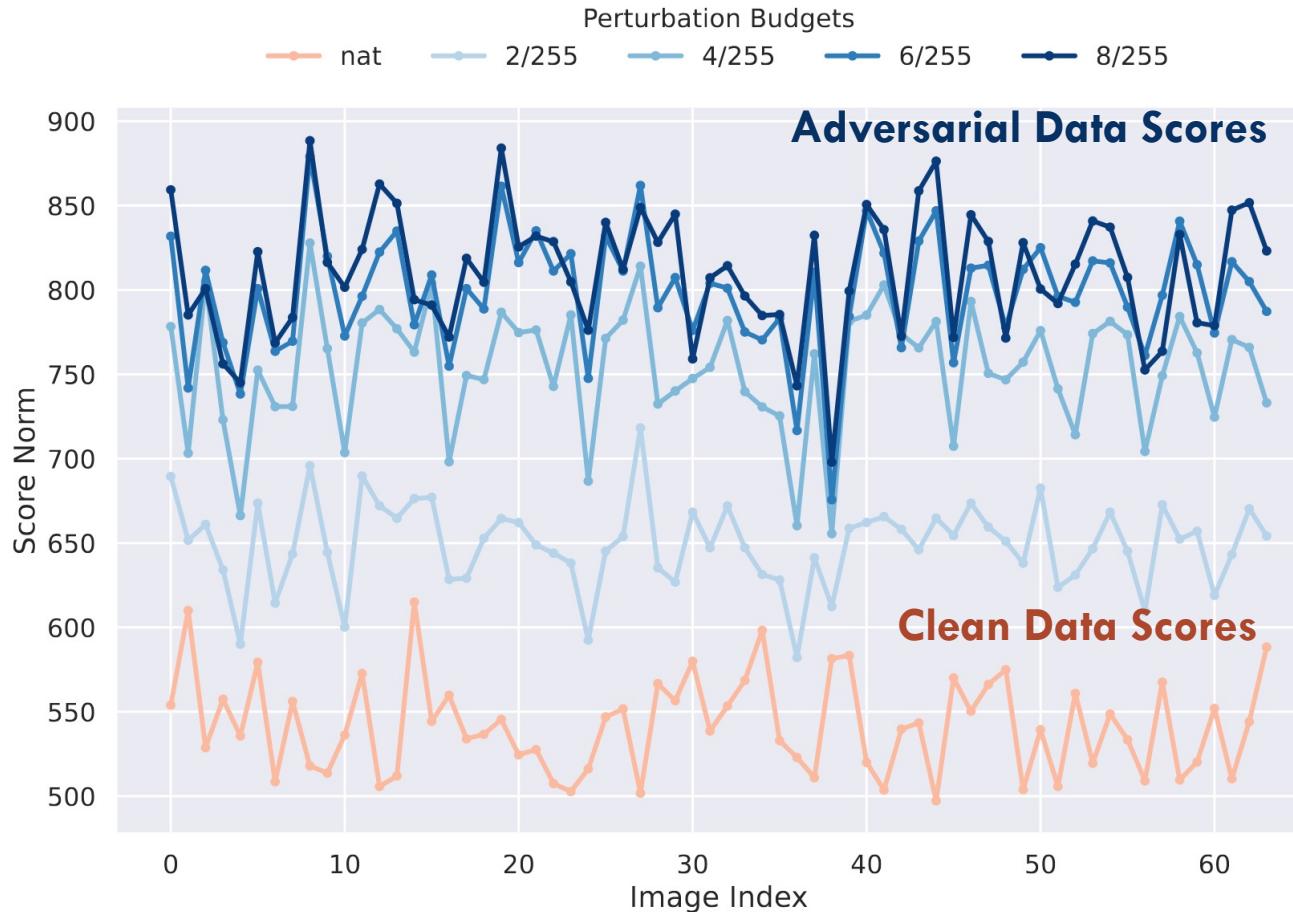
- Score $\nabla_x \log p(x)$ represents the momentum of the sample towards **high density areas** of natural data distribution (Song et al., 2019)



- A lower score norm $\|\nabla_x \log p(x)\|$ indicates the sample is **closer** to the high-density areas of natural data distribution

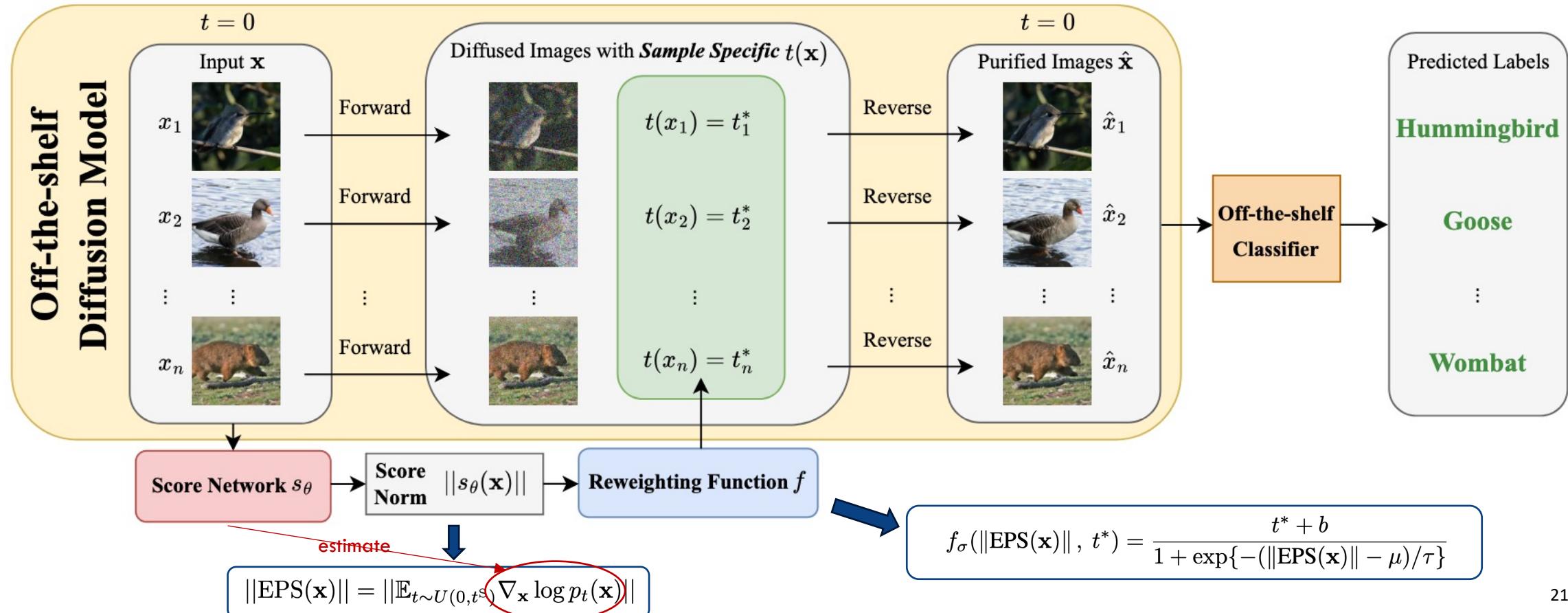


Score norms vs perturbation budgets

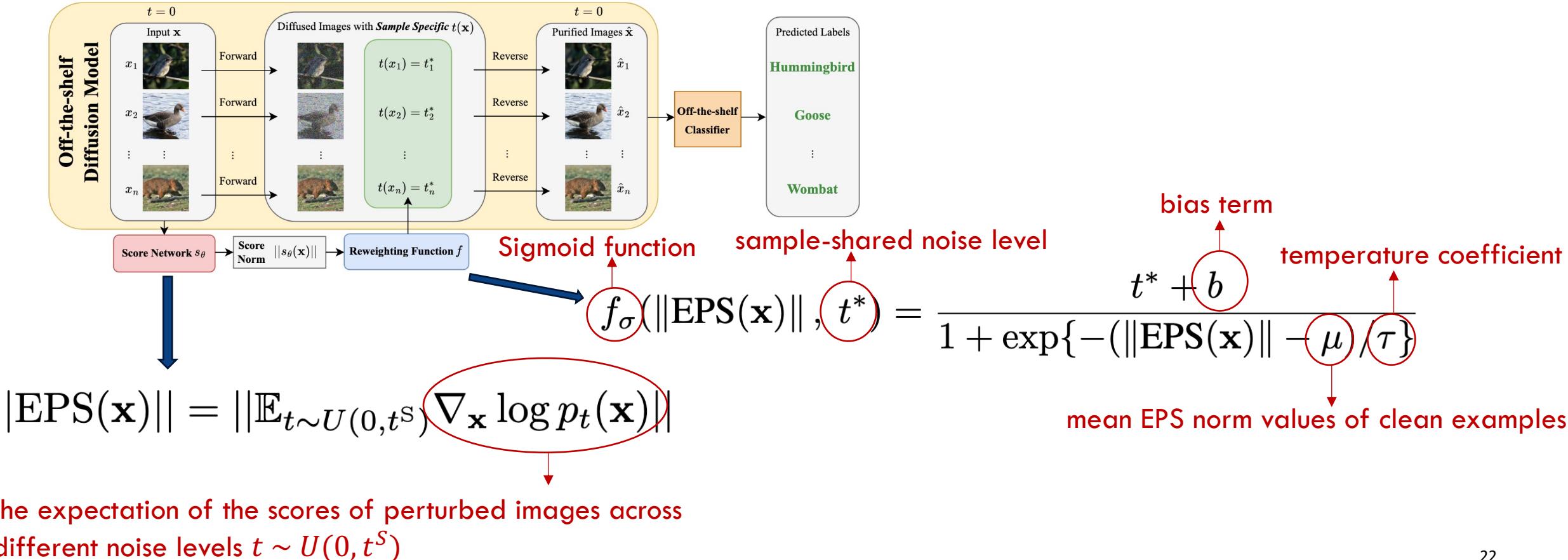


- We further find that score norms **scale directly** with perturbation budgets.
- Score norms can act as **proxies** for estimating the sample-specific noise level.

Sample-specific Score-aware Noise Injection (SSNI)



Sample-specific Score-aware Noise Injection (SSNI)



Main results: CIFAR10

PGD+EOT ℓ_∞ ($\epsilon = 8/255$)		
	Standard	Robust
WRN-28-10	Nie et al. (2022)	89.71±0.72
	+ SSNI-N	93.29±0.37 (+3.58)
	Wang et al. (2022)	92.45±0.64
	+ SSNI-N	94.08±0.33 (+1.63)
WRN-70-16	Lee & Kim (2023)	90.10±0.18
	+ SSNI-N	93.55±0.55 (+2.66)
	Nie et al. (2022)	90.89±1.13
	+ SSNI-N	94.47±0.51 (+3.58)
WRN-70-16	Wang et al. (2022)	93.10±0.51
	+ SSNI-N	95.57±0.24 (+2.47)
	Lee & Kim (2023)	89.39±1.12
	+ SSNI-N	93.82±0.24 (+4.44)

PGD+EOT ℓ_2 ($\epsilon = 0.5$)		
	Standard	Robust
WRN-28-10	Nie et al. (2022)	91.80±0.84
	+ SSNI-N	93.95±0.70 (+2.15)
	Wang et al. (2022)	92.45±0.64
	+ SSNI-N	94.08±0.33 (+1.63)
WRN-70-16	Lee & Kim (2023)	90.10±0.18
	+ SSNI-N	93.55±0.55 (+3.45)
	Nie et al. (2022)	92.90±0.40
	+ SSNI-N	95.12±0.58 (+2.22)
WRN-70-16	Wang et al. (2022)	93.10±0.51
	+ SSNI-N	95.57±0.24 (+2.47)
	Lee & Kim (2023)	89.39±1.12
	+ SSNI-N	93.82±0.24 (+4.43)

Main results: ImageNet-1K

PGD+EOT ℓ_∞ ($\epsilon = 4/255$)			
	DBP Method	Standard	Robust
RN-50	Nie et al. (2022)	68.23±0.92	30.34±0.72
	+ SSNI-N	70.25±0.56 (+2.02)	33.66±1.04 (+3.32)
	Wang et al. (2022)	74.22±0.12	0.39±0.03
	+ SSNI-N	75.07±0.18 (+0.85)	5.21±0.24 (+4.82)
	Lee & Kim (2023)	70.18±0.60	42.45±0.92
	+ SSNI-N	72.69±0.80 (+2.51)	43.48±0.25 (+1.03)

AutoAttack, DiffAttack and Diff-PGD

$\ell_\infty (\epsilon = 8/255)$					
	DBP Method	Standard	AutoAttack	DiffAttack	Diff-PGD
WRN-28-10	Nie et al. (2022)	89.71±0.72	66.73±0.21	47.16±0.48	54.95±0.77
	+ SSNI-N	93.29±0.37 (+3.58)	66.94±0.44 (+0.21)	48.15±0.22 (+0.99)	56.10±0.35 (+1.15)
WRN-28-10	Wang et al. (2022)	92.45±0.64	64.48±0.62	54.27±0.72	41.45±0.60
	+ SSNI-N	94.08±0.33 (+1.63)	66.53±0.46 (+2.05)	55.81±0.33 (+1.54)	42.91±0.56 (+1.46)
WRN-28-10	Lee & Kim (2023)	90.10±0.18	69.92±0.30	56.04±0.58	59.02±0.28
	+ SSNI-N	93.55±0.55 (+3.45)	72.27±0.19 (+2.35)	56.80±0.41 (+0.76)	61.43±0.58 (+2.41)

Inference Time

DBP Method	Noise Injection Method	Time (s)
Nie et al. (2022)	-	3.934
	SSNI-L	4.473
	SSNI-N	4.474
Wang et al. (2022)	-	5.174
	SSNI-L	5.793
	SSNI-N	5.829
Lee & Kim (2023)	-	14.902
	SSNI-L	15.624
	SSNI-N	15.534

DBP Method	Noise Injection Method	Time (s)
Nie et al. (2022)	-	8.980
	SSNI-L	14.515
	SSNI-N	14.437
Wang et al. (2022)	-	11.271
	SSNI-L	16.657
	SSNI-N	16.747
Lee & Kim (2023)	-	35.091
	SSNI-L	40.526
	SSNI-N	40.633

Limitations of DBP framework & SSNI

- ❑ **Limitation 1:** Having a pre-trained diffusion model is not always feasible, training a diffusion model is resource-consuming.
- ❑ **Limitation 2:** The inference speed of DBP-based methods is slow.
- ❑ **Limitation 3:** SSNI still injects noise to clean samples, which cannot fully preserve the utility (i.e., clean accuracy) of the model.

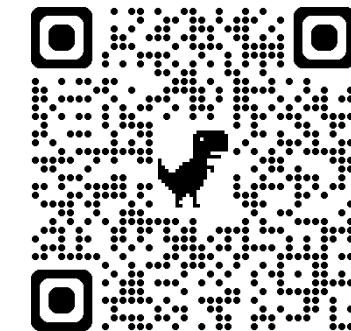
One Stone, Two Birds: Enhancing Adversarial Defense Through the Lens of Distributional Discrepancy

Jiacheng Zhang, Benjamin I. P. Rubinstein, Jingfeng Zhang, Feng Liu*

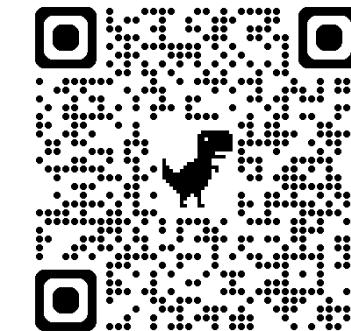
(* Corresponding authors)

In ICML, 2025.

Paper

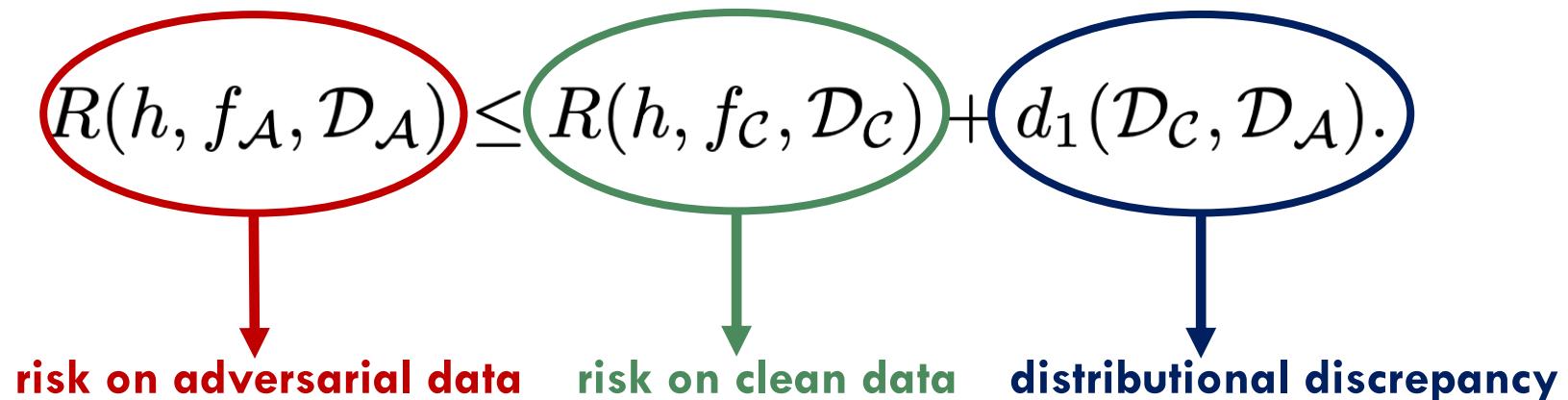


Code



Distributional discrepancy minimization improves robustness

Theorem 1. *For a hypothesis $h \in \mathcal{H}$ and a distribution $\mathcal{D}_A \in \mathbb{D}$:*

$$R(h, f_A, \mathcal{D}_A) \leq R(h, f_C, \mathcal{D}_C) + d_1(\mathcal{D}_C, \mathcal{D}_A).$$


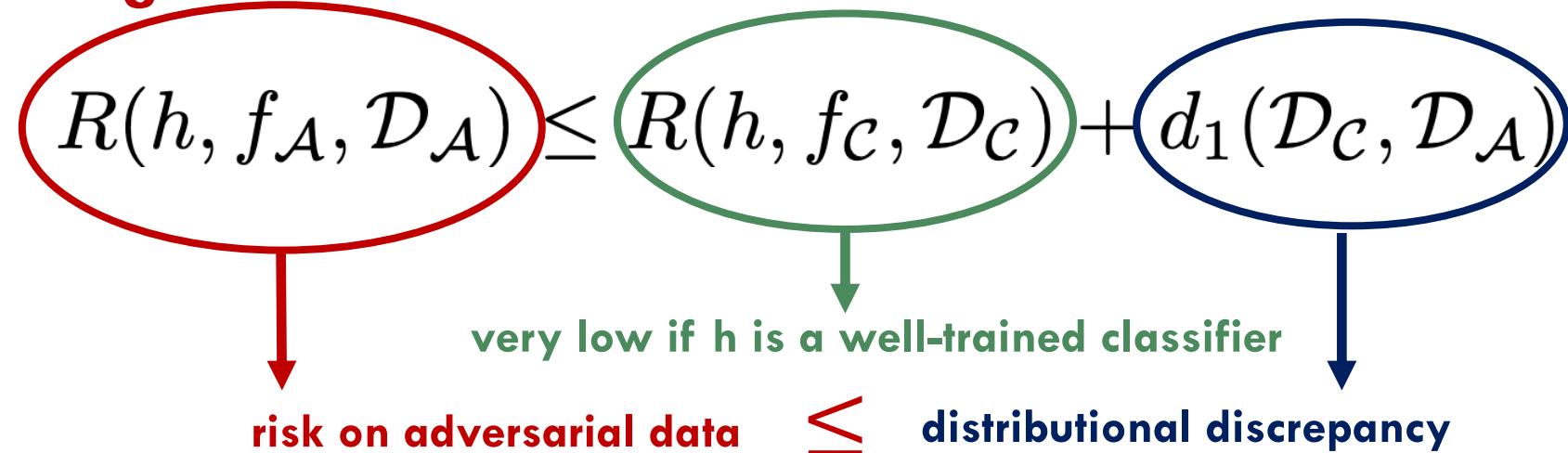
The diagram illustrates the components of the theorem. Three ovals represent the terms in the inequality: a red oval for $R(h, f_A, \mathcal{D}_A)$, a green oval for $R(h, f_C, \mathcal{D}_C)$, and a blue oval for $d_1(\mathcal{D}_C, \mathcal{D}_A)$. Below each oval is a downward-pointing arrow and a corresponding label: a red arrow labeled "risk on adversarial data" under the red oval, a green arrow labeled "risk on clean data" under the green oval, and a blue arrow labeled "distributional discrepancy" under the blue oval.

Distributional discrepancy minimization improves robustness

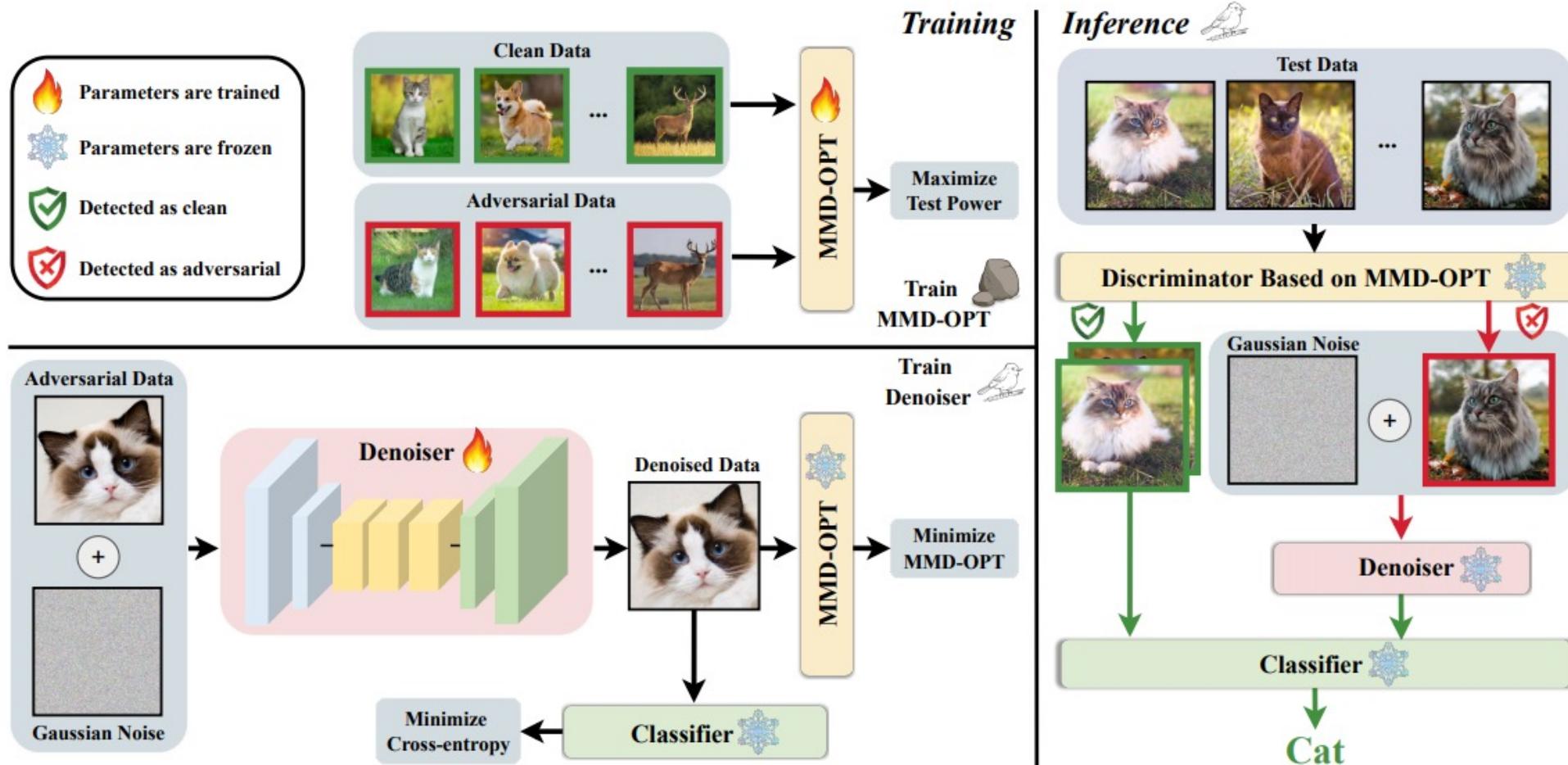
- Previous Studies: loose bound due to **an extra constant**

$$R(h, f_A, \mathcal{D}_A) \leq R(h, f_C, \mathcal{D}_C) + d_1(\mathcal{D}_C, \mathcal{D}_A) + \mathbf{C}$$

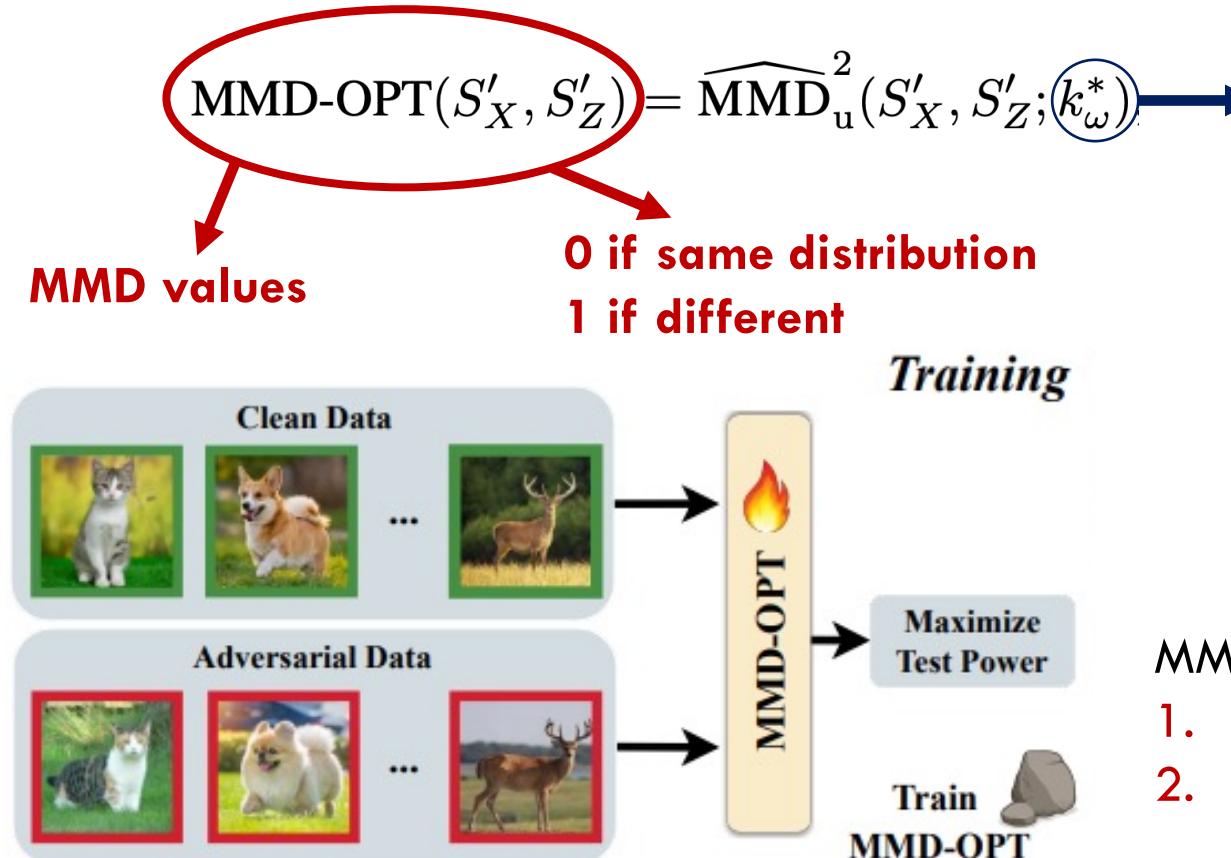
- Ours: **tight bound** without extra constants



Distributional-discrepancy-based Adversarial Defense (DAD)



One stone: optimized MMD



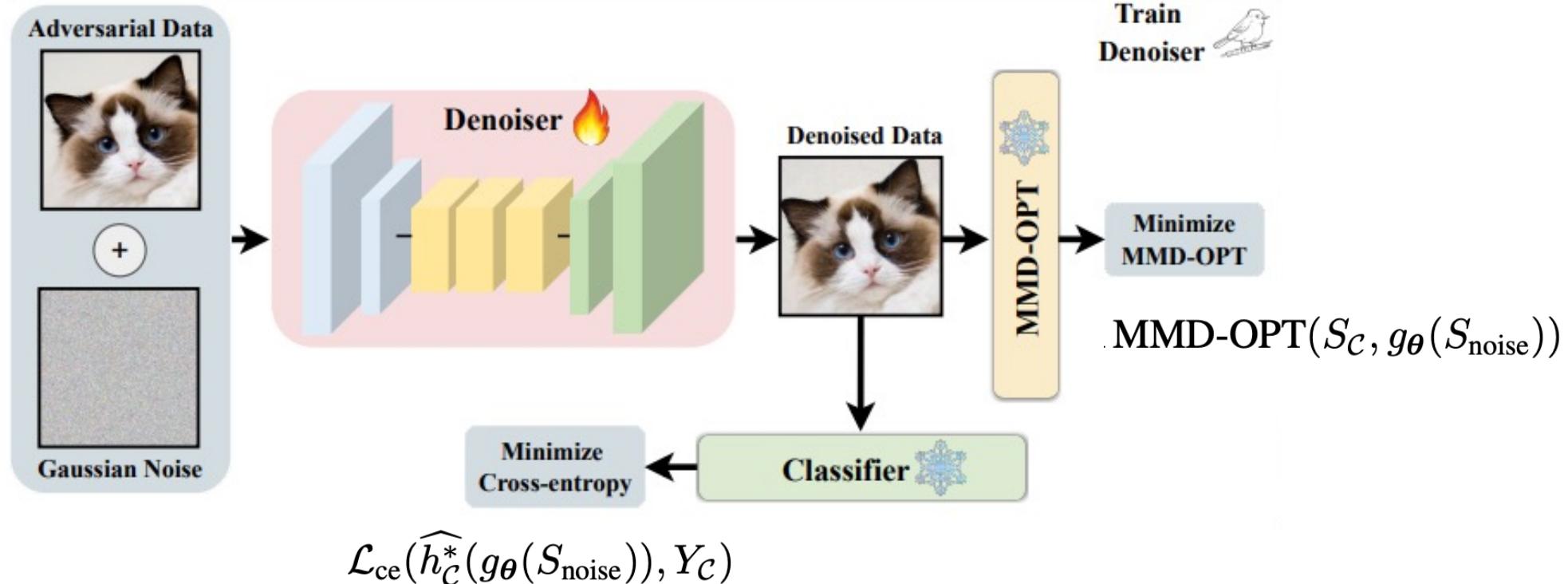
Algorithm 1 Optimizing MMD (Liu et al., 2020).

- 1: **Input:** clean data S_C^{train} , adversarial data S_A^{train} , learning rate η , epoch T ;
- 2: Initialize $\omega \leftarrow \omega_0$; $\lambda \leftarrow 10^{-8}$;
- 3: **for** epoch = 1, ..., T **do**
- 4: $S'_C \leftarrow$ minibatch from S_C^{train} ;
- 5: $S'_A \leftarrow$ minibatch from S_A^{train} ;
- 6: $k_\omega \leftarrow$ kernel function with parameters ω using Eq. (3);
- 7: $M(\omega) \leftarrow \widehat{\text{MMD}}^2_u(S'_C, S'_A; k_\omega)$ using Eq. (2);
- 8: $V_\lambda(\omega) \leftarrow \hat{\sigma}_\lambda(S'_C, S'_A; k_\omega)$ using Eq. (5);
- 9: $\hat{J}_\lambda(\omega) \leftarrow M(\omega)/\sqrt{V_\lambda(\omega)}$ using Eq. (4);
- 10: $\omega \leftarrow \omega + \eta \nabla_{\text{Adam}} \hat{J}_\lambda(\omega)$;
- 11: **end for**
- 12: **Output:** k_ω^*

MMD-OPT serves as:

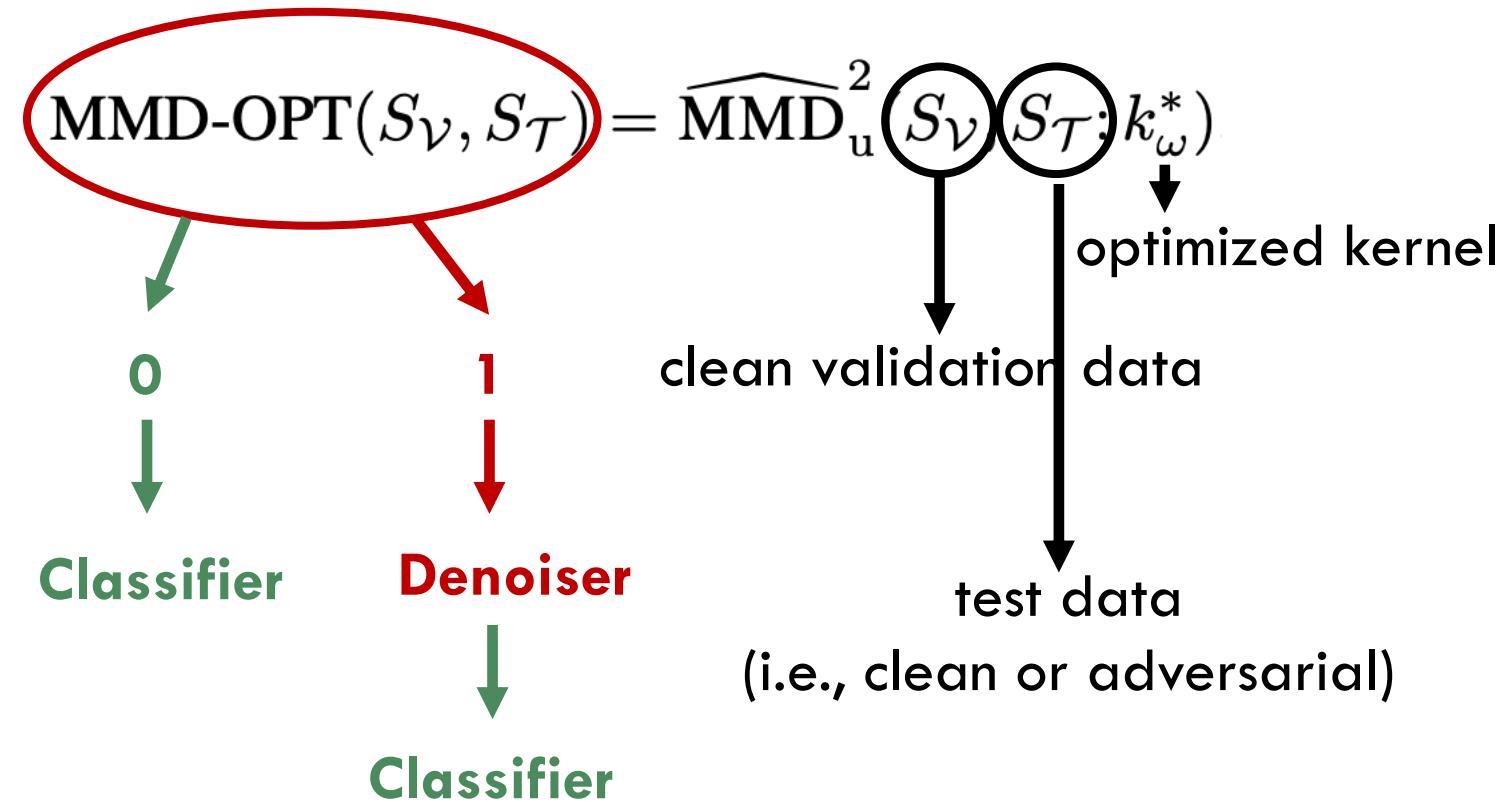
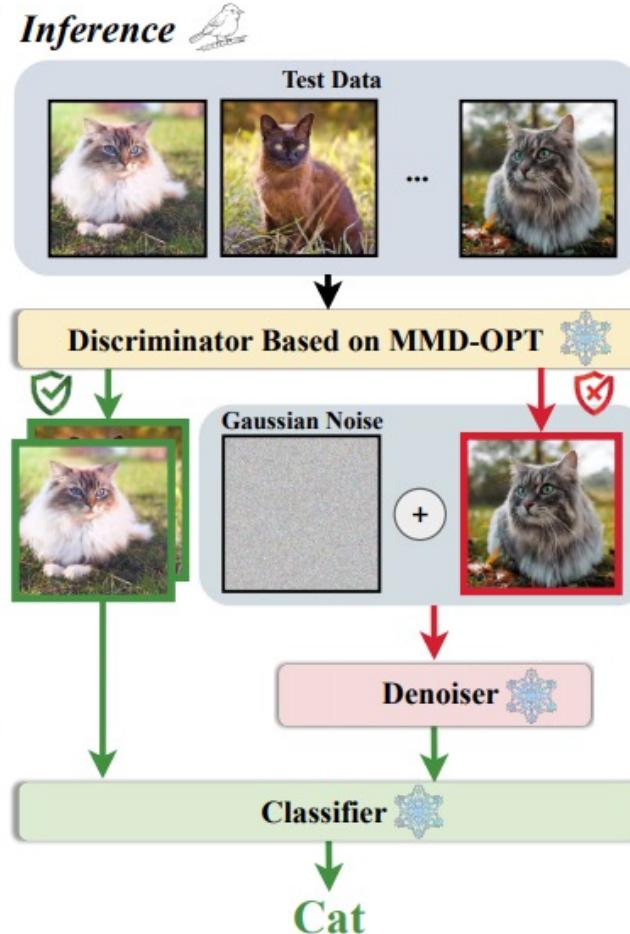
1. Guiding signal to train a denoiser.
2. Discriminator to differentiate clean data and adversarial data during inference

First bird: MMD-OPT-based denoiser



Objective: $g_{\theta^*} = \arg \min_{\theta} \text{MMD-OPT}(S_C, g_\theta(S_{\text{noise}})) + \alpha \cdot \mathcal{L}_{\text{ce}}(\widehat{h}_C^*(g_\theta(S_{\text{noise}})), Y_C)$

Second bird: MMD-OPT-based discriminator



Adaptive Attack based on PGD+EOT

Algorithm 3 Adaptive white-box PGD+EOT attack for DAD.

```

1: Input: clean data-label pairs  $(S_C, Y_C)$ , optimized characteristic kernel  $k_\omega^*$  by Algorithm 1, pre-trained classifier  $\widehat{h}_C^*$ , denoiser  $g$  with parameters  $\theta$ , maximum allowed perturbation  $\epsilon$ , step size  $\eta$ , PGD iteration  $T$ , EOT iteration  $K$ ;
2: Initialize adversarial data  $S_A \leftarrow S_C$ ;  $\mu \leftarrow 0$ ;  $\sigma \leftarrow 0.25$ ;  $\alpha \leftarrow 10^{-2}$ ;  $t \leftarrow 0.05$ ;
3: for PGD iteration  $1, \dots, T$  do
4:   Initialize gradients over EOT  $\mathcal{G}_{\text{EOT}} \leftarrow \mathbf{0}$ ;
5:   Compute MMD-OPT( $S_C, S_A$ ) by Eq. (6);
6:   for EOT iteration  $1, \dots, K$  do
7:     if MMD-OPT( $S_C, S_A$ )  $< t$  then
8:        $\mathcal{G}_{\text{EOT}} \leftarrow \mathcal{G}_{\text{EOT}} + \nabla_{S_A}(\text{MMD-OPT}(S_C, S_A) + \alpha \cdot \mathcal{L}_{\text{ce}}(\widehat{h}_C^*(S_A), Y_C))$ ;
9:     else
```

```

9:     else
10:      Generate Gaussian noise:  $\mathbf{n} \sim \mathcal{N}(\mu, \sigma^2)$ ;
11:       $S_{\text{noise}} \leftarrow S_A + \mathbf{n}$ ;
12:       $\mathcal{G}_{\text{EOT}} \leftarrow \mathcal{G}_{\text{EOT}} + \nabla_{S_A}(\text{MMD-OPT}(S_C, S_A) + \alpha \cdot \mathcal{L}_{\text{ce}}(\widehat{h}_C^*(g_\theta(S_{\text{noise}})), Y_C))$ ;
13:    end if
14:  end for
15:   $\mathcal{G}_{\text{EOT}} \leftarrow \frac{1}{K} \mathcal{G}_{\text{EOT}}$ ;
16:  Update  $S_A \leftarrow \Pi_{\mathcal{B}_\epsilon(S_C)}(S_A + \eta \cdot \text{sign}(\mathcal{G}_{\text{EOT}}))$ ;
17: end for
18: Output:  $S_A$ 
```

Aims to mislead MMD-OPT,
and then, mislead the denoiser and the
classifier correspondingly

Main results: CIFAR-10

$\ell_\infty (\epsilon = 8/255)$			
Type	Method	Clean	Robust
WRN-28-10			
AT	Gowal et al. (2021)	87.51	63.38
	Gowal et al. (2020)*	88.54	62.76
	Pang et al. (2022a)	88.62	61.04
AP	Yoon et al. (2021)	85.66	33.48
	Nie et al. (2022)	90.07	46.84
	Lee & Kim (2023)	90.16	55.82
Ours	DAD	94.16 ± 0.08	67.53 ± 1.07
WRN-70-16			
AT	Rebuffi et al. (2021)*	92.22	66.56
	Gowal et al. (2021)	88.75	66.10
	Gowal et al. (2020)*	91.10	65.87
AP	Yoon et al. (2021)	86.76	37.11
	Nie et al. (2022)	90.43	51.13
	Lee & Kim (2023)	90.53	56.88
Ours	DAD	93.91 ± 0.11	67.68 ± 0.87

$\ell_2 (\epsilon = 0.5)$			
Type	Method	Clean	Robust
WRN-28-10			
AT	Rebuffi et al. (2021)*	91.79	78.80
	Augustin et al. (2020)†	93.96	78.79
	Sehwag et al. (2022)†	90.93	77.24
AP	Yoon et al. (2021)	85.66	73.32
	Nie et al. (2022)	91.41	79.45
	Lee & Kim (2023)	90.16	83.59
Ours	DAD	94.16 ± 0.08	84.38 ± 0.81
WRN-70-16			
AT	Rebuffi et al. (2021)*	95.74	82.32
	Gowal et al. (2020)*	94.74	80.53
	Rebuffi et al. (2021)	92.41	80.42
AP	Yoon et al. (2021)	86.76	75.66
	Nie et al. (2022)	92.15	82.97
	Lee & Kim (2023)	90.53	83.57
Ours	DAD	93.91 ± 0.11	84.03 ± 0.75

Main results: ImageNet-1K

$\ell_\infty (\epsilon = 4/255)$			
Type	Method	Clean	Robust
RN-50			
AT	Salman et al. (2020a)	64.02	34.96
	Engstrom et al. (2019)	62.56	29.22
	Wong et al. (2020)	55.62	26.24
AP	Nie et al. (2022)	71.48	38.71
	Lee & Kim (2023)	70.74	42.15
Ours	DAD	78.61 ± 0.04	53.85 ± 0.23

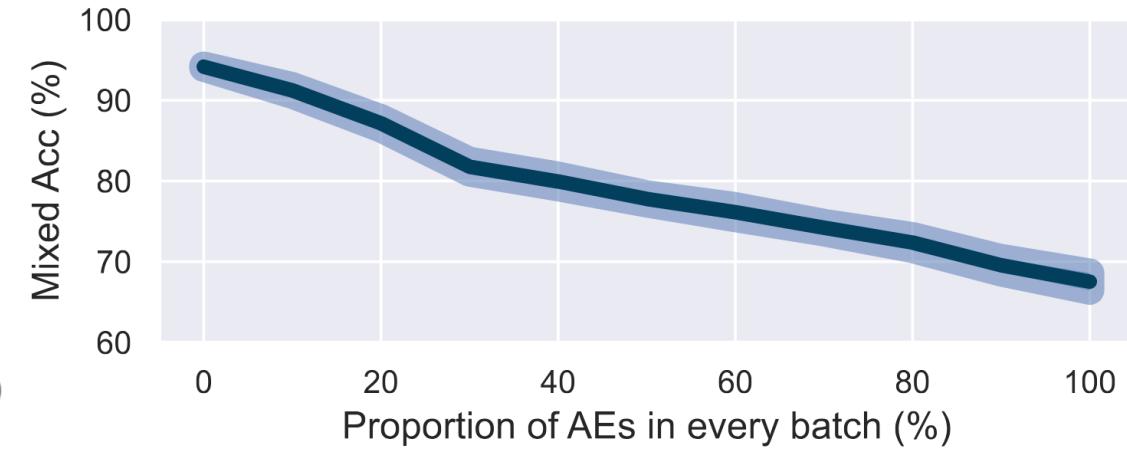
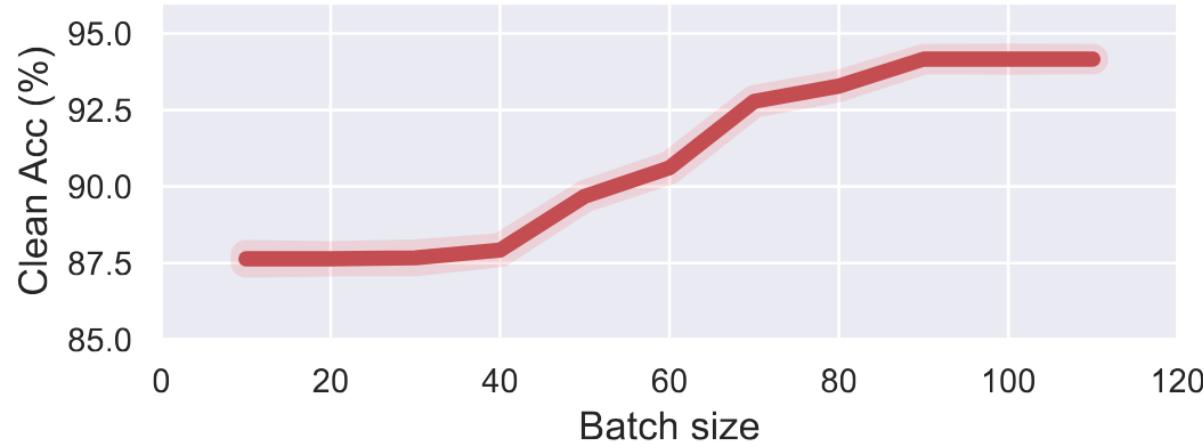
Transferability

Trained on WRN-28-10					
Unseen Transfer Attack		WRN-70-16	RN-18	RN-50	Swin-T
PGD+EOT (ℓ_∞)	$\epsilon = 8/255$	80.84 ± 0.46	80.78 ± 0.60	81.47 ± 0.30	81.46 ± 0.29
	$\epsilon = 12/255$	80.26 ± 0.60	80.54 ± 0.45	80.98 ± 0.36	80.40 ± 0.41
C&W (ℓ_2)	$\epsilon = 0.5$	82.45 ± 0.19	91.30 ± 0.20	89.26 ± 0.11	93.45 ± 0.17
	$\epsilon = 1.0$	81.20 ± 0.39	90.37 ± 0.17	88.65 ± 0.22	93.41 ± 0.18

Strength of DAD

- **Strength 1:** DAD can largely preserve the original utility (i.e., clean accuracy of the classifier).
- **Strength 2:** Compared to DBP methods that reply on density estimation, learning distributional discrepancies is a simpler and more feasible task.
- **Strength 3:** DAD is efficient in both training and inferencing.

Limitations of DAD



Thank You!