$$\nabla_{\phi} f(w, \phi) = \sum_{i} \nabla_{\phi} \mathbb{E}_{q(t_i \mid x_i, \phi)} \log p(x_i \mid t_i, w)$$

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$$t_i = \varepsilon_i \odot s_i + m_i$$

$$\varepsilon_i \sim p(\varepsilon_i) = \mathcal{N}(0, I)$$

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$$t_i = \varepsilon_i \odot s_i + m_i = g(\varepsilon_i, x_i, \phi)$$

$$\varepsilon_i \sim p(\varepsilon_i) = \mathcal{N}(0, I)$$

$$\nabla_{\phi} f(w, \phi) = \sum_{i} \nabla_{\phi} \mathbb{E}_{q(t_{i}|x_{i}, \phi)} \log p(x_{i} \mid t_{i}, w)$$
$$= \sum_{i} \nabla_{\phi} \mathbb{E}_{p(\varepsilon_{i})} \log p(x_{i} \mid g(\varepsilon_{i}, x_{i}, \phi), w)$$

$$t_i \sim q(t_i \mid x_i, \phi) = \mathcal{N}(m_i, \operatorname{diag}(s_i^2))$$
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$$= \sum_{i} \mathbb{E}_{p(\varepsilon_{i})} \nabla_{\phi} \log p(x_{i} \mid g(\varepsilon_{i}, x_{i}, \phi), w)$$

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$$t_{i} = \varepsilon_{i} \odot s_{i} + m_{i} = g(\varepsilon_{i}, x_{i}, \phi)$$

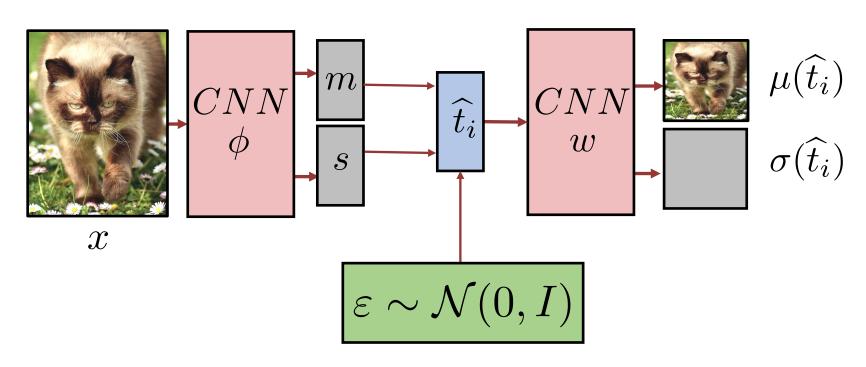
$$\varepsilon_{i} \sim p(\varepsilon_{i}) = \mathcal{N}(0, I)$$

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$$p(\varepsilon_{i}) = \mathcal{N}(0, I)$$
$$t_{i} = \varepsilon_{i} \odot s_{i} + m_{i} = g(\varepsilon_{i}, x_{i}, \phi)$$



# **Variational Autoencoder summary**

- Infinite mixture of Gaussians
- To learn: EM + approximate q with Gaussians + stochastic variational inference
- Like plain autoencoder, but with noise and KL regularization
- Generates nice images