

Ensemble methods: boosting

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Examined ensemble methods

- Averaging (or blending)
- Weighted averaging
- Conditional averaging
- Bagging
- **Boosting**
- Stacking
- StackNet



What is Boosting

A form of weighted averaging of models where each model is built sequentially via taking into account the past model performance.



Main boosting types

- Weight based
- Residual based



Weight based boosting

| Rownum | x0 | x1 | x2 | x3 | y |
|--------|------|------|------|------|---|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 1 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 1 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 1 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | 0 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | 0 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 1 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | 0 |



Weight based boosting

| Rownum | x0 | x1 | x2 | x3 | y | pred |
|--------|------|------|------|------|---|------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 1 | 0.80 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 1 | 0.75 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 1 | 0.65 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | 0 | 0.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | 0 | 0.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 1 | 0.34 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | 0 | 0.02 |

















Weight based boosting

| Rownum | x0 | x1 | x2 | x3 | y | pred | abs.error |
|--------|------|------|------|------|---|------|------------------------------------------------------------------------------------------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 1 | 0.80 |  0.20 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 1 | 0.75 |  0.25 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 1 | 0.65 |  0.35 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | 0 | 0.40 |  0.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | 0 | 0.55 |  0.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 1 | 0.34 |  0.66 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | 0 | 0.02 |  0.02 |



Weight based boosting

| Rownum | x0 | x1 | x2 | x3 | y | pred | abs.error | weight |
|--------|------|------|------|------|---|------|------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 1 | 0.80 |  0.20 |  1.20 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 1 | 0.75 |  0.25 |  1.25 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 1 | 0.65 |  0.35 |  1.35 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | 0 | 0.40 |  0.40 |  1.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | 0 | 0.55 |  0.55 |  1.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 1 | 0.34 |  0.66 |  1.66 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | 0 | 0.02 |  0.02 |  1.02 |



Weight based boosting

| Rownum | x0 | x1 | x2 | x3 | y | weight |
|--------|------|------|------|------|---|--------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 1 | 1.20 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 1 | 1.25 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 1 | 1.35 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | 0 | 1.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | 0 | 1.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 1 | 1.66 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | 0 | 1.02 |



Weight based boosting parameters

- Learning rate (or shrinkage or eta)
- Number of estimators
- Input model – can be anything that accepts weights
- Sub boosting type:
 - AdaBoost – Good implementation in sklearn (python)
 - LogitBoost - Good implementation in Weka (Java)



Residual based boosting

| Rownum | x0 | x1 | x2 | x3 | y |
|--------|------|------|------|------|---|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 1 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 1 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 1 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | 0 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | 0 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 1 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | 0 |



Residual based boosting

| Rownum | x0 | x1 | x2 | x3 | y | pred |
|--------|------|------|------|------|---|------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 1 | 0.80 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 1 | 0.75 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 1 | 0.65 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | 0 | 0.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | 0 | 0.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 1 | 0.34 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | 0 | 0.02 |



Residual based boosting

| Rownum | x0 | x1 | x2 | x3 | y | pred | error |
|--------|------|------|------|------|---|------|-------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 1 | 0.80 | 0.20 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 1 | 0.75 | 0.25 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 1 | 0.65 | 0.35 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | 0 | 0.40 | -0.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | 0 | 0.55 | -0.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 1 | 0.34 | 0.66 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | 0 | 0.02 | -0.02 |



Residual based boosting

| Rownum | x0 | x1 | x2 | x3 | y |
|--------|------|------|------|------|-------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 0.2 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 0.25 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 0.35 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | -0.4 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | -0.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 0.66 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | -0.02 |



Residual based boosting

| Rownum | x0 | x1 | x2 | x3 | y | new pred |
|--------|------|------|------|------|-------|----------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 0.2 | 0.15 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 0.25 | 0.20 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 0.35 | 0.40 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | -0.4 | -0.30 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | -0.55 | -0.20 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 0.66 | 0.24 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | -0.02 | -0.01 |



Residual based boosting

| Rownum | x0 | x1 | x2 | x3 | y | new pred | old pred |
|--------|------|------|------|------|-------|----------|----------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 0.2 | 0.15 | 0.80 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 0.25 | 0.20 | 0.75 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 0.35 | 0.40 | 0.65 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | -0.4 | -0.30 | 0.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | -0.55 | -0.20 | 0.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 0.66 | 0.24 | 0.34 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | -0.02 | -0.01 | 0.02 |



Residual based boosting

| Rownum | x0 | x1 | x2 | x3 | y | new pred | old pred |
|--------|------|------|------|------|-------|----------|----------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 0.2 | 0.15 | 0.80 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 0.25 | 0.20 | 0.75 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 0.35 | 0.40 | 0.65 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | -0.4 | -0.30 | 0.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | -0.55 | -0.20 | 0.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 0.66 | 0.24 | 0.34 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | -0.02 | -0.01 | 0.02 |

To predict Rownum=1 we would say :

Final prediction = $0.75 + 0.20 = \mathbf{0.95}$



Residual based boosting

| Rownum | x0 | x1 | x2 | x3 | y | new pred | old pred |
|--------|------|------|------|------|-------|----------|----------|
| 0 | 0.94 | 0.27 | 0.80 | 0.34 | 0.2 | 0.15 | 0.80 |
| 1 | 0.84 | 0.79 | 0.89 | 0.05 | 0.25 | 0.20 | 0.75 |
| 2 | 0.83 | 0.11 | 0.23 | 0.42 | 0.35 | 0.40 | 0.65 |
| 3 | 0.74 | 0.26 | 0.03 | 0.41 | -0.4 | -0.30 | 0.40 |
| 4 | 0.08 | 0.29 | 0.76 | 0.37 | -0.55 | -0.20 | 0.55 |
| 5 | 0.71 | 0.76 | 0.43 | 0.95 | 0.66 | 0.24 | 0.34 |
| 6 | 0.08 | 0.72 | 0.97 | 0.04 | -0.02 | -0.01 | 0.02 |

To predict Rownum=1 we would say :

Final prediction = $0.75 + 0.20 = \mathbf{0.95}$



Residual based boosting parameters

- Learning rate (or shrinkage or eta)
- Number of estimators
- Row (sub) sampling
- Column (sub) sampling
- Input model – better be trees.
- Sub boosting type:
 - Fully gradient based
 - Dart



Residual based favourite implementations

- Xgboost
- Lightgbm
- H2O's GBM
- Catboost
- Sklearn's GBM

