```
clear;
clc;
t_0 = 0;
t f = 10;
num\_steps = 64;
% ACADO optimization
BEGIN ACADO;
                                            % Always start with "BEGIN ACADO".
    acadoSet('problemname', 'hw8_1');
    % (a) Define states and controls
    DifferentialState px py theta delta v;
    Control u_a u_delta;
    % (a) Differential Equation
    f = acado.DifferentialEquation(0, t_f);
    f.add(dot(px) == v * cos(theta));
    f.add( dot(py) == v * sin(theta) );
    f.add( dot(theta) == v * tan(delta) );
    f.add(dot(v) == u_a);
    f.add( dot(delta) == u_delta );
    % (b) Optimal Control )
    ocp = acado.OCP(0.0, t_f, num_steps);
    % (b) Minimize control effort
    ocp.minimizeLSQ( [u_a; u_delta], 0 );
    % (c) Path constraints
    ocp.subjectTo( f );
    ocp.subjectTo( -5 <= v <= 5 );
    ocp.subjectTo( -5 <= u_a <= 5 );
    ocp.subjectTo( -pi/4 <= delta <= pi/4 );
    ocp.subjectTo( -pi/6 <= u_delta <= pi/6 );
    % (d) Initial Conditions
    ocp.subjectTo( 'AT_START', px == -10.0 );
    ocp.subjectTo( 'AT_START', py == 1.0 );
    ocp.subjectTo( 'AT_START', v == 0.0 );
    ocp.subjectTo( 'AT_START', theta == 0.0 );
    ocp.subjectTo( 'AT_START', delta == 0.0 );
    % (d) Final boundary conditions
    ocp.subjectTo( 'AT_END', px == 0.0 );
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ocp.subjectTo( 'AT_END', py == 0.0 );
    ocp.subjectTo( 'AT END', v == 0.0 );
    ocp.subjectTo( 'AT_END', theta == 0.0 );
    % (e) Optimization Algorithm
    algo = acado.OptimizationAlgorithm( ocp );
    % algorithm parameters
    algo.set( 'KKT_TOLERANCE', 1e-8 );
    algo.set( 'DISCRETIZATION_TYPE', 'MULTIPLE_SHOOTING' );
    algo.set( 'MAX_NUM_ITERATIONS', 500 );
END ACADO;
                     % Always end with "END ACADO".
                     % This will generate a file problemname_ACADO.m.
                     % Run this file to get your results. You can
                     % run the file problemname_ACADO.m as many
                     % times as you want without having to compile again.
% Run the test
out = hw8_1_RUN();
% Plotting
x = out.STATES;
u = out.CONTROLS;
figure;
title('Trajectory');
plot(x(:,2), x(:,3), '-r', 'DisplayName', 'trajectory');
hold on;
plot(x(1,2), x(1,3), '*g', 'DisplayName', 'start');
plot(x(end,2), x(end,3), '*b', 'DisplayName', 'end');
grid on;
legend();
xlabel('x');
ylabel('y');
figure;
title('States');
plot(x(:,1), x(:,4), '-r', 'DisplayName', 'theta');
hold on;
plot(x(:,1), x(:,5), '-g', 'DisplayName', 'v');
hold on;
plot(x(:,1), x(:,6), '-b', 'DisplayName', 'delta');
hold on;
plot(x(:,1), x(:,2), '-k', 'DisplayName', 'x');
hold on;
plot(x(:,1), x(:,3), '-c', 'DisplayName', 'y');
hold on;
grid on;
legend();
xlabel('t');
```

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figure;
title('Controls');
plot(u(:,1), u(:,2),'-r', 'DisplayName', 'u_a');
hold on;
plot(u(:,1), u(:,3),'-b', 'DisplayName', 'u_\delta');
grid on;
legend();
xlabel('t');
ylabel('value');
```

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